

## 4. PRÄSENZÜBUNG FOR QUANTUM MECHANICS (PTP 4)

To be jointly discussed in the tutorial on the 28.4.

Two points are given for active participation

**Q P10:** 3D Fourier transformation

$$\hat{\phi}(\vec{k}) = \int_{-\infty}^{\infty} d^3x e^{-i\vec{k}\vec{x}} \phi(\vec{x}) \quad \phi(\vec{x}) = \int_{-\infty}^{\infty} \frac{d^3k}{(2\pi)^3} e^{i\vec{k}\vec{x}} \hat{\phi}(\vec{k}).$$

As an example calculate the Fourier transformation of

$$\phi(\vec{x}) = \frac{e^{-\mu|\vec{x}|}}{|\vec{x}|}.$$

**Q P11:** Hermite polynomials

The Hermite polynomials  $H_n(\xi)$  arise when describing the Eigenfunctions of the harmonic oscillator. Their representation comes from the following generating function:

$$Z(\xi, \lambda) = e^{-\lambda^2 + 2\lambda\xi} = \sum_n \frac{H_n(\xi)}{n!} \lambda^n.$$

(a) With help of the generating function show that:

$$H'_n(\xi) = 2nH_{n-1}(\xi).$$

(b) Use the generating function to show that  $H_n(\xi)$  satisfies the following differential equation:

$$H''_n(\xi) - 2\xi H'_n(\xi) + 2nH_n(\xi) = 0.$$

(c) Show the representation:

$$H_n(\xi) = (-1)^n e^{\xi^2} \frac{d^n}{d\xi^n} e^{-\xi^2}.$$

(d) Calculate the polynomials  $H_0, \dots, H_3$ .

*Nicht einmal falsch/Not even wrong*

Wenn PAULI an einem Gedanken oder einer Theorie überhaupt keinen Gefallen fand, sagte er: "Nicht einmal falsch."