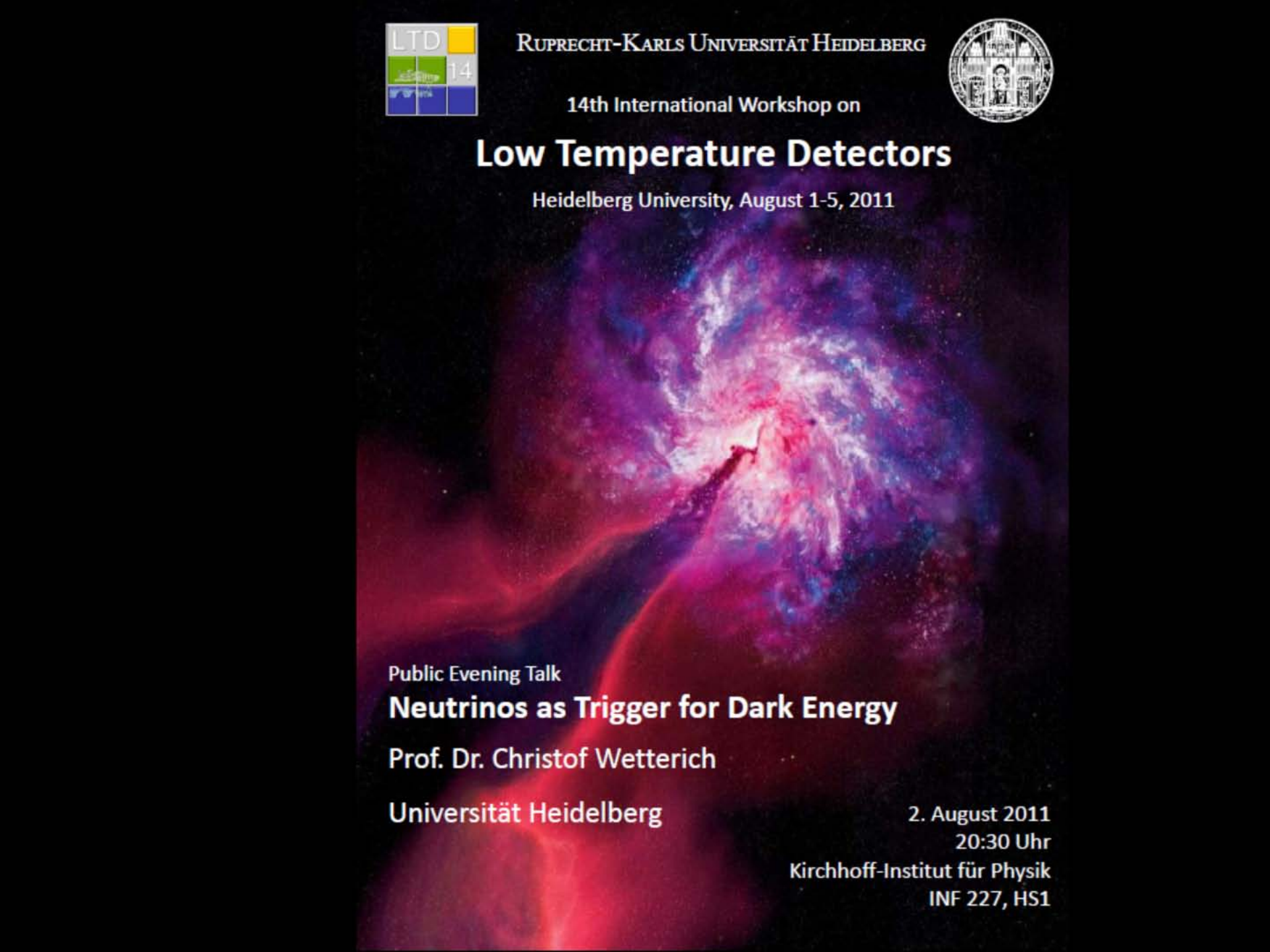

LTD 14
Ruprecht-Karls Universität Heidelberg
14th International Workshop on
Low Temperature Detectors
Heidelberg University, August 1-5, 2011
Public Evening Talk
Neutrinos as Trigger for Dark Energy
Prof. Dr. Christof Wetterich
Universität Heidelberg
2. August 2011
20:30 Uhr
Kirchhoff-Institut für Physik
INF 227, HS1

What is our universe made of ?

Dark Energy dominates the Universe

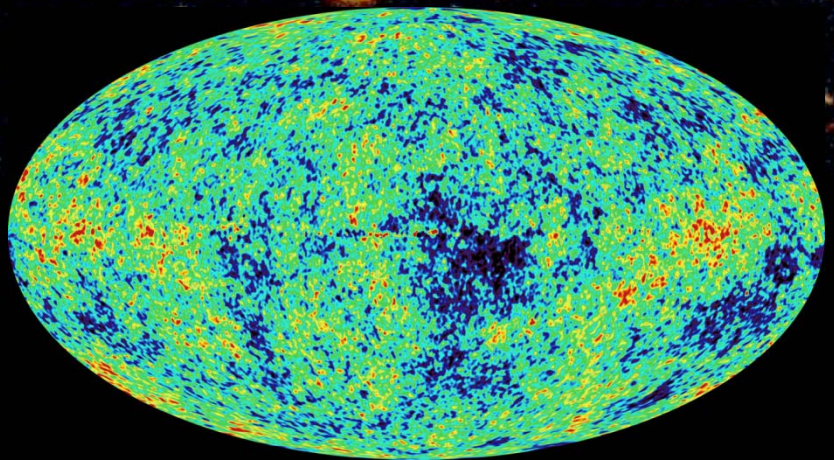
Energy - density in the Universe

=

Matter + Dark Energy

25 % + 75 %

What is Dark Energy ?



Composition of the universe

Atoms : $\Omega_b = 0.045$

Dark Matter : $\Omega_{dm} = 0.225$

Dark Energy : $\Omega_h = 0.73$

critical density

- $\varrho_c = 3\,H^2\,M^2$

  critical energy density of the universe

  (M : reduced Planck-mass , H : Hubble parameter)

- $\Omega_b = \varrho_b / \varrho_c$

  fraction in baryons

  energy density in baryons over critical energy density

$$H = \dot{a}/a$$

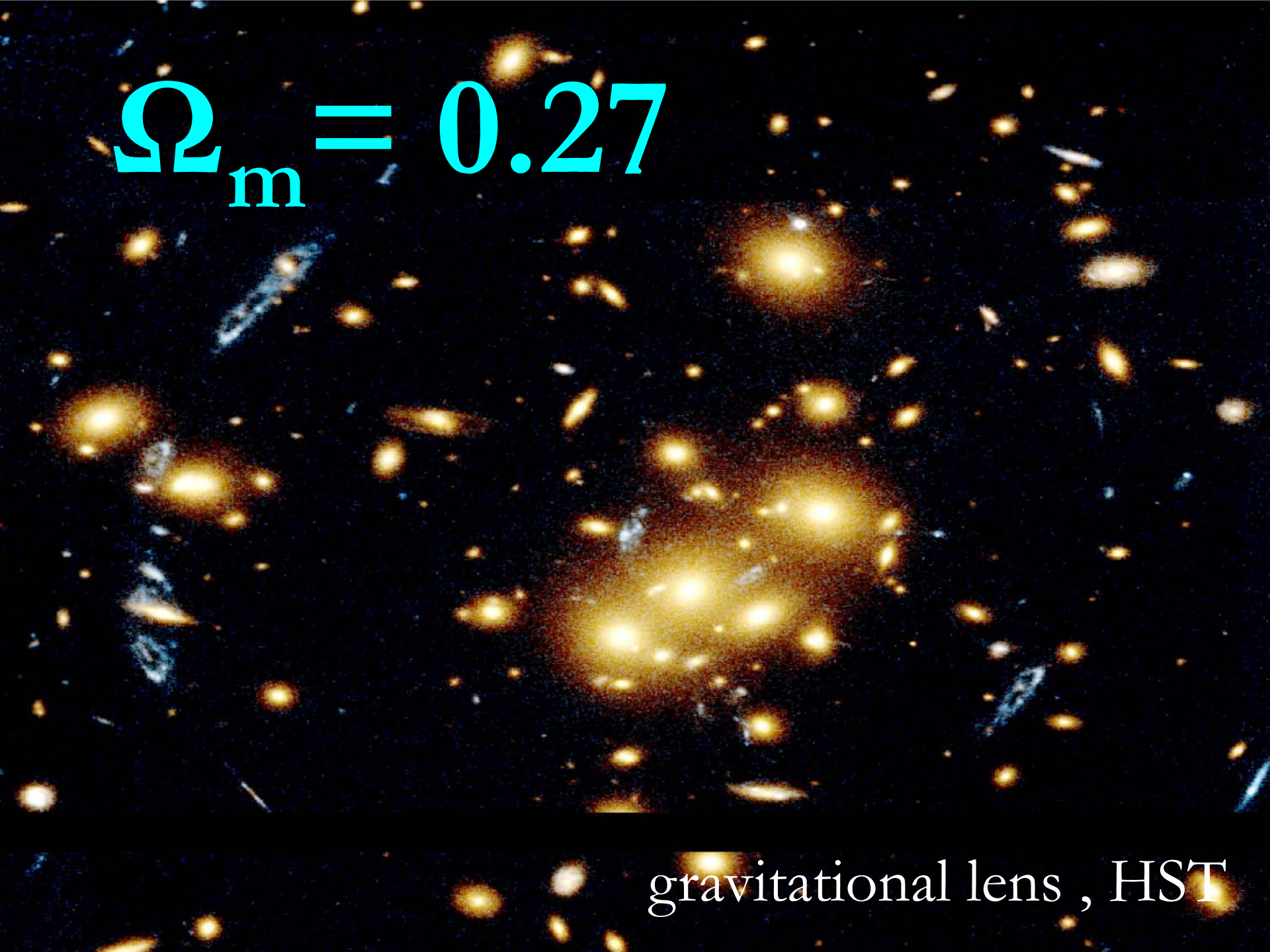
Matter : Everything that clumps

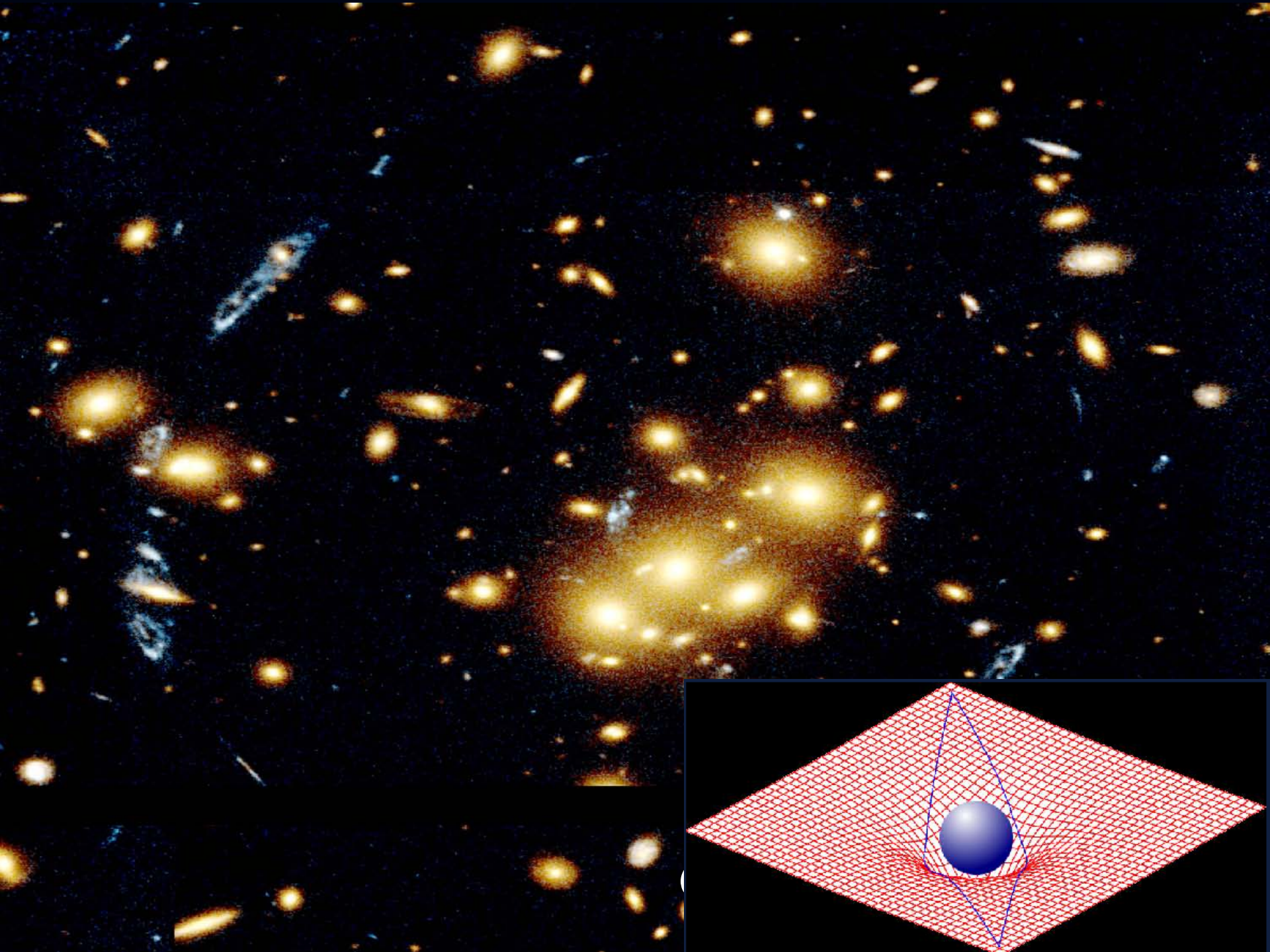
Abell 2255 Cluster
~300 Mpc

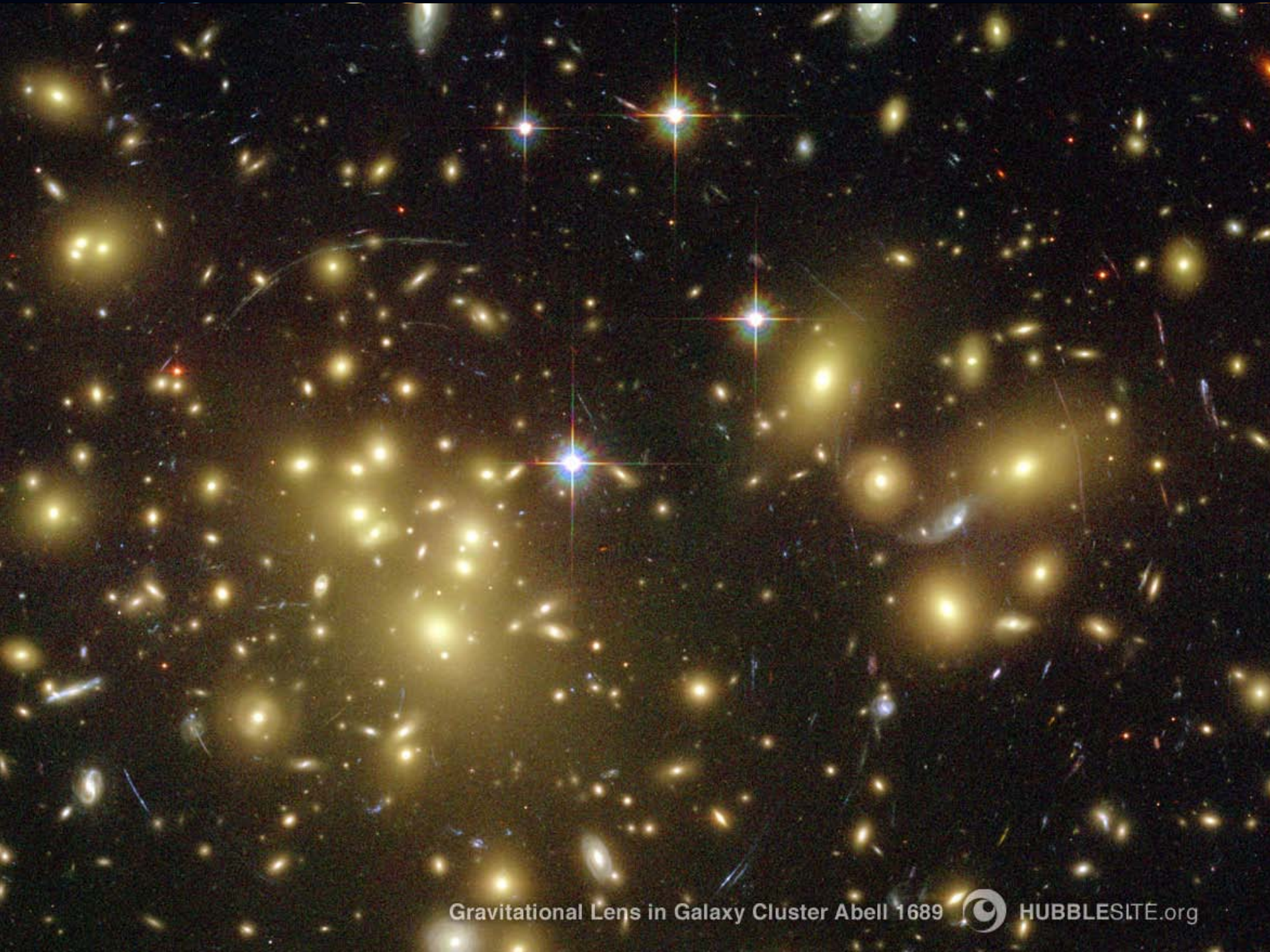
Dark Matter

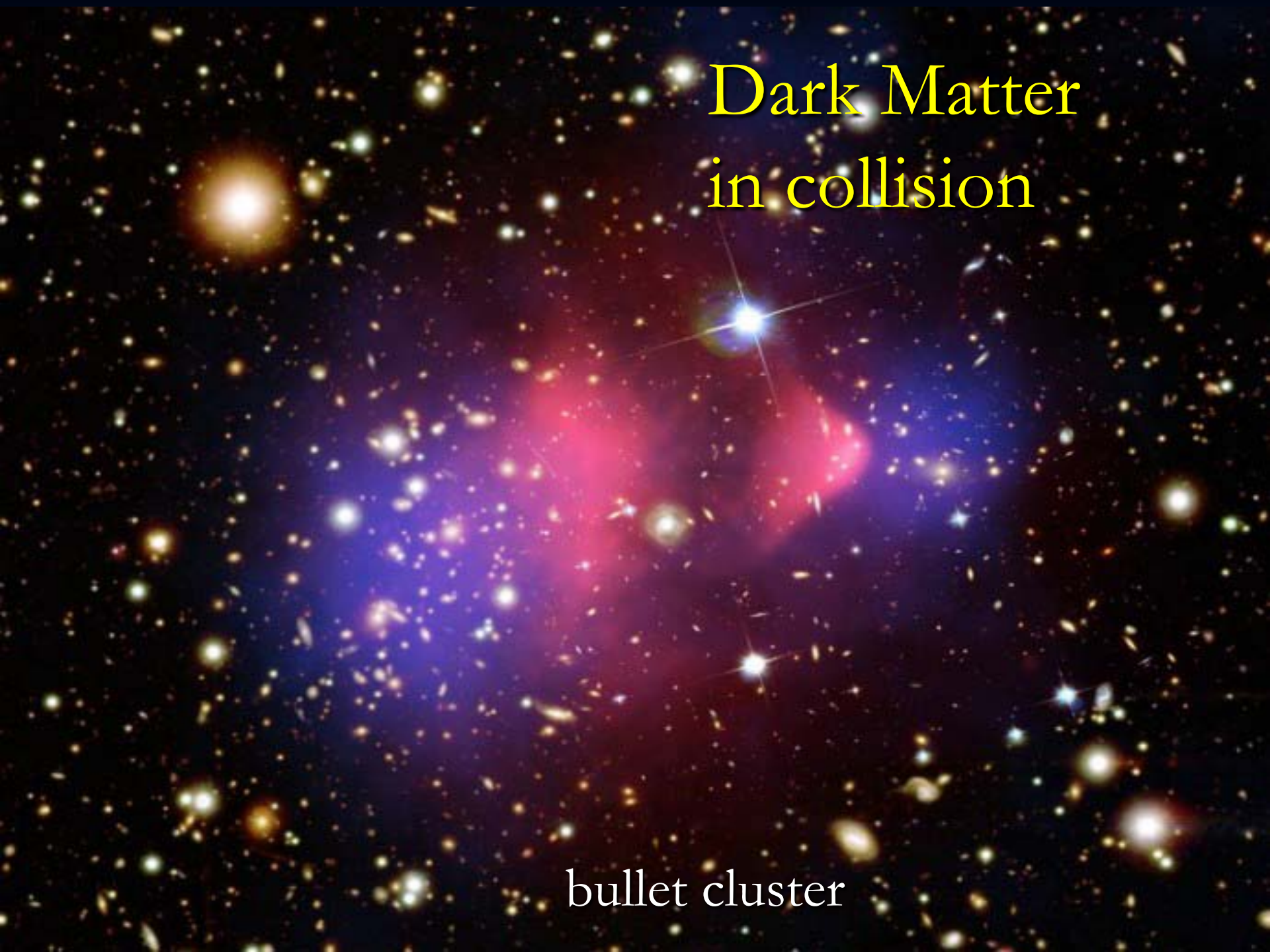
- $\Omega_m = 0.23$ total "matter"
- Most matter is dark !
- So far tested only through gravity
- Every local mass concentration → gravitational potential
- Orbits and velocities of stars and galaxies → measurement of gravitational potential

  and therefore of local matter distribution


$\Omega_m = 0.27$
gravitational lens , HST

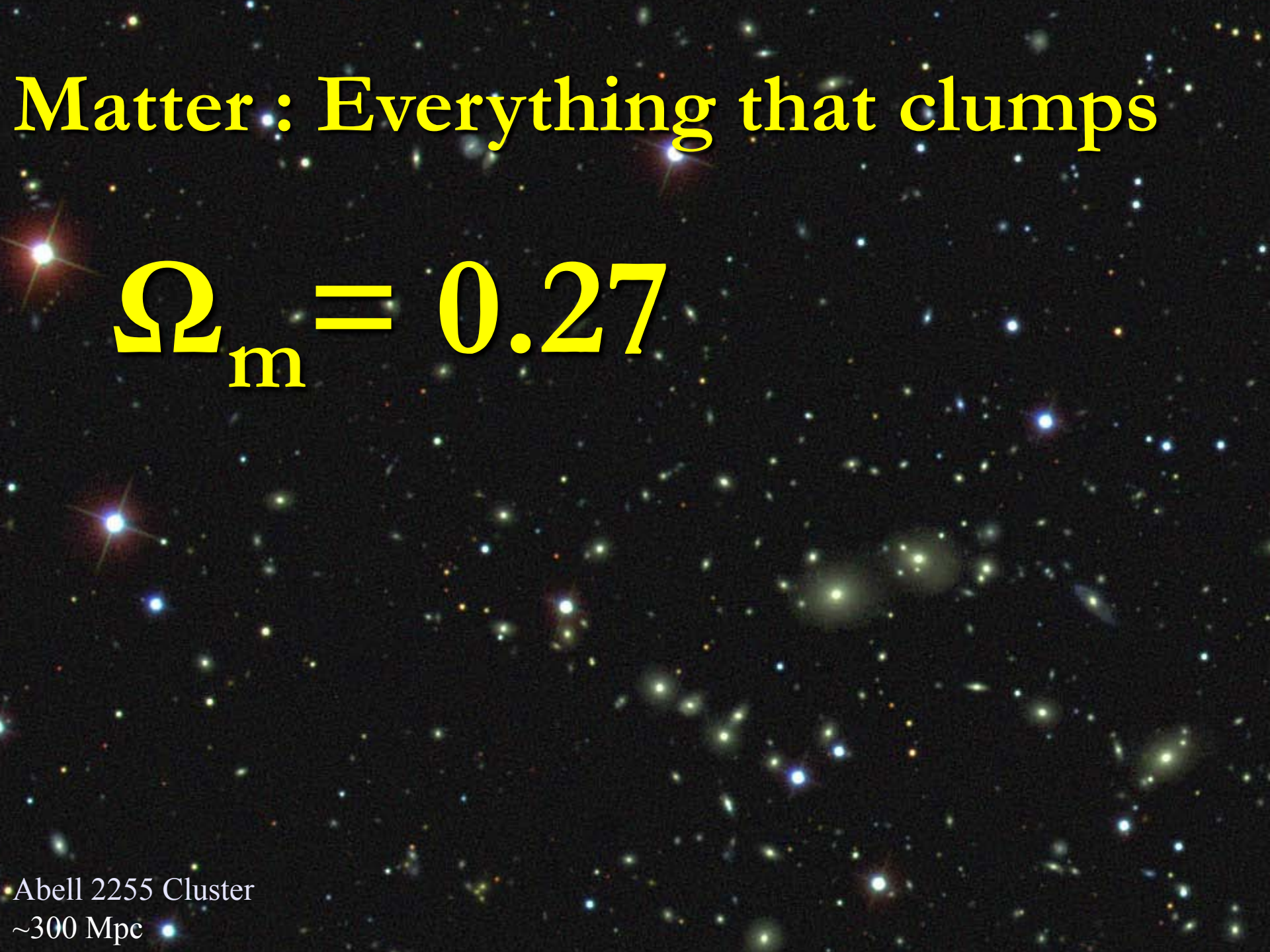



Gravitational Lens in Galaxy Cluster Abell 1689
HUBBLESITE.org


Dark Matter
in collision
bullet cluster

Matter : Everything that clumps

$$\Omega_m = 0.27$$



Abell 2255 Cluster
~300 Mpc


Dark Energy :
Energy density that does not clump
Photons , gravitons : insignificant

spatially flat universe

$$\Omega_{tot} = 1$$

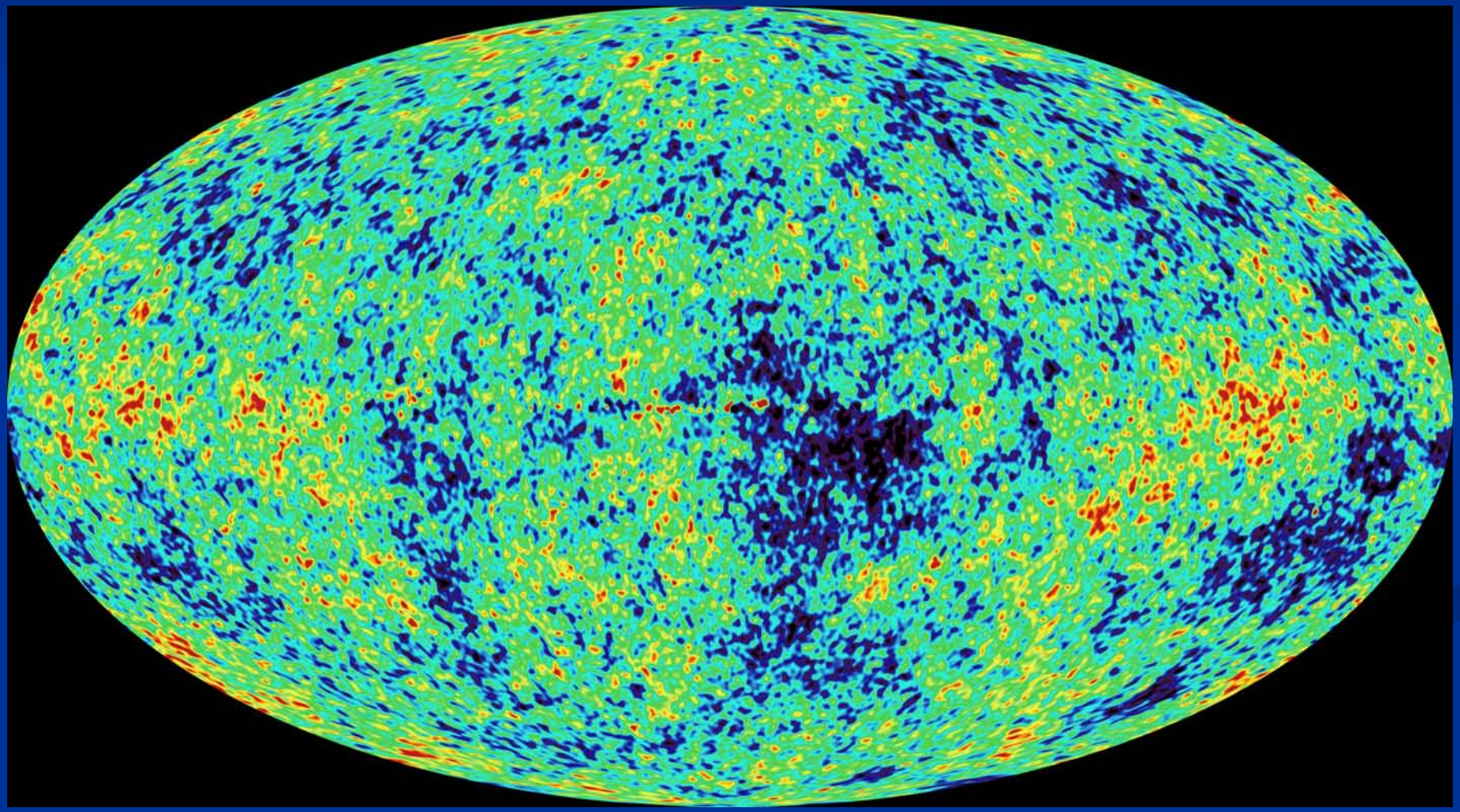
- theory (inflationary universe)

  Ω_{tot} =1.0000……x

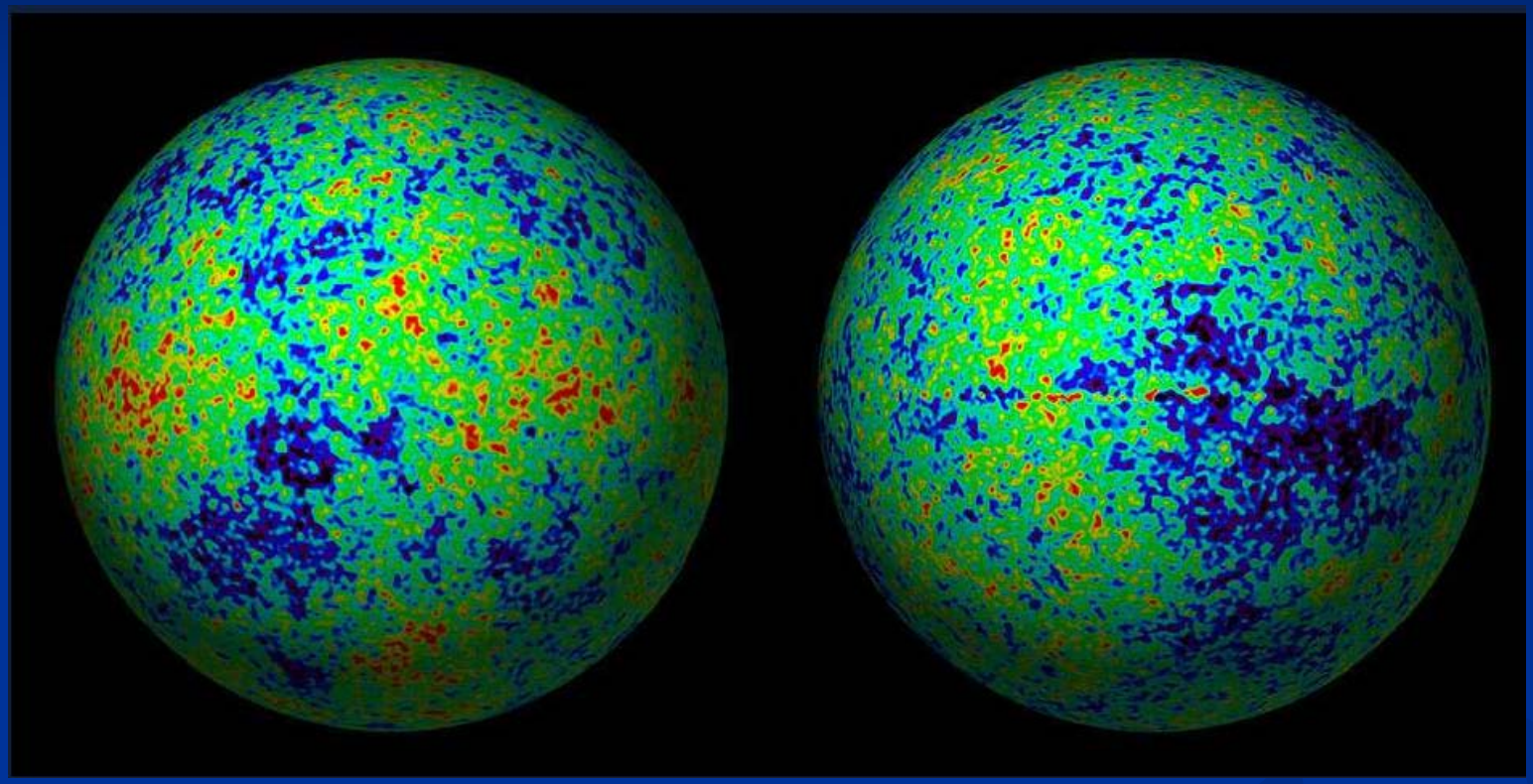
- observation (WMAP)

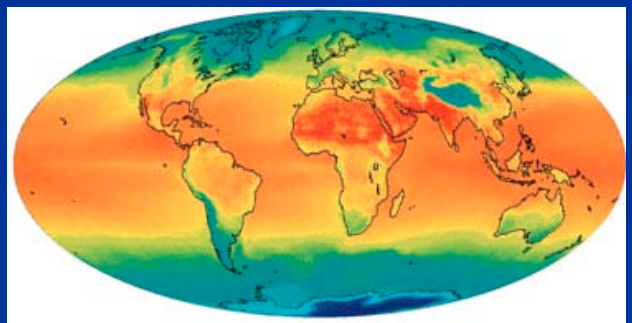
  Ω_{tot} =1.02 (0.02)

Picture of the big bang

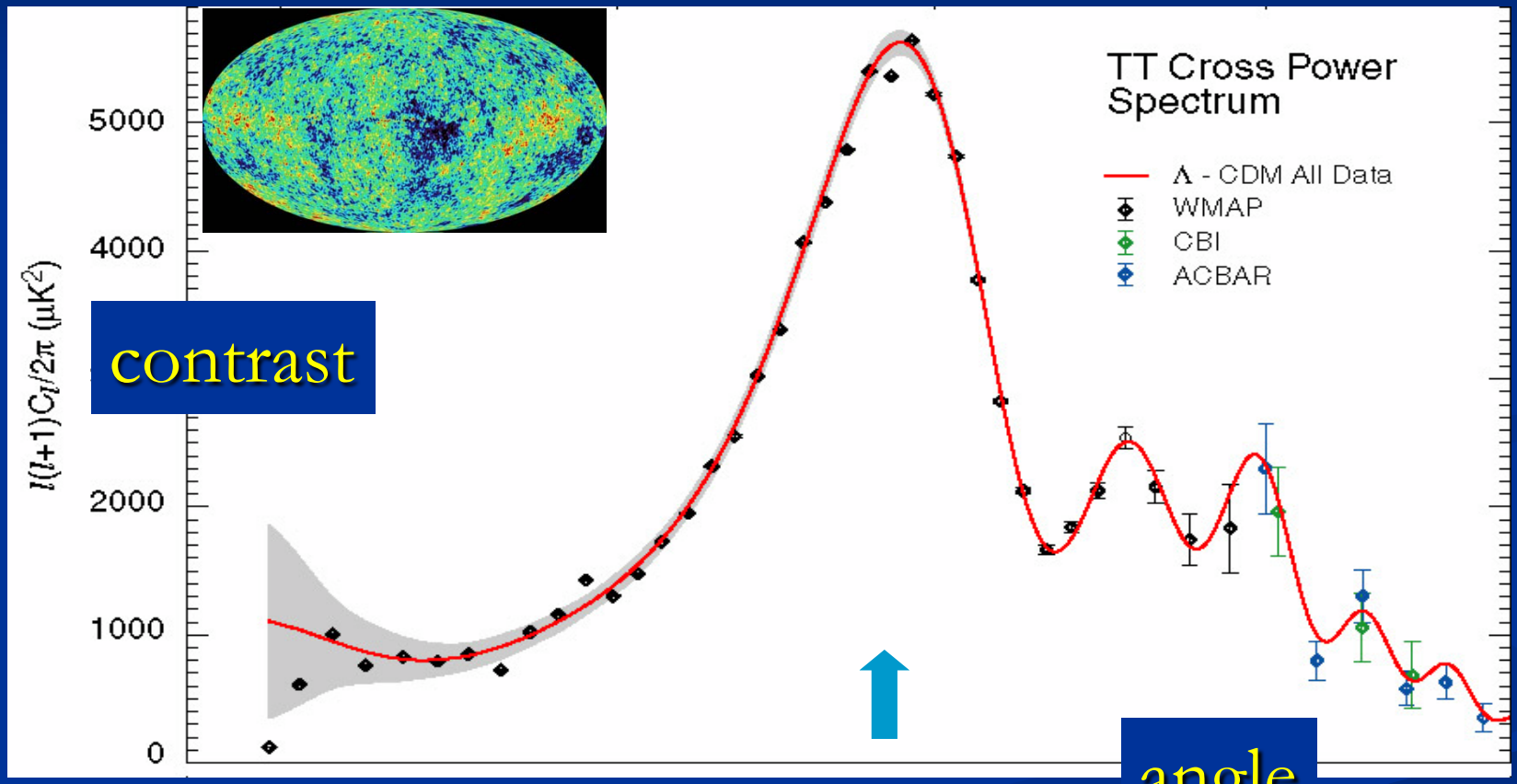


Anisotropy of background radiation : size of hot and cold spots

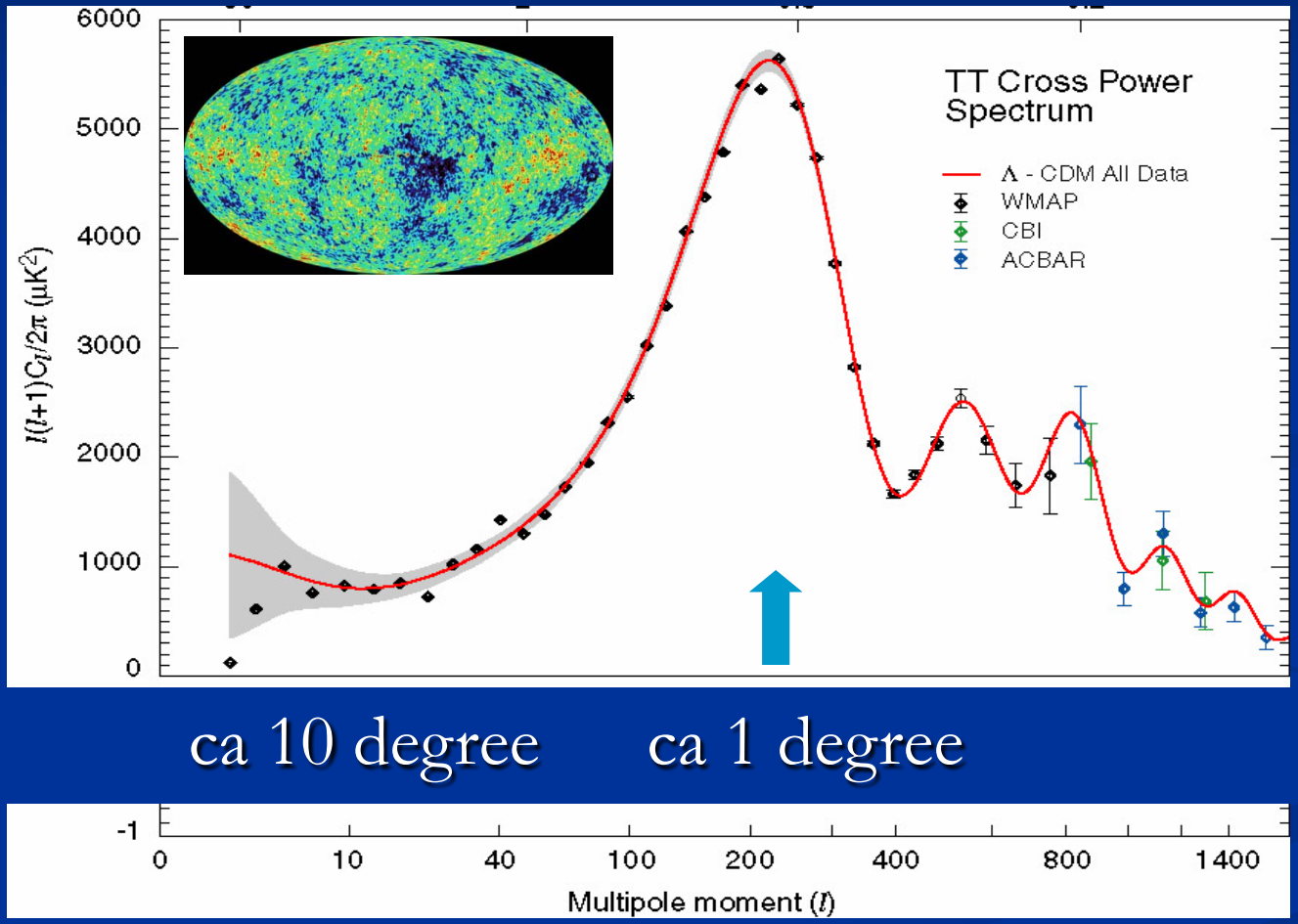




Size of temperature fluctuations in dependence on size of anisotropies (angle)

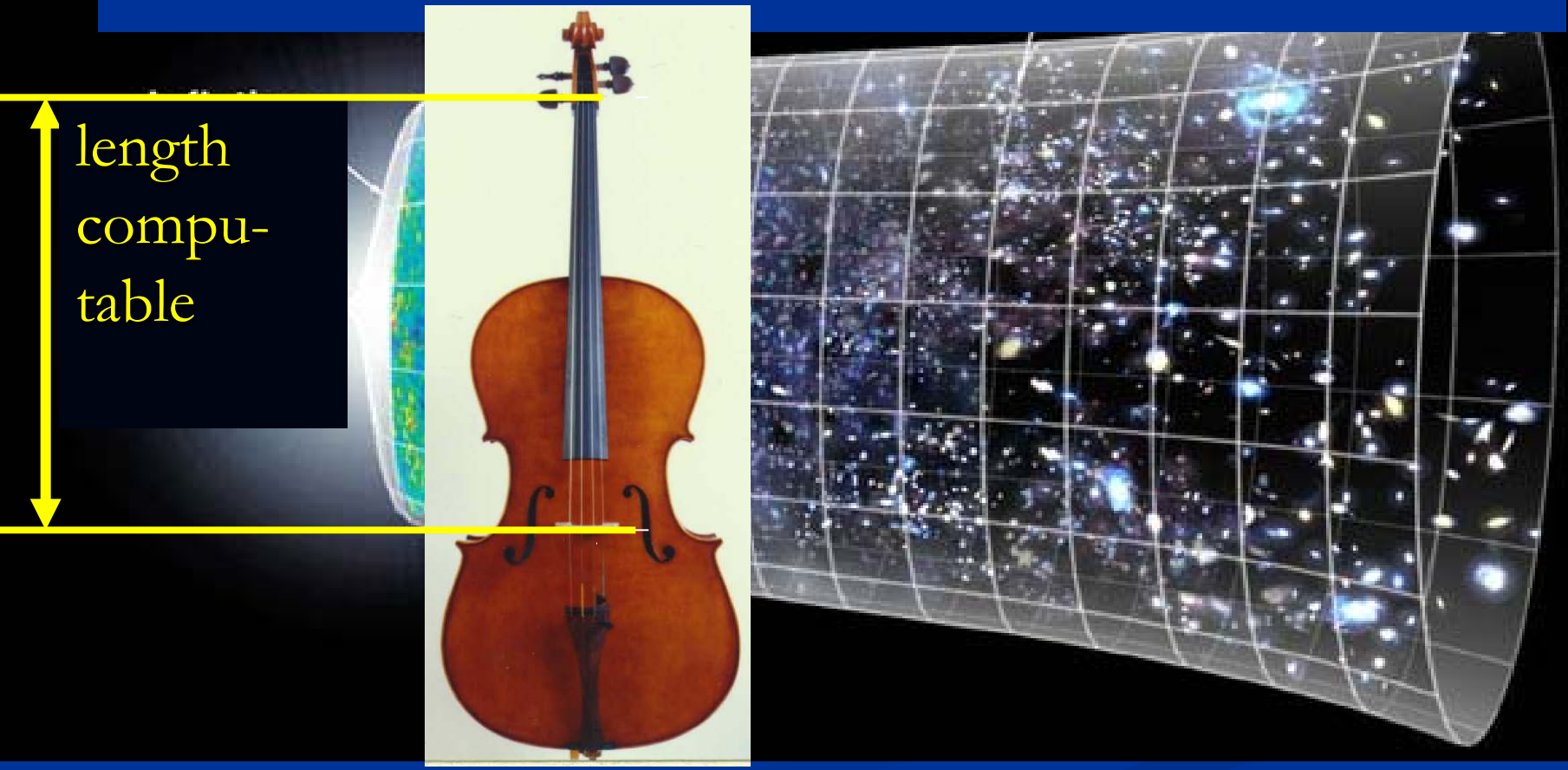


Acoustic oscillations in plasma

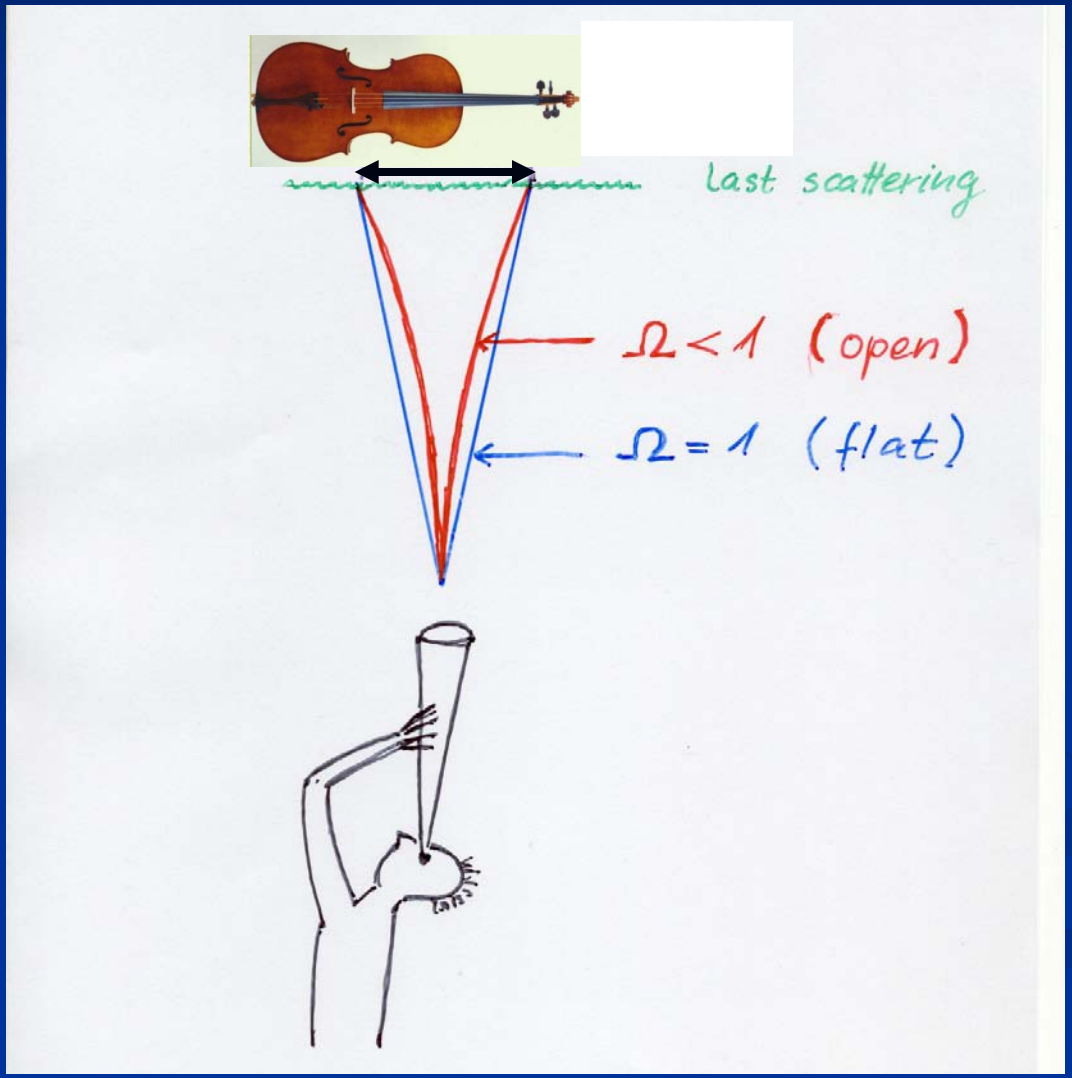


ca 10 degree ca 1 degree

acoustic waves in the early Universe

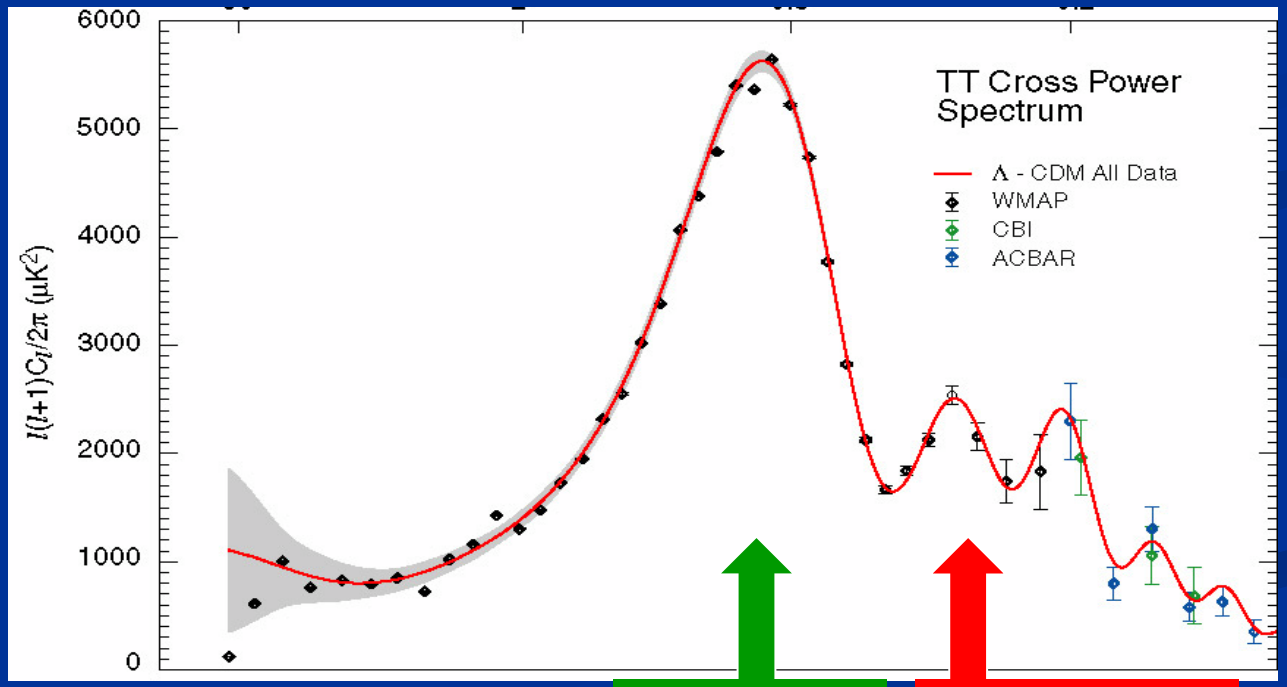


$\Omega_{tot}=1$

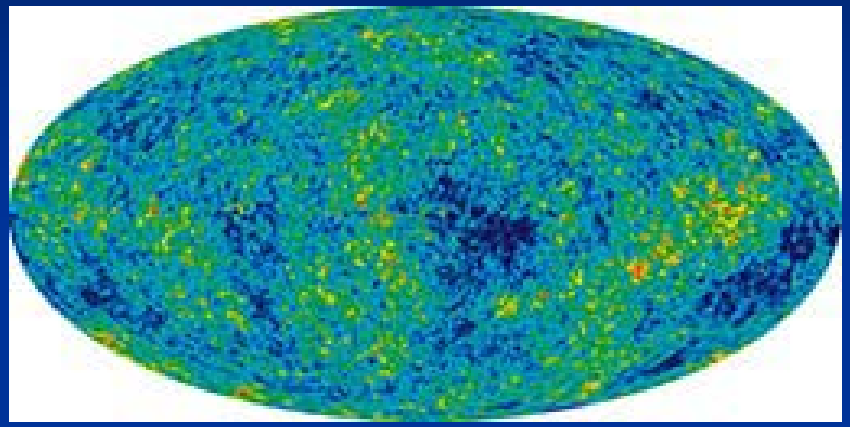


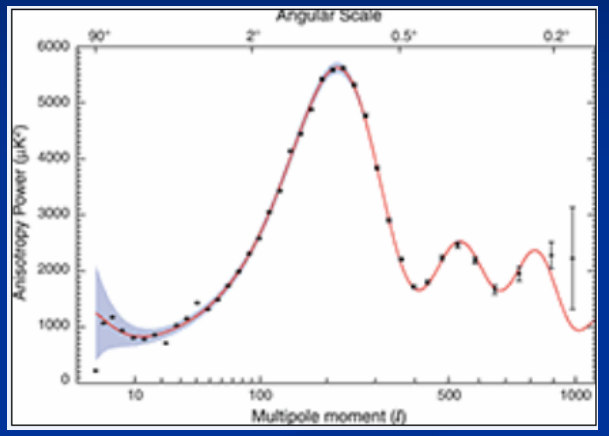
spatially flat Universe

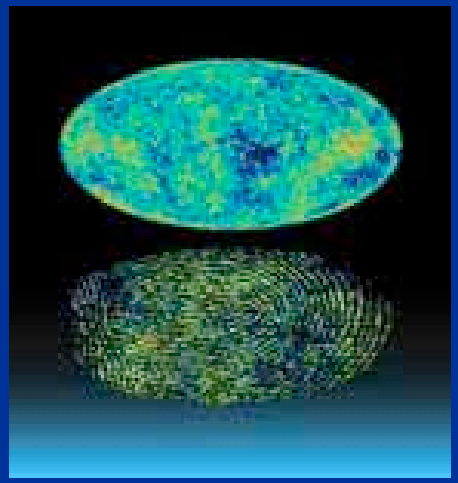
$$\Omega_{tot} = 1$$



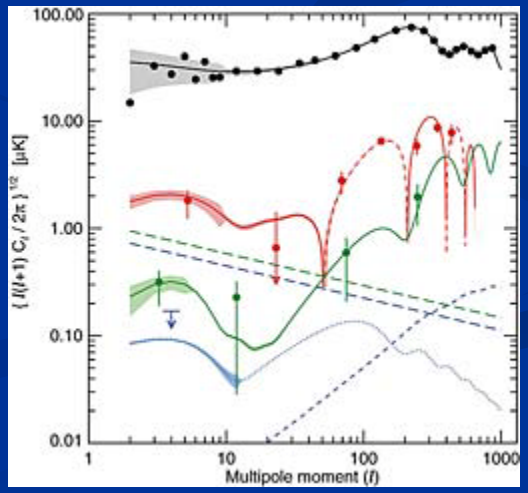
WMAP 2006

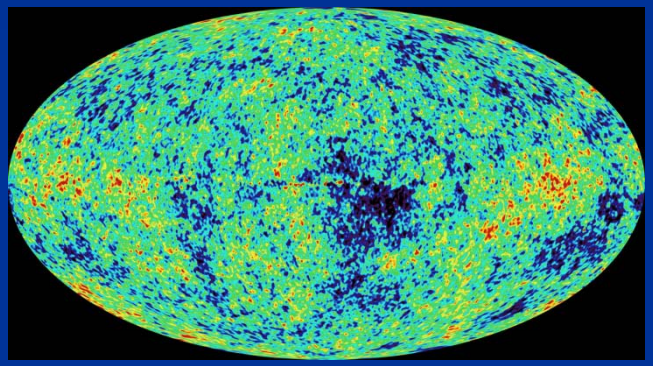


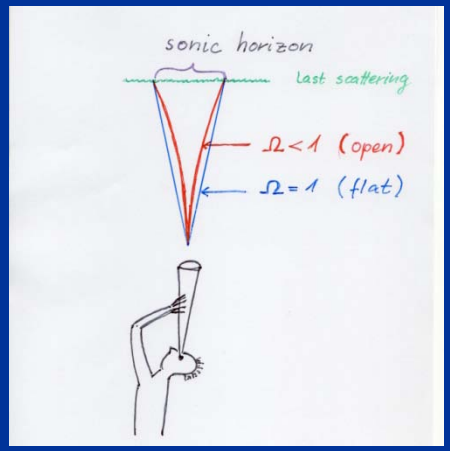




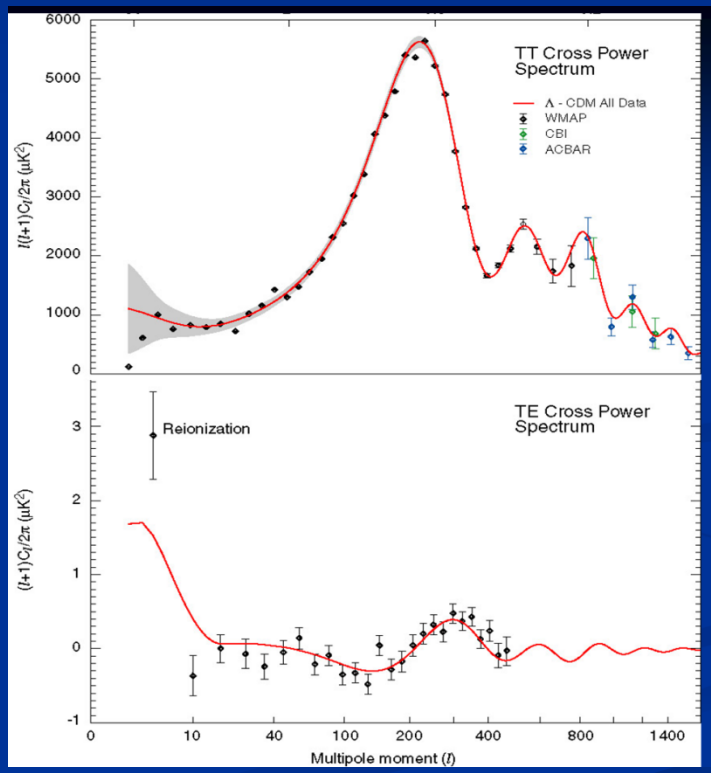
Polarization







$\Omega_{tot}=1$



mean values

$\Omega_{tot}=1.02$

$\Omega_{m}=0.27$

$\Omega_{b}=0.045$

$\Omega_{dm}=0.225$

Dark Energy

$\Omega_m + X = 1$

Ω_m : 25%

Ω_h : 75% Dark Energy

h : homogenous , often Ω_Λ instead of Ω_h

Space between clumps is not empty :

Dark Energy !

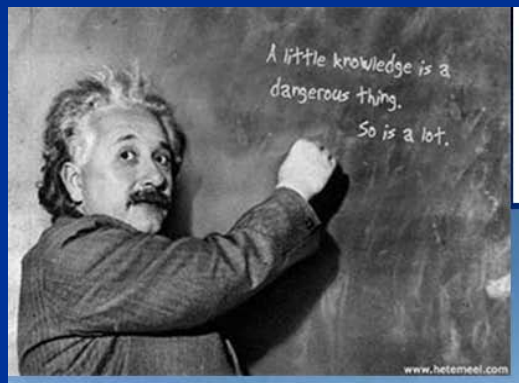
Dark Energy : Homogeneously distributed

Dark Energy density is the same at every point of space

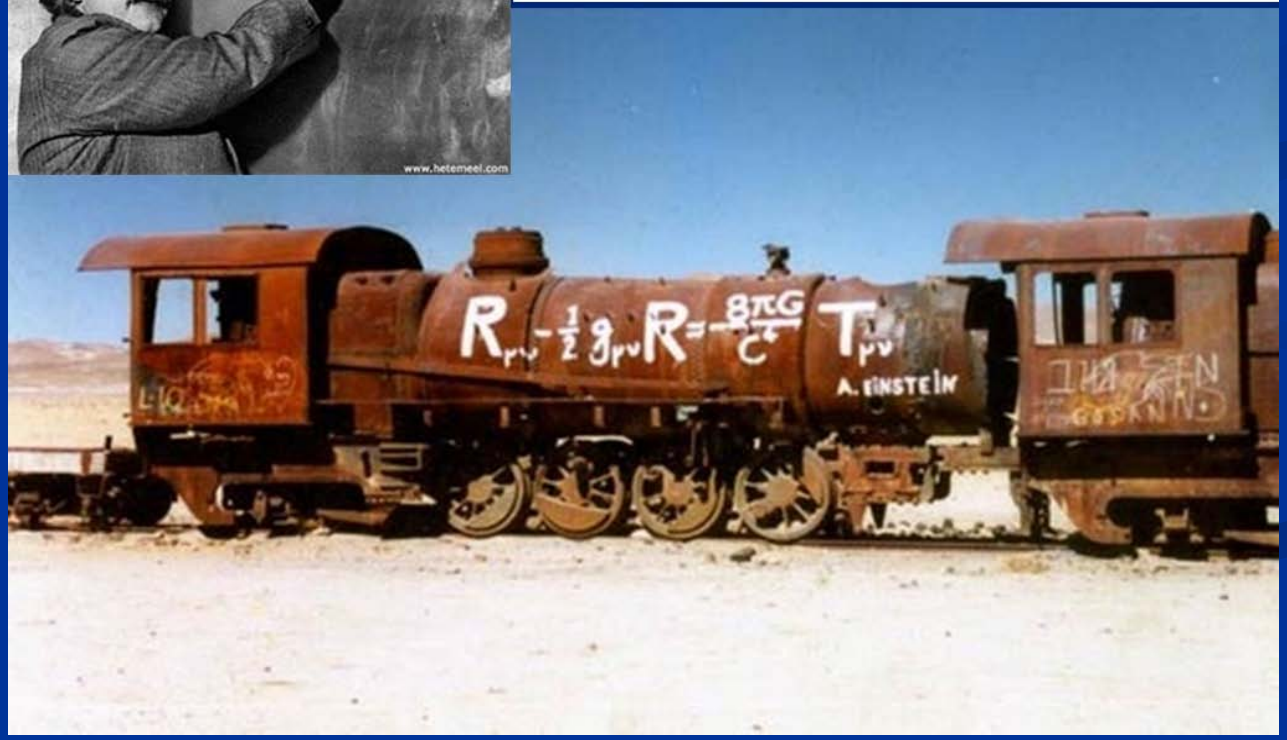
“ homogeneous “

No force in absence of matter – “ In what direction should it draw ? “

Einstein's equations : almost static Dark Energy predicts accelerated expansion of Universe



$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

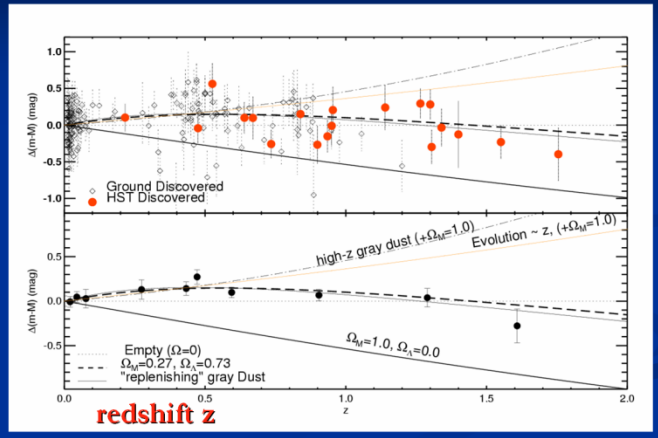


Predictions for dark energy cosmologies

The expansion of the Universe

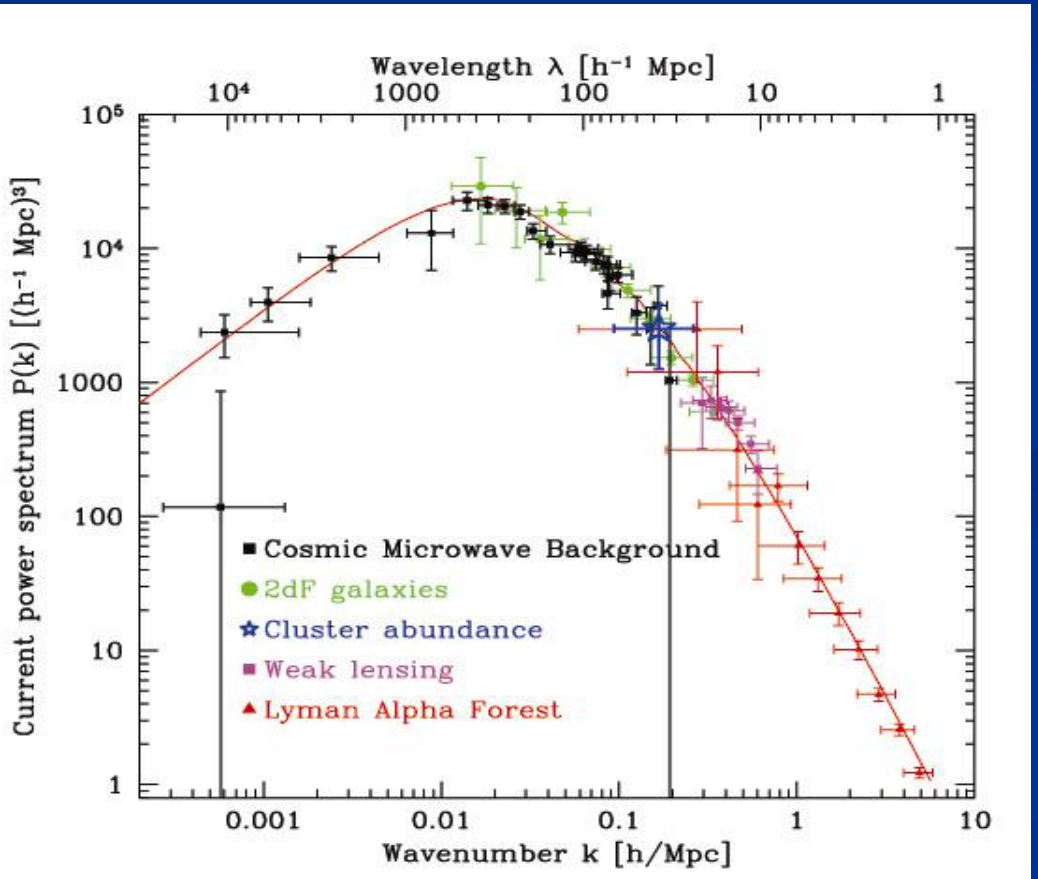
accelerates today !

Supernovae 1a Hubble diagram



Riess et al. 2004

Structure formation :
One primordial fluctuation spectrum



Waerbeke

CMB agrees with

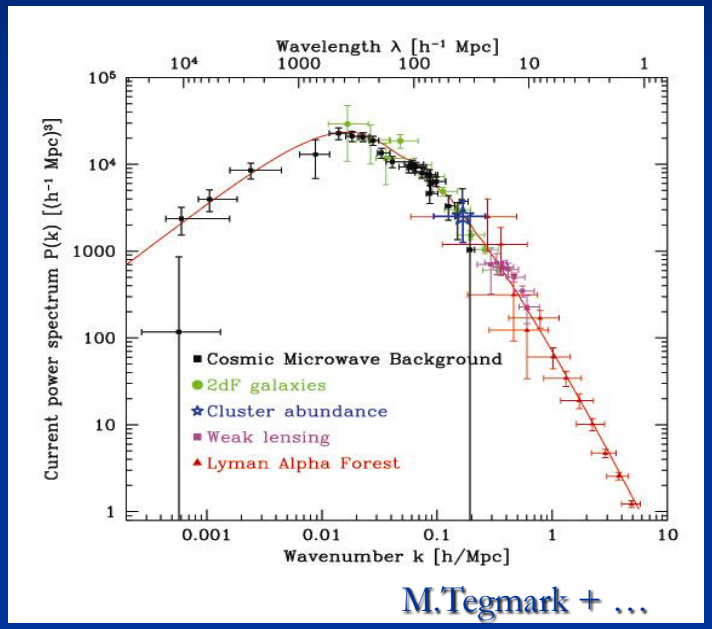
Galaxy distribution

Lyman – α

and

Gravitational Lensing !

Power spectrum

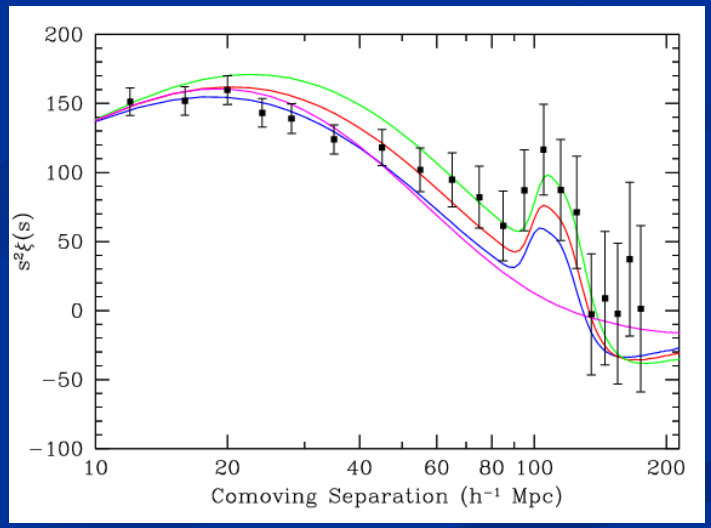


M.Tegmark + …

Structure formation :
One primordial
fluctuation- spectrum

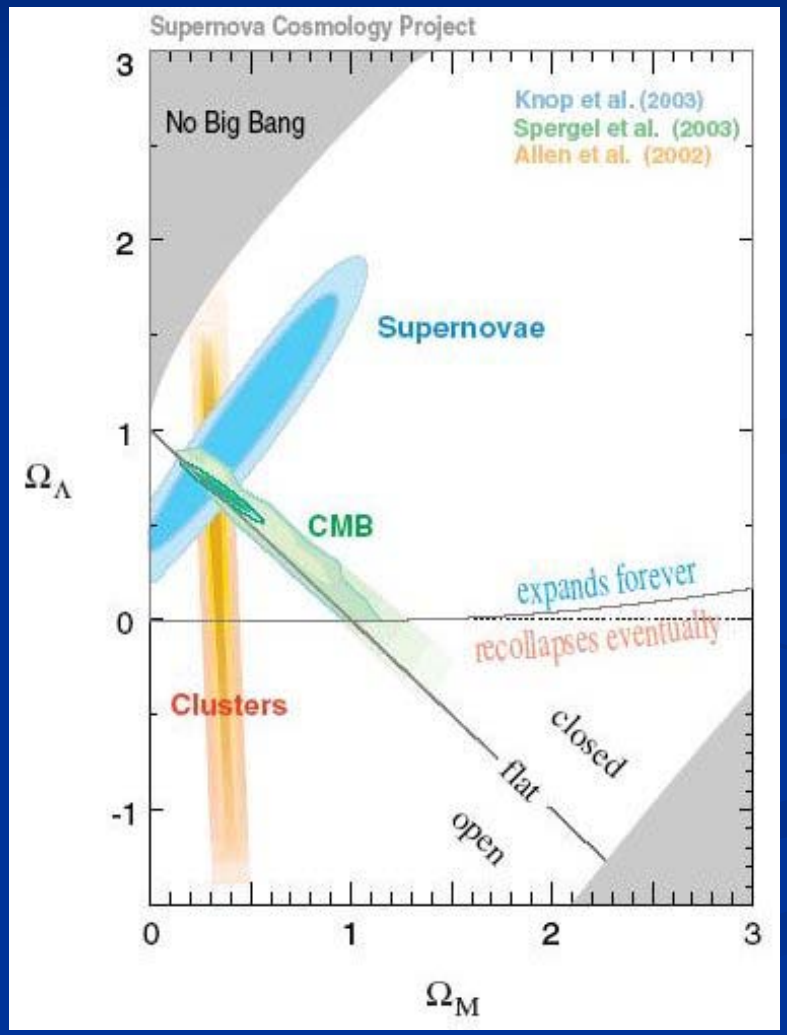
Baryon - Peak

galaxy –
correlation –
function



SDSS

Dunkle Energie :
die Beobachtungen passen zusammen !

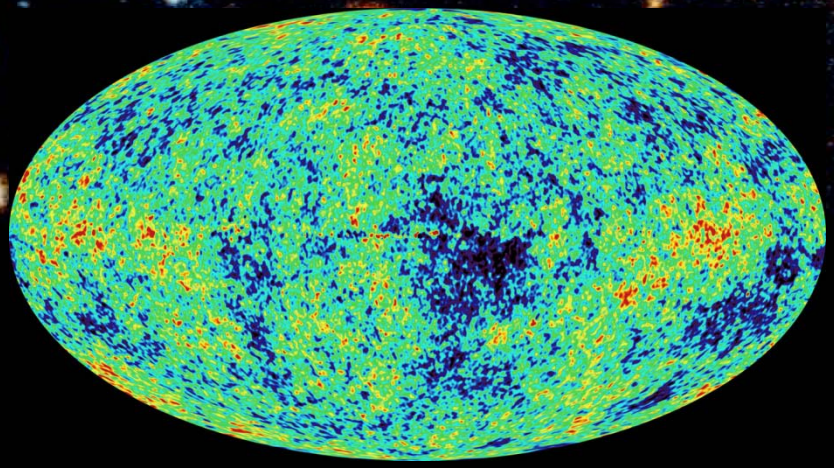


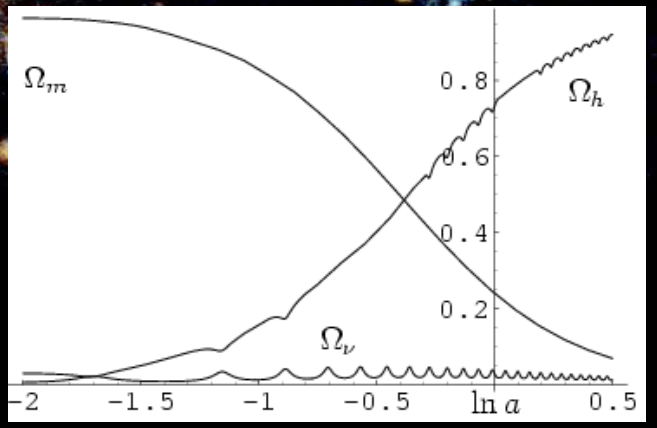
consistent cosmological model !

Composition of the Universe

$\Omega_b = 0.045$	visible	clumping
$\Omega_{dm} = 0.2$	invisible	clumping
$\Omega_h = 0.75$	invisible	homogeneous

Dark Energy – a cosmic mystery





What is Dark Energy ?

Cosmological Constant

or

Quintessence ?

Cosmological Constant
- Einstein -

- Constant λ compatible with all symmetries
- No time variation in contribution to energy density

- Why so small ? $\lambda/M^4 = 10^{-120}$

- Why important just today ?

Cosmological mass scales

- Energy density

  $\varrho \sim (2.4\times10^{-3}\ \mathrm{eV})^{-4}$

- Reduced Planck mass

  $M=2.44\times10^{27}\ \mathrm{eV}$

- Newton's constant

  $G_N=(8\pi M^2)$

Only ratios of mass scales are observable !

homogeneous dark energy: $\rho_h/M^4 = 6.5\ 10^{-121}$

matter: $\rho_m/M^4 = 3.5\ 10^{-121}$

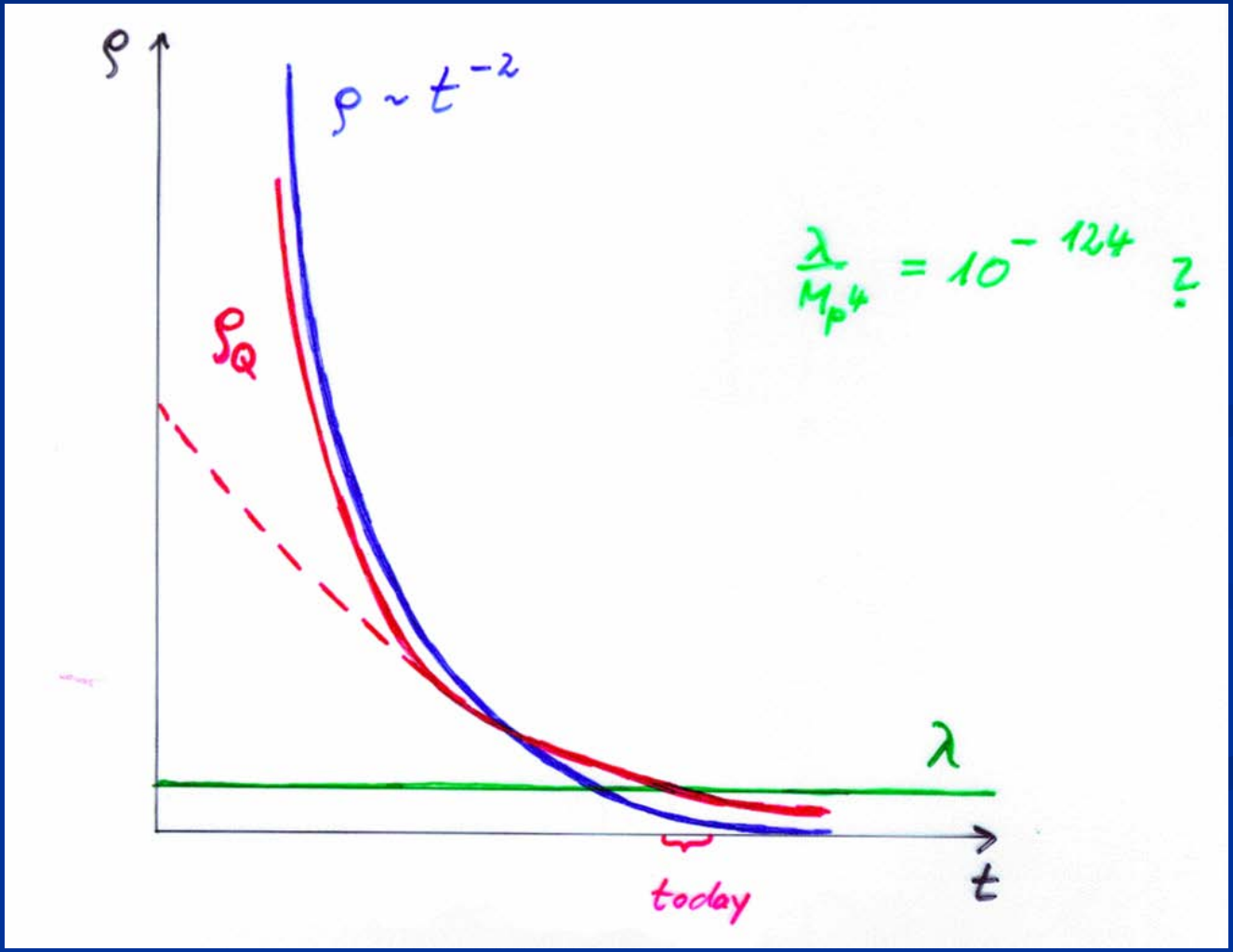
Time evolution

- $\varrho_m/M^4 \sim a^{-3} \sim$ t^{-2} matter dominated universe
  $t^{-3/2}$ radiation dominated universe
- $\varrho_r/M^4 \sim a^{-4} \sim t^{-2}$ radiation dominated universe

Huge age ⇨ small ratio

Same explanation for small dark energy?

Cosm. Const.	Quintessence
static	dynamical



Quintessence

Dynamical dark energy , generated by scalar field (cosmon)

C.Wetterich,Nucl.Phys.B302(1988)668, 24.9.87
P.J.E.Peebles,B.Ratra,ApJ.Lett.325(1988)L17, 20.10.87

Prediction :

homogeneous dark energy influences recent cosmology

- of same order as dark matter -

Original models do not fit the present observations …. modifications

Quintessence

Cosmon – Field $\varphi(x,y,z,t)$

similar to electric field , but no direction (scalar field)

Homogeneous und isotropic Universe : $\varphi(x,y,z,t)=\varphi(t)$

Potential und kinetic energy of the cosmon -field contribute to a dynamical energy density of the Universe !

Cosmon

- *Scalar field changes its value even in the* ***present*** *cosmological epoch*
- *Potential und kinetic energy of cosmon contribute to the energy density of the Universe*
- *Time - variable dark energy :*

  $\varrho_h(t)$ *decreases with time !*

Evolution of cosmon field

Field equations $\ddot{\phi} + 3H\dot{\phi} = -dV/d\phi$

$3M^2H^2 = V + \frac{1}{2}\dot{\phi}^2 + \rho$

Potential V(φ) determines details of the model

$$V(\varphi) = M^4 \exp(- \alpha\varphi/M)$$

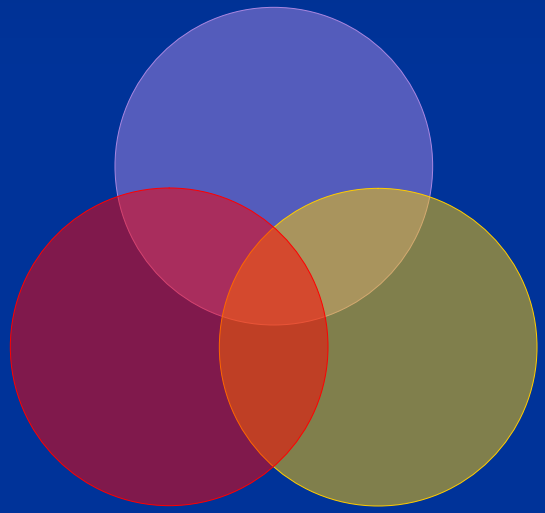
for increasing φ the potential decreases towards zero !

Cosmon

- *Tiny mass*
- $m_c \sim H$ *(depends on time !)*
- *New long - range interaction*

“Fundamental” Interactions

Strong, electromagnetic, weak interactions



gravitation cosmodynamics

On astronomical length scales:

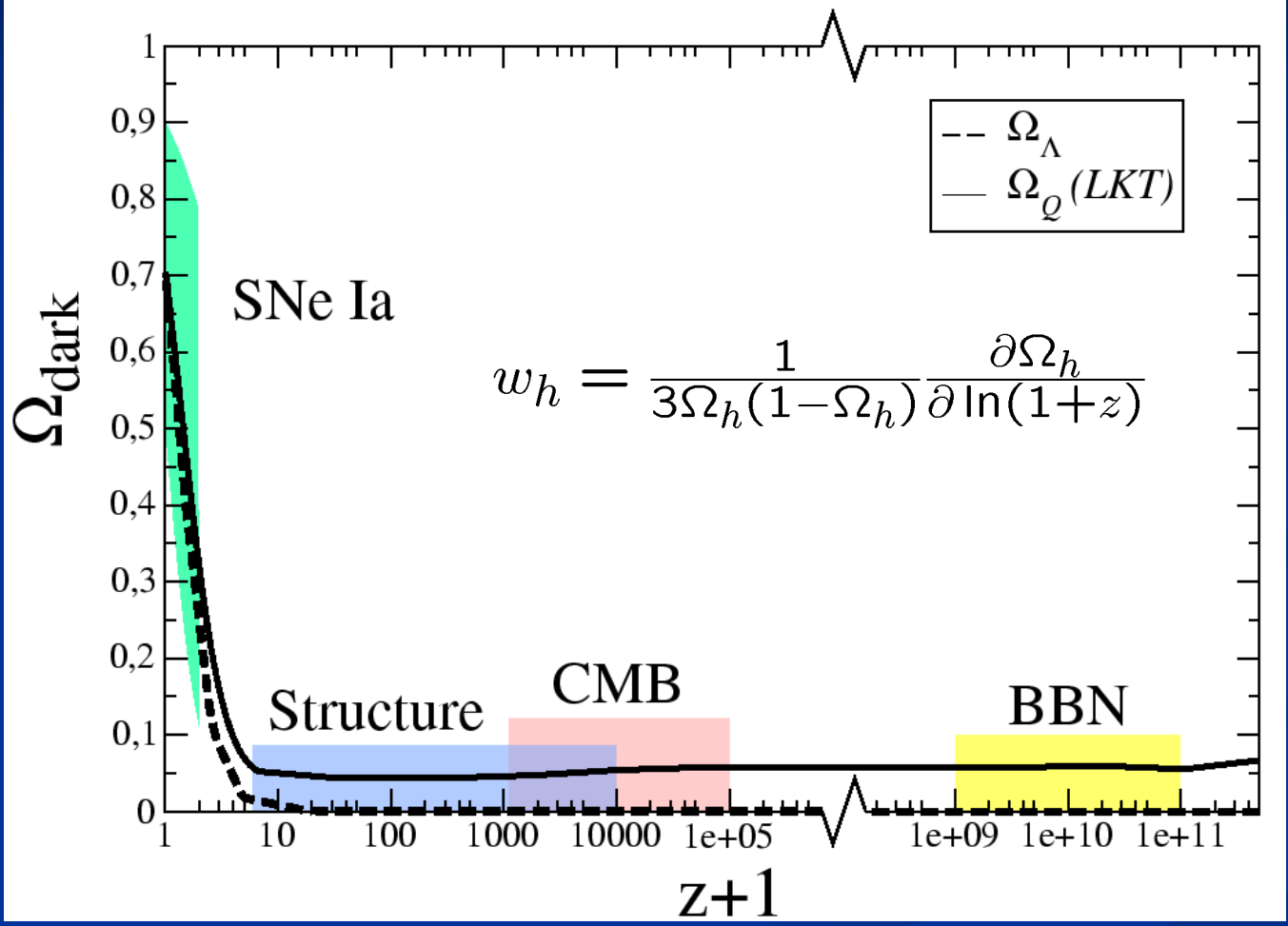
graviton

+

cosmon

observation will decide !

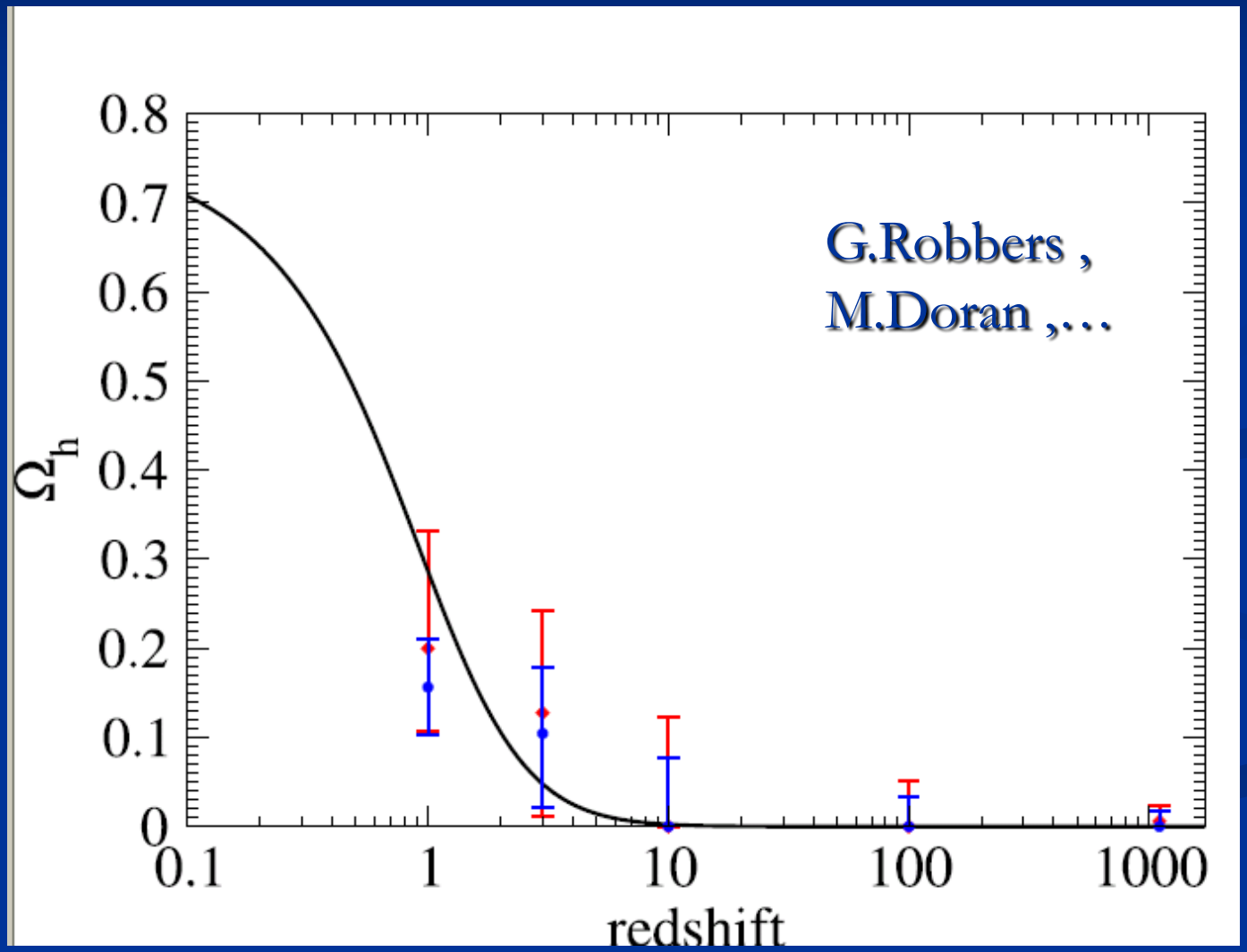
Time dependence of dark energy



cosmological constant : $\Omega_h \sim t^2 \sim (1+z)^{-3}$

M.Doran,…

Observational bounds on Ω_h

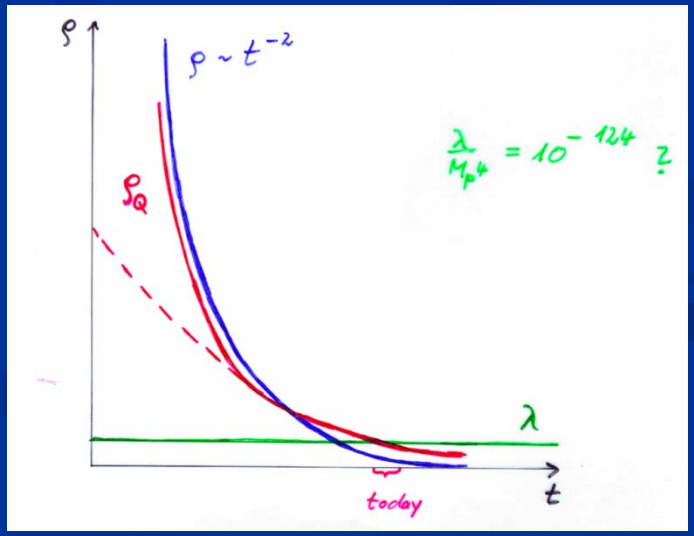


exponential potential ➡
constant fraction in dark energy

$$\Omega_h = 3/\alpha^2$$

$$V(\varphi) = M^4 \exp(- \alpha\varphi/M)$$

can explain order
of magnitude
of dark energy !



Cosmic Attractors

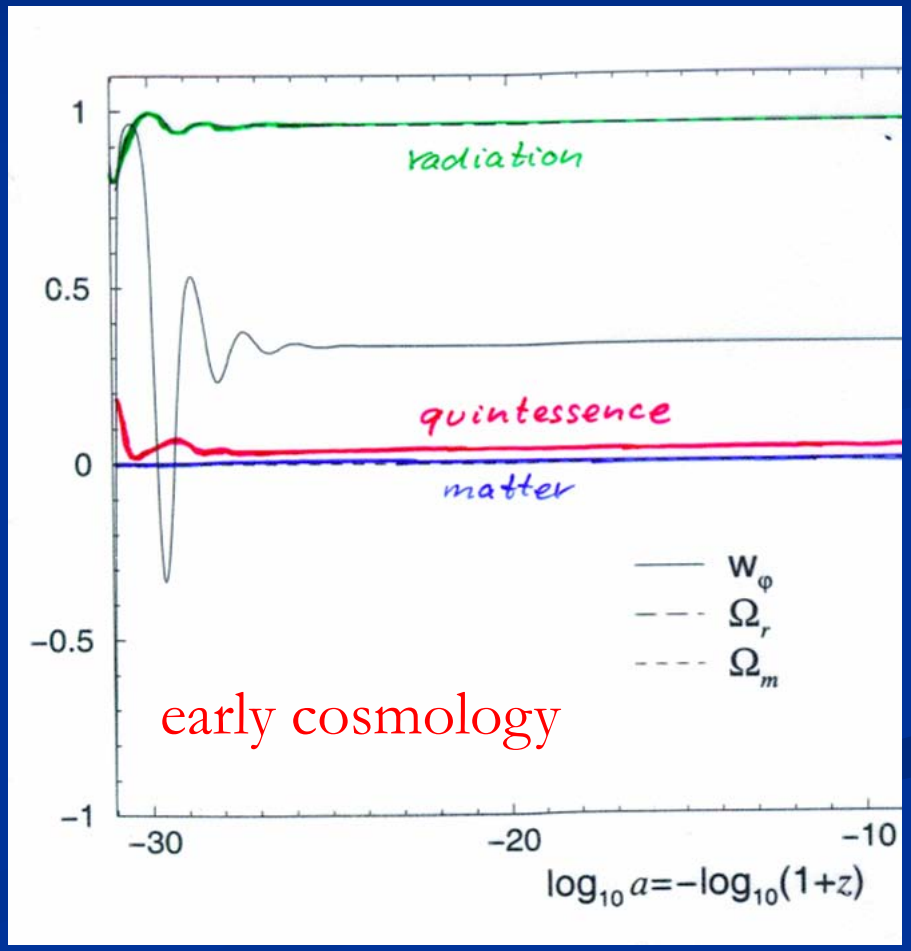
Solutions independent of initial conditions

typically $V \sim t^{-2}$

$\varphi \sim \ln(t)$

$\Omega_h \sim$ const.

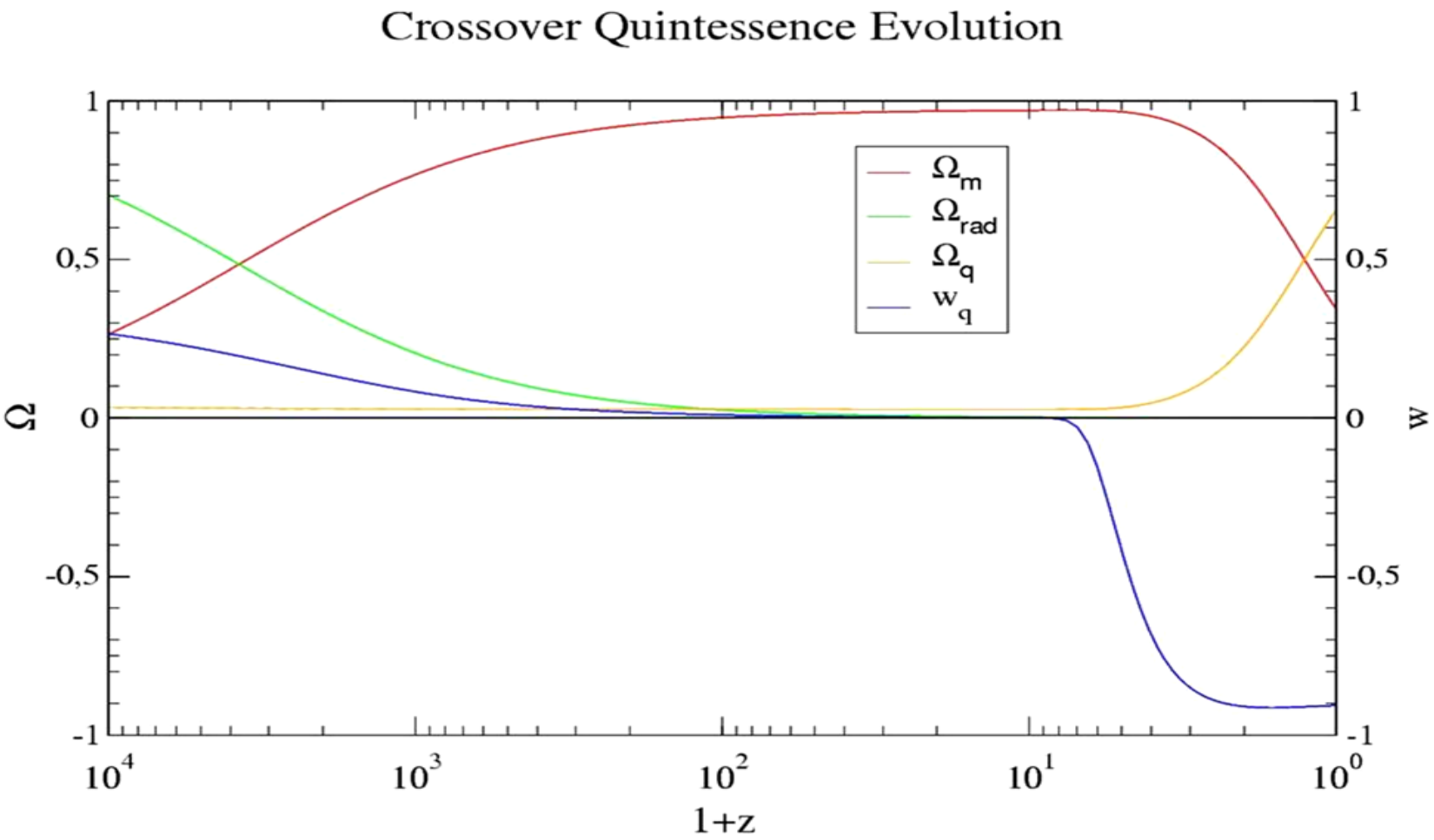
details depend on $V(\varphi)$ or kinetic term



realistic quintessence

fraction in dark energy has to increase in "recent time" !

Quintessence becomes important "today"



Key questions for quintessence

- Why does cosmon potential vanish for infinite time ? $V(\varphi) = M^4 \exp(- \alpha\varphi/M)$

- Why is time variation of fundamental couplings small ? (e.g. fine structure constant , electron-proton mass ratio)

- Why does Dark Energy dominate only in recent cosmology (Why now ? – problem)

Key questions for quintessence

- Why does cosmon potential vanish for infinite time ?
  $V(\varphi) = M^4 \exp(- \alpha\varphi/M)$

  Dilatation symmetry in higher dimensions – not today

- Why is time variation of fundamental couplings small ?
  (e.g. fine structure constant , electron-proton mass ratio)

  Fixed point behavior – not today

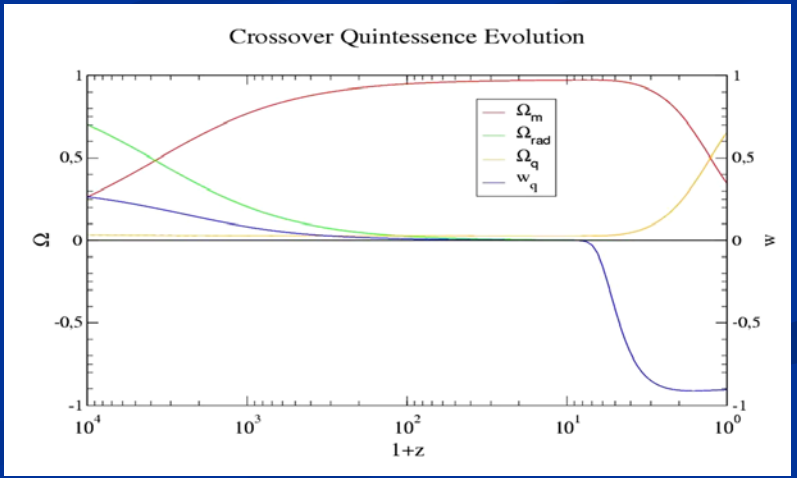
- Why does Dark Energy dominate only in recent cosmology
  (Why now ? – problem)

  Growing neutrino mass - today

coincidence problem

What is responsible for increase of Ω_h for $z < 6$?

Why now ?



Neutrinos in cosmology

only small fraction of energy density

only sub-leading role ?

Cosmon – neutrino coupling

- Can be somewhat stronger than gravitational coupling
- Neutrino mass depends on value of cosmon field

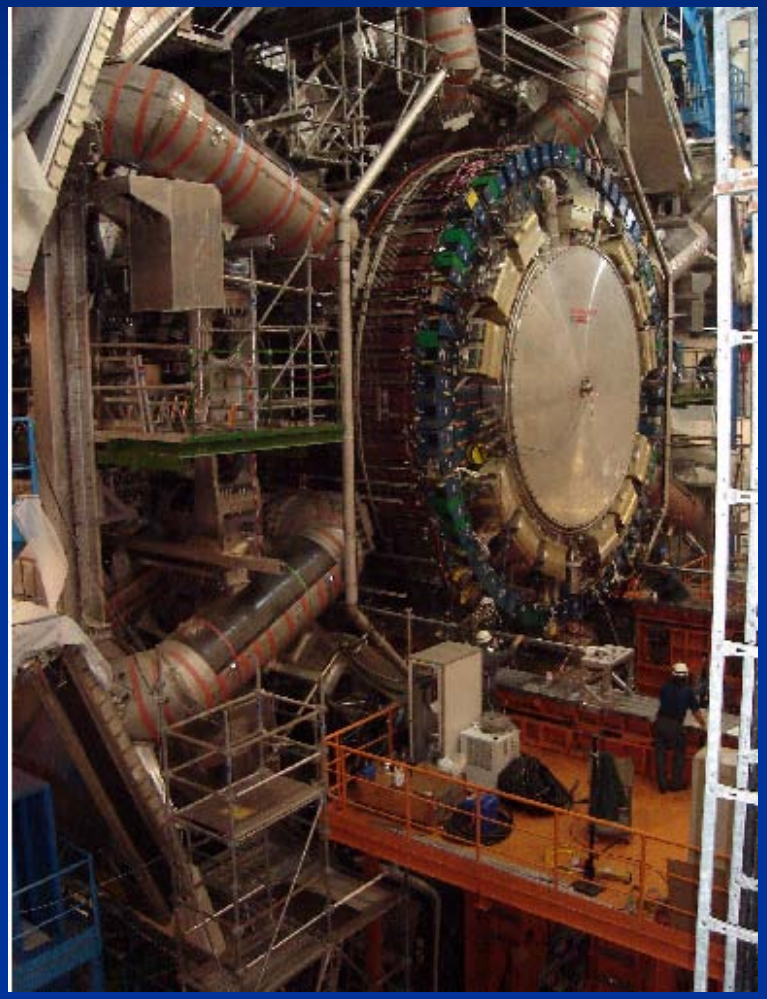
In contrast : cosmon – atom coupling must be weaker than gravity

Fundamental couplings in quantum field theory

Masses and coupling constants are determined by properties of ***vacuum*** *!*

Similar to Maxwell – equations in matter

Spontaneous symmetry breaking to be confirmed at the LHC

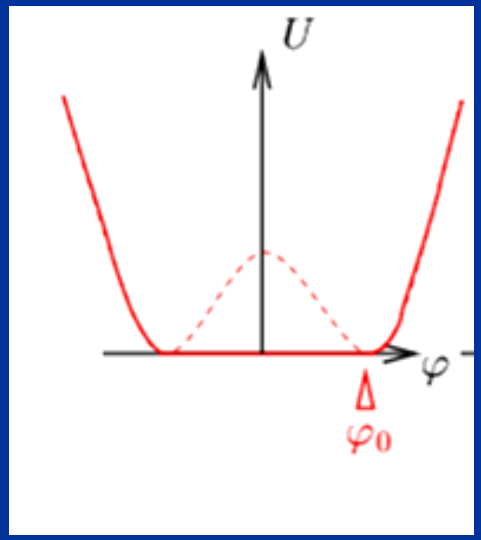


Have coupling constants in the early Universe other values ?

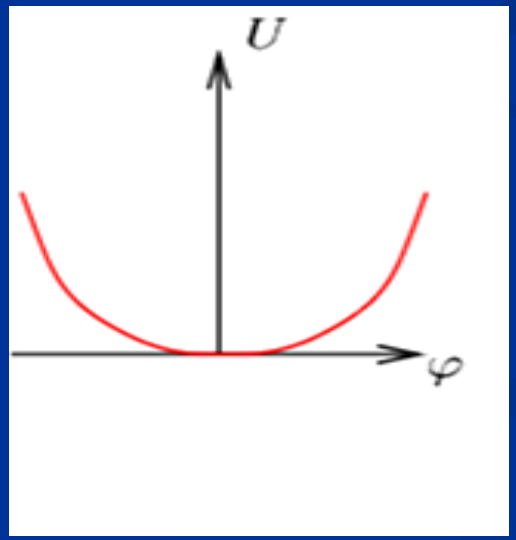
Yes !

Restoration of symmetry at high temperature in the early Universe

Low T
SSB
$<\varphi>=\varphi_0 \neq 0$



High T
SYM
$<\varphi>=0$



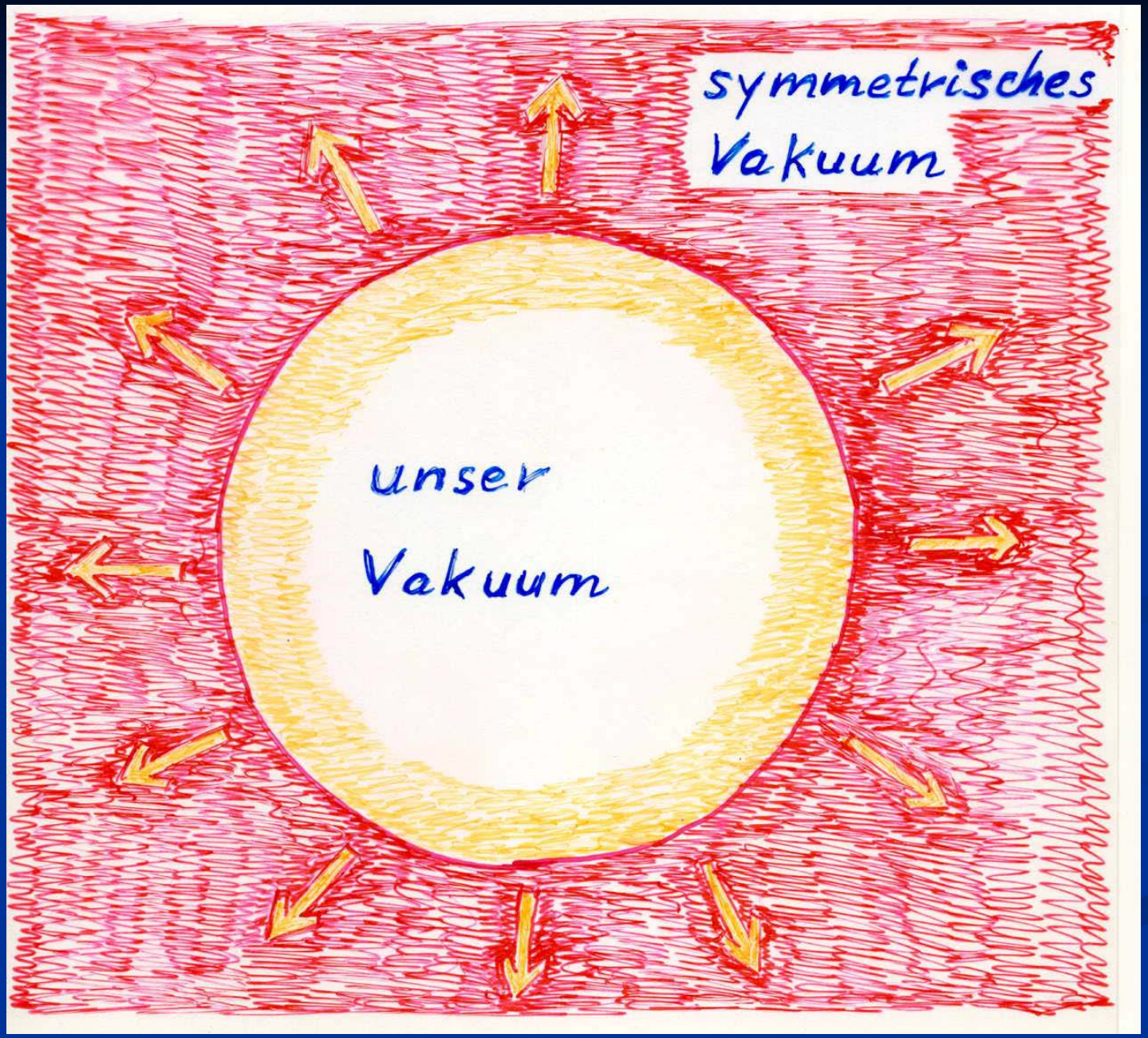
high T :
Less order
More symmetry

Example:
Magnets

In hot plasma
of early Universe :

masses of electron und myon
not different!

similar strength of electromagnetic
and weak interaction


symmetrisches
Vakuum
unser
Vakuum

Particle masses in quintessence cosmology

can depend on value of cosmon field

Varying couplings

only question :

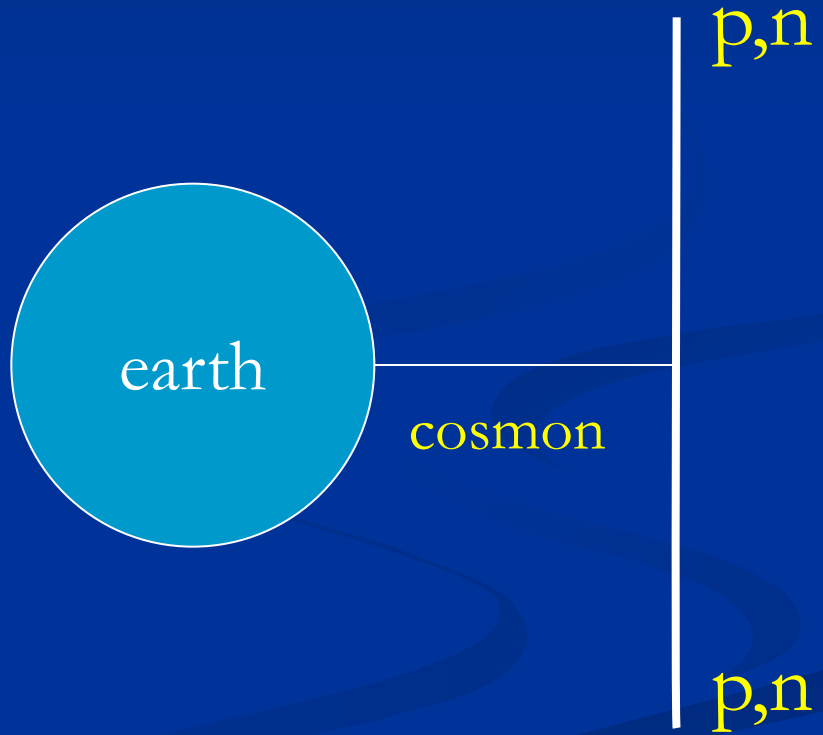
How strong is **present** variation of couplings ?

Cosmon – atom coupling induces violation of equivalence principle

Different couplings of cosmon to proton and neutron

Differential acceleration

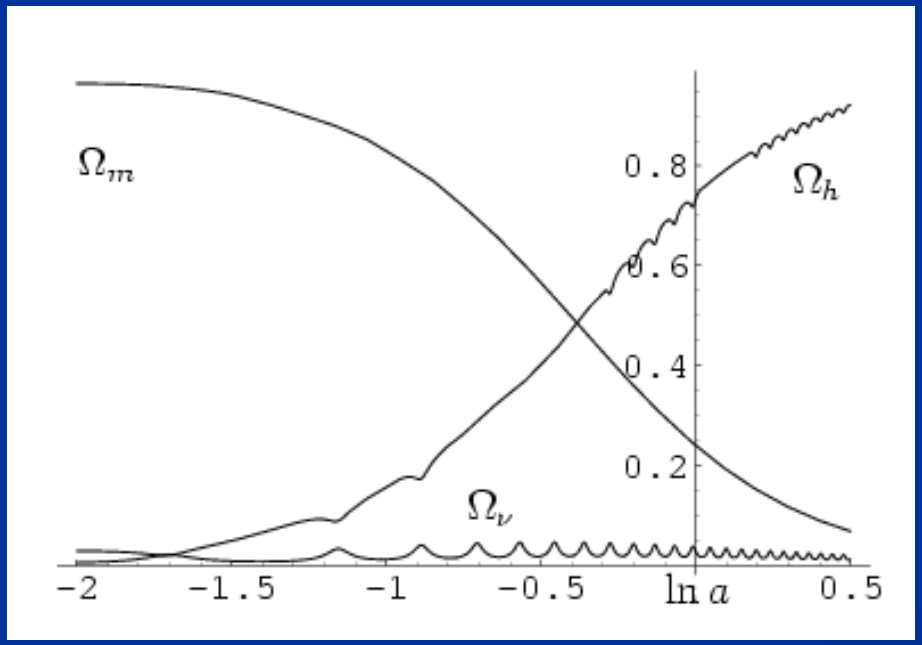
"Violation of equivalence principle"

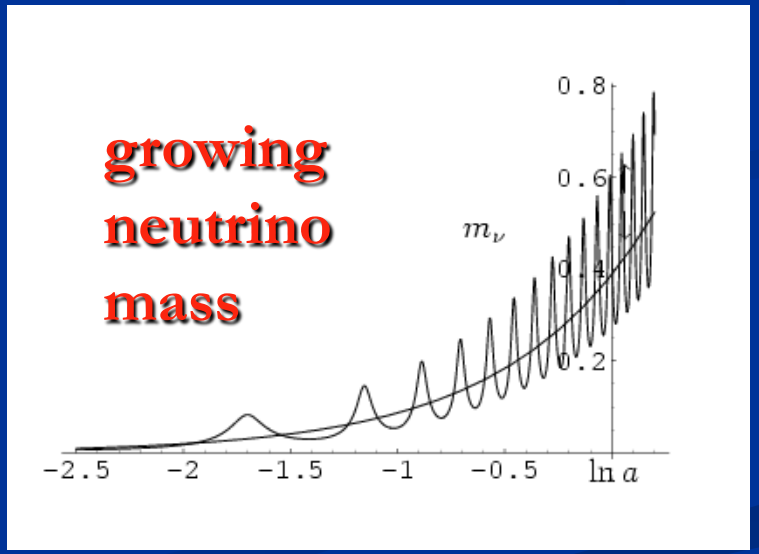


only apparent : new "fifth force" !

growing neutrino quintessence

growing neutrino mass triggers transition to almost static dark energy





L.Amendola, M.Baldi,…

effective cosmological trigger for stop of cosmon evolution : neutrinos get non-relativistic

- this has happened recently !
- sets scales for dark energy !

connection between dark energy and neutrino properties

$$[\rho_h(t_0)]^{\frac{1}{4}} = 1.27 \left(\frac{\gamma m_\nu(t_0)}{eV}\right)^{\frac{1}{4}} 10^{-3} eV$$

present dark energy density given by neutrino mass

present equation of state given by neutrino mass !

$$w_0 \approx -1 + \frac{m_\nu(t_0)}{12\mathrm{eV}}$$

cosmological selection

- present value of dark energy density set by cosmological event :

  neutrinos become non – relativistic

- not given by ground state properties !

basic ingredient :

cosmon coupling to neutrinos

Cosmon coupling to neutrinos

- can be large !

Fardon,Nelson,Weiner

- interesting effects for cosmology if neutrino mass is growing
- growing neutrinos can stop the evolution of the cosmon
- transition from early scaling solution to cosmological constant dominated cosmology

L.Amendola,M.Baldi,…

dark energy fraction determined by neutrino mass

$$\Omega_h(t_0) \approx \frac{\gamma m_\nu(t_0)}{16eV}$$

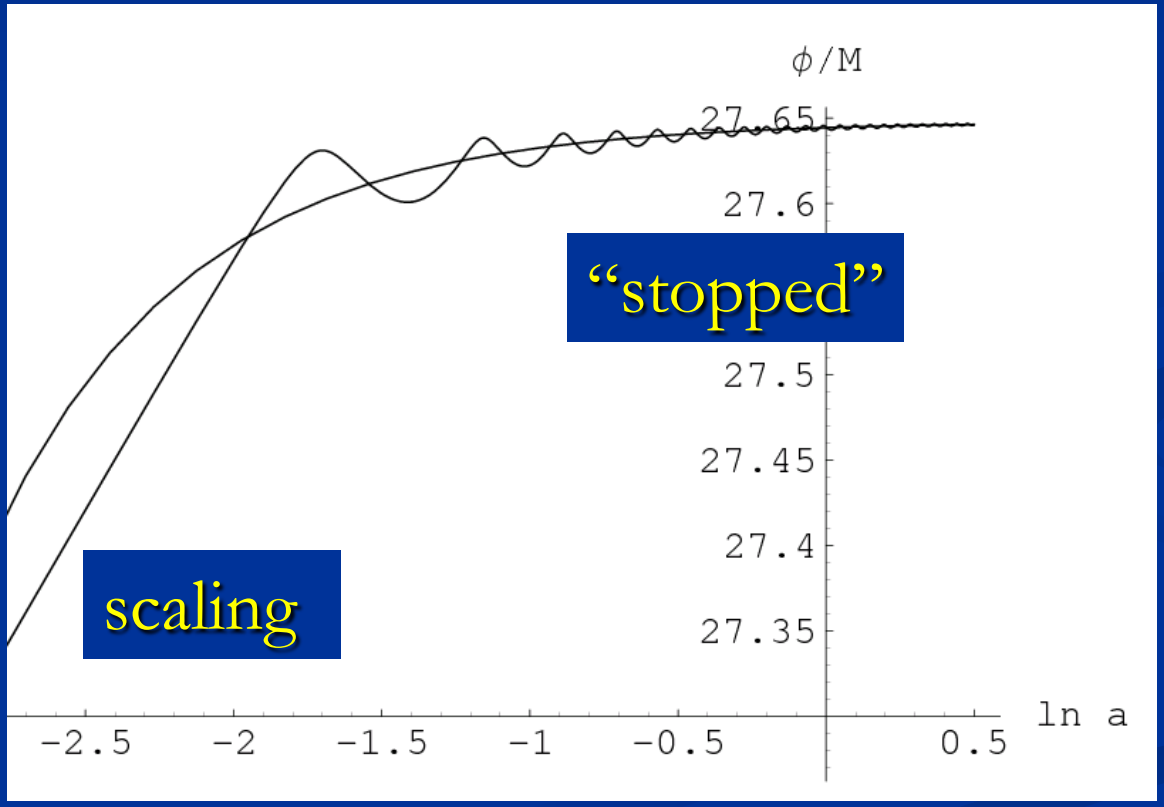
$$\gamma = -\frac{\beta}{\alpha}$$

constant neutrino - cosmon coupling β

$$\Omega_h(t_0) \approx -\frac{\epsilon}{\alpha}\,\frac{m_\nu(t_0)}{\bar{m}_\nu}\,\frac{m_\nu(t_0)}{16eV}$$

variable neutrino - cosmon coupling

cosmon evolution



stopped scalar field mimicks a cosmological constant (almost …)

rough approximation for dark energy :

- before redshift 5-6 : scaling (dynamical)
- after redshift 5-6 : almost static

  (cosmological constant)

growing neutrinos change cosmon evolution

$$\ddot{\varphi} + 3H\dot{\varphi} = -\frac{\partial V}{\partial \varphi} + \frac{\beta(\varphi)}{M}(\rho_\nu - 3p_\nu),$$
$$\beta(\varphi) = -M\frac{\partial}{\partial \varphi}\ln m_\nu(\varphi) = \frac{M}{\varphi - \varphi_t}$$

modification of conservation equation for neutrinos

$$\dot{\rho}_\nu + 3H(\rho_\nu + p_\nu) = -\frac{\beta(\varphi)}{M}(\rho_\nu - 3p_\nu)\dot{\varphi}$$
$$= -\frac{\dot{\varphi}}{\varphi - \varphi_t}(\rho_\nu - 3p_\nu)$$

effective stop of cosmon evolution

cosmon evolution almost stops once

- neutrinos get non –relativistic
- ß gets large

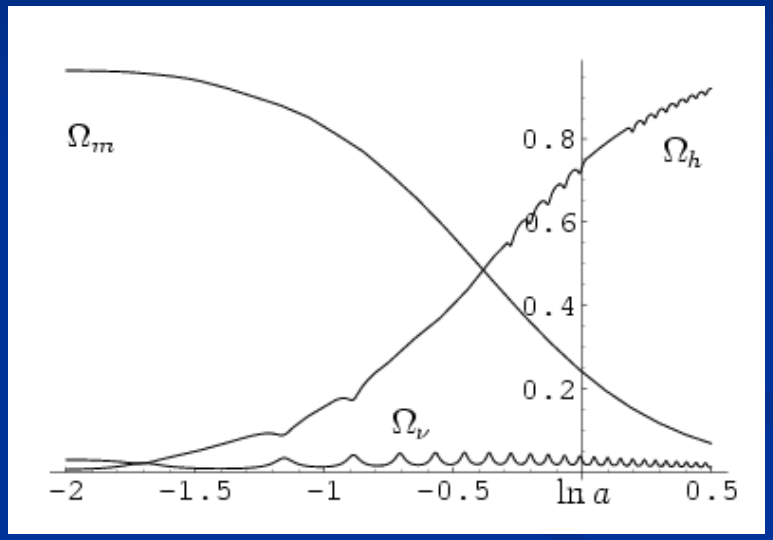
$$\ddot{\varphi} + 3H\dot{\varphi} = -\frac{\partial V}{\partial \varphi} + \frac{\beta(\varphi)}{M}(\rho_\nu - 3p_\nu)$$

$$\beta(\varphi) = -M\frac{\partial}{\partial \varphi}\ln m_\nu(\varphi) = \frac{M}{\varphi - \varphi_t}$$

$$m_\nu(\varphi) = \frac{\beta(\varphi)}{\epsilon}\bar{m}_\nu$$

This always happens for $\varphi \longrightarrow \varphi_t$!

crossover to dark energy dominated universe



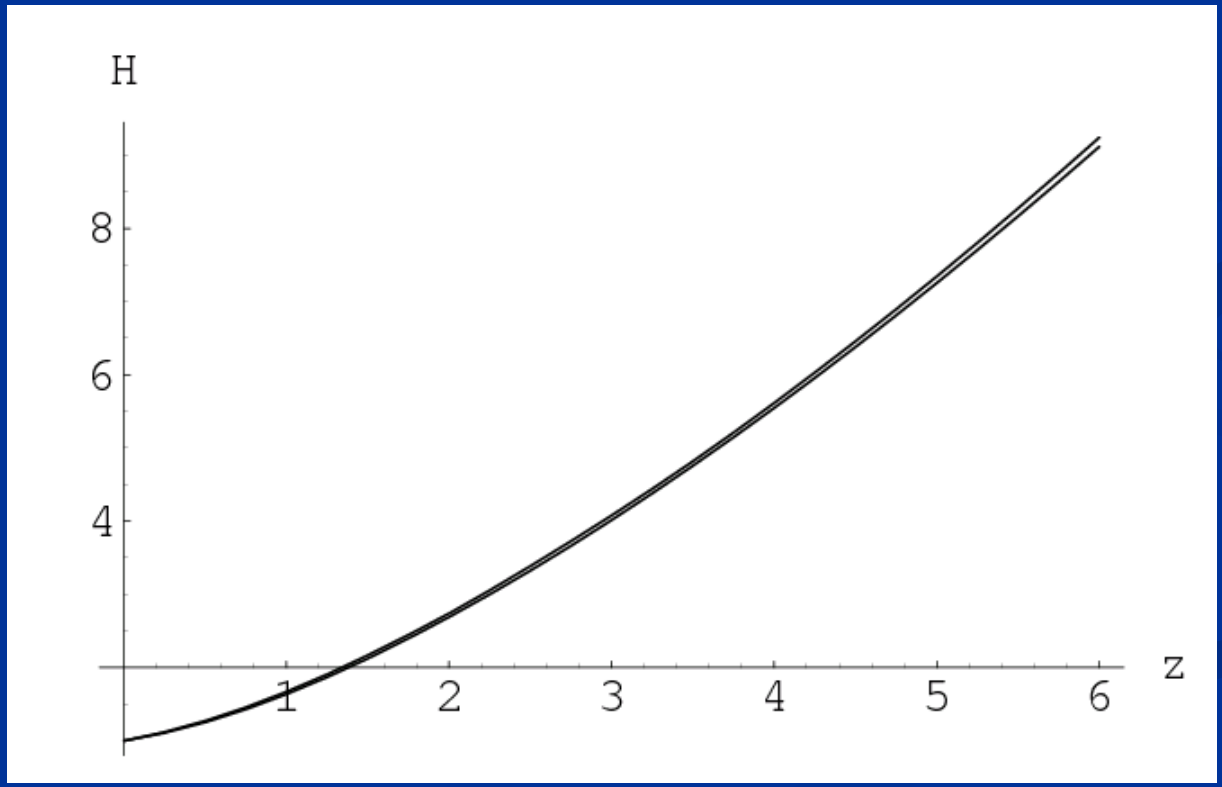
starts at time when "neutrino force" becomes important for the evolution of the cosmon field

cosmological selection !

Tests for growing neutrino quintessence

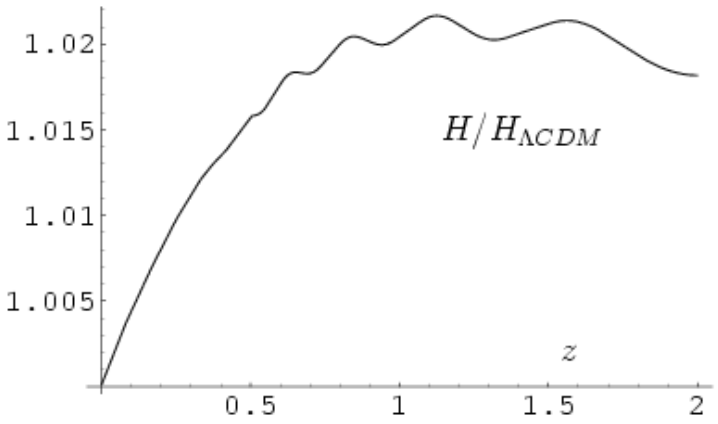
Hubble parameter

as compared to ΛCDM



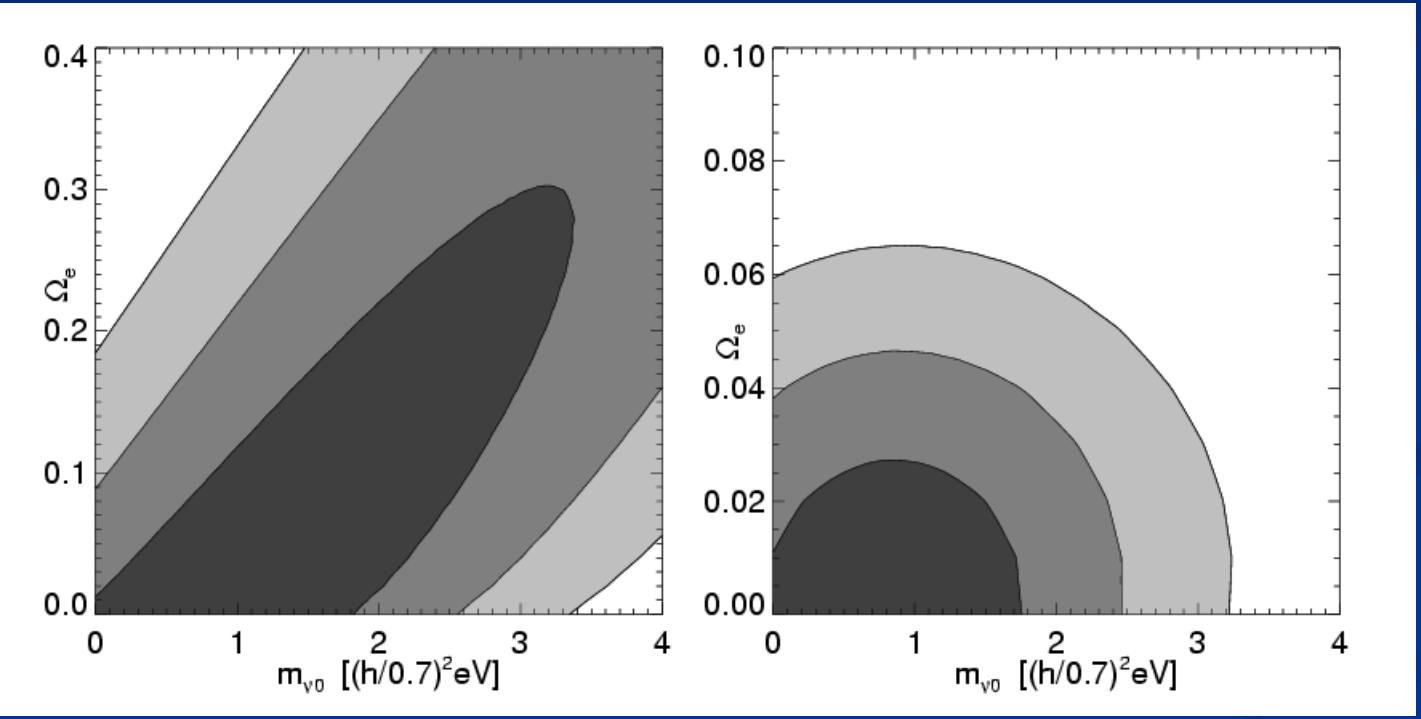
Hubble parameter ($z < z_c$)

$$H^2 = \frac{1}{3M^2}\left\{V_t + \rho_{m,0}a^{-3} + 2\tilde{\rho}_{\nu,0}a^{-\frac{3}{2}}\right\}$$



only small difference from ΛCDM !

bounds on average neutrino mass



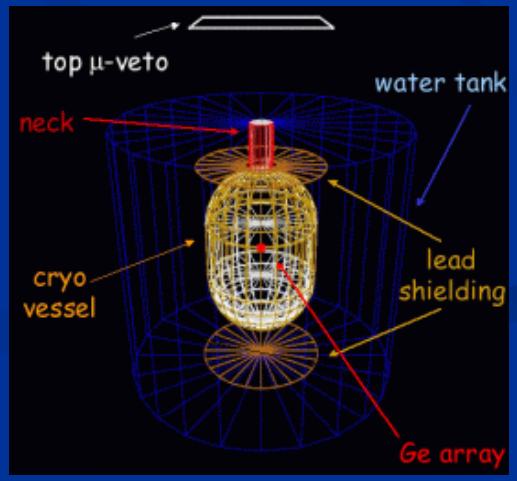
Looking Beyond Lambda with the Union Supernova Compilation

D. Rubin[1,2], E. V. Linder[1,3], M. Kowalski[4], G. Aldering[1], R. Amanullah[1,3], K. Barbary[1,2], N. V. Connolly[5], K. S. Dawson[1], L. Faccioli[1,3], V. Fadeyev[6], G. Goldhaber[1,2], A. Goobar[7], I. Hook[8], C. Lidman[9], J. Meyers[1,2], S. Nobili[7], P. E. Nugent[1], R. Pain[10], S. Perlmutter[1,2], P. Ruiz-Lapuente[11], A. L. Spadafora[1], M. Strovink[1,2], N. Suzuki[1], and H. Swift[1,2]
(Supernova Cosmology Project)

Can time evolution of neutrino mass be observed ?

Experimental determination of neutrino mass may turn out higher than cosmological upper bound in model with constant neutrino mass

(KATRIN, neutrino-less double beta decay)

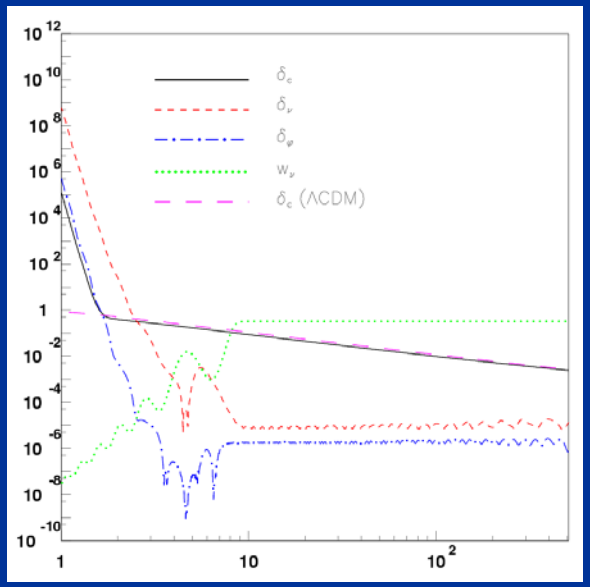


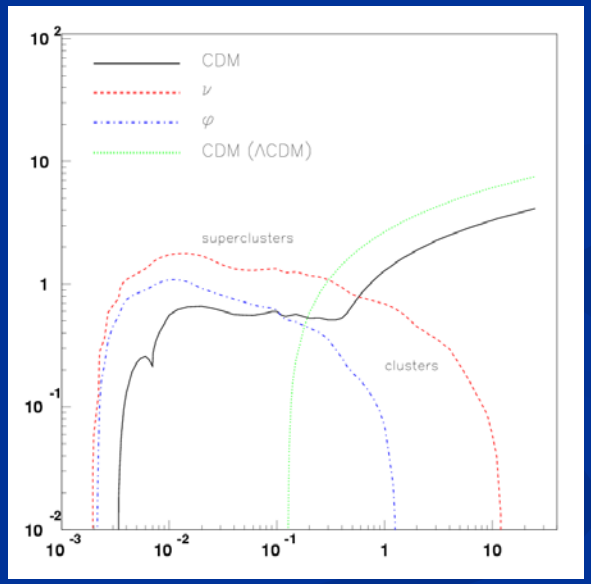
GERDA

neutrino fluctuations

neutrino structures become nonlinear at z~1 for supercluster scales

D.Mota , G.Robbers , V.Pettorino , …

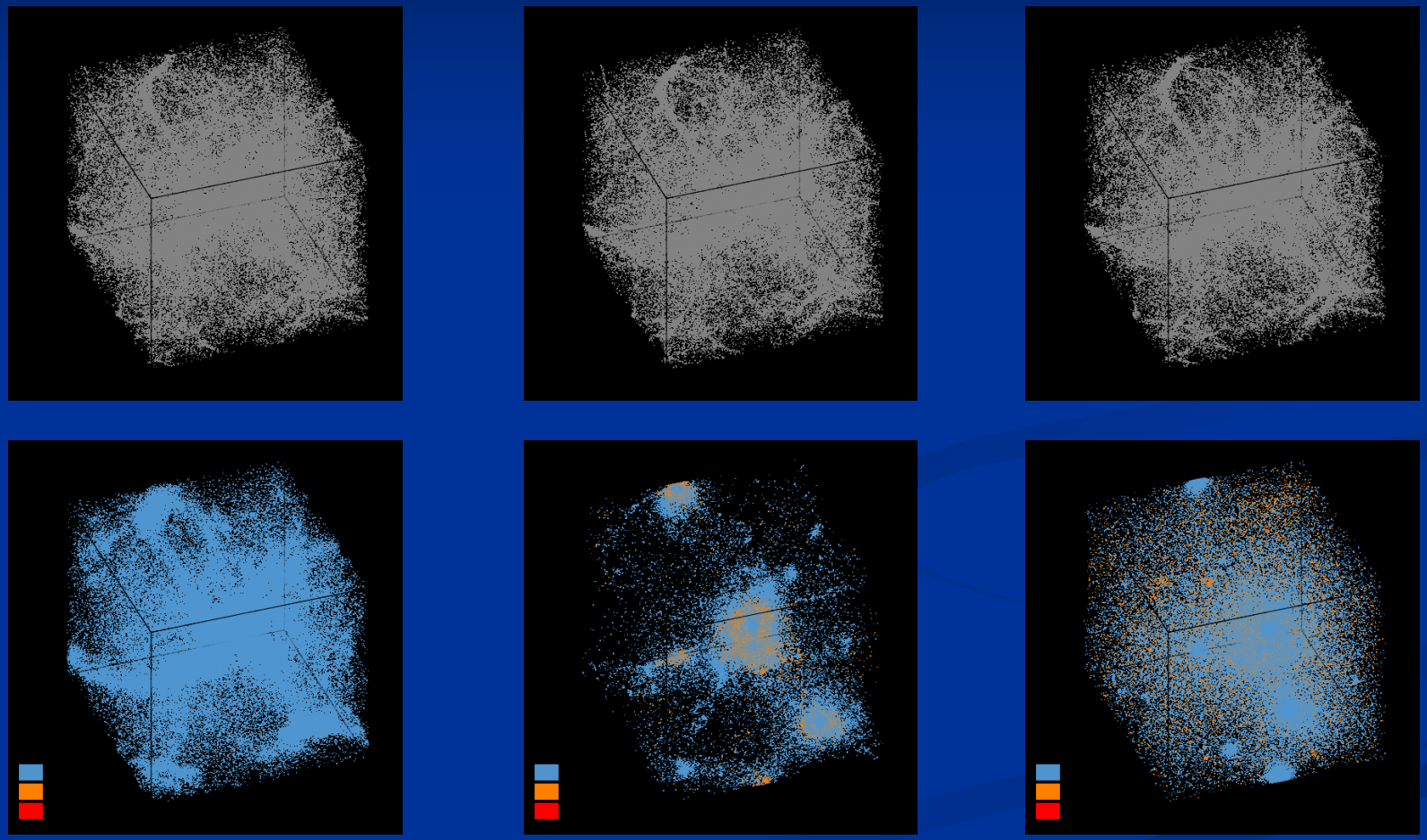




stable neutrino-cosmon lumps exist

N.Brouzakis , N.Tetradis ,…

Formation of neutrino lumps



N- body simulation M.Baldi et al

Conclusions

- Cosmic event triggers qualitative change in evolution of cosmon
- Cosmon stops changing after neutrinos become non-relativistic
- Explains why now
- Cosmological selection
- Model can be distinguished from cosmological constant

Summary

- $\Omega_h = 0.73$
- Q/Λ : dynamical und static dark energy will be distinguishable
- growing neutrino mass can explain why now problem
- Q : time varying fundamental coupling "constants"
  violation of equivalence principle

End

varying neutrino – cosmon coupling

- specific model
- can naturally explain why neutrino – cosmon coupling is much larger than atom – cosmon coupling

neutrino mass

$$M_\nu = M_D M_R^{-1} M_D^T + M_L$$

$$M_L = h_L \gamma \frac{d^2}{M_t^2}$$

seesaw and cascade mechanism

triplet expectation value ~ doublet squared

$$m_\nu = \frac{h_\nu^2 d^2}{m_R} + \frac{h_L \gamma d^2}{M_t^2}$$

omit generation structure

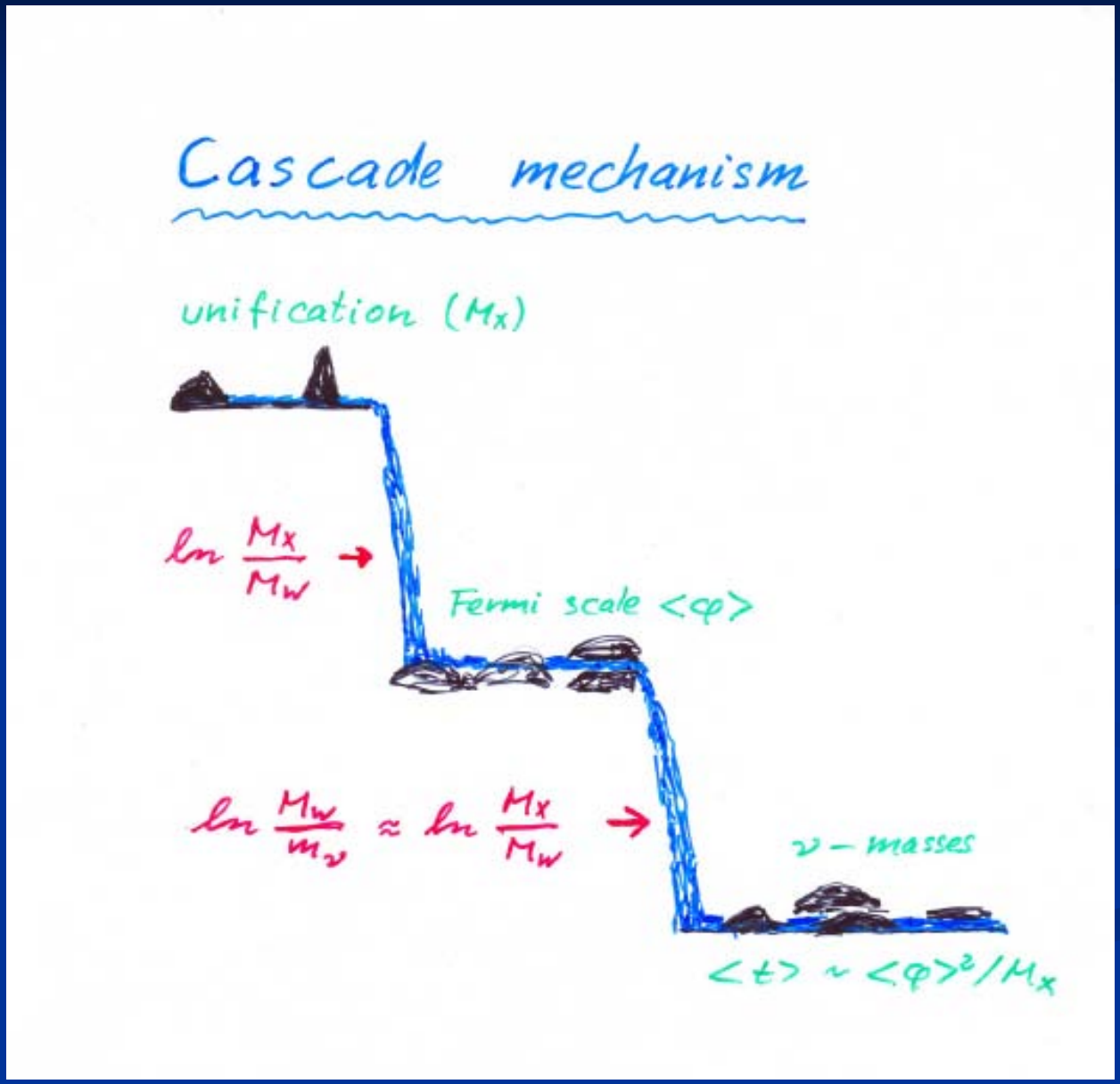
cascade mechanism

$$U = U_0(\varphi) + \frac{\lambda}{2}(d^2 - d_0^2)^2 + \frac{1}{2}M_t^2(\varphi)t^2 - \gamma d^2 t$$

triplet expectation value ~ $\gamma \frac{d^2}{M_t^2}$

M.Magg , …
G.Lazarides , Q.Shafi , …

cascade


Cascade mechanism
unification (M_X)
$\ln \frac{M_X}{M_W}$
Fermi scale $\langle\varphi\rangle$
$\ln \frac{M_W}{m_\nu} \approx \ln \frac{M_X}{M_W}$
ν – masses
$\langle t\rangle \sim \langle\varphi\rangle^2/M_X$

varying neutrino mass

$$M_t^2 = c_t M_{GUT}^2 \left[1 - \frac{1}{\tau} \exp\left(-\epsilon \frac{\varphi}{M}\right)\right]$$

$\varepsilon \approx -0.05$

triplet mass depends on cosmon field φ

$$m_\nu(\varphi) = \bar{m}_\nu \left\{1 - \exp\left[-\frac{\epsilon}{M}(\varphi - \varphi_t)\right]\right\}^{-1}$$

➡ neutrino mass depends on φ

cascade mechanism

$$U = U_0(\varphi) + \frac{\lambda}{2}(d^2 - d_0^2)^2 + \frac{1}{2}M_t^2(\varphi)t^2 - \gamma d^2 t$$

triplet expectation value ~ $\gamma \dfrac{d^2}{M_t^2}$

$$M_t^2(\varphi) = \bar{M}_t^2 \left[1 - \exp\left(-\frac{\epsilon}{M}(\varphi - \varphi_t\right)\right]$$

“singular” neutrino mass

$$M_t^2 = c_t M_{GUT}^2 \left[1 - \frac{1}{\tau}\exp\left(-\epsilon\frac{\varphi}{M}\right)\right]$$

triplet mass vanishes for $\varphi \longrightarrow \varphi_t$

$$\frac{\varphi_t}{M} = -\frac{\ln\tau}{\epsilon}$$

$$m_\nu(\varphi) = \frac{\bar{m}_\nu M}{\epsilon(\varphi - \varphi_t)}$$

⟹ neutrino mass diverges for $\varphi \longrightarrow \varphi_t$

strong effective neutrino – cosmon coupling for $\varphi \longrightarrow \varphi_t$

$$\beta(\varphi) = -M\frac{\partial}{\partial\varphi}\ln m_\nu(\varphi) = \frac{M}{\varphi - \varphi_t}$$

typical present value : $\beta \approx 50$ ⇒

cosmon mediated attraction between neutrinos is about 50^2 stronger than gravitational attraction

crossover from
early scaling solution to
effective cosmological constant

early scaling solution (tracker solution)

$$V(\varphi) = M^4 \exp\left(-\alpha \frac{\varphi}{M}\right)$$

$$\varphi = \varphi_0 + (2M/\alpha)\ln(t/t_0)$$

$$\Omega_{h,e} = \frac{n}{\alpha^2}$$

neutrino mass unimportant in early cosmology

effective cosmological trigger for stop of cosmon evolution : neutrinos get non-relativistic

- this has happened recently !
- sets scales for dark energy !

dark energy fraction determined by neutrino mass

$$\Omega_h(t_0) \approx \frac{\gamma m_\nu(t_0)}{16eV}$$

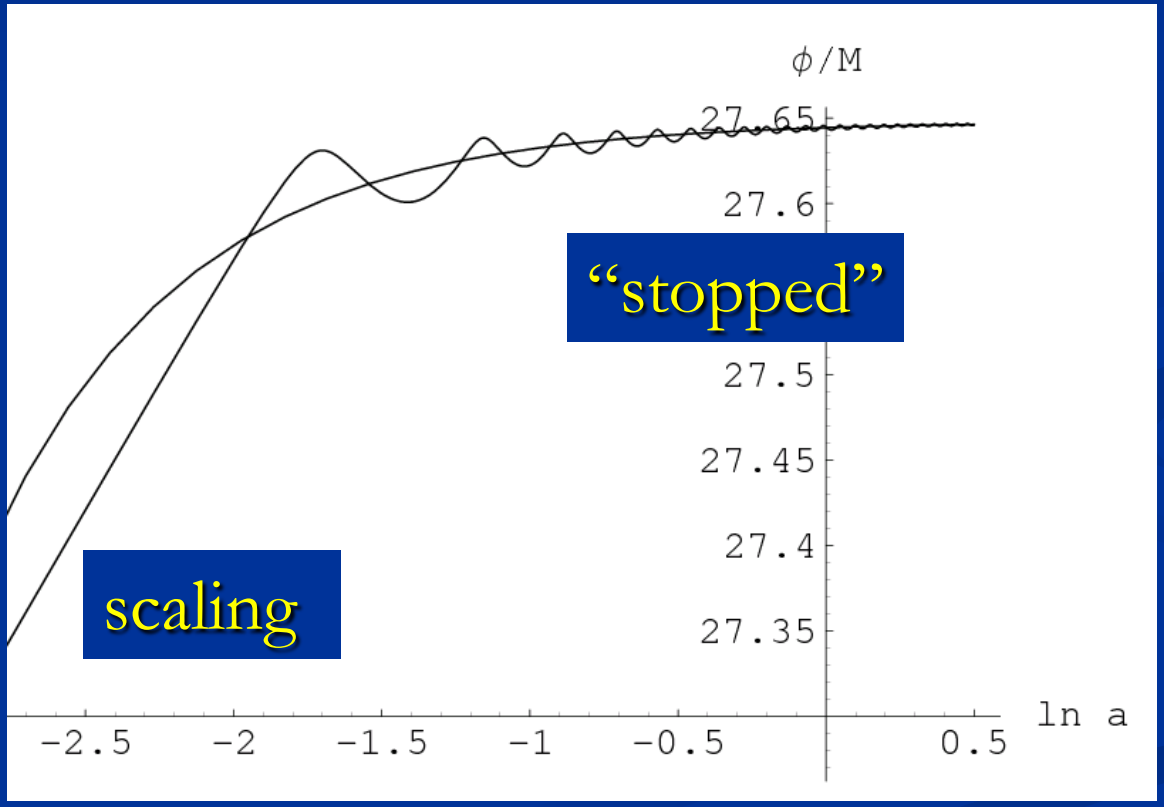
$$\gamma = -\frac{\beta}{\alpha}$$

constant neutrino - cosmon coupling β

$$\Omega_h(t_0) \approx -\frac{\epsilon}{\alpha}\,\frac{m_\nu(t_0)}{\bar{m}_\nu}\,\frac{m_\nu(t_0)}{16eV}$$

variable neutrino - cosmon coupling

cosmon evolution



Equation of state

p=T-V pressure

ϱ=T+V energy density

kinetic energy

$T = \frac{1}{2}\dot{\phi}^2$

Equation of state

$$w = \frac{p}{\rho} = \frac{T-V}{T+V}$$

Depends on specific evolution of the scalar field

Negative pressure

- w < 0 Ω_h increases (with decreasing z)

late universe with
small radiation component :

$$w_h = \frac{1}{3\Omega_h(1-\Omega_h)} \frac{\partial \Omega_h}{\partial \ln(1+z)}$$

- w < -1/3 expansion of the Universe is accelerating

- w = -1 cosmological constant

A few references

C.Wetterich , Nucl.Phys.B302,668(1988) , received 24.9.1987

P.J.E.Peebles,B.Ratra , Astrophys.J.Lett.325,L17(1988) , received 20.10.1987

B.Ratra,P.J.E.Peebles , Phys.Rev.D37,3406(1988) , received 16.2.1988

J.Frieman,C.T.Hill,A.Stebbins,I.Waga , Phys.Rev.Lett.75,2077(1995)

P.Ferreira, M.Joyce , Phys.Rev.Lett.79,4740(1997)

C.Wetterich , Astron.Astrophys.301,321(1995)

P.Viana, A.Liddle , Phys.Rev.D57,674(1998)

E.Copeland,A.Liddle,D.Wands , Phys.Rev.D57,4686(1998)

R.Caldwell,R.Dave,P.Steinhardt , Phys.Rev.Lett.80,1582(1998)

P.Steinhardt,L.Wang,I.Zlatev , Phys.Rev.Lett.82,896(1999)