The Interplay of Quantum Gravity and Gauge Theories

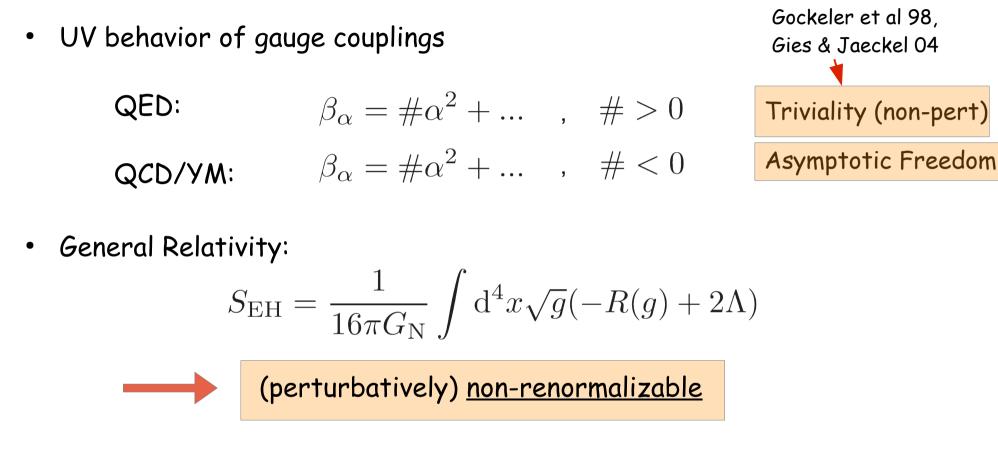
NC, Eichhorn: arXiv:1702.07724 NC, Litim, Pawlowski: in prep NC, Eichhorn, Held: in prep

Heidelberg, FRG-Meeting 2017 March 8, 2017

Outline

- UV Completions: Asymptotic Safety
 - The Standard Model and Quantum Gravity
- Gravity Coupled to Gauge Theories
 - General Structure: "Interacting Asymptotic Freedom"
 - Quantum Gravity Corrections to U(1): A solution to the triviality problem and the role of higher order operators
 - Gravity and SU(N)
 - UV-safe Gauge-Yukawa Models
- Summary and Outlook

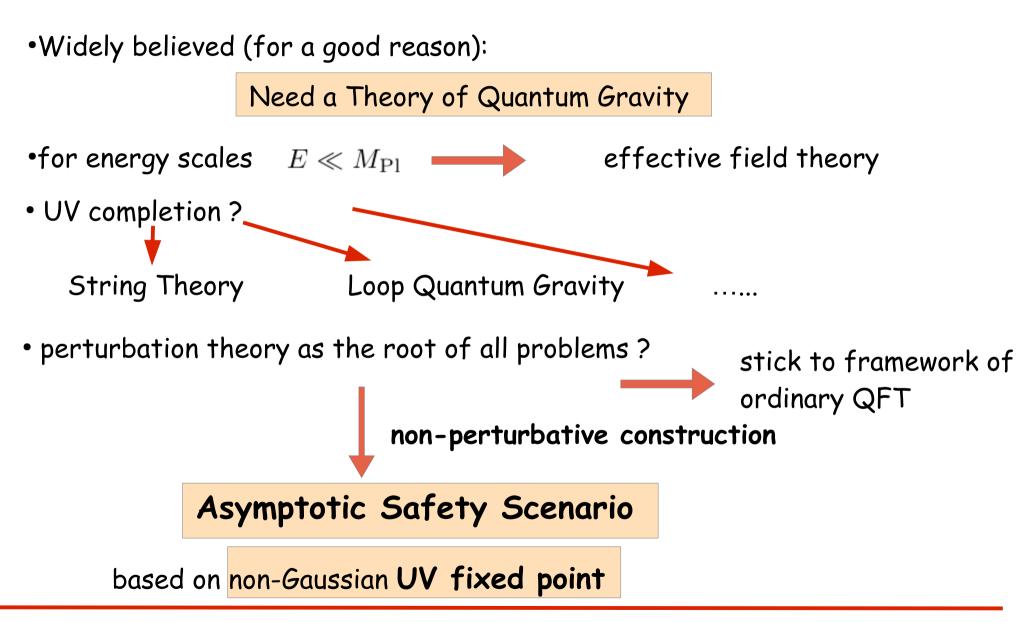
...known territory ...



• Ultimate goal:

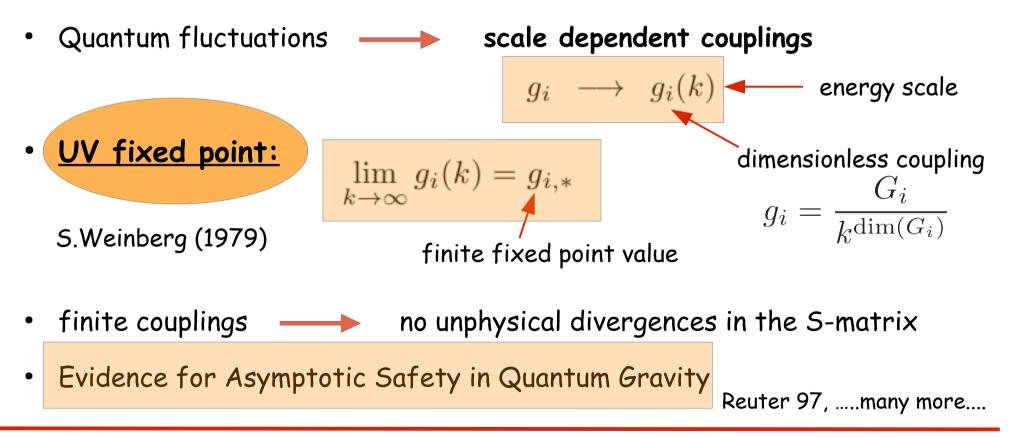
UV-completion of: Standard Model (+ something?) + Gravity

...what nobody really knows: UV completion



Asymptotic Safety in a Nutshell

- properties of fundamental theory:
 - finiteness
 finite number of free parameters (predictive)
- Parametrization of correlation functions with coupling constants G_i



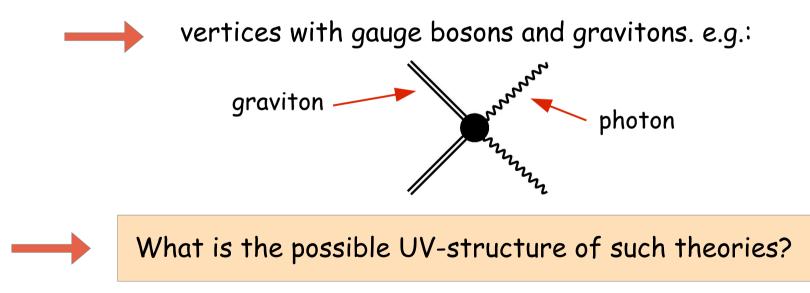
Gauge Theories & Gravity

• Can we find Asymptotic Safety in coupled gauge-gravity systems?

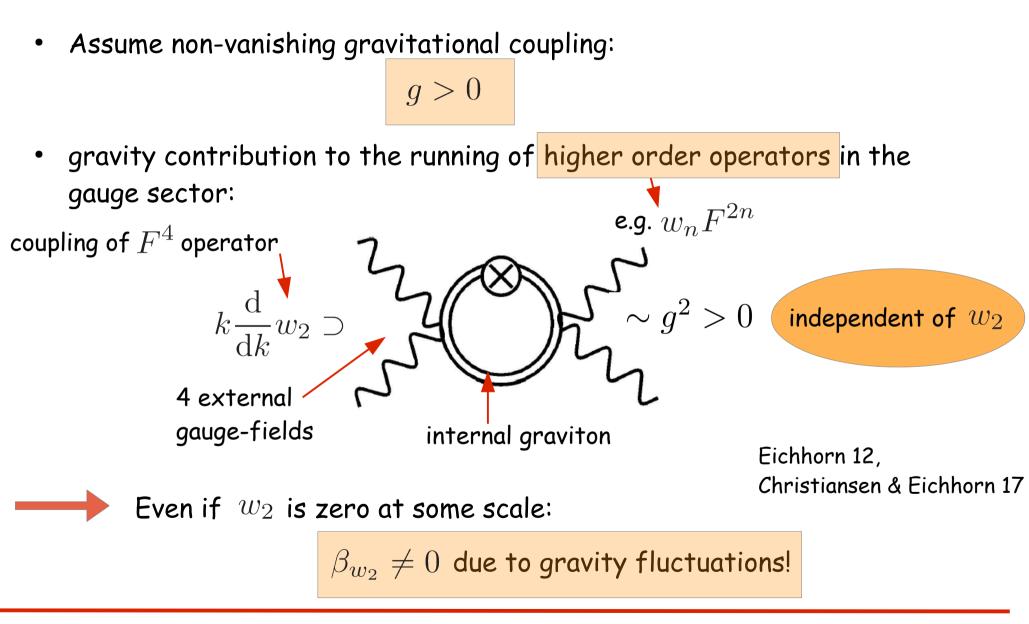
$$\Gamma[g, A] = \Gamma_{\text{grav}}[g] + \Gamma_{\text{gauge}}[g, A]$$

• Minimal coupling of gravity to gauge theories already in $\ F^2$ term

$$\int \mathrm{d}^4 x \sqrt{g} \, g^{\mu\alpha} g^{\nu\beta} F_{\alpha\beta} F_{\mu\nu}$$



"Interacting Asymptotic Freedom" I



"Interacting Asymptotic Freedom" II

• Structure of the beta-function

$$\beta_{w_n} = A + Bg^2 \qquad \text{gravitational couplings}$$

$$A\left((g_{\text{gauge}}, \vec{w}) = 0\right) = 0$$

$$(g_{\text{gauge}}, \vec{w}) = 0 \qquad \text{is not a fixed point}$$
For $q > 0$ only non-Gaussian FP possible: $\vec{w}^* \neq 0$

• Fixed point can be fully interacting $\,g^*_{
m gauge}>0\,$ or

 $\left(g^*_{
m gauge}=0,ec{w}^*
eq 0
ight)$ "Interacting Asymptotic Freedom"

• Beta function of U(1) gauge coupling

 $\beta_{g^2_{U(1)}} = g^2_{U(1)} \, \eta_A$ \checkmark anomalous dimension

anomalous dimension of the photon

 $\eta_A\equiv 0~~$ without fermions and gravitons (free theory)

 $\eta_A > 0$ with fermions only (triviality)

• As argued: Gravity and higher order operators are important!

$$\begin{split} \Gamma[g,A] = \int (R-2\Lambda) + \frac{1}{g_{U(1)}^2} \int F^2 + \bar{w}_2 \int F^4 + \text{gauge} \\ \text{gravity} & \text{min. term} & \text{higher order op.} \end{split}$$

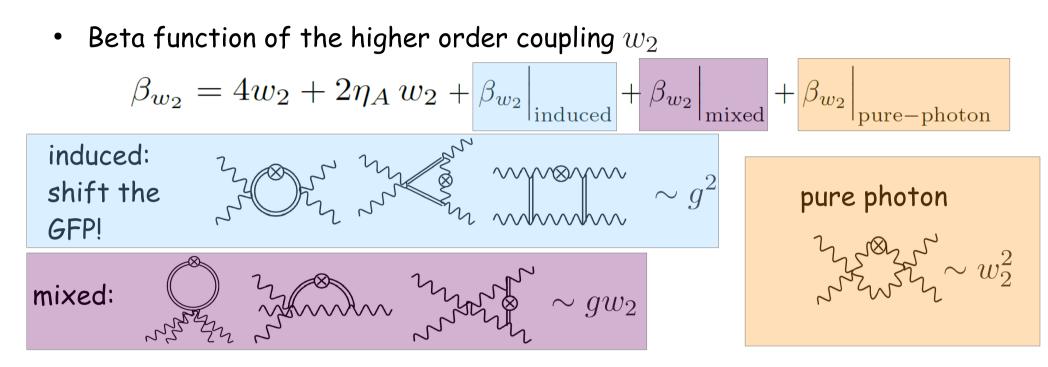
• Can gravity cure UV-problems?

Christiansen, Eichhorn 17

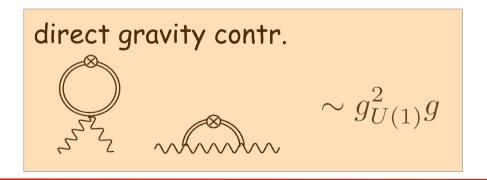


Beta functions using the Wetterich equation (FRG)

Harst & Reuter 11



• Beta function of the gauge coupling $\,g^2_{U(1)}\,$

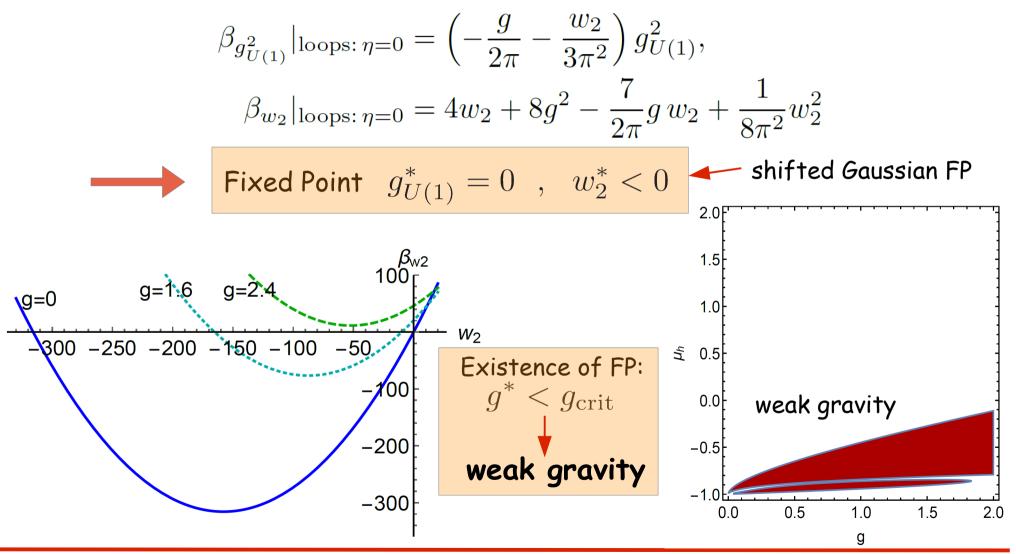


mediated contr.

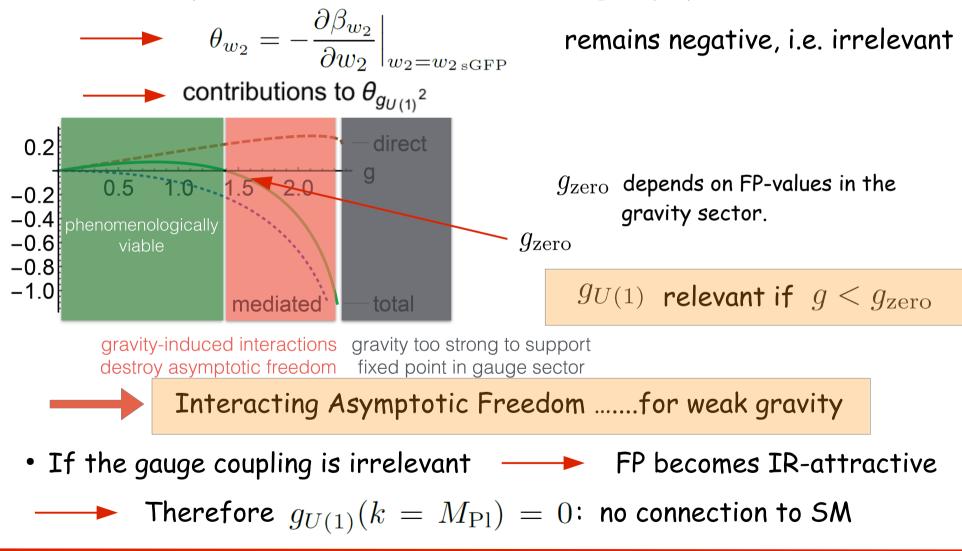
$$\sim g_{U(1)}^2 w_2$$

Nicolai Christiansen (ITP Heidelberg)

• Qualitative effects all visible in approximated beta-functions



• Critical exponents and stability: Interacting Asymptotic Freedom?



Adding Fermions does not change that picture • Fermions contribute at $\mathcal{O}\left(g_{U(1)}^4\right)$ Leading contribution from gravity! $\beta_{g_{U(1)}^2} = A g g_{U(1)}^2 + B w_2 g_{U(1)}^2 + C g_{U(1)}^4 + \dots$ gravity, direct gravity, mediated fermions → At $g^*_{U(1)} = 0$ fermions do not contribute to the critical exp. \blacktriangleright If $g < g_{
m zero}$ QED coupled to QG exhibits Interacting Asymptotic Freedom Harst, Reuter 11 With fermions — also NGFP possible: Eichhorn, Versteegen in prep

- YM-theory: Does Asymptotic Freedom survive when coupled to gravity?
- Calculation is similar to U(1)
 direct gravity contributions support Asymptotic Freedom
 Daum, Harst, Reuter 09 Folkerts, Litim, Pawlowski 12
 Also in extended approximation Christiansen, Litim, Pawlowski in prep.
- Gluon contributions to the gravity sector: Fully coupled system

stability of the NGFP in gravity

Preliminary!

Christiansen, Litim, Pawlowski in prep.

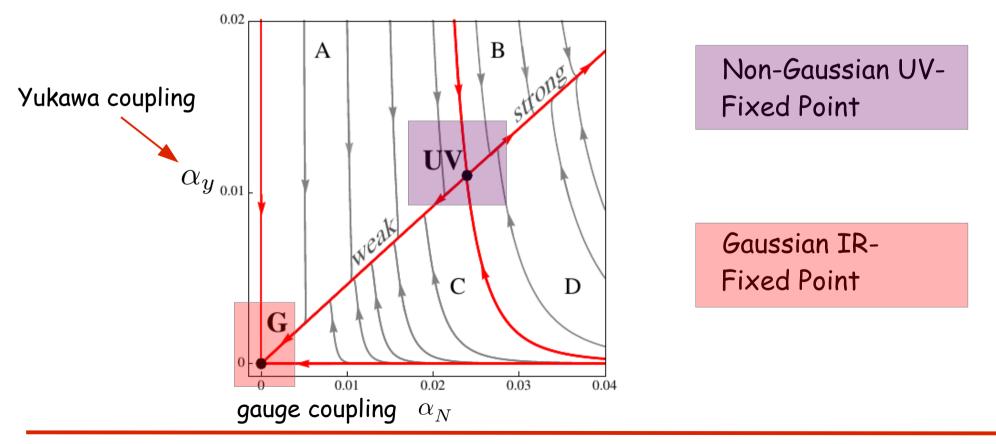
UV safe Gauge-Yukawa models

• Perturbative asymptotic safety in gauge-Yukawa models:

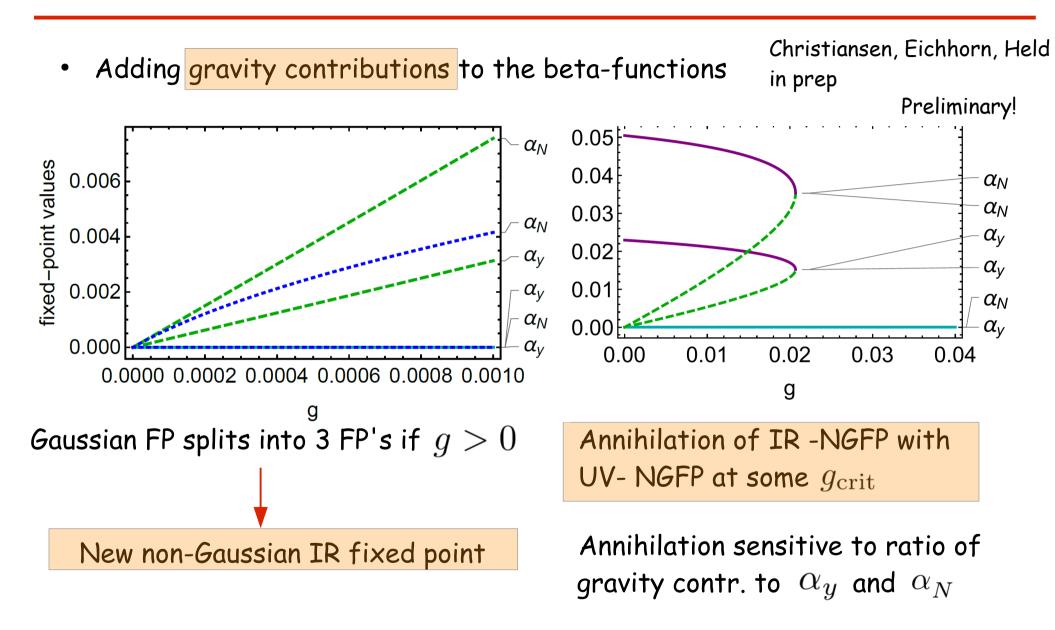
— Veneziano Limit: $\epsilon = \frac{N_F}{N_c} - \frac{11}{2} \ll 1$

Litim & Sannino 14

• Fixed points and phase diagram without gravity



UV safe matter models



Summary and Outlook

- Quantum Gravity coupled to gauge theories:
 - gravity induces higher order operators: Interacting Asymptotic Freedom
- gravity and U(1) gauge theories:



- gravity induces non-Gaussian FP in F^4 coupling
- "weak gravity": gravity induces Asymptotic Freedom in F² coupling

solution to the triviality problem

<u>Outlook</u>

- Non-Abelian gauge theories
- Fully coupled gauge-gravity system
- More gerneal matter sector!

weak gravity bound!

Thank You!!!