

Charting Hadronic Interiors

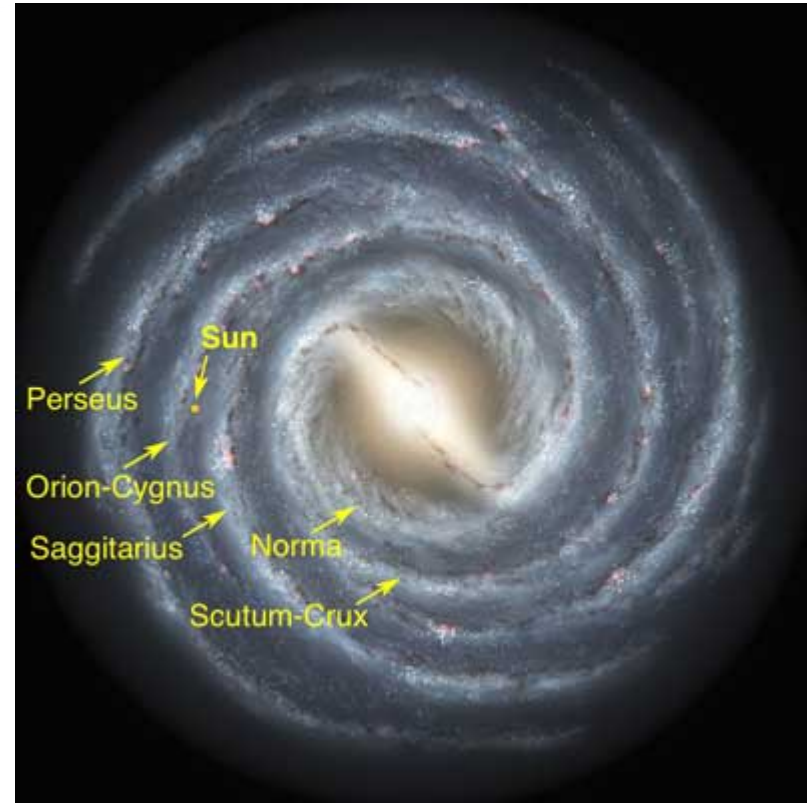


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Emergent Phenomena in the Standard Model

Existence of the Universe as we know it depends critically on the following empirical facts:

- Proton is massive, *i.e.* the mass-scale for strong interactions is vastly different to that of electromagnetism
- Proton is absolutely stable, despite being a composite object constituted from three valence quarks
- Pion is unnaturally light (not massless, but lepton-like mass), despite being a strongly interacting composite object built from a valence-quark and valence antiquark



Emergence: low-level rules producing high-level phenomena, with enormous apparent complexity



FUTURE

PRESENT

PAST

A New Era

- Strong-QCD is the first place we fully experience the collisions and collisions between relativity and quantum mechanics.
- In attempting to match QCD with Nature, we confront the diverse complexities of nonperturbative, nonlinear dynamics in relativistic quantum field theory, *e.g.*
 - loss of particle number conservation,
 - frame and scale dependence of the explanations and interpretations of observable processes,
 - and evolving character of the relevant degrees-of-freedom.

Model independent statement:

There is quark orbital angular momentum in the pion

Probable corollary: What is true in the pion, is true in the proton

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 - loss of particle number conservation,
 - frame and scale dependence of the explanations and interpretations of observable processes,
 - and evolving character of the relevant degrees-of-freedom.
- Origin and distribution of mass, momentum, spin, *etc.* within hadrons? *e.g.* where is the proton's spin and how is the pion spinless?
 - Don't forget the latter!
 - How do all the spin-1/2 quarks and spin-1 gluons combine to make a massless, $J=0$ composite mode?

Model independent statement:

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A New Era

➤ Strong-QCD is the first place we fully experience the collisions and collisions between relativity and quantum mechanics.

➤ In attempting to understand QCD with N_{eff} = 3, we face the difficulties of the complexities of quantum field theory

– loss of parton picture

– frame and reference dependence of observable

– and evolution

Answer depends on the the observer's frame and scale at which observations are made!

So-called spin crisis is largely the consequence of ignoring these facts

➤ Origin and distribution of mass, momentum, spin, etc. within hadrons? e.g. where is the proton's spin and how is the pion spinless?

– Don't forget the latter!

– How do all the spin-1/2 quarks and spin-1 gluons combine to make a massless, $J=0$ composite mode?

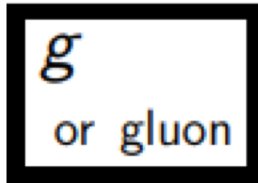
Ideas: Old & New

1960s: O19 & M6M



Particle Data Group

Citation: C. Patrignani *et al.* (Particle Data Group), *Chin. Phys. C*, **40**, 100001 (2016) and 2017 update



$$I(J^P) = 0(1^-)$$

SU(3) color octet

Mass $m = 0$.

Theoretical value. A mass as large as a few MeV may not be precluded, see YNDURAIN 95.

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
• • • We do not use the following data for averages, fits, limits, etc. • • •			
	ABREU 92E	DLPH	Spin 1, not 0
	ALEXANDER 91H	OPAL	Spin 1, not 0
	BEHREND 82D	CELL	Spin 1, not 0
	BERGER 80D	PLUT	Spin 1, not 0
	BRANDELIK 80C	TASS	Spin 1, not 0

gluon REFERENCES

YNDURAIN 95	PL B345 524	F.J. Yndurain	(MADU)
ABREU 92E	PL B274 498	P. Abreu <i>et al.</i>	(DELPHI Collab.)
ALEXANDER 91H	ZPHY C52 543	G. Alexander <i>et al.</i>	(OPAL Collab.)
BEHREND 82D	PL B110 329	H.J. Behrend <i>et al.</i>	(CELLO Collab.)
BERGER 80D	PL B97 459	C. Berger <i>et al.</i>	(PLUTO Collab.)
BRANDELIK 80C	PL B97 453	R. Brandelik <i>et al.</i>	(TASSO Collab.)

$$\Delta_{\mu\nu}^{-1}(q) = \underbrace{\left[\text{tree} + \frac{1}{2} \text{(a)} + \frac{1}{2} \text{(b)} + \text{(c)} + \frac{1}{6} \text{(d)} + \frac{1}{2} \text{(e)} \right]}_{\Pi_{\mu\nu}(q)}$$

$\Pi_{\mu\nu}(q) = P_{\mu\nu}(q)\Pi(q)$

$P_{\mu\nu}(q) = g_{\mu\nu} - q_\mu q_\nu / q^2$

Gluon Gap Equation

In QCD: Gluons become massive!

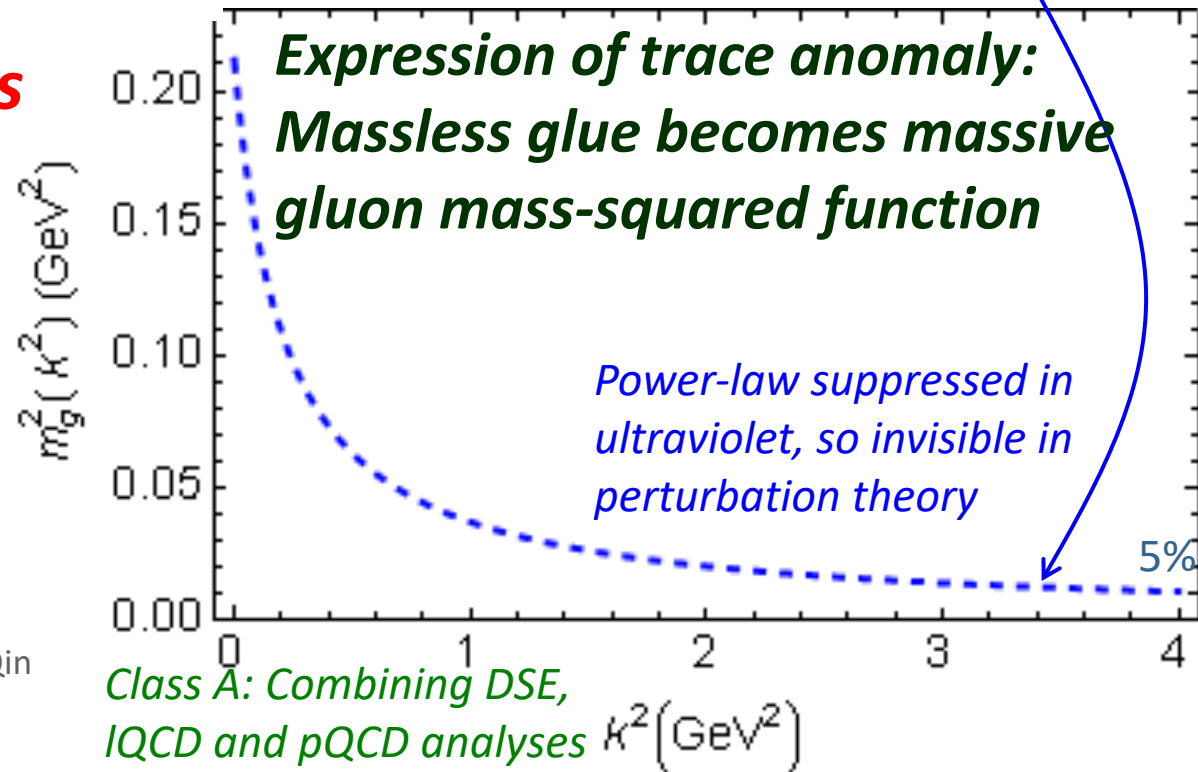
➤ Running gluon mass

$$d(k^2) = \frac{\alpha(\zeta)}{k^2 + m_g^2(k^2; \zeta)}$$

$$\alpha_s(0) = 2.77 \approx 0.9\pi, \quad m_g^2(0) = (0.46 \text{ GeV})^2$$

$$m_g^2(k^2) \approx \frac{\mu_g^4}{\mu_g^2 + k^2} \quad \mu_g \approx \frac{1}{2} m_p$$

- Gluons are **cannibals** – a particle species whose members become massive by eating each other!



Interaction model for the gap equation, S.-x. Qin et al., arXiv:1108.0603 [nucl-th], Phys. Rev. C **84** (2011) 042202(R) [5 pages]

Craig Roberts. Charting Hadronic Interiors (64p)



Massive Gauge Bosons!



- Gauge boson cannibalism
 - ... a new physics frontier ... within the Standard Model
- Asymptotic freedom means
 - ... ultraviolet behaviour of QCD is controllable
- Dynamically generated masses for gluons and quarks means that **QCD dynamically generates** its own **infrared cutoffs**
 - Gluons and quarks with
 - wavelength $\lambda > 1/\text{mass} \approx 0.5 \text{ fm}$
 - decouple from the dynamics ... **Confinement?!**
- How does that affect observables?
 - It will have an impact in any continuum study
 - Possibly (probably?) plays a role in gluon saturation ...
In fact, could be a harbinger of gluon saturation?

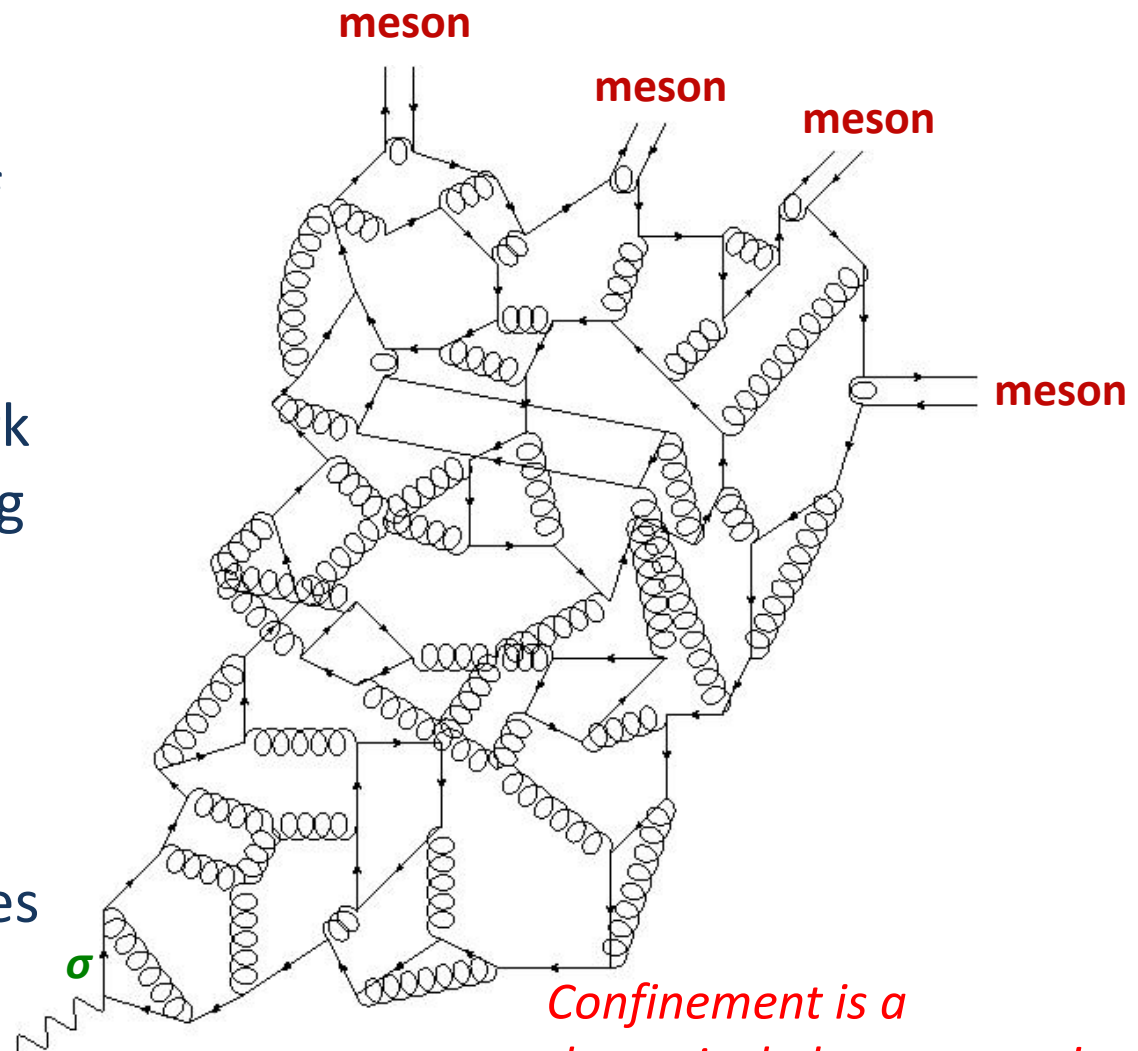
**Electron Ion Collider:
The Next QCD Frontier**



Confinement is dynamical

Quark Fragmentation

- A quark begins to propagate
- But after each “step” of length $\sigma \approx 1/m_g$, on average, an interaction occurs, so that the quark *loses* its identity, sharing it with other partons
- Finally, a cloud of partons is produced, which coalesces into colour-singlet final states

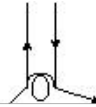


Confinement is a dynamical phenomenon!

Quark Fragmentation

➤ A quark begins to propagate

meson



meson



meson



➤ But length scales are so small that the identification of other particles is difficult

Confinement in hadron physics is largely a dynamical phenomenon, intimately connected with the fragmentation effect.

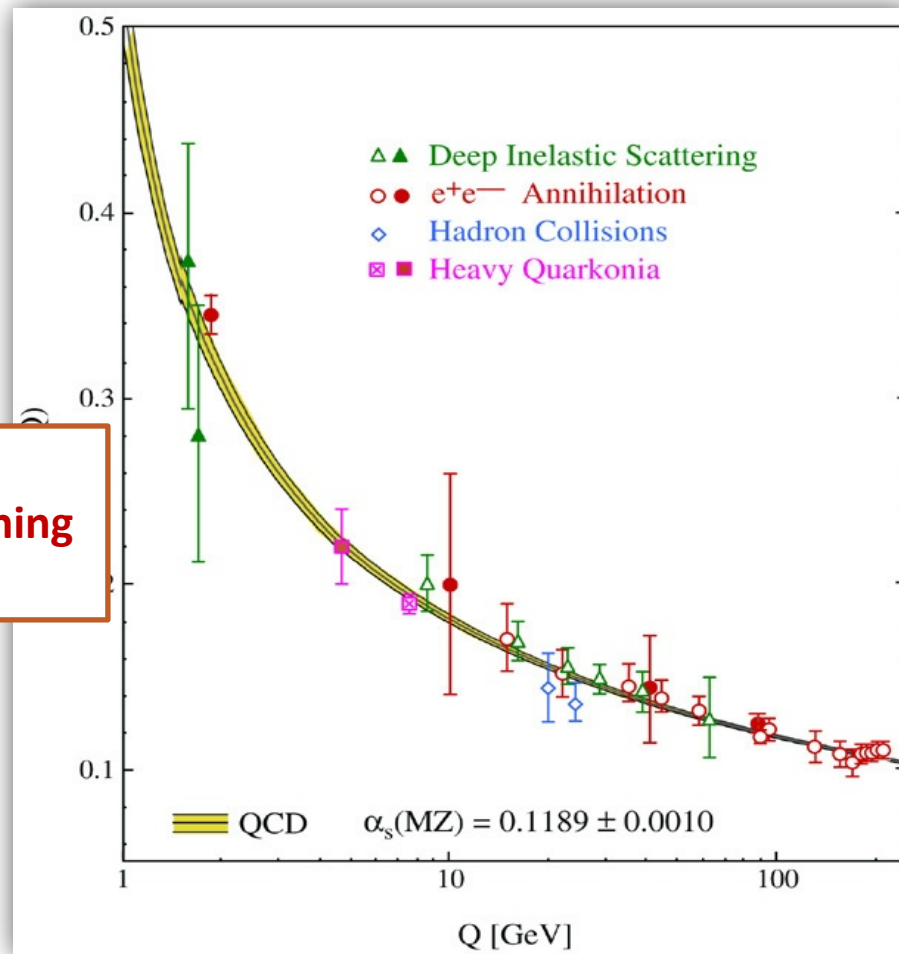
on

➤ Finally, partons are confined within colorless hadrons

It is unlikely to be comprehended without simultaneously understanding dynamical chiral symmetry breaking, which is the origin of a nearly-massless hadron (pion).



Confinement is a dynamical phenomenon!

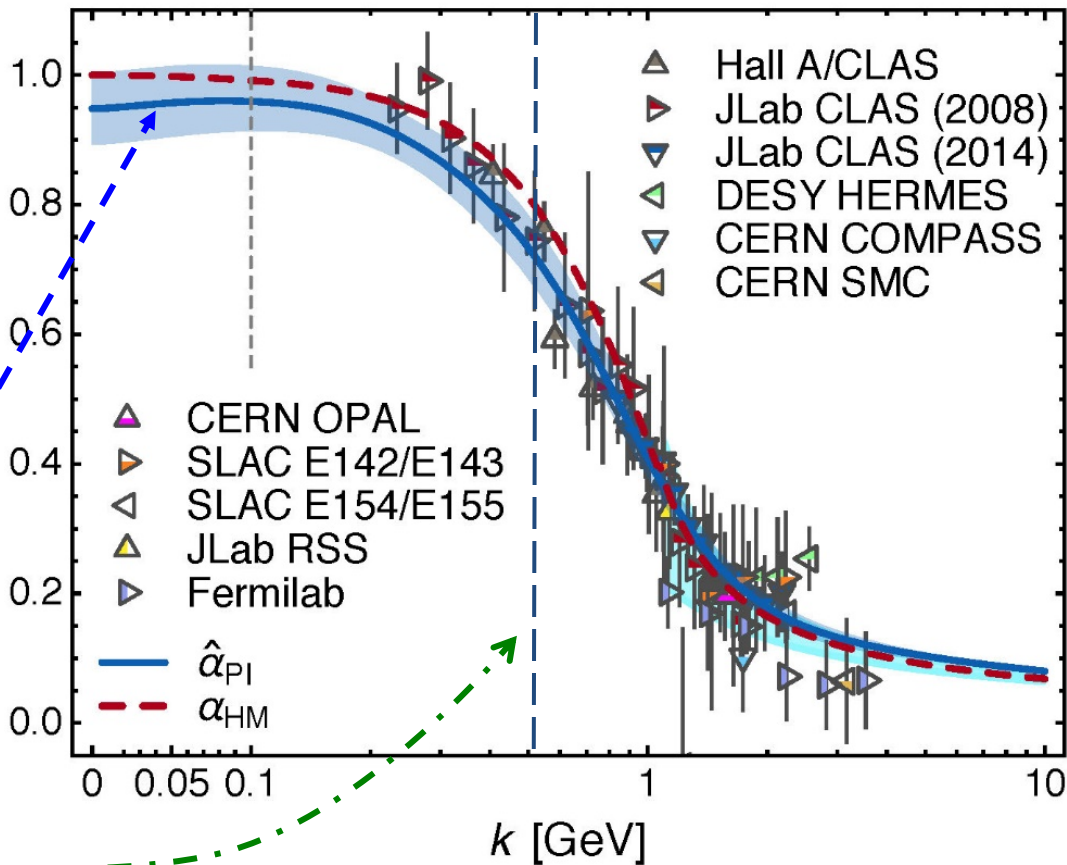


←
 What's happening
 out here?!

QCD's Running Coupling

Process-independent effective-charge in QCD

- Modern continuum & lattice methods for analysing gauge sector enable “Gell-Mann – Low” running charge to be defined in QCD
- Combined continuum and lattice analysis of QCD’s gauge sector yields a parameter-free prediction
- N.B. Qualitative change in $\hat{\alpha}_{PI}(k)$ at $k \approx \frac{1}{2} m_p$



- Near precise agreement between process-independent $\hat{\alpha}_{PI}$ and α_{g1} and $\hat{\alpha}_{PI} \approx \alpha_{HM}$

- Perturbative domain:

$$\alpha_{g1}(k^2) = \alpha_{\overline{MS}}(k^2)(1 + 1.14 \alpha_{\overline{MS}}(k^2) + \dots),$$

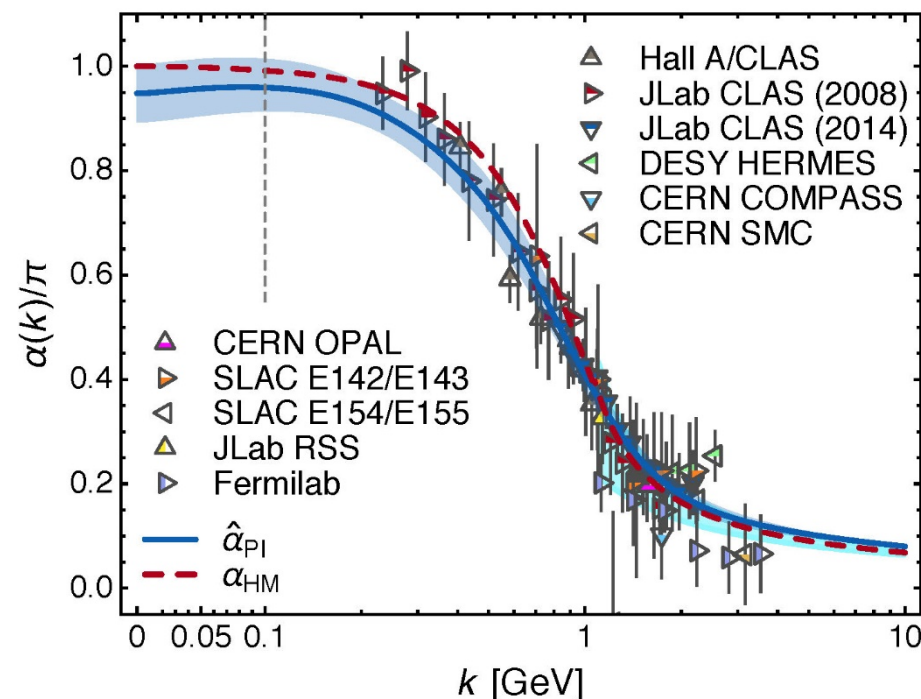
$$\hat{\alpha}_{PI}(k^2) = \alpha_{\overline{MS}}(k^2)(1 + 1.09 \alpha_{\overline{MS}}(k^2) + \dots),$$

$$\text{difference} = (1/20) \alpha_{\overline{MS}}^2$$

- Parameter-free prediction:

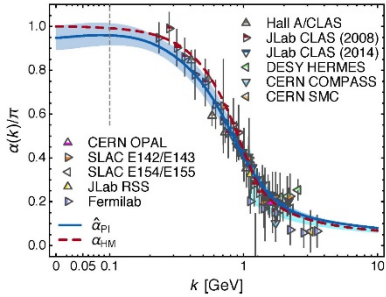
- curve completely determined by results obtained for gluon & ghost two-point functions using continuum and lattice-regularised QCD.

QCD Effective Charge



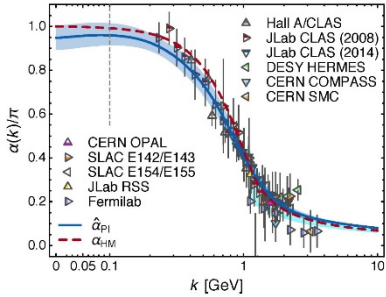
Data = process dependent effective charge:
 α_{g1} , defined via Bjorken Sum Rule

QCD Effective Charge



- $\hat{\alpha}_{PI}$ is a new type of effective charge
 - direct analogue of the Gell-Mann–Low effective coupling in QED, *i.e.* completely determined by the gauge-boson two-point function.
- $\hat{\alpha}_{PI}$ is
 - process-independent
 - appears in every one of QCD's dynamical equations of motion
 - known to unify a vast array of observables
- $\hat{\alpha}_{PI}$ possesses an infrared-stable fixed-point
 - Nonperturbative analysis demonstrating absence of a Landau pole in QCD
- QCD is IR finite, owing to dynamical generation of gluon mass-scale, which also serves to eliminate the Gribov ambiguity
- Asymptotic freedom \Rightarrow QCD is well-defined at UV momenta
- **QCD is therefore unique amongst known 4D quantum field theories**
 - **Potentially, defined & internally consistent at all momenta**

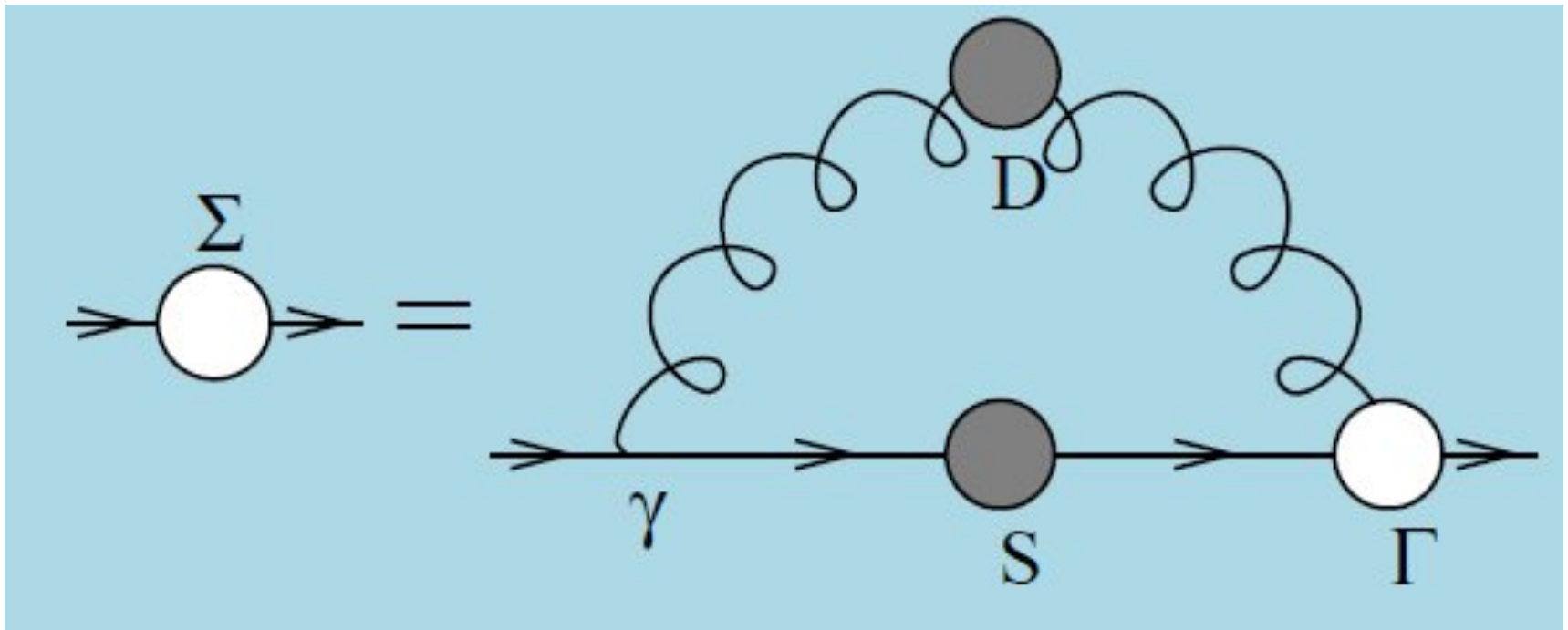
QCD Effective Charge



- $\hat{\alpha}_{PI}$ is a new type of effective charge
 - direct analogue of the Gell-Mann–Low effective coupling in QED, *i.e.* completely determined by the gauge boson self-energy equation.
- $\hat{\alpha}_{PI}$ is
 - pro
 - app
 - know
- $\hat{\alpha}_{PI}$ posse
 - Nonp
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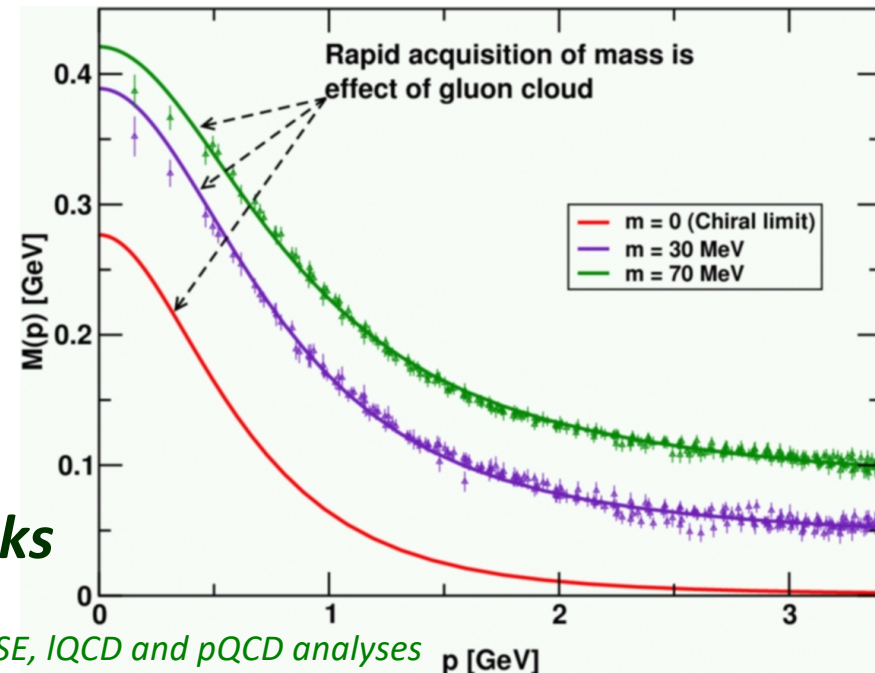
Conceivably, therefore, QCD can serve as a basis for theories that take physics beyond the Standard Model

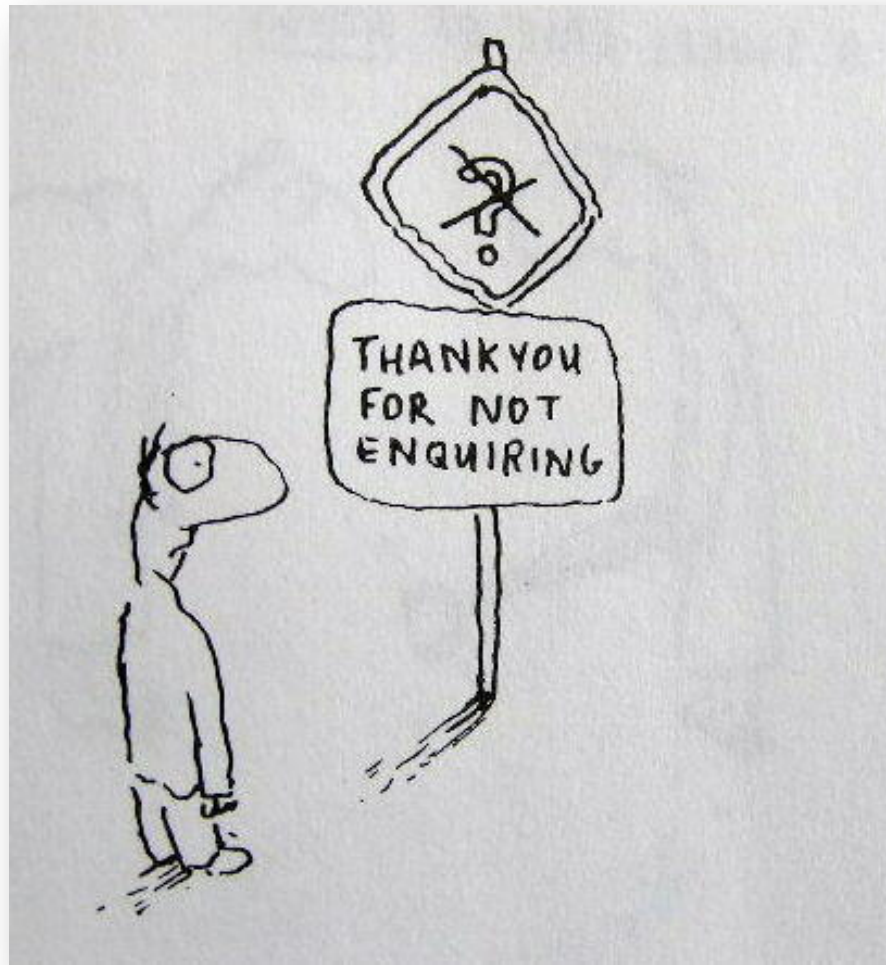
$$S(p) = \frac{Z(p^2)}{i\gamma \cdot p + M(p^2)}$$



Quark Gap Equation

- Dynamical chiral symmetry breaking (DCSB) is a key emergent phenomenon in QCD
- Expressed in hadron wave functions not in vacuum condensates
- Contemporary theory indicates that DCSB is responsible for more than 98% of the visible mass in the Universe; namely, given that classical massless-QCD is a conformally invariant theory, then DCSB is the origin of *mass from nothing*.
- **Dynamical**, not spontaneous
 - Add nothing to **QCD**,
No Higgs field, nothing!
Effect achieved purely through quark+gluon dynamics.
 - ✓ **Trace anomaly: massless quarks become massive**





Enigma of Mass

Pion's Goldberger-Treiman relation

- Pion's Bethe-Salpeter amplitude

Solution of the Bethe-Salpeter equation

$$\Gamma_{\pi^j}(k; P) = \tau^{\pi^j} \gamma_5 \left[iE_\pi(k; P) + \gamma \cdot P F_\pi(k; P) + \gamma \cdot k k \cdot P G_\pi(k; P) + \sigma_{\mu\nu} k_\mu P_\nu H_\pi(k; P) \right]$$

- Dressed-quark propagator $S(p) = \frac{1}{i\gamma \cdot p A(p^2) + B(p^2)}$

- Axial-vector Ward-Takahashi identity entails

$$f_\pi E_\pi(k; P = 0) = B(k^2)$$

Owing to DCSB
& Exact in
Chiral QCD

Miracle: two body problem solved, almost completely, once solution of one body problem is known

*Rudimentary version of this relation is
apparent in Nambu's Nobel Prize work*

**Model independent
Gauge independent
Scheme independent**

$$f_{\pi} E_{\pi}(p^2) = B(p^2)$$

The most fundamental
expression of Goldstone's
Theorem and PCAC

*Rudimentary version of this relation is
apparent in Nambu's Nobel Prize work*

Model independent
Gauge independent
Scheme independent

$$f_{\pi} E_{\pi}(p^2) \Leftrightarrow B(p^2)$$

Pion exists if, and only if,
mass is dynamically
generated

$$f_{\pi} E_{\pi}(p^2) = B(p^2)$$

This algebraic identity is why QCD's pion is massless in the chiral limit

Enigma of mass

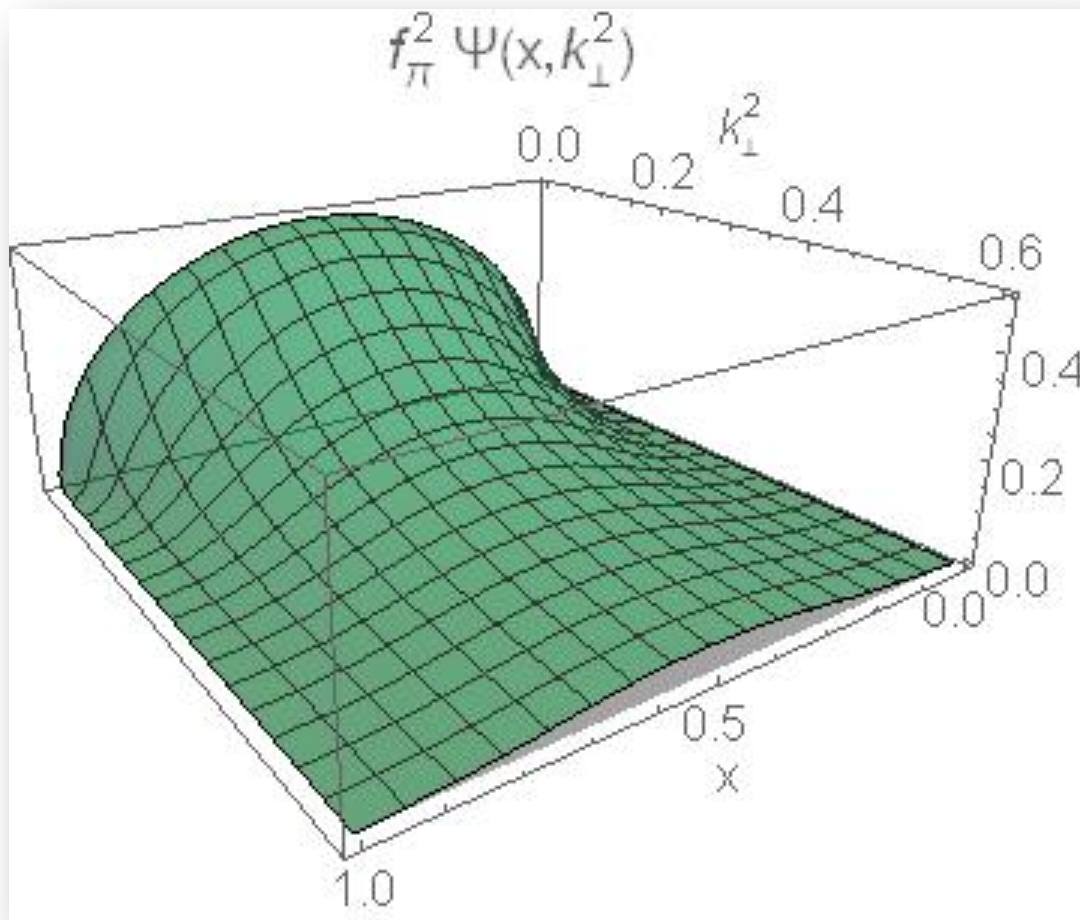


- The quark level Goldberger-Treiman relation shows that DCSB has a very deep and far reaching impact on physics within the strong interaction sector of the Standard Model; viz.,
 - Goldstone's theorem is fundamentally an expression of equivalence between the one-body problem and the two-body problem in the pseudoscalar channel.
- This emphasises that Goldstone's theorem has a pointwise expression in QCD
- Hence, pion properties are an almost direct measure of the dressed-quark mass function.
- Thus, enigmatically, the properties of the *massless* pion are the cleanest expression of the mechanism that is responsible for almost all the visible mass in the universe.





Observing Mass



Pion's Wave Function

Pion's valence-quark Distribution Amplitude

- Methods have been developed that enable direct computation of the pion's light-front wave function
- $\varphi_\pi(x)$ = twist-two parton distribution amplitude = projection of the pion's Poincaré-covariant wave-function onto the light-front

$$\varphi_\pi(x) = Z_2 \text{tr}_{CD} \int \frac{d^4 k}{(2\pi)^4} \delta(n \cdot k - x n \cdot P) \gamma_5 \gamma \cdot n S(k) \Gamma_\pi(k; P) S(k - P)$$

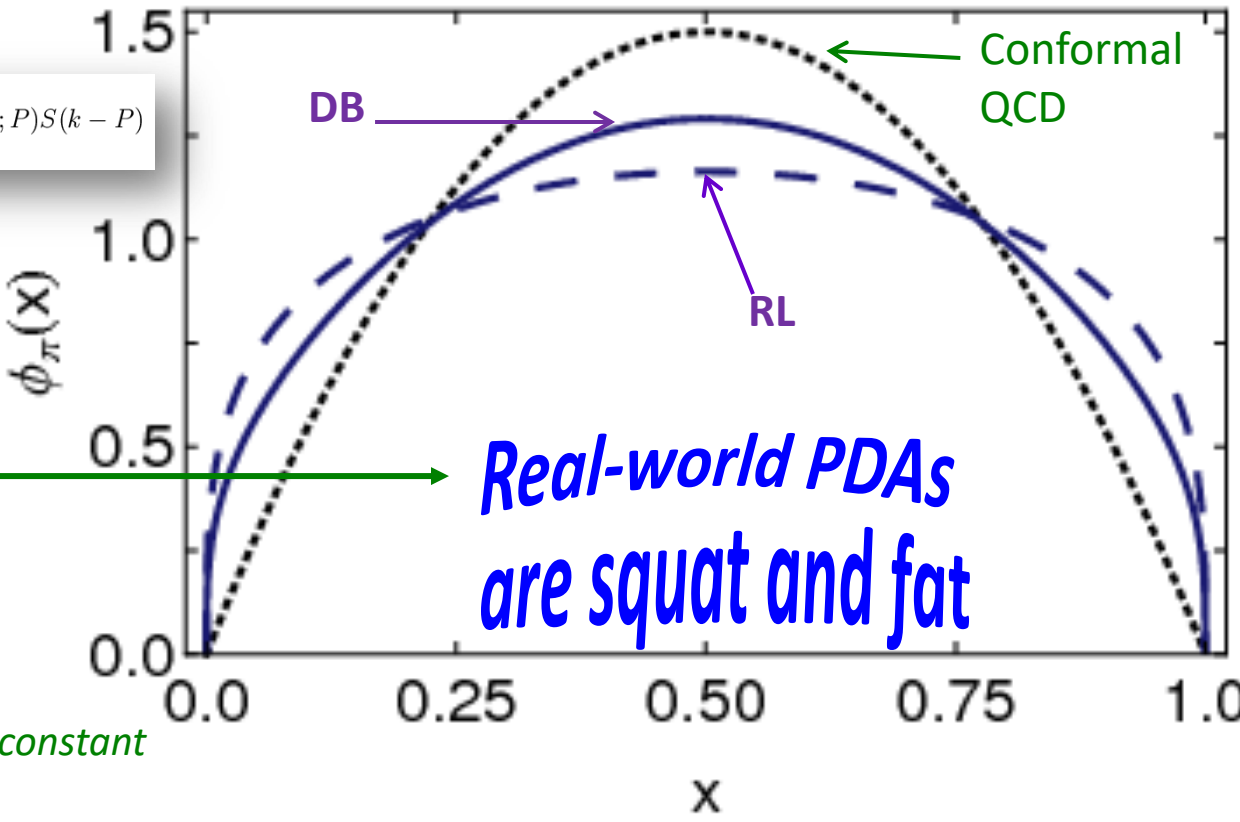
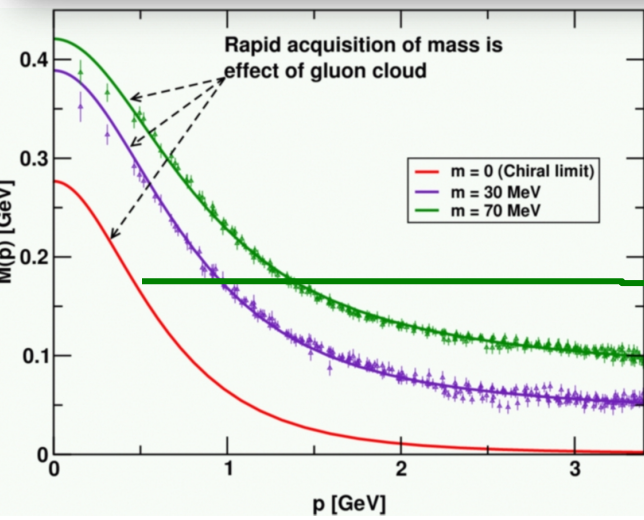
- Results have been obtained with the DCSB-improved DSE kernel, which unifies matter & gauge sectors

$$\varphi_\pi(x) \propto x^\alpha (1-x)^\alpha, \text{ with } \alpha \approx 0.5$$

Pion's valence-quark Distribution Amplitude

➤ Continuum-QCD prediction: marked broadening of $\phi_\pi(x)$, which owes to DCSB

$$\phi_\pi(x) = Z_2 \text{tr}_{CD} \int \frac{d^4k}{(2\pi)^4} \delta(n \cdot k - xn \cdot P) \gamma_5 \gamma \cdot n S(k) \Gamma_\pi(k; P) S(k - P)$$



A theory that produces $M(p)=\text{constant}$ also produces $\phi(x)=\text{constant}$

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Leading-twist PDAs of S-wave light-quark mesons

- End of a *long* story (longer than 30 years war)
- Continuum predictions that pion and kaon PDAs are broad, concave functions confirmed by simulations of lattice-regularised QCD
 - *Pion Distribution Amplitude from Lattice QCD*, Jian-Hui Zhang *et al.*, Phys.Rev. D95 (2017) 094514; 1702.00008
 - *Kaon Distribution Amplitude from Lattice QCD and the Flavor SU(3) Symmetry*, Jiunn-Wei Chen *et al.*, arXiv:1712.10025 [hep-ph]
 - *Pion and kaon valence-quark parton quasidistributions*, S.-S. Xu, L. Chang *et al.* arXiv:1802.09552 [nucl-th]
- Continuum analyses predict that these properties characterise the leading-twist PDAs of *all* S-wave light-quark mesons
- *Numerous empirically verifiable predictions*

Pion's electromagnetic form factor

A: Internally-consistent
DSE prediction

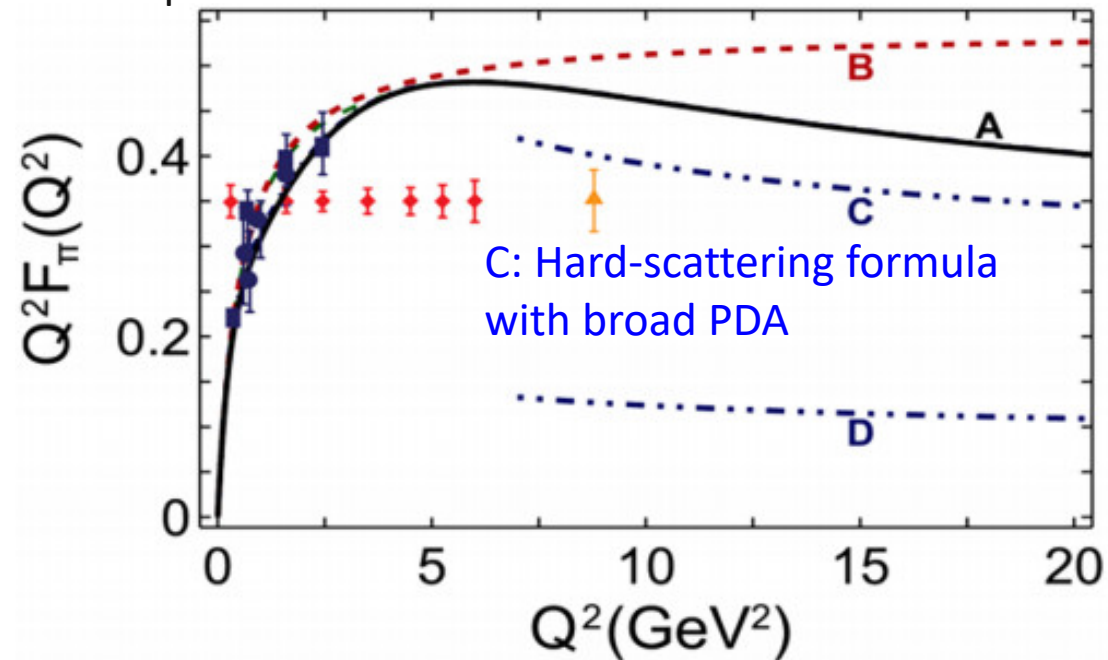


Figure 2.2: Existing (dark blue) data and projected (red, orange) uncertainties for future data on the pion form factor. The solid curve (A) is the QCD-theory prediction bridging large and short distance scales. Curve B is set by the known long-distance scale—the pion radius. Curves C and D illustrate calculations based on a short-distance quark-gluon view.

Pion's electromagnetic form factor

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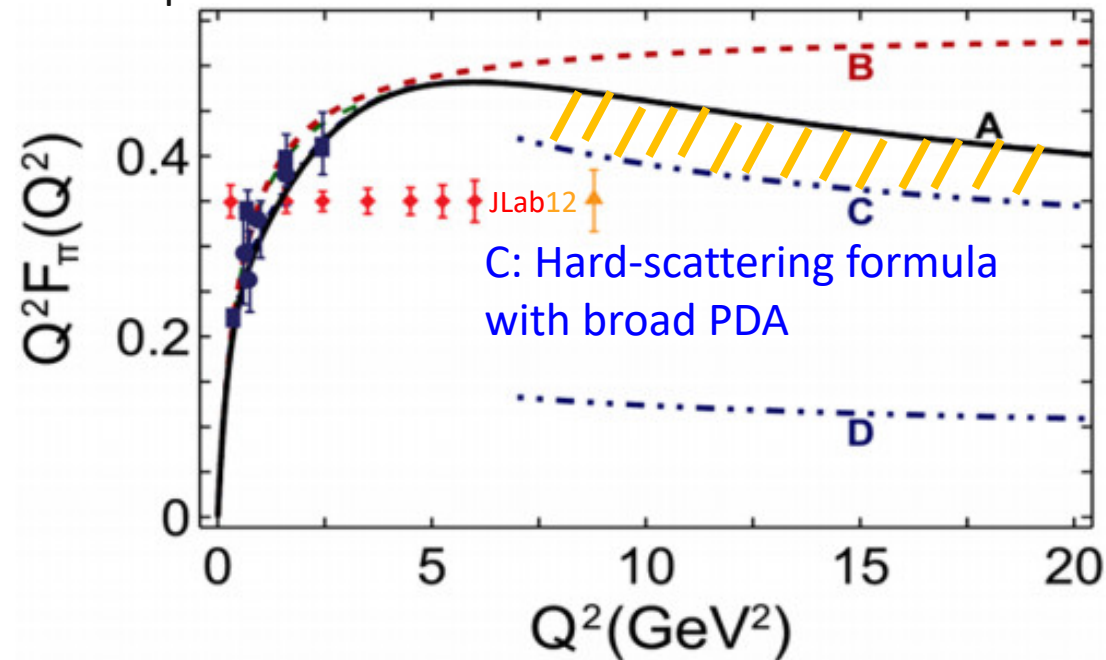


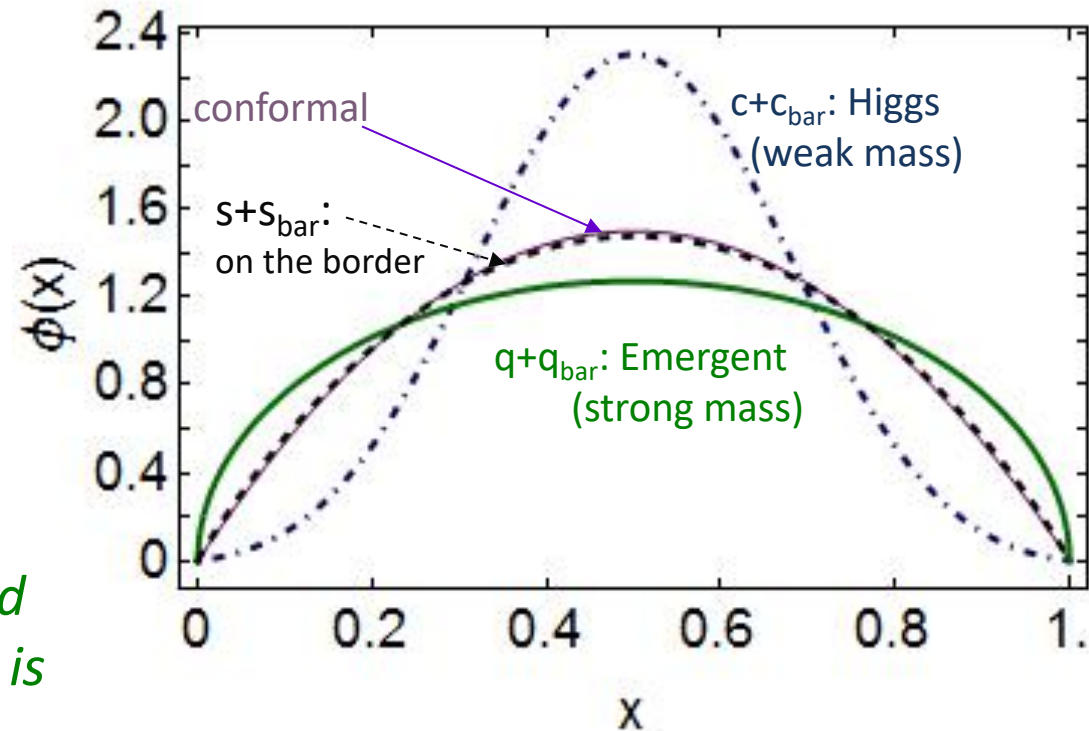
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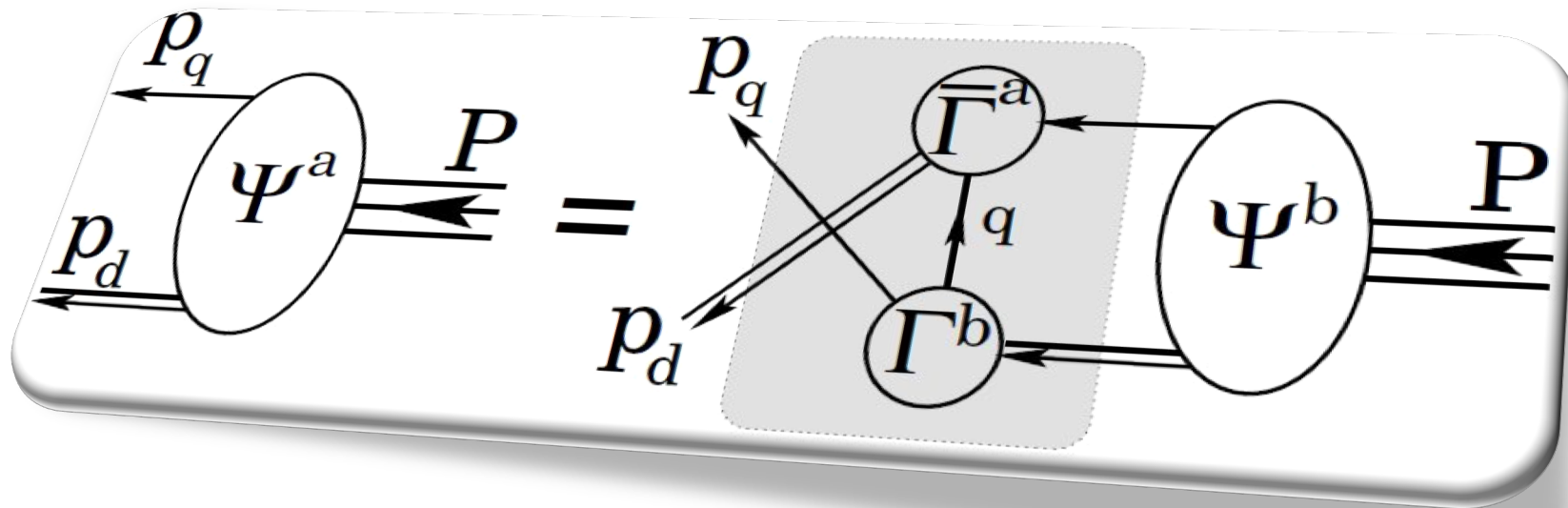
- Example:
PDA Broadening has enormous impact on understanding $F_\pi(Q^2)$
- Appears that JLab12 is within reach of first verification of a QCD hard-scattering formula

Unified with kaon ... Exposing strangeness: projections for kaon electromagnetic form factors, Fei Gao, L. Chang et al. Phys. Rev. D **96** (2017) 034024

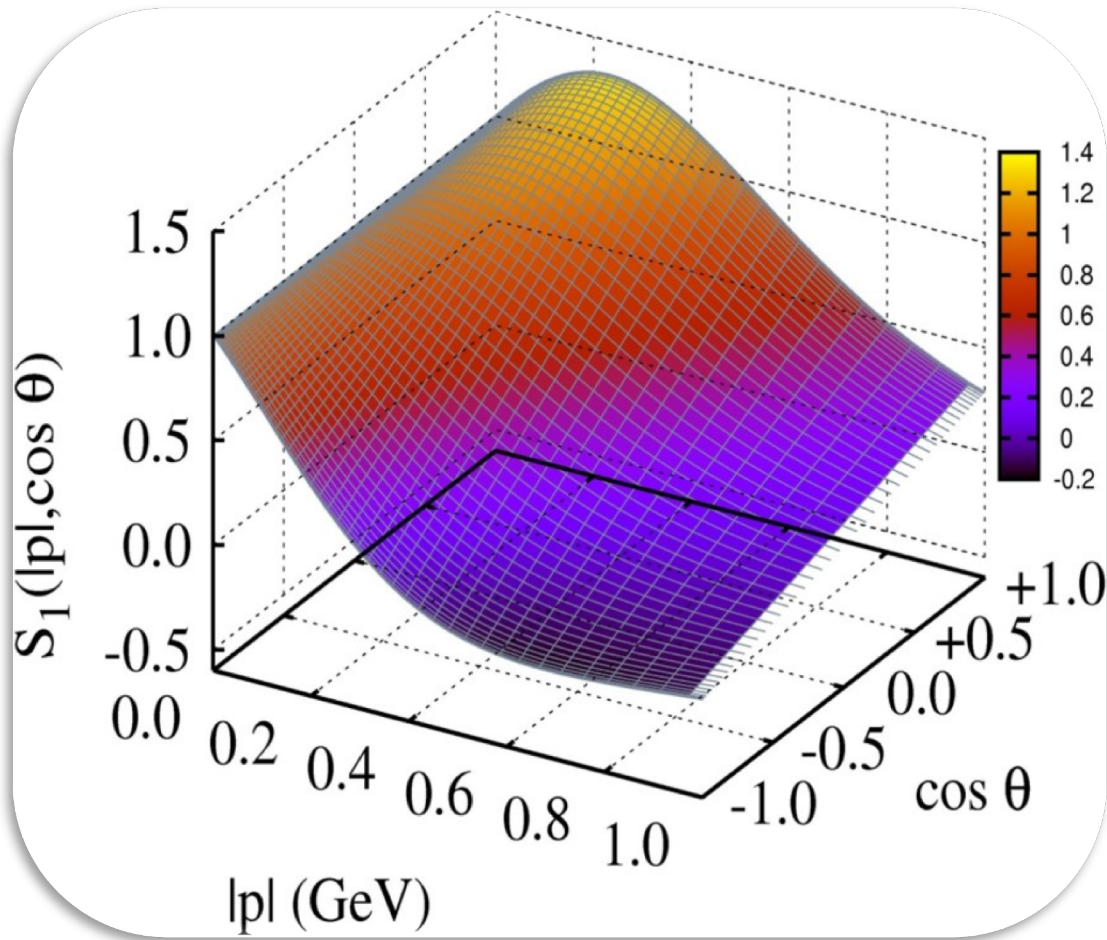
Emergent Mass vs. Higgs Mechanism

- When does Higgs mechanism begin to influence mass generation?
- limit $m_{\text{quark}} \rightarrow \infty$
 $\varphi(x) \rightarrow \delta(x-\frac{1}{2})$
- limit $m_{\text{quark}} \rightarrow 0$
 $\varphi(x) \sim (8/\pi) [x(1-x)]^{\frac{1}{2}}$
- Transition boundary lies just above m_{strange}
- *Comparison between distributions of light-quarks and those involving strange-quarks is good place to seek signals for strong-mass generation*





Structure of Baryons



Baryon Wave Functions

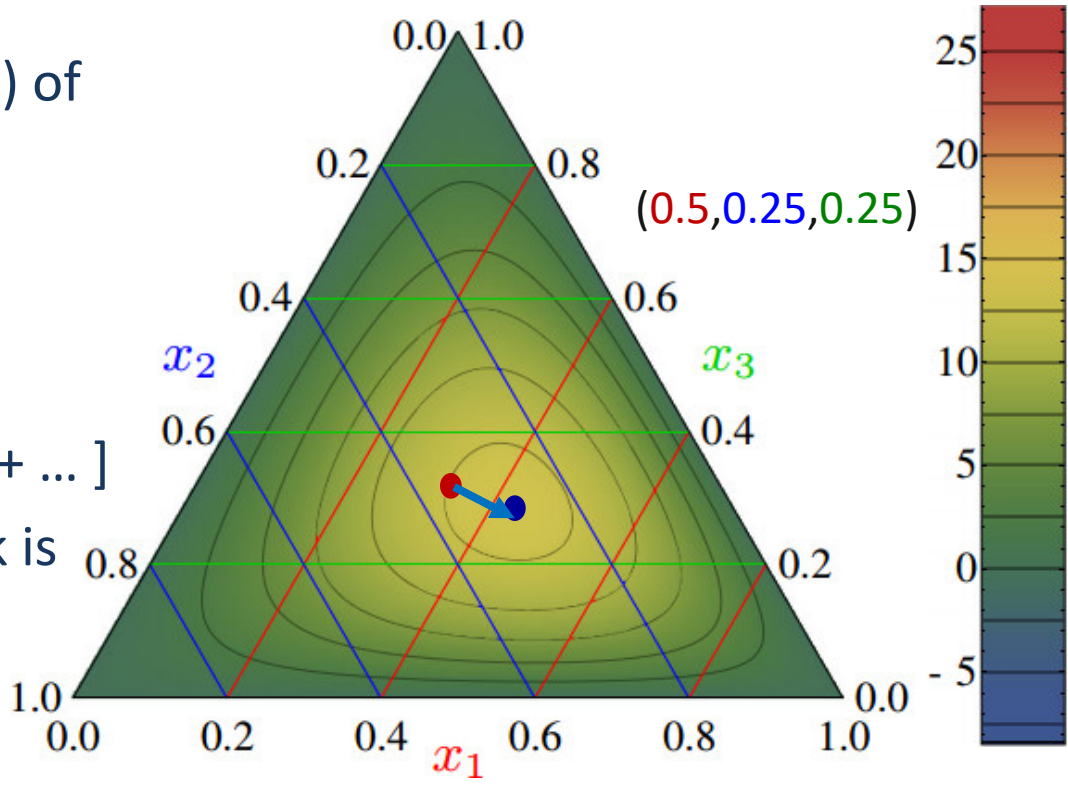
Nucleon PDAs & IQCD

Light-cone distribution amplitudes of the nucleon and negative parity nucleon resonances from lattice QCD
 V. M. Braun *et al.*, [Phys. Rev. D 89 \(2014\) 094511](#)
 Light-cone distribution amplitudes of the baryon octet
 G. S. Bali *et al.* [JHEP 1602 \(2016\) 070](#)

- First IQCD results for $n=0, 1$ moments of the leading twist PDA of the nucleon are available
- Used to constrain strength (a_{11}) of the leading-order term in a conformal expansion of the nucleon's PDA:

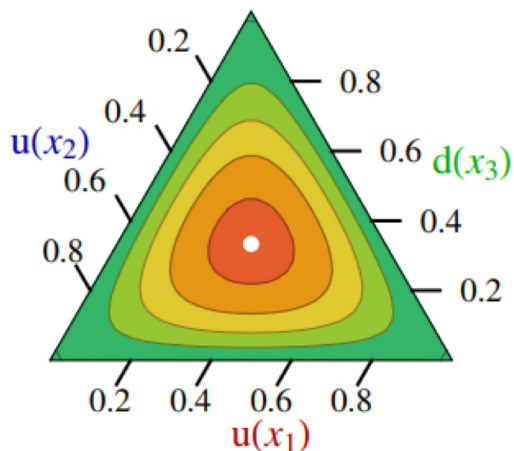
$$\Phi(x_1, x_2, x_3) = 120 x_1 x_2 x_3 [1 + a_{11} P_{11}(x_1, x_2, x_3) + \dots]$$

- Shift in location of central peak is consistent with existence of diquark correlations within the nucleon

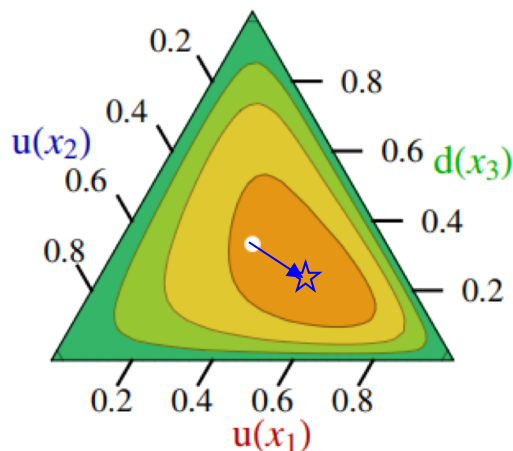


PDAs of Nucleon & its 1st Radial Excitation

- Methods used for mesons can be extended to compute pointwise behaviour of baryon PDAs



conformal

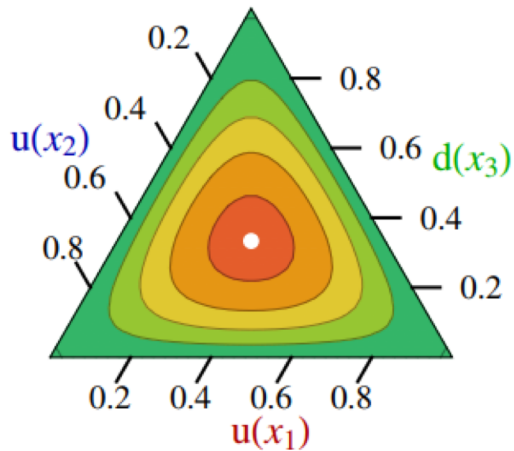


nucleon

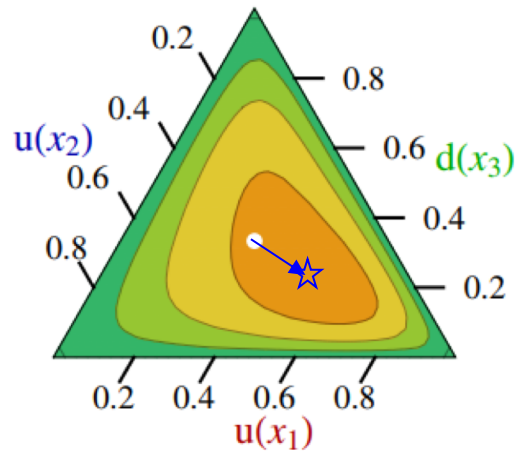
Diquark clustering skews the distribution toward the dressed-quark bystander, which therefore carries more of the proton's light-front momentum

PDAs of Nucleon & its 1st Radial Excitation

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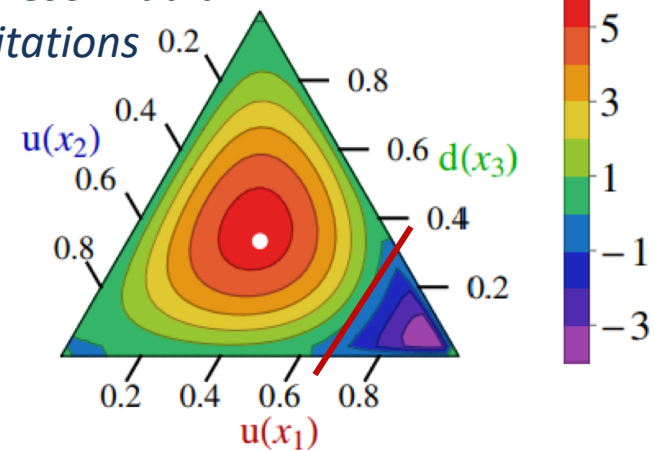
conformal



nucleon

Diquark clustering skews the distribution toward the dressed-quark bystander, which therefore carries more of the proton's light-front momentum

Just like QM & PDAs of meson radial excitations



Roper's quark core

Excitation's PDA is not positive definite ... there is a prominent locus of zeros in the lower-right corner of the barycentric plot

Diquark correlations in the nucleon

- Agreement between continuum and lattice results
 - ONLY when nucleon contains scalar & axial-vector diquark correlations
- Nucleon with only a scalar-diquark, omitting the axial-vector diquark, ruled-out by this confluence between continuum and lattice results

TABLE I. A – Eq. (13) interpolation parameters for the proton and Roper PDAs in Fig. 2. B – Computed values of the first four moments of the PDAs. Our error on f_N reflects a scalar diquark content of $65 \pm 5\%$; and values in rows marked with “ $\not\propto$ av” were obtained assuming the baryon is constituted solely from a scalar diquark. (All results listed at $\zeta = 2 \text{ GeV}$.)

A	$n_{\hat{\varphi}}$	α	β	w_{01}	w_{11}	w_{02}	w_{12}	w_{22}
p	65.8	1.47	1.28	0.096	0.094	0.15	-0.053	0.11
R	14.4	1.42	0.78	-0.93	0.22	-0.21	-0.057	-1.24

B	$10^3 f_N / \text{GeV}^2$	$\langle x_1 \rangle_u$	$\langle x_2 \rangle_u$	$\langle x_3 \rangle_d$
conformal PDA		0.333	0.333	0.333
lQCD [17]	2.84(33)	0.372(7)	0.314(3)	0.314(7)
lQCD [18]	3.60(6)	0.358(6)	0.319(4)	0.323(6)
herein proton	3.78(14)	0.379(4)	0.302(1)	0.319(3)
herein proton $\not\propto$ av	2.97	0.412	0.295	0.293
herein Roper	5.17(32)	0.245(13)	0.363(6)	0.392(6)
herein Roper $\not\propto$ av	2.63	0.010	0.490	0.500

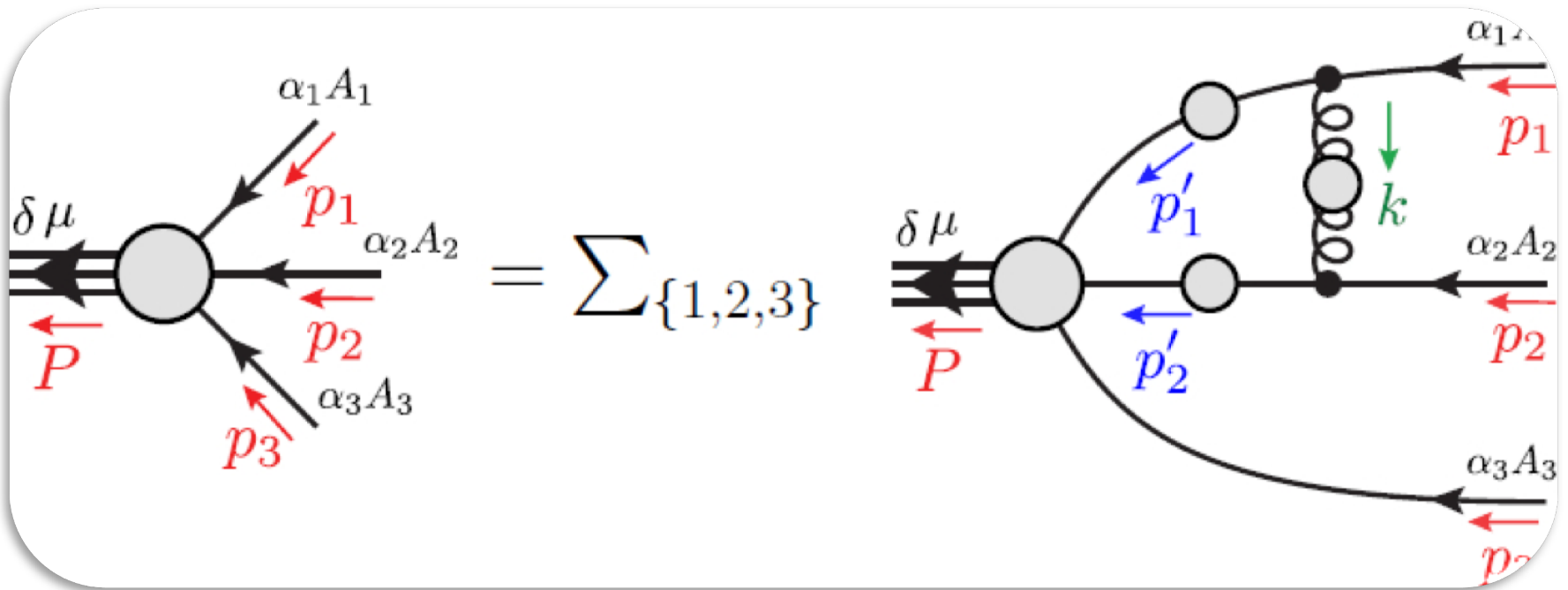
Parton distribution amplitudes: revealing diquarks in the proton and Roper resonance, Cédric Mezrag, Jorge Segovia, Lei Chang and Craig D. Roberts [arXiv:1711.09101 \[nucl-th\]](https://arxiv.org/abs/1711.09101)

Nucleon and Roper PDAs

No humps or bumps in leading-twist PDAs of ground-state S-wave baryons

- The proton's PDA is a broad, concave function
 - maximum shifted relative to peak in QCD's conformal limit expression
 - Magnitude of shift signals presence of both scalar & axial-vector diquark correlations in the nucleon
 - scalar generates around 60% of the proton's normalisation.
- The radial-excitation (Roper) is constituted similarly
 - Pointwise form of its PDA
 - Negative on a material domain
 - Is result of marked interferences between the contributions from both scalar and axial-vector diquarks
 - particularly, the locus of zeros, which highlights its character as a radial excitation.
- These features originate with the emergent phenomenon of dynamical chiral symmetry breaking in the Standard Model.





Heavy Baryons

Heavy Baryons

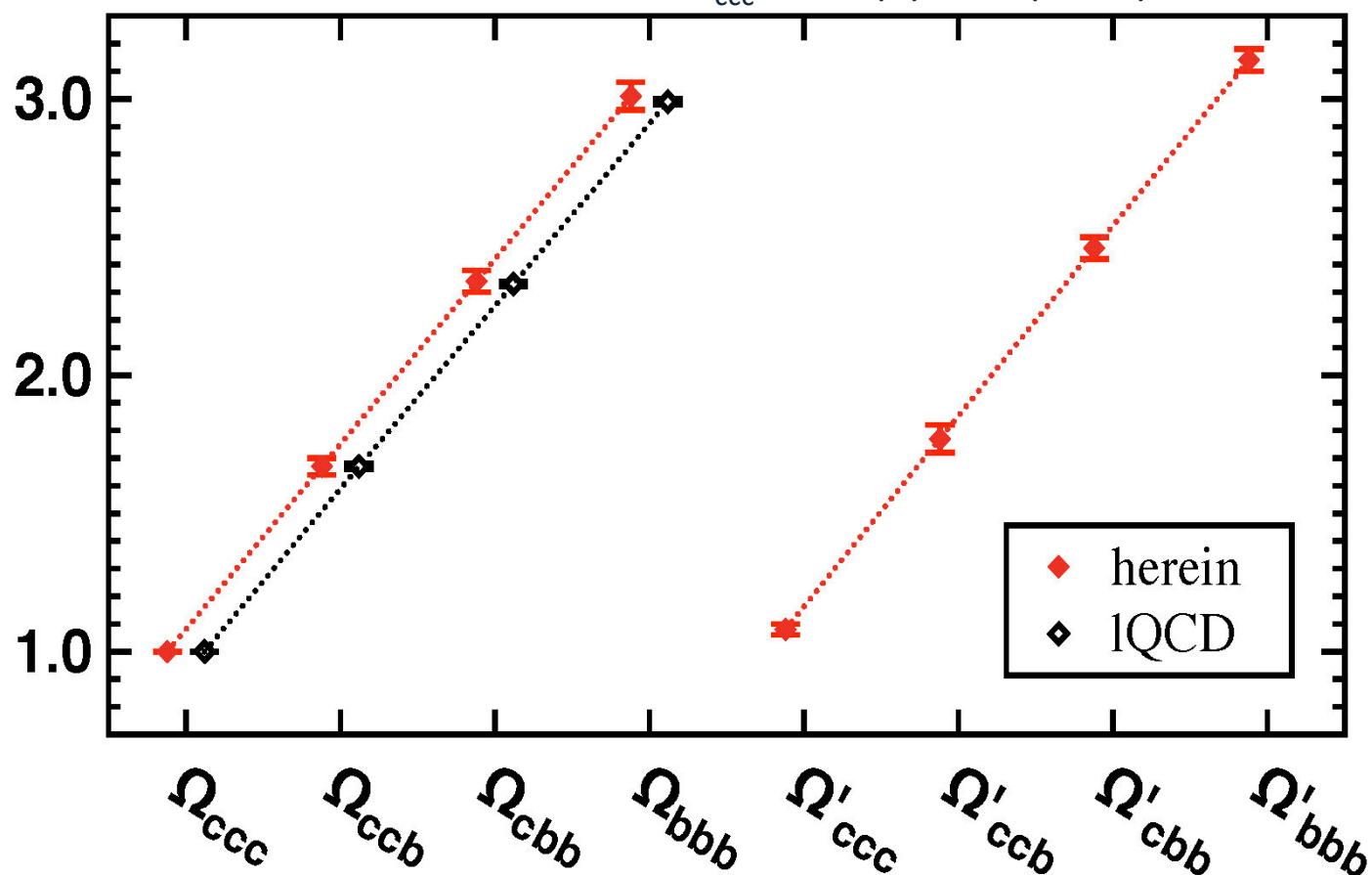
- Unified study of an array of mesons and baryons constituted from light- and heavy-quarks
 - Symmetry-preserving rainbow-ladder truncation of all relevant bound-state equations:
 - Gap equations
 - Bethe-Salpeter equations
 - and Faddeev-equations \Leftarrow *pioneered by Gernot Eichmann*
- Produced spectrum and decay constants of ground-state pseudoscalar- and vector-mesons:
 - $q' \bar{q}$ & $Q' \bar{Q}$, with $q', q = u, d, s$, $Q', Q = c, b$& masses of $J^P = 3/2^+$ qqq , QQQ ground state baryons and their first positive-parity excitations.

Triply Heavy Baryons

$\Omega_{ccc} = 4.76(7)$ GeV (RL DSE)

$\Omega_{ccc} = 4.80(2)$ GeV (IQCD)

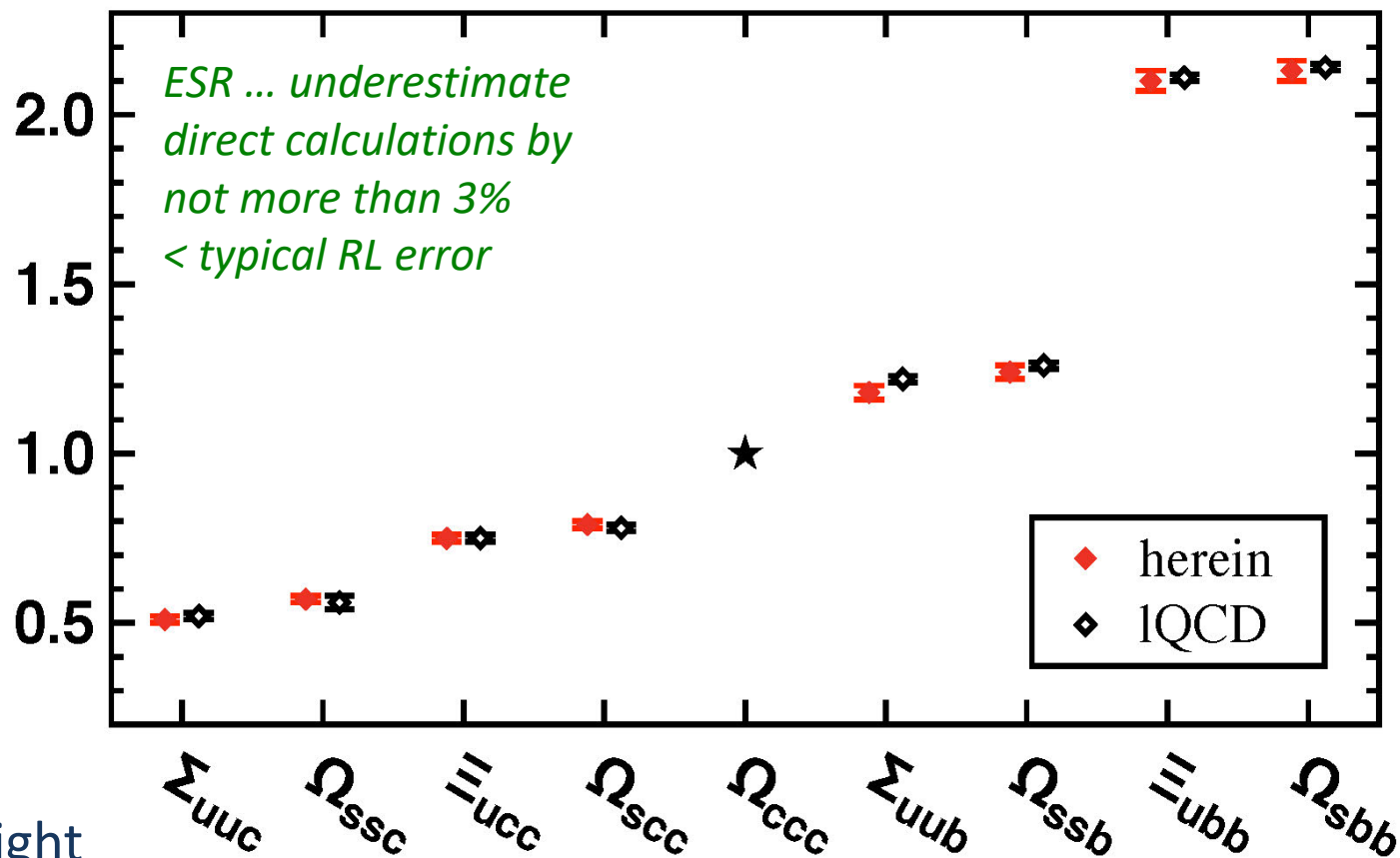
- Solved Faddeev equation in RL-truncation directly for $n=0,1$ ccc & bbb
- Used equal spacing rule (Gell-Mann+Okubo) for other states



IQCD = Z. S. Brown, W. Detmold, S. Meinel and K. Orginos, Phys. Rev. D 90, 094507 (2014).

Heavy Baryons

- Equal spacing rule provides sound estimates for
 - masses
 - decay constants
 of all systems considered



- Obvious in hindsight
 - ... QCD's interaction is flavour-independent
 - ... need only survey DSE studies of these observables in kindred systems

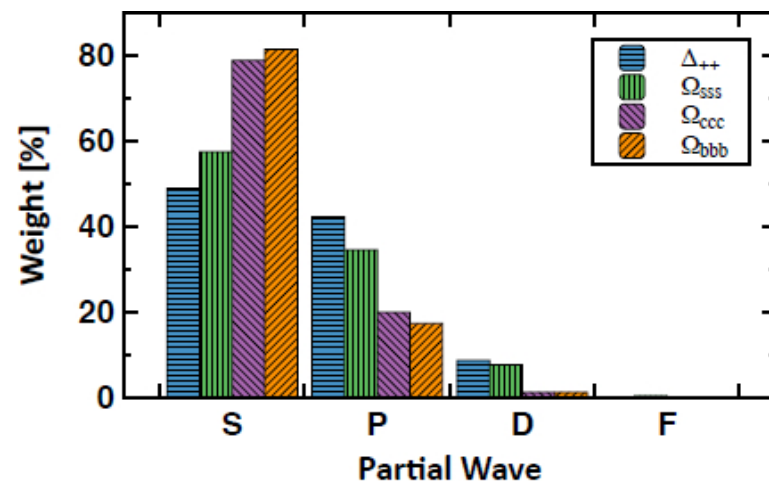
Heavy Baryons

➤ Analysed internal structure of the ground and first positive-parity excited states of qqq , QQQ

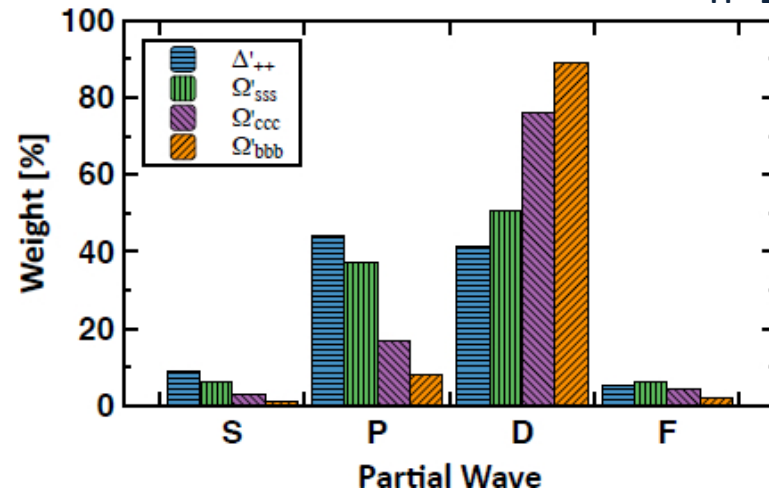
– Each system has a complicated angular momentum structure, e.g.

- Ground states
 - primarily S-wave
 - but each possesses P-, D- and F-wave components
 - P-wave fraction is large in the u and s -quark states;
- First positive-parity excitation
 - large D-wave component,
 - grows with increasing current-quark mass
 - but state also exhibits features consistent with a radial excitation.

$n=0$

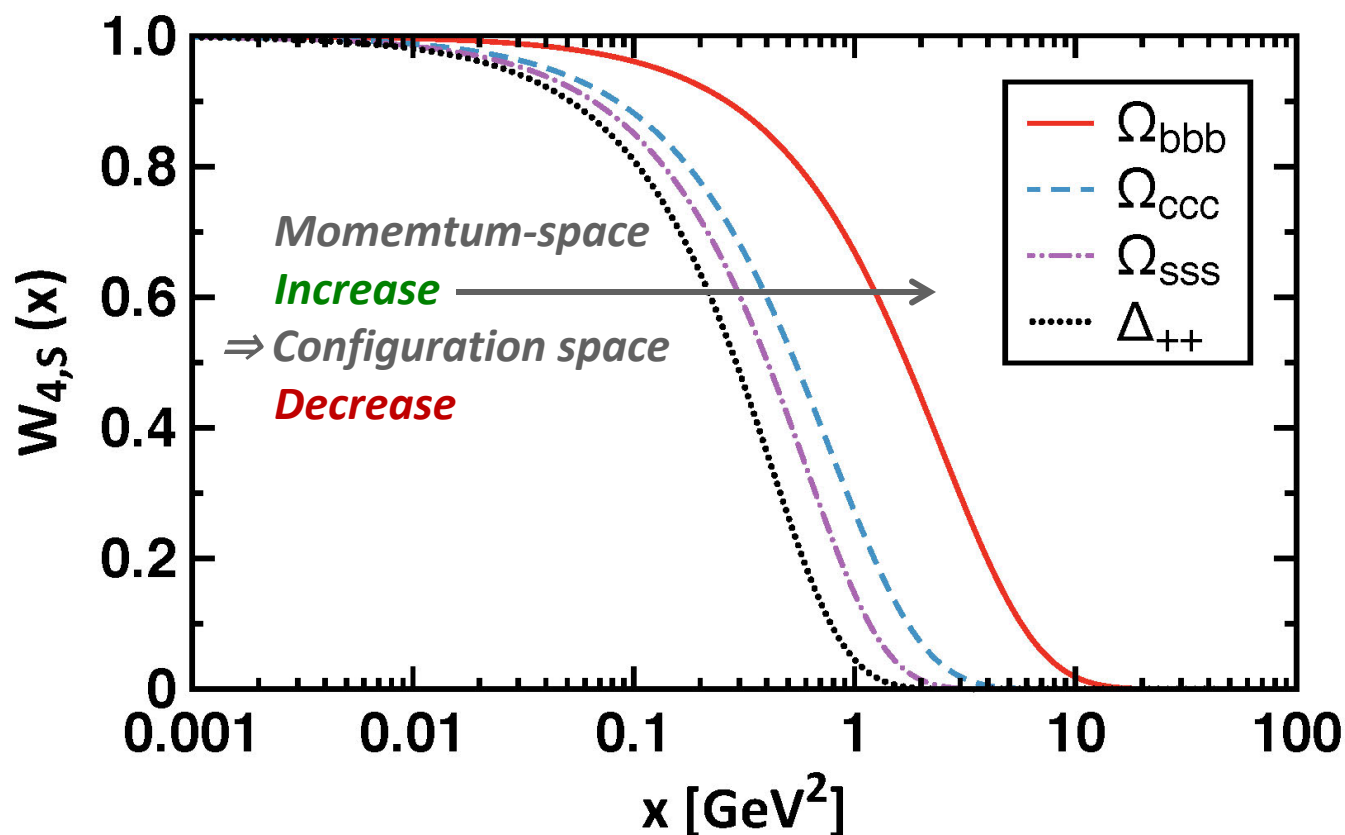


$n=1$



Heavy Baryons

➤ Pointwise behaviour of Faddeev wave functions
 ⇒ configuration space extent of such bound states *decreases* as the mass of the valence-quark constituents *increases*.



GLUEX
citations
periment

The logo for the GLUEX experiment. The word "GLUEX" is written in a stylized font. "GLUE" is in blue with a textured, crystalline appearance. "X" is in red with a similar textured appearance. To the right of "X", the words "citations" and "periment" are written in a red, sans-serif font, stacked vertically. A green wavy line is positioned between "citations" and "periment".

Hybrids & Exotics

New Window on Hybrids/Exotics

The diagram shows an equality between three Feynman diagrams. On the left is a tree-level vertex where a gluon (curly line) meets a quark (solid line) at a red circular vertex. This is equal to the sum of two diagrams. The first is the same tree-level vertex. The second is a loop diagram where a gluon line forms a loop with a quark line, and a box labeled 'C' is inserted into the quark line. Below the diagrams, the text reads: $C = 1\text{PI}$ gluon-quark scattering amplitude.

➤ Foundation:

Observation that one can represent the gluon-quark vertex in terms of a gluon-quark scattering amplitude

- Described in *Symmetry preserving truncations of the gap and Bethe-Salpeter equations*, Binosi, Chang, Papavassiliou, Qin, Roberts, [arXiv:1601.05441 \[nucl-th\]](https://arxiv.org/abs/1601.05441), Phys. Rev. D **93** (2016) 096010/1-7

➤ Exploiting this, one arrives at Faddeev equation for colour-singlet gluon+quark+antiquark bound-states

Hybrids/Exotics - Preliminary Results

Calc ⁿ /GeV	0 ⁺⁺	1 ⁺⁻	1 ⁻⁻	0 ⁺⁻	0 ⁻⁻
S.-S Xu et al. Rainbow Ladder	1.23	1.78	1.61	1.69	1.73
S.-S Xu <i>et al.</i> Faddeev	1.67	1.72	1.86	1.87	1.93
[1]	2.13	2.17	2.25	2.43	
[2]	2.1	1.9	2.3	2.3	

1. IQCD, $m_\pi > 0.4$ GeV ... Dudek *et al.* e-Print: [arXiv:1004.4930](https://arxiv.org/abs/1004.4930) [hep-ph]
2. Meyer and Swanson, e-Print: [arXiv:1502.07276](https://arxiv.org/abs/1502.07276) [hep-ph]

Remarks:

- ✓ Xu *et al.* is a beyond-rainbow-ladder (BRL) Faddeev equation calculation
 - ✓ BRL structure is essential to reproducing IQCD ordering of states
- ✓ Xu *et al.* masses are lower than IQCD.
 - Perhaps IQCD results too high because use inflated pion masses?
 - This is being studied.

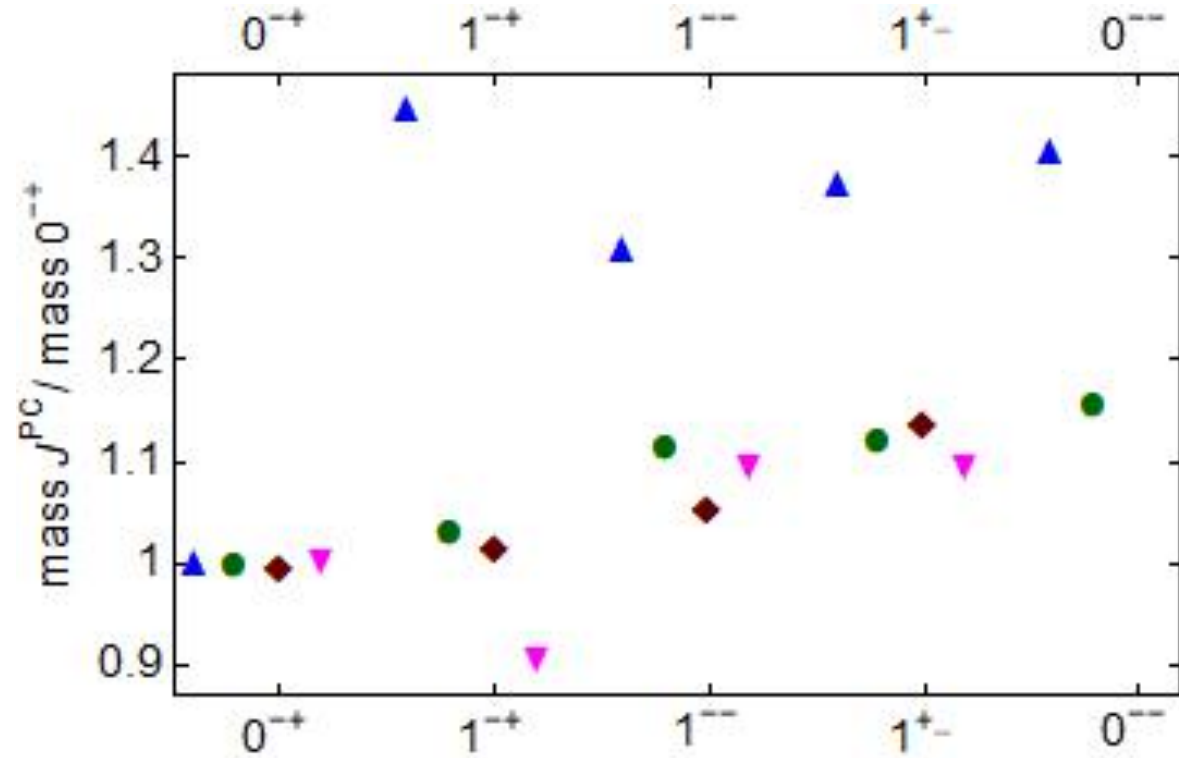
Hybrids/Exotics

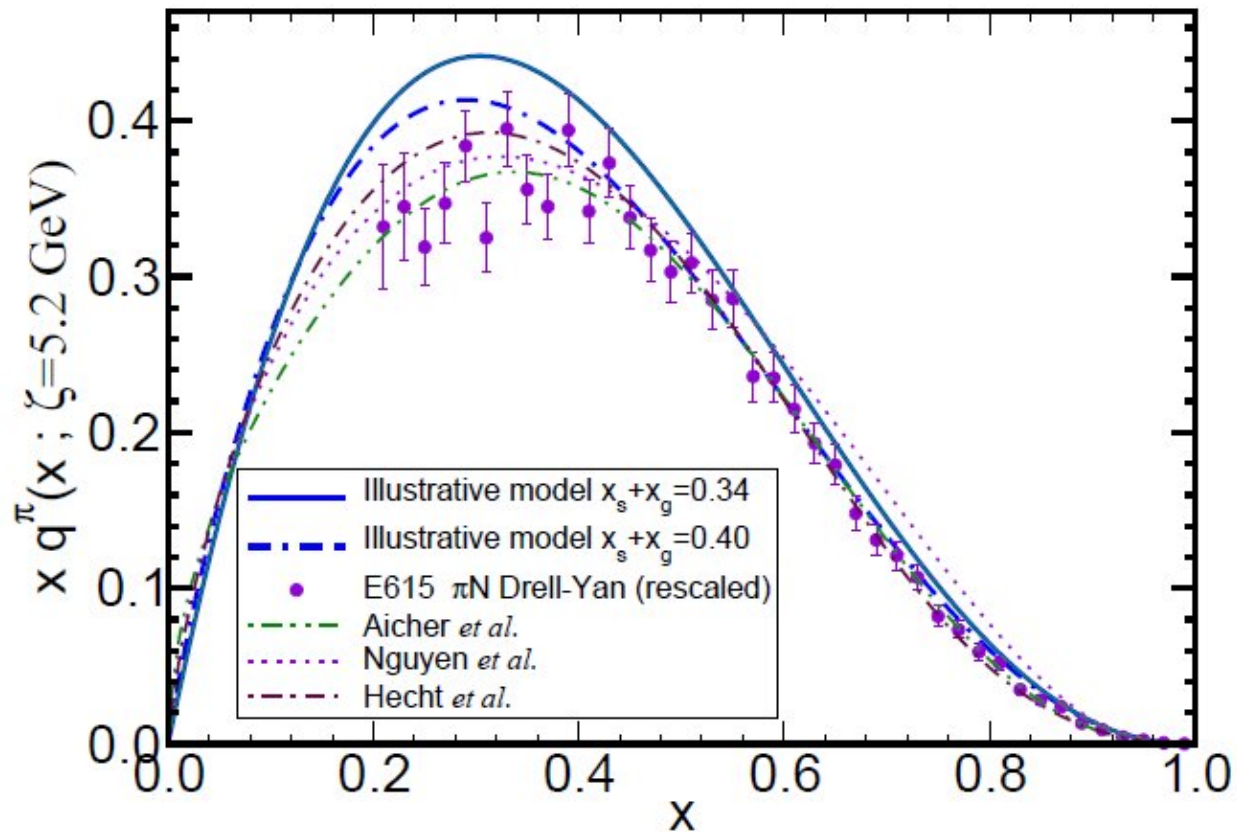
Preliminary Results

S.-S. Xu, L. Chang, J. Papavassiliou, C. D. Roberts, H.-S Zong

- Xu *et al.*, Faddeev
- ◆ Dudek, *et al.*, IQCD

✓ Only Faddeev (Xu *et al.*) produces spectrum with same ordering as IQCD





π & K Valence-quark Distribution Functions

π & K PDFs

- Experimental data on π & K PDFs obtained in mesonic Drell-Yan scattering from nucleons in heavy nuclei; but it's old: 1980-1989
- Newer data would be welcome:
 - persistent doubts about the Bjorken- $x \simeq 1$ behaviour of the pion's valence-quark PDF
 - single modest-quality measurement of $u^K(x)/u^\pi(x)$ cannot be considered definitive.
- Approved experiment, using tagged DIS at JLab 12, should contribute to a resolution of pion question; and a similar technique might also serve for the kaon.
- Future:
 - new mesonic Drell-Yan measurements at modern facilities could yield valuable information on π and K PDFs,
 - as could two-jet experiments at the large hadron collider;
 - **EIC would be capable of providing access to π and K PDFs through measurements of forward nucleon structure functions.**
- Gribov-Lipatov reciprocity (crossing symmetry) entails connection between PDFs and fragmentation functions on $z \simeq 1$ ($z \geq 0.75$)

$$D_{H/q}(z) \approx z q^H(z)$$

Reliable information on meson fragmentation functions is critical if the worldwide programme aimed at determining TMDs is to be successful

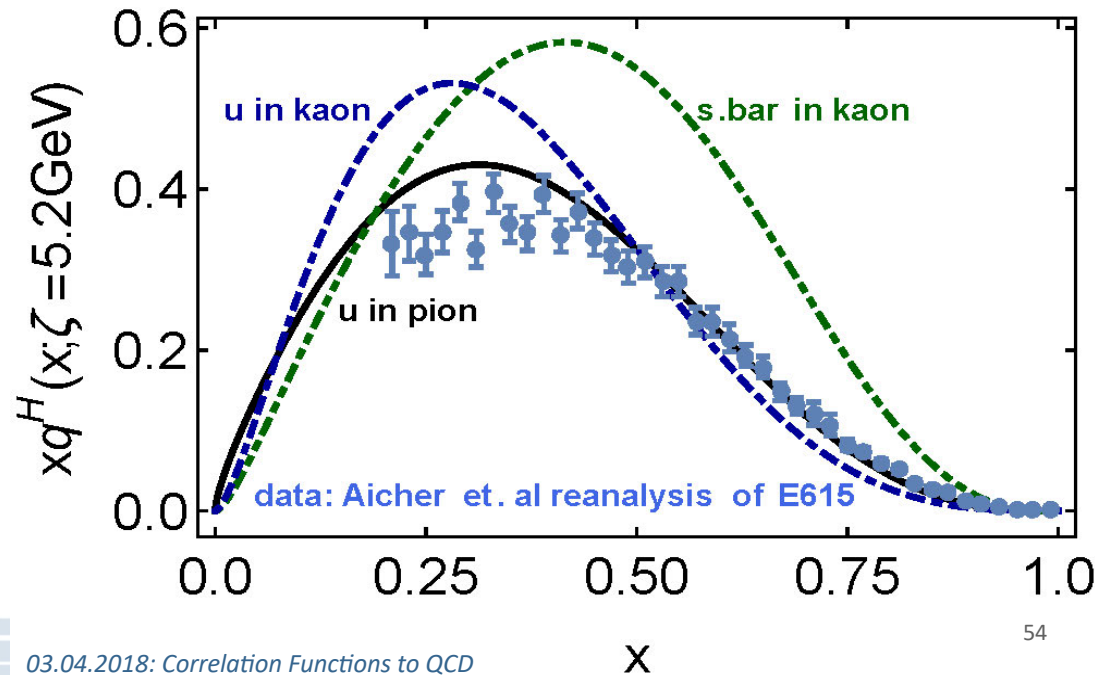
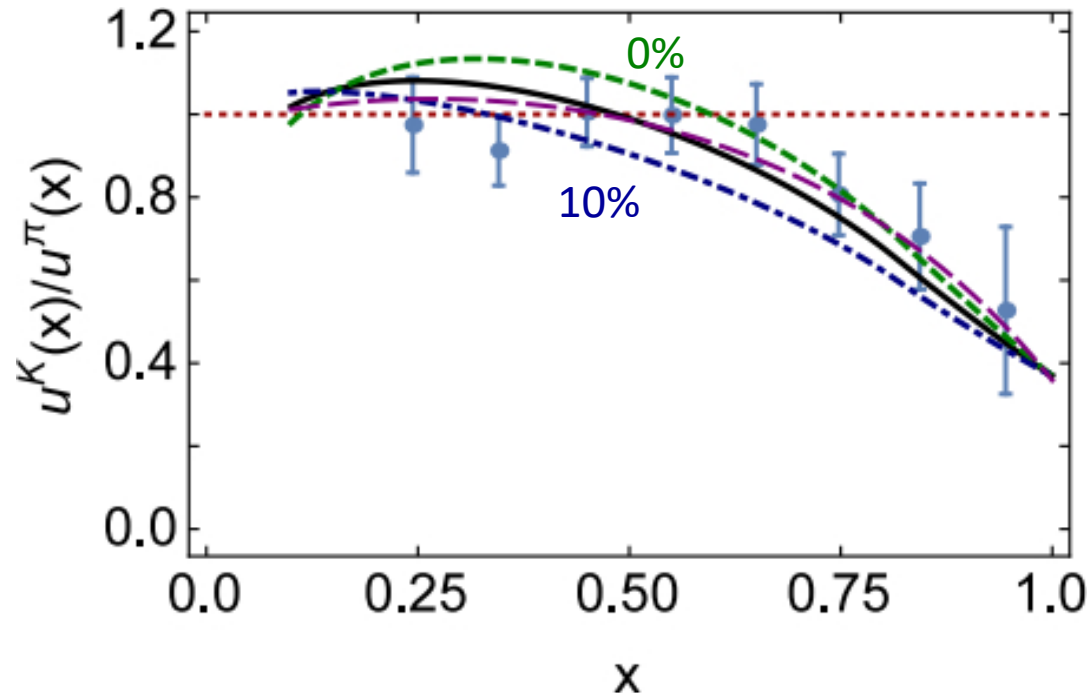
Kaon's gluon content

- $\langle x \rangle_g^K(\zeta_H) = 0.05 \pm 0.05$
 \Rightarrow Valence quarks carry 95% of kaon's momentum at ζ_H
- DGLAP-evolved to ζ_2

q	$\langle x \rangle_q^K$	$\langle x^2 \rangle_q^K$	$\langle x^3 \rangle_q^K$
u	0.28	0.11	0.048
\bar{s}	0.36	0.17	0.092

Valence-quarks carry $\frac{2}{3}$ of kaon's light-front momentum

Cf. Only $\frac{1}{2}$ for the pion



π & K PDFs

- Marked differences between π & K gluon content
 - ζ_H :
 - Whilst $\frac{1}{3}$ of pion's light-front momentum carried by glue
 - *Only* $\frac{1}{20}$ of the kaon's light-front momentum lies with glue
 - $\zeta_2^2 = 4 \text{ GeV}^2$
 - Glue carries $\frac{1}{2}$ of pion's momentum and $\frac{1}{3}$ of kaon's momentum
 - Evident in differences between large- x behaviour of valence-quark distributions in these two mesons
- Signal of Nambu-Goldstone boson character of π
 - Nearly complete cancellation between one-particle dressing and binding attraction in this almost massless pseudoscalar system
$$2 \text{ Mass}_Q + U_g \approx 0$$



π & K PDFs

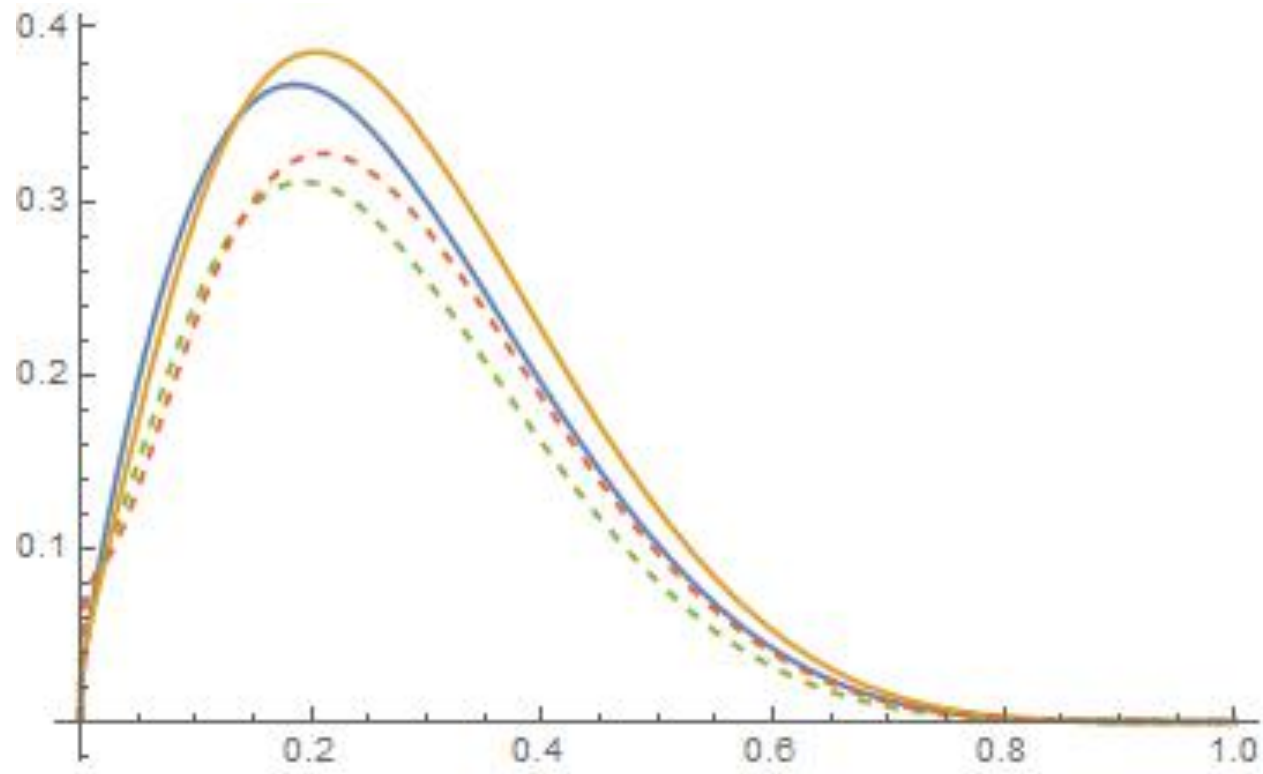
- Existing textbook description of Goldstone's theorem via pointlike modes is *outdated* and *simplistic*

π & K PDFs

- The appearance of Nambu-Goldstone modes in the Standard Model is far more interesting
 - Nambu-Goldstone modes are nonpointlike!
 - Intimately connected with origin of mass!
 - Possibly/Probably(?) inseparable from expression of confinement!
- Difference between gluon content of π & K is measurable ... using well-designed EIC
- Write a definitive new chapter in future textbooks on the Standard Model



**Electron Ion Collider:
The Next QCD Frontier**



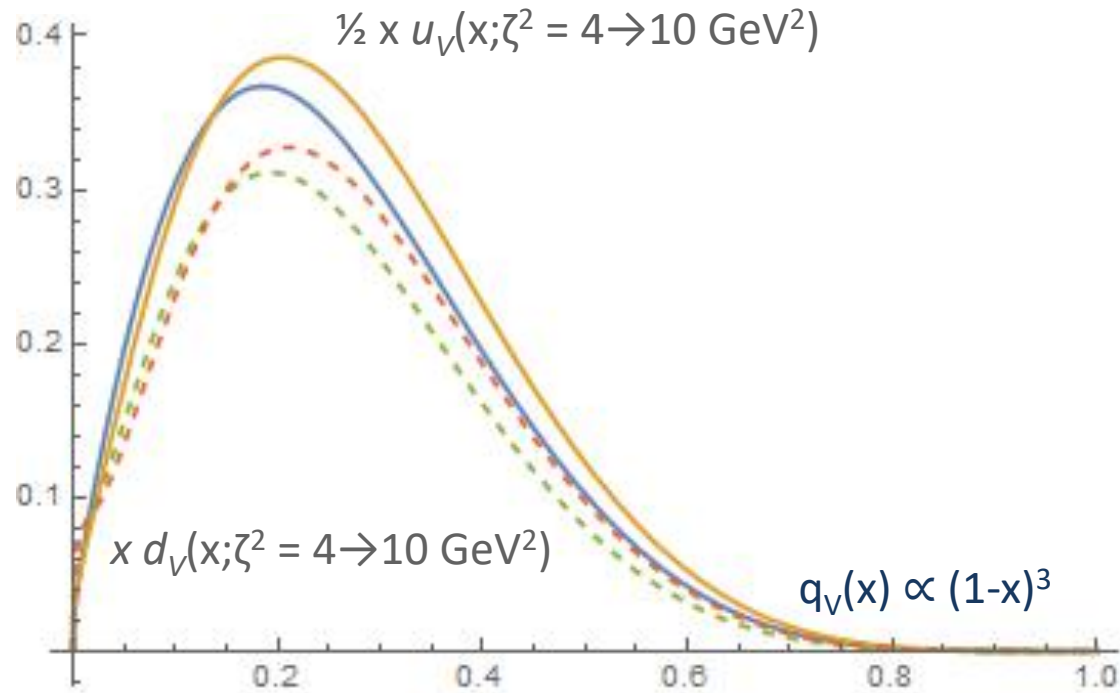
Proton Valence-quark Distribution Functions

Craig Roberts. Charting Hadronic Interiors (64p)



Proton valence-quark PDFs

- ✓ Methods used for mesons can be generalised to baryons
- ✓ Yield pointwise form for $u(x)$ & $d(x)$ in proton
 - ✓ $x \simeq 1$: $q_V(x) \propto (1-x)^3$
- ✓ Relative strength $0^+ : 1^+$ determines
 - ✓ shift in location and size of peaks: $d_V(x)$ compared with $u_V(x)$
 - ✓ $d_V(x)/u_V(x)$ on $x \simeq 1$



$$\langle x u_V(x; \zeta_4^2) \rangle = 0.32$$

$$\langle x d_V(x; \zeta_4^2) \rangle = 0.13$$

$$\langle x u_V(x; \zeta_4^2) + x d_V(x; \zeta_4^2) \rangle = 0.45$$

Ratio of proton valence-quark PDFs

✓ Value of

$$d_V(x)/u_V(x)|_{x=1}$$

is fixed under

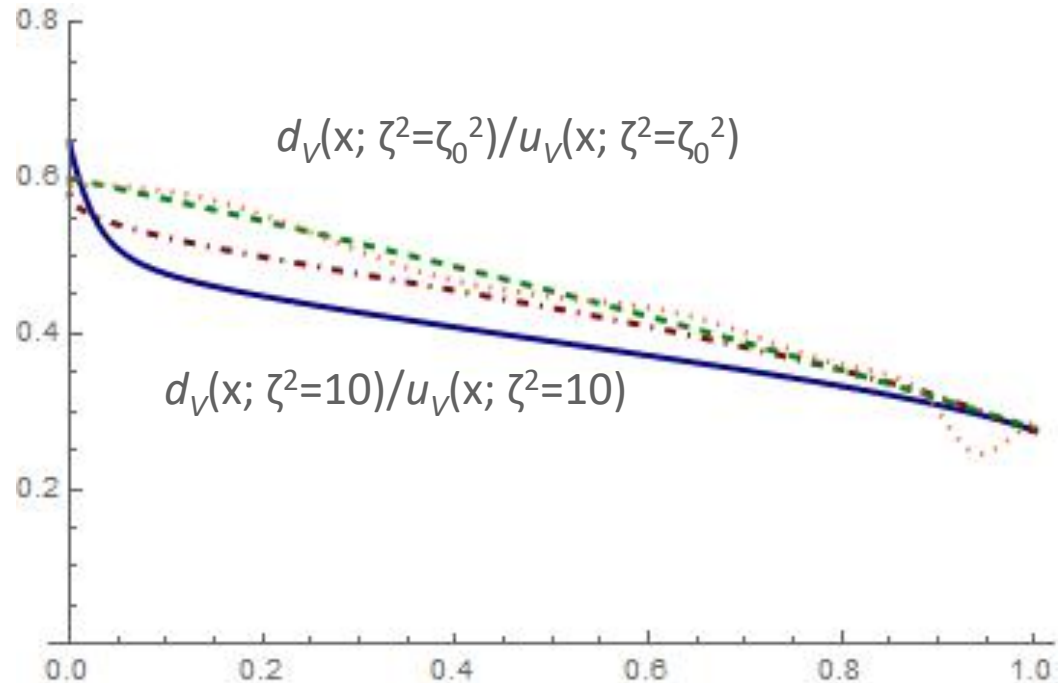
DGLAP evolution

✓ Without axial-vector diquarks,

$$d_V(x)/u_V(x)|_{x=1} \approx 0$$

✓ Prediction derived from Faddeev amplitude that produces nucleon PDA

✓ $d_V(x)/u_V(x)|_{x=1} = 0.28$



Ratio of proton valence-quark PDFs

✓ Value of

$$d_V(x)/u_V(x)|_{x=1}$$

is fixed under DGLAP evolution

✓ Without axial-vector diquarks,

$$d_V(x)/u_V(x)|_{x=1} \approx 0$$

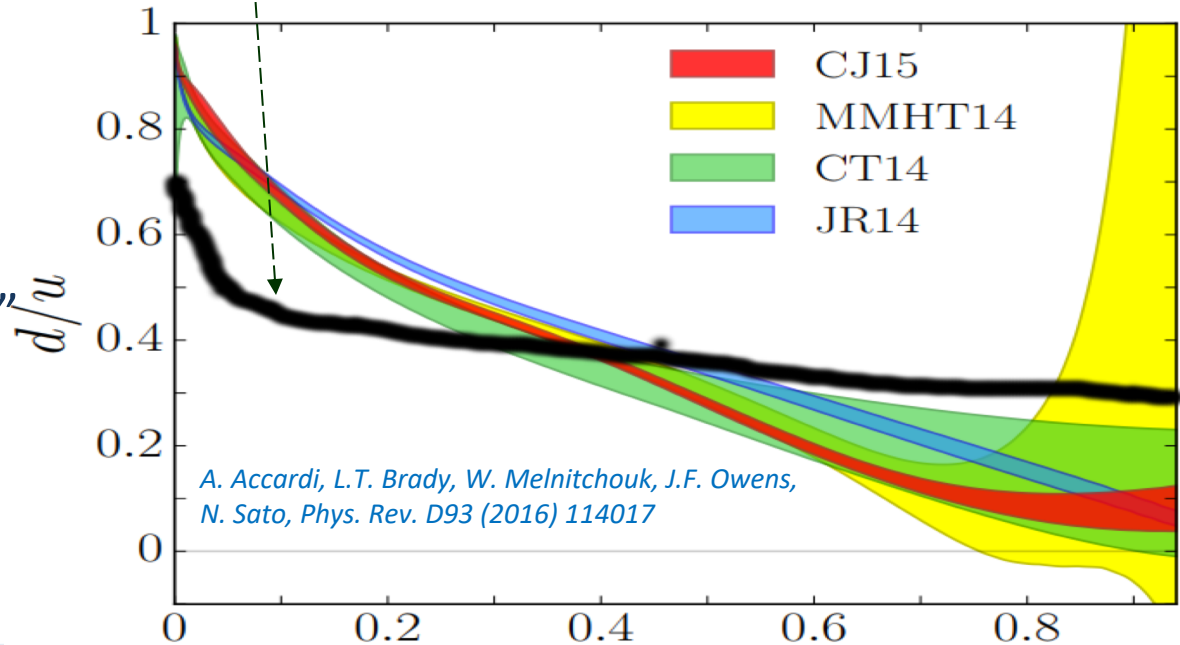
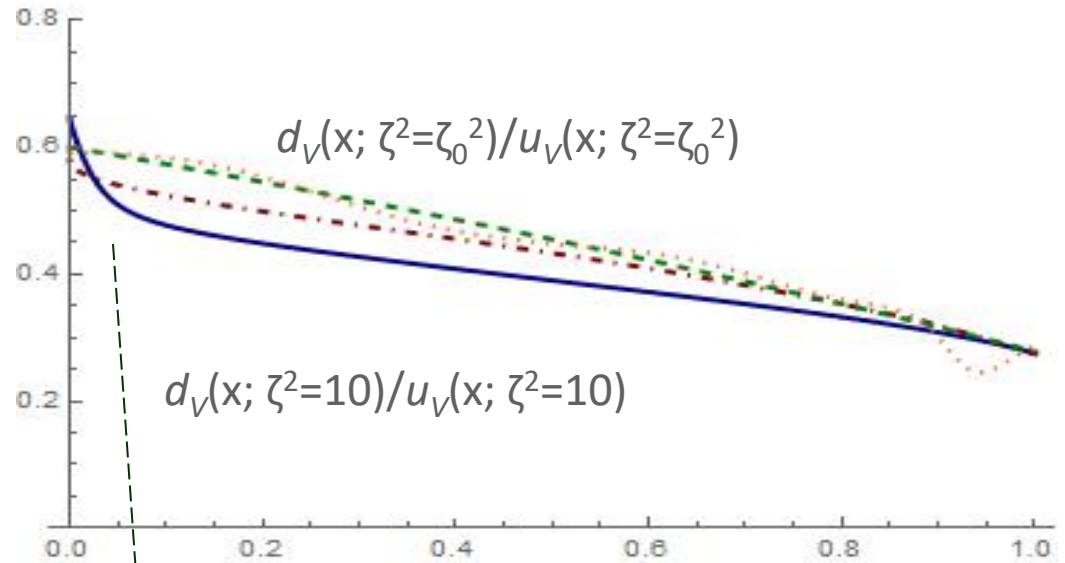
✓ Prediction derived from Faddeev amplitude that produces nucleon PDA

$$d_V(x)/u_V(x)|_{x=1} = 0.28$$

✓ Comparison with “modern” PDF parametrisations

✓ As learnt from pion PDF, parametrisations can be misleading

F. Gao, L. Chang, Y.-X. Liu, J. Papavassiliou C. D. Roberts, *in progress*



A. Accardi, L.T. Brady, W. Melnitchouk, J.F. Owens, N. Sato, Phys. Rev. D93 (2016) 114017





Epilogue



- Challenge: Explain and Understand the Origin and Distribution of the Vast Bulk of Visible Mass
- Current Paradigm: Quantum Chromodynamics
- QCD is plausibly a mathematically well-defined quantum field theory,
The only one we've ever produced
 - Consequently, it is a worthwhile paradigm for developing Beyond-SM theories
- Challenge is to reveal the content of strong-QCD
- Continuum strong-QCD
 - Past 20 years have seen vast improvement in understanding and spread in diversity of applications
 - Exist now an array of predictions; ripe for validation
 - Raft of existing and future applications includes
 - parton distributions of all types
 - spectrum of hadrons, including hybrids/exotics
 - elastic and transition form factors of mesons and baryons

- Challenge: Explain and Understand the Origin and Distribution of the Vast Bulk of Visible Mass
- Current Paradigm: Quantum Chromodynamics

Electron Ion Collider: The Next QCD Frontier

- Exist now an array of predictions; ripe for validation
- Raft of existing and future applications includes
 - parton distributions of all types
 - spectrum of hadrons, including hybrids/exotics
 - elastic and transition form factors of mesons and baryons

Strong Interactions in the Standard Model

$$\mathcal{L}_{\text{QCD}} = \bar{\psi}_i (i(\gamma^\mu D_\mu)_{ij} - m \delta_{ij}) \psi_j - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}$$

- Only apparent scale in chromodynamics is mass of the quark field
- Quark mass is said to be generated by Higgs boson.
- In connection with everyday matter, that mass is 1/250th of the natural (empirical) scale for strong interactions, *viz.* more-than two orders-of-magnitude smaller
- Plainly, the Higgs-generated mass is very far removed from the natural scale for strongly-interacting matter
- *Nuclear physics mass-scale* – 1 GeV – is an *emergent feature of the Standard Model*
 - No amount of staring at \mathcal{L}_{QCD} can reveal that scale
- Contrast with quantum electrodynamics, *e.g.* spectrum of hydrogen levels measured in units of m_e , which appears in \mathcal{L}_{QED}

$$\mathcal{L}_{\text{QCD}} = \bar{\psi}_i (i(\gamma^\mu D_\mu)_{ij} - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}) \psi_j$$

Whence Mass?

- Classical chromodynamics ... non-Abelian local gauge theory
- Remove the current mass ... there's no energy scale left
- *No dynamics in a scale-invariant theory*; only kinematics ... the theory looks the same at all length-scales ... there can be no clumps of anything ... *hence bound-states are impossible*.
- *Our Universe can't exist*
- *Higgs boson doesn't solve this problem* ...
 - normal matter is constituted from light-quarks &
 - the mass of protons and neutrons, the kernels of all visible matter, are 100-times larger than anything the Higgs can produce
- *Where did it all begin?*
... becomes ... Where did it all come from?

Trace Anomaly

- Classically, in a **scale invariant theory** the **energy-momentum tensor must be traceless: $T_{\mu\mu} \equiv 0$**
- Classical chromodynamics is meaningless ... must be quantised
- Regularisation and renormalisation of (ultraviolet) divergences introduces a mass-scale
... *dimensional transmutation*: mass-dimensionless quantities become dependent on a mass-scale, ζ

- $\alpha \rightarrow \alpha(\zeta)$ in QCD's (massless) Lagrangian density, $\mathcal{L}(m=0)$ QCD β function
Under a scale transformation $\zeta \rightarrow e^\sigma \zeta$, then $\alpha \rightarrow \sigma \alpha\beta(\alpha)$

$$\mathcal{L} \rightarrow \sigma \alpha\beta(\alpha) d\mathcal{L}/d\alpha$$

$$\Rightarrow \partial_\mu \mathcal{D}_\mu = \delta\mathcal{L}/\delta\sigma = \alpha\beta(\alpha) d\mathcal{L}/d\alpha = \beta(\alpha) \frac{1}{4} G_{\mu\nu} G_{\mu\nu} = T_{\rho\rho} =: \Theta_0$$

Trace
anomaly

- Straightforward, nonperturbative derivation, without need for diagrammatic analysis ...

Quantisation of renormalisable four-dimensional theory forces nonzero value for trace of energy-momentum tensor

$$\mathcal{L}_{\text{QCD}} = \bar{\psi}_i (i(\gamma^\mu D_\mu)_{ij} - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}) \psi_j$$

Whence?

- Classical chromodynamics ... non-Abelian local gauge theory
- Local gauge invariance; but there is no confinement without a mass-scale
 - Three quarks can still be colour-singlet
 - Colour rotations will keep them colour singlets
 - But they need have no proximity to one another
 - ... proximity is meaningless in a scale-invariant theory
- Whence mass ... equivalent to whence a mass-scale ... equivalent to whence a confinement scale
- *Understanding the origin of mass in QCD is quite likely inseparable from the task of understanding confinement.*
- Existence alone of a scale anomaly answers neither question*



Where is the mass?



$$T_{\mu\mu} = \frac{1}{4}\beta(\alpha(\zeta))G_{\mu\nu}^a G_{\mu\nu}^a$$

Trace Anomaly

- Knowing that a trace anomaly exists does not deliver a great deal ... indicates only that a mass-scale exists
- Can one compute and/or understand the magnitude of that scale?
- One can certainly *measure* the magnitude ... consider proton:

$$\langle p(P) | T_{\mu\nu} | p(P) \rangle = -P_\mu P_\nu$$

$$\begin{aligned} \langle p(P) | T_{\mu\mu} | p(P) \rangle &= -P^2 = m_p^2 \\ &= \langle p(P) | \Theta_0 | p(P) \rangle \end{aligned}$$

- In the chiral limit the entirety of the proton's mass is produced by the trace anomaly, Θ_0
 - ... In QCD, Θ_0 measures the strength of gluon self-interactions
 - ... so, from one perspective, m_p is completely generated by glue.



On the other hand ...

$$T_{\mu\mu} = \frac{1}{4}\beta(\alpha(\zeta))G_{\mu\nu}^a G_{\mu\nu}^a$$

Trace Anomaly

- In the chiral limit

$$\langle \pi(q) | T_{\mu\nu} | \pi(q) \rangle = -q_\mu q_\nu \Rightarrow \langle \pi(q) | \Theta_0 | \pi(q) \rangle = 0$$

- **Does this mean** that the scale anomaly vanishes trivially in the pion state, *i.e.* **gluons contribute nothing to the pion mass?**
- Difficult way to obtain “zero”!
- Easier to imagine that “zero” owes to cancellations between different operator contributions to the expectation value of Θ_0 .
- Of course, such precise cancellation should not be an accident.
It could only arise naturally because of some symmetry and/or symmetry-breaking pattern.

Whence “1” and yet “0” ?

$$\langle p(P) | \Theta_0 | p(P) \rangle = m_p^2, \quad \langle \pi(q) | \Theta_0 | \pi(q) \rangle = 0$$

➤ *No statement of the question*

“Whence the proton's mass?”

is complete without the additional clause

*“Whence the **absence** of a pion mass?”*

- Natural visible-matter mass-scale must emerge simultaneously with apparent preservation of scale invariance in related systems
- Expectation value of Θ_0 in pion is always zero, irrespective of the size of the natural mass-scale for strong interactions = m_p