

# Measuring $|V_{ub}|$ at LHCb

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RTG Students Lecture

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- 1 Lecture
  - CKM Mechanism
  - How to measure CKM matrix elements in general?
- 2 Lecture Today: How to measure CKM matrix elements in B-decays?
  - Differences between B-factories and Hadron colliders
  - $|V_{cb}|$
  - $|V_{ub}|$
- 3 Lecture: Specific LHCb measurements
  - $\Lambda_b \rightarrow p \mu \nu$
  - $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$

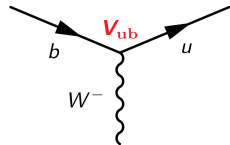
# Recap of the first two lectures

## Why is $|V_{ub}|$ important?

- Quarks change their flavour in the SM by the emission of a W-Boson
- The rate is proportional to the coupling strength  $|V_{ub}|^2$
- These 9 different couplings form the CKM matrix:

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}, \quad \frac{\sigma(V_{CKM})}{|V_{CKM}|} = \begin{pmatrix} 0.02\% & 0.3\% & 12\% \\ 4\% & 2\% & 2\% \\ 7\% & 7\% & 3\% \end{pmatrix} \quad [\text{PDG 2014}]$$

→  $|V_{ub}|$  is least well known element of the CKM matrix



# Recap of the first two lectures

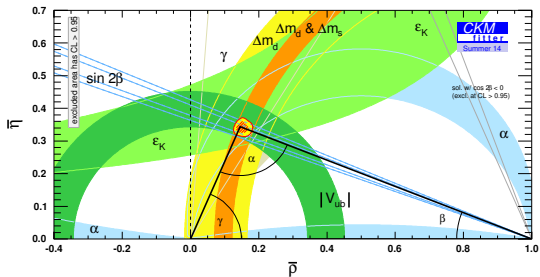
## CKM unitarity

- In the SM the CKM matrix is unitary
- Leads to several unitarity equations, e.g.:

$$\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} + \frac{V_{cd}V_{cb}^*}{V_{cd}V_{cb}^*} + \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} = 0$$

- Precision limited by magnitude and phase of  $|V_{ub}|$

→ If it is no triangle → New Physics



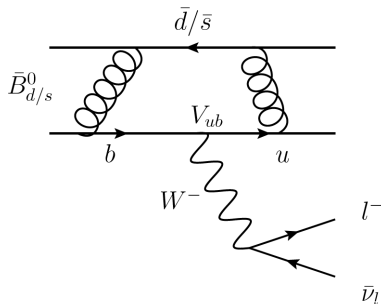


# Recap of the first two lectures

## Measuring $|V_{ub}|$

- $|V_{ub}|$  measured using (semi-)leptonic decays
- 3 different strategies:
  - **exclusive:** semileptonic decays such as  $\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}$
  - **inclusive:** all semileptonic  $B \rightarrow X_u l^- \bar{\nu}$  transitions
  - measure pure leptonic decay  $B^+ \rightarrow \tau \nu$
- Factorise electroweak and strong parts of the decay:
 
$$\frac{d\Gamma}{dq^2} \propto G_F^2 |V_{ub}|^2 |f^+(q^2)|^2$$

→ Semileptonic decays rely on non-perturbative FF calculations from LQCD or QCD sum rules



# Recap of the first two lectures

## Hadron colliders

### Advantages

- **large production cross section** of beauty quarks:  $\sigma(pp \rightarrow b\bar{b}X) = 284 \pm 20 \pm 49 \mu\text{b}$  at 7 TeV
- Millions of B candidates available, **all b-hadrons produced**:  $B^0, B^+, B_s, B_c, \Lambda_b, \dots$
- Excellent vertex separation, tracking and PID systems

### Disadvantages

- but **dirty environment**: many other particles produced in pp collisions  
→ No possibility to use beam energy constraints
- No kinematic constraints from other (tagging) B, also b-hadron production fractions poorly known
- **unknown initial state** which makes reconstruction of neutrino challenging
- must trigger on **specific exclusive decay modes** and typically charged hadrons in final state  
→ no inclusive measurements possible, hard to reconstruct neutrals

# The $|V_{ub}|$ puzzle - Status of 2014

- **Discrepancy between exclusive vs. inclusive measurement:**

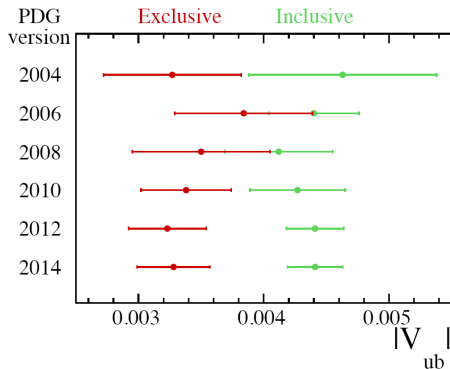
excl.:  $(3.28 \pm 0.29) \times 10^{-3}$  [PDG 2014]

incl.:  $(4.14 \pm 0.15^{+0.15}_{-0.19}) \times 10^{-3}$

→  $\sim 3\sigma$  deviation

- Leptonic measurements not precise enough, favours inclusive results

→ More precise measurements needed

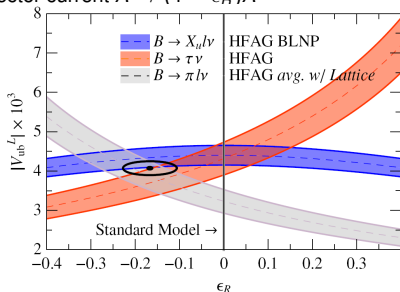


# The $|V_{ub}|$ puzzle - Tension be due to New Physics?

Idea: add right-handed charged current to SM [Phys. Rev. D 90, 094003 (2014)]

$$\mathcal{L}_{\text{eff}} = \frac{-4G_F}{\sqrt{2}} V_{ub}^L (\bar{u}\gamma_\mu P_L b + \epsilon_R \bar{u}\gamma_\mu P_R b) (\bar{\nu}\gamma_\mu P_L l) + h.c.$$

- $B \rightarrow \pi l \nu$  is purely a vector current whereas  $B \rightarrow X_U l \nu$  is a V-A
- Adding right-handed current (V+A), increases vector current  $V \rightarrow (1 + \epsilon_R)V$  but decreases axial-vector current  $A \rightarrow (1 - \epsilon_R)A$



⇒ negative right-handed can reduce tension between inclusive and exclusive result

⇒ new measurement with different sensitivity needed

# Is it possible to measure $|V_{ub}|$ at LHCb ?

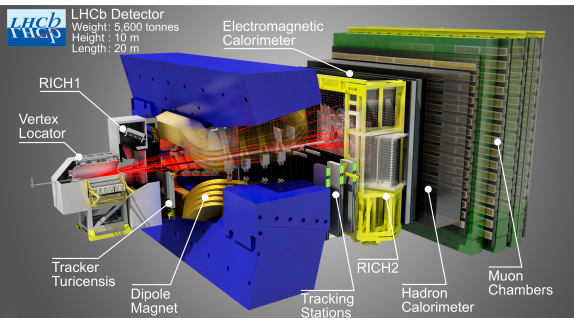
- Long thought that measuring  $|V_{ub}|$  is impossible at hadron colliders
- Lack the beam energy constraints of  $e^+e^-$  colliders

“

It is particularly important to stress that many of the measurements that constitute the primary physics motivation for SuperB cannot be performed in the hadronic environment. For example, modes with missing energy, such as  $B^+ \rightarrow \ell^+ \nu_\ell$  and  $B^+ \rightarrow K^+ \nu \bar{\nu}$ , measurements of the CKM matrix elements  $|V_{cb}|$  and  $|V_{ub}|$ , and inclusive analyses of processes such as  $b \rightarrow s\gamma$  are unique to SuperB.

”

CDR, SuperB factory, arXiv 0709.0451



## LHCb

- forward spectrometer covering pseudorapidity  $2 < \eta < 5$
- $26 \times 10^{10} b\bar{b}$  pairs

First LHCb measurement on exclusive

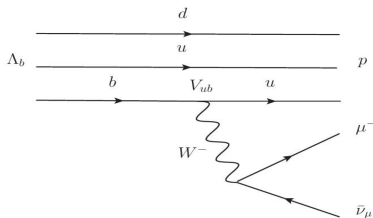
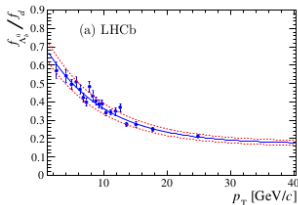
$$|V_{ub}|:$$
$$\Lambda_b \rightarrow p \mu^- \nu_\mu$$

# Experimental Challenge at LHCb

- Missing neutrino momentum  $\rightarrow$  B not fully reconstructed
- Generally affected by much higher (x10)  $X_b \rightarrow X_c \mu \nu$  backgrounds
- "Golden channel"  $\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}$  suffers from high pion background at LHC

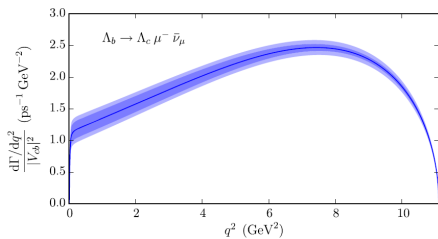
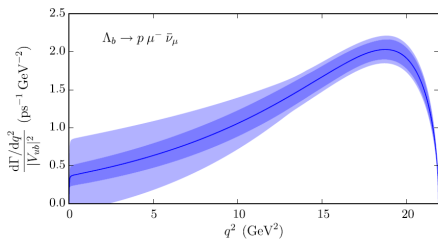
BUT: use  $\Lambda_b \rightarrow p \mu^- \nu_\mu$

- Excellent  $\mu$  and  $p$  PID at LHCb from RICH/Muon systems
- precision vertexing and tracking used  $\rightarrow$  displaced  $p\mu$  vertex as signature in detector
- High production fraction of  $\Lambda_b$ :  $\sim 20\%$  of b-hadrons [JHEP08(2014)143]



# Analysis strategy

- 2012 Dataset ( $\sim 2 \text{ fb}^{-1}$ )
- Normalise signal yield to a  $|V_{cb}|$  decay:  $\Lambda_b \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu$ 
  - cancels many systematic uncertainties
  - especially the production rate of  $\Lambda_b$  baryons
- Improved FF calculations from theory for  $\Lambda_b \rightarrow p \mu^- \bar{\nu}_\mu$  and  $\Lambda_b \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu$  in high  $q^2$  region  
 $\rightarrow$  there FF calculations from theory are most precise



[Phys. Rev. D 92, 034503 (2015)]



# How to extract $|V_{ub}|$ ?

$$\underbrace{\frac{\mathcal{B}(\Lambda_b \rightarrow p\mu^- \nu_\mu)}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+ \mu^- \nu_\mu)}}_{\text{experimental measurement}} = \underbrace{R_{\text{FF}}}_{\text{theoretical calculations}} \times \frac{|V_{ub}|^2}{|V_{cb}|^2}$$

- Reduce systematic uncertainties by restricting measurement to  $q^2 > 15(7) \text{ GeV}^2$   
→ LQCD here most precise
- $R_{\text{FF}} = \frac{(\Lambda_b \rightarrow p\mu^- \nu_\mu)_{q^2 > 15 \text{ GeV}^2}}{(\Lambda_b \rightarrow \Lambda_c^+ \mu^- \nu_\mu)_{q^2 > 7 \text{ GeV}^2}} = 0.68 \pm 0.07$  [Phys. Rev. D 92, 034503 (2015)]  
→ 5% uncertainty on  $|V_{ub}|$  from theory

# Analysis strategy

$$\frac{\mathcal{B}(\Lambda_b \rightarrow p\mu^- \nu_\mu)_{q^2 > 15 \text{ GeV}^2}}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+ \mu^- \nu_\mu)_{q^2 > 7 \text{ GeV}^2}} = \frac{N(\Lambda_b \rightarrow p\mu^- \nu_\mu)}{N(\Lambda_b \rightarrow \Lambda_c^+ \rightarrow pK^- \pi^+)_{\mu^- \nu_\mu}} \times \frac{\epsilon(\Lambda_b \rightarrow (\Lambda_c^+ \rightarrow pK^- \pi^+)_{\mu^- \nu_\mu})}{\epsilon(\Lambda_b \rightarrow p\mu^- \nu_\mu)} \times \mathcal{B}(\Lambda_c^+ \rightarrow pK^- \pi^+)$$

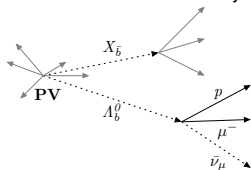
- Determine yields of  $\Lambda_b \rightarrow p\mu^- \nu_\mu$  and  $\Lambda_b \rightarrow (\Lambda_c^+ \rightarrow pK^- \pi^+)_{\mu^- \nu_\mu}$
- Estimate relative experimental efficiency with high precision
- Use  $\mathcal{B}(\Lambda_c^+ \rightarrow pK^- \pi^+)$  from Belle [PRL 113,042002(2014)]
- even though  $\Lambda_b \rightarrow p\mu^- \nu_\mu$  is suppressed, not rare:
  - expect 500,000 signal decays after trigger and pre-selection
  - Only need  $\sim 10000$  to get good enough statistical uncertainty  
 → very tight selection to control background and systematic effects

# Selection

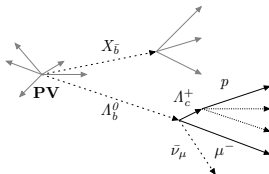
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Main bkg comes from  $|V_{cb}|$  decays:

- Charm has significant lifetime: cut on vertex quality
- apply tight PID cuts on the proton
- Dedicated MVA classifier used to remove backgrounds with additional charged tracks that vertex with  $p\mu$  candidate  
→ track isolation: 90% rejection with 80% efficiency



signal



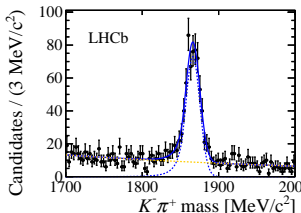
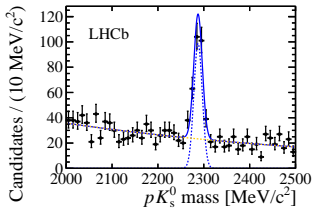
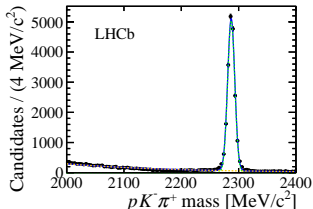
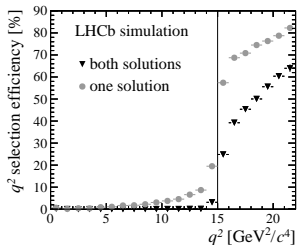
background

- Very difficult to isolate against neutral particles

# Selection

- Difficult to calculate  $q^2$  with missing neutrino
- Use pointing and  $\Lambda_b$  mass constraints to solve for  $q^2$  up to a two-fold ambiguity
- Correct solution has a resolution of  $1 \text{ GeV}^2/c^4$  whereas incorrect is  $4 \text{ GeV}^2/c^4$
- Require both solutions to full fill  $> q_{cut}^2$  to minimise migration from low  $q^2$
- reconstruct additional tracks to determine background yields:

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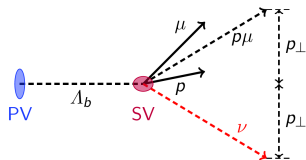
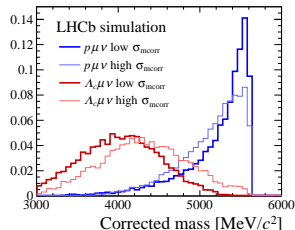


# Selection

- Corrected mass resolution  $\sim 10$  times worse than for fully reconstructed decays
- Uncertainty dominated by resolution of PV and  $\Lambda_b$  vertex
- Calculate uncertainty for each event and reject candidates if  $\sigma_{m_{corr}} > 100 \text{ MeV}/c^2$  ( $\sim 23\%$  survive) to increase separation to background in signal fit
- Fit to corrected mass
 
$$m_{corr} = \sqrt{m_{h\mu}^2 + p_{\perp}^2} + p_{\perp}, \quad h = p, \Lambda_c$$

$$\rightarrow \text{peaks at } \Lambda_b \text{ mass if only neutrino is missing}$$

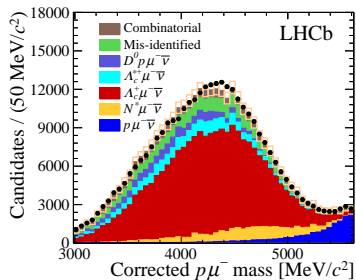
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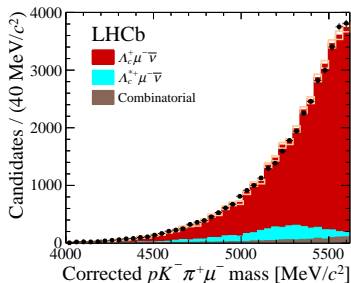
# Extracting Yields

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template fit is performed for signal and normalisation separately:



$$N(\Lambda_b \rightarrow \rho\mu^- \nu_\mu) = 17687 \pm 733$$



$$N(\Lambda_b \rightarrow (\Lambda_c^+ \rightarrow \rho K^-\pi^+)\mu^- \nu_\mu) = 34255 \pm 571$$

→ First observation of the decay  $\Lambda_b \rightarrow \rho\mu^- \nu_\mu$

→ Separate ground state and excited modes from fit to corrected mass in normalisation channel

# Relative efficiencies

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- Relative efficiency determined from simulation
- Difference between data and simulation calculated from control sample with data-driven corrections

$$\frac{\epsilon(\Lambda_b \rightarrow p\mu^-\nu_\mu)}{\epsilon(\Lambda_b \rightarrow (\Lambda_c^+ \rightarrow pK^-\pi^+)\mu^-\nu_\mu)} = 3.52 \pm 0.20$$

- Main differences in efficiency due to:
  - Two extra tracks for normalisation
  - Vertex efficiency ( $\Lambda_c$  lifetime)
  - Corrected mass error cut on signal
- Uncertainty of ratio is dominated by systematic uncertainties

# Systematic uncertainties

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- Dominated by  $\mathcal{B}(\Lambda_c^+ \rightarrow pK^- \pi^+)$  from Belle [PRL 113,042002(2014)]
- Trigger uncertainties can be further reduced  
→ size of control sample in data
- Tracking uncertainties dominated by material interaction of kaon and  $\pi$
- $\Lambda_c^+ \rightarrow pK^- \pi^+$  selection efficiency from knowledge on its Dalitz structure
- Fit systematic dominated by form factors of  $\Lambda_b \rightarrow N^* \mu^- \nu_\mu$  decays

Source	Relative uncertainty (%)
$\mathcal{B}(\Lambda_c^+ \rightarrow pK^+ \pi^-)$	+4.7 -5.3
Trigger	3.2
Tracking	3.0
$\Lambda_c^+$ selection efficiency	3.0
$\Lambda_b^0 \rightarrow N^* \mu^- \bar{\nu}_\mu$ shapes	2.3
$\Lambda_b^0$ lifetime	1.5
Isolation	1.4
Form factor	1.0
$\Lambda_b^0$ kinematics	0.5
$q^2$ migration	0.4
PID	0.2
Total	+7.8 -8.2



# Results I

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- Measure the relative branching fraction:

$$\frac{\mathcal{B}(\Lambda_b \rightarrow p \mu^- \nu_\mu)_{q^2 > 15 \text{ GeV}^2}}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+ \mu^- \nu_\mu)_{q^2 > 7 \text{ GeV}^2}} = (1.00 \pm 0.04(\text{stat}) \pm 0.08(\text{syst})) \times 10^{-2}$$

- Including  $\frac{\mathcal{B}(\Lambda_b \rightarrow p \mu^- \nu_\mu)}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+ \mu^- \nu_\mu)} = R_{\text{FF}} \times \frac{|V_{ub}|^2}{|V_{cb}|^2}$  with  $R_{\text{FF}} = 0.68 \pm 0.07$  [Phys. Rev. D 92, 034503 (2015)] gives

$$\frac{|V_{ub}|}{|V_{cb}|} = 0.083 \pm 0.004(\text{exp.}) \pm 0.004(\text{theo.}) \quad (1)$$

- Use world average for exclusive  $|V_{cb}| = (39.5 \pm 0.8) \times 10^{-3}$  measurements [PDG 2014]

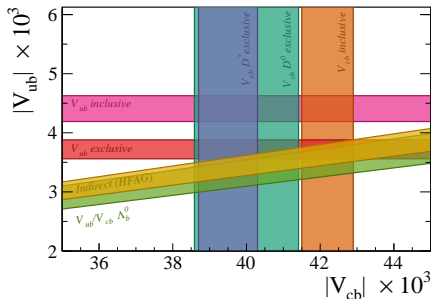
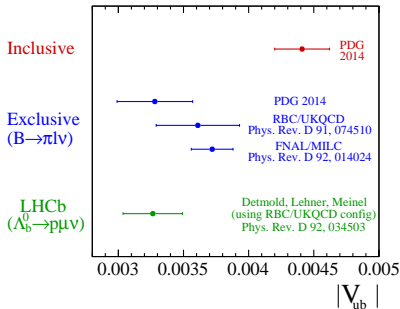
exclusive  $|V_{ub}|$  LHCb result

$$|V_{ub}| = (3.27 \pm 0.15(\text{exp.}) \pm 0.16(\text{theo.}) \pm 0.06(|V_{cb}|)) \times 10^{-3}$$

# Results II

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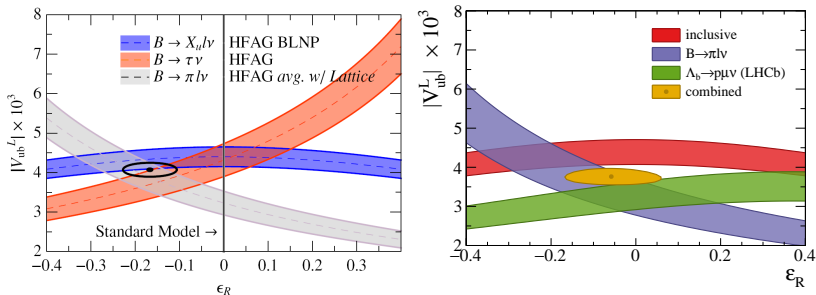
- LHCb is  $3.5\sigma$  away from inclusive measurement of  $|V_{ub}|$
- Consistent with other exclusive measurements



# Results III

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- $|V_{ub}|$  measurement depends on possible right-handed current in SM  
[Phys. Rev. D 81, 031301 (2010)]
- Previously exclusive/inclusive discrepancy suggested significant right-handed coupling fraction ( $\epsilon_R$ )  $\rightarrow$  solution to  $|V_{ub}|$  puzzle?



[Phys. Rev. D 90, 094003 (2014)]

 $\rightarrow$  LHCb results does not support that

exclusive  $|V_{ub}|$ :  
 $B_S^0 \rightarrow K^- \mu^+ \nu_\mu$

# Introduction

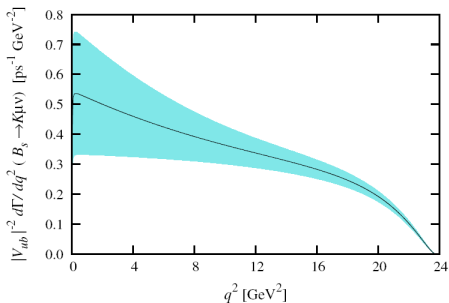
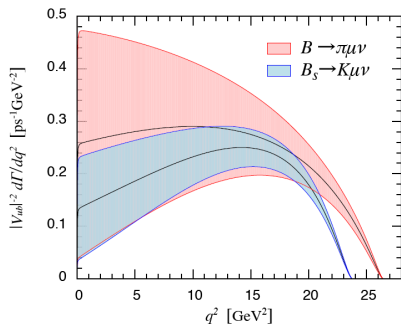
- first  $|V_{ub}|$  measurement from a  $B_s^0$  decay
- $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$  has been never measured before
- comparison with  $\Lambda_b^0 \rightarrow p \mu^- \nu_\mu$ :

Decay	$\Lambda_b \rightarrow p \mu^- \nu_\mu$	$B_s^0 \rightarrow K^- \mu^+ \nu_\mu$
Production fraction	20%	10%
Branching fraction	$4 \times 10^{-4}$	$1 \times 10^{-4}$ (expected)
Source of backgrounds	$\Lambda_c^+$	$\Lambda_c^+, D_s, D^+, D^0, \dots$
$\mathcal{B}(X_c)$ error	3.72%	3.9%
Form factor error	5%	$\sim 3\%$

- expect smaller FF uncertainties
- many more challenging bkg  
 $\Rightarrow$  clearly more difficult due to many more contributing bkg, but might have better ultimate precision

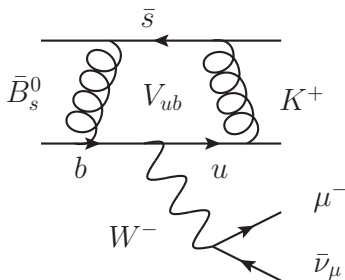
$B_s^0 \rightarrow K^- \mu^+ \nu_\mu$  Form factor calculations

- Form factor calculations available from Lattice for  $q^2 \geq 12 \text{ GeV}^2$ 
  - Flynn et al. Phys. Rev. D 91, 074510 (2015)
  - Bouchard et al., Phys. Rev. D 90, 054506 (2014)
- LCSR predictions at low  $q^2$ : arXiv 1703.04765
- perform measurements in both  $q^2$  bin



# Analysis Strategy

- normalise wrt.  $|V_{cb}|$  decay mode:  $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$   
 → very well understood
- use full Run-I statistics:  $3fb^{-1}$
- look for displaced  $K\mu$  vertex
- apply tight PID constraints to select K and suppress high  $\pi$  background
- remove background with add. charged tracks with isolation variables

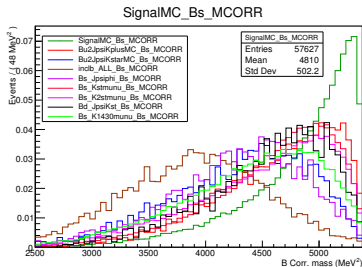


# Main Backgrounds to $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$

- partially reconstructed background with **additional charged track(s)**:  
 $B^+ \rightarrow J/\psi K^+$ ,  $B^+ \rightarrow J/\psi K^{*+}$ ,  $B_s \rightarrow J/\psi \phi$ ,  $B_s \rightarrow D_s \mu \nu$ ,  $B_d \rightarrow \rho \mu \nu$ , ...  
 → use charge track isolation tools → **isolation BDT**

- additional neutral particles** from higher excited modes:  
 $B_s^0 \rightarrow K^* \mu \nu \mu$ ,  $B_s^0 \rightarrow K_2^* \mu \nu \mu$ ,  $B_s^0 \rightarrow K^*(1430) \mu \nu \mu$   
 → use **neutral isolation** tools: dedicated  $\pi^0$  reconstruction to veto  $K^*$  candidates

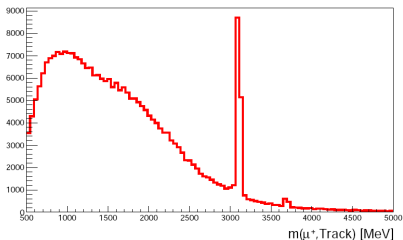
- combinatorial bkg: use SS data as a proxy  
 trained dedicated **BDT against SS sample**
- miss-ID bkg





# Charged Track Isolation

- Tool developed to compare every track in the event with the signal candidate:
  - Search through every track in event
    - Does the track originate from the same decay? (bad)
    - Or is the track isolated? (good)
- isolation variables as output of tool:

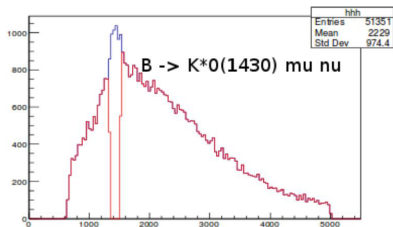
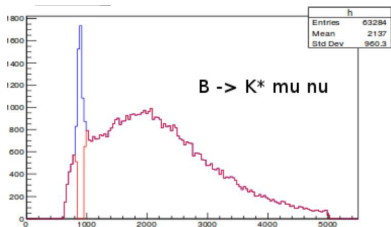


→ apply  $J/\psi$  veto

- Train BDT to discriminate against charged backgrounds
- Training variables include output of charged isolation tool, kinematics

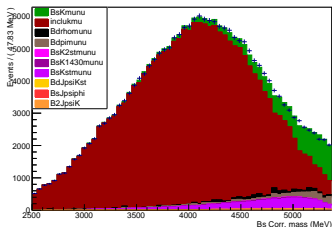
# Neutral Isolation

- Draw cones around track in  $\Delta R$
- Search for hits in neutral calorimeters
- Reconstruct photons or  $\pi^0$
- Veto event if high pion likelihood and  $m(K^\pm \pi^0) \approx m(K^*)$

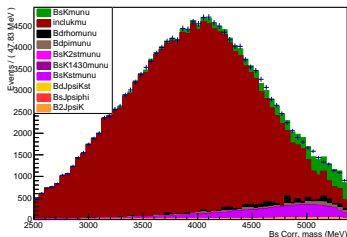
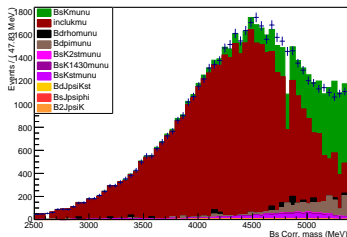


→ apply vetos on  $\pi^0$ ,  $K^*$  and  $K^*(1430)$  mass

## Signal Fit

full  $q^2$ 

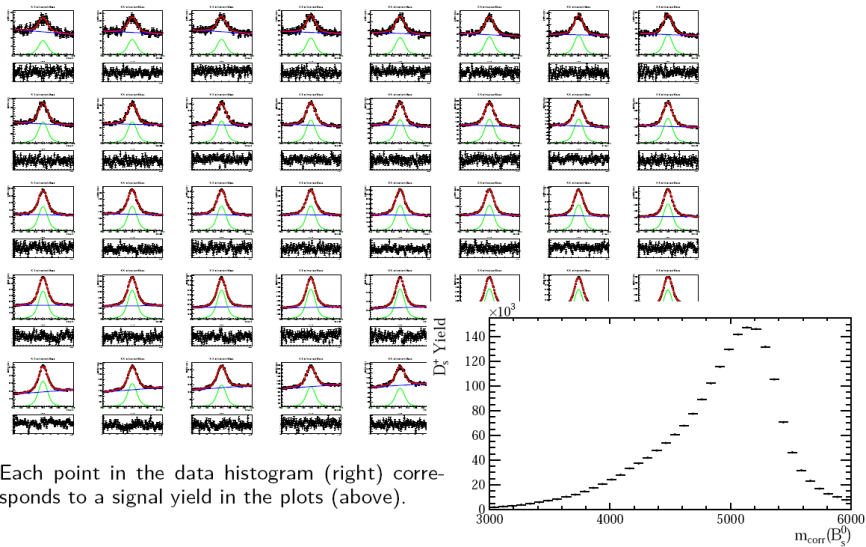
- perform binned template fit to corrected  $B_s$  mass
- templates from MC, constrained from data
- not yet all possible backgrounds included
- so far gives  $\sim 10000$  signal events per bin
- needs to be finalised and validated

low  $q^2$ high  $q^2$ 

# $B_s^0 \rightarrow D_s \mu \nu$ Normalisation channel

- **Selection** is similar to that of the  $K^- \mu^+ \nu_\mu$  mode, in order to try and cancel efficiency ratio systematics
- problem: can't use sPlot technique to remove combinatorial bkg under  $D_s$  peak  
→ correlations between  $KK\pi$  invariant mass and  $B_s^0$  corrected mass
- split  $B_s^0$  corrected mass range of 3000-6000 MeV into 40 bins
- in each bin perform fit to invariant  $KK\pi$  mass to extract the  $D_s$  yield  
→ subtract the  $KK\pi$  combinatorial component  
→ still remaining  $D_s \mu$  combinatorial background

## Control Fit templates

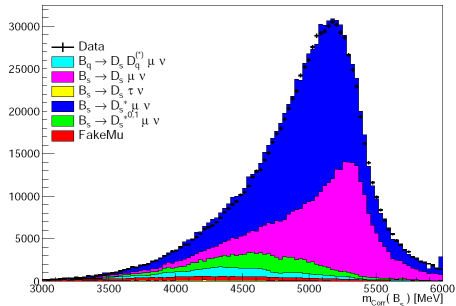


Each point in the data histogram (right) corresponds to a signal yield in the plots (above).

# Control Fit Results

- main challenge: separate  $D_s^*$  and  $D_s$
- feed down from higher excited D resonances, taonic modes and double charm modes taken from MC
- combinatorial  $D_s\mu$  background obtained from data:
  - SS: Real  $D_s^+ + \mu^+$
  - Real  $D_s^+ + \text{fake } \mu^-$  ( $DLL_{\mu\pi}(\mu) < 0$ )

→ gives  $B_s^0 \rightarrow D_s\mu\nu \sim 300000$



Finalising  $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ 

- BDT optimization ongoing
- Signal Fit need to be finalized including all backgrounds, also needs validations
- Efficiency calculations almost done
- Systematic uncertainty evaluation started
- Expect new form factor calculations soon, including ratio  $B_s^0 \rightarrow K^- \mu^+ \nu_\mu / B_s^0 \rightarrow D_s \mu \nu$
- Aiming for publication very soon

⇒ Stay tuned!

# Conclusions

- LHCb performed a precise measurement of  $|V_{ub}|$  using the decay  $\Lambda_b \rightarrow p\mu^-\nu_\mu$
- First determination of  $|V_{ub}|$  in a hadron collider and in a baryonic decay

$$|V_{ub}| = (3.27 \pm 0.15(\text{exp.}) \pm 0.16(\text{theo.}) \pm 0.06(|V_{cb}|)) \times 10^{-3}$$

- Consistent with other exclusive  $|V_{ub}|$  measurements in  $\bar{B}^0 \rightarrow \pi^+ l^- \nu_\mu$
- Measurement is  $3.5\sigma$  below inclusive measurement of  $|V_{ub}|$
- Right-handed currents can no longer explain the  $|V_{ub}|$  puzzle
- We are in the final months to determine  $|V_{ub}|$  in  $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$  decays

⇒ **Very interesting time ahead of us, also with start of Belle II soon!**



**Thanks for your attention!**

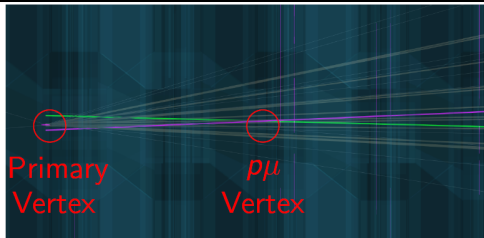
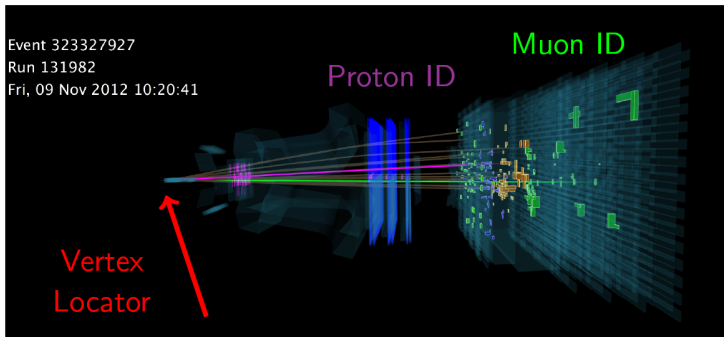
# Backup Slides

# Signal Selection

Event 323327927

Run 131982

Fri, 09 Nov 2012 10:20:41



# Neutrino reconstruction

due to missing neutrino, events are only partially reconstructed:  
 → use pointing and  $\Lambda_b$  mass to solve for  $q^2$  up to 2-fold ambiguity:  
 neutrino momentum parallel to flight direction is unknown  $p(\nu)_{||}$ :

$$(p_\nu + p_{h\mu})^2 = m_{\Lambda_b}^2$$

with  $p_\nu = (\sqrt{p^2(\nu)_{||} + p_\perp^2}, 0, -p_\perp, p(\nu)_{||})$  and

$p_{h\mu} = (\sqrt{p^2(h\mu)_{||} + p_\perp^2 + m_{h\mu}^2}, 0, p_\perp, p(h\mu)_{||})$

gives

$$p(\nu)_{||} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

with  $a = |2p(h\mu)_{||} m_{h\mu}|^2$ ,  $b = 4p(h\mu)(2p_\perp p(h\mu) - m_{miss}^2)$ ,

$c = 4p_\perp^2 (p^2(h\mu) + m_{\Lambda_b}^2) - |m_{miss}^2|$ ,  $m_{miss}^2 = m_{\Lambda_b}^2 - m_{h\mu}^2$

# Lattice Calculations

- Calculate 6 form factors (3 vector, 3 axial) for each decay. Lattice QCD with 2 + 1 dynamical domain-wall fermions.
- Calculation performed with six pion masses and two different lattice spacings.
- b and c quarks implemented with relativistic heavy-quark actions.
- Uses gauge-field configurations generated by the RBV and UKQCD collaborations.
- $b \rightarrow u$  and  $b \rightarrow c$  currents renormalised with a mostly non-perturbative method.
- Parametrises the form factor  $q^2$  dependence with a  $z$  expansion.
- Systematics include: the continuum extrapolation uncertainty, the kinematic ( $q^2$ ) extrapolation uncertainty, the perturbative matching uncertainty, the uncertainty due to the finite lattice volume and the uncertainty from the missing isospin breaking effects.

W. Detmold, C. Lehner and S. Meinel [Phys. Rev. D 92, 034503 (2015)]

# Theory ratio

- Use the latest Lattice QCD results for these decays to calculate:

$$R_{\text{FF}} = \frac{\int_{15 \text{ GeV}/c^2}^{q_{\text{max}}} \frac{d\Gamma(\Lambda_b \rightarrow p \mu^- \nu_\mu)}{dq^2} / |V_{ub}|^2 dq^2}{\int_{7 \text{ GeV}/c^2}^{q'_{\text{max}}} \frac{d\Gamma(\Lambda_b \rightarrow \Lambda_c^+ \mu^- \nu_\mu)}{dq^2} / |V_{cb}|^2 dq^2}$$

# Branching fraction extrapolation factor

- convert measured ratio into bf using:

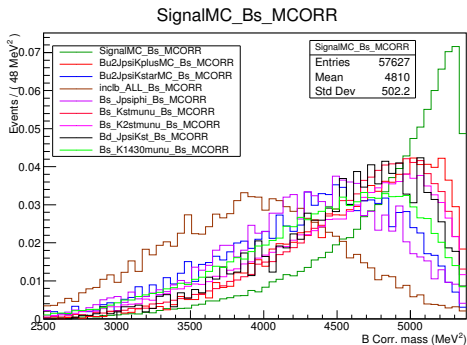
$$\begin{aligned}
 \mathcal{B}(\Lambda_b \rightarrow p\mu^-\nu_\mu) &= \tau_{\Lambda_b} \frac{\mathcal{B}(\Lambda_b \rightarrow p\mu^-\nu_\mu)_{q^2 > 15 \text{ GeV}^2/c^2}}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+\mu^-\nu_\mu)_{q^2 > 7 \text{ GeV}^2/c^2}} |V_{cb}|^2 R_{FF} \\
 &= \tau_{\Lambda_b} \mathcal{B}_{ratio} \int_{7 \text{ GeV}^2/c^2}^{q'_{max}} \frac{d\Gamma(\Lambda_b \rightarrow \Lambda_c^+\mu^-\nu_\mu)}{dq^2} / |V_{cb}|^2 dq^2 \\
 &\quad \times \frac{\int_{0 \text{ GeV}^2/c^4}^{q_{max}} \frac{d\Gamma(\Lambda_b \rightarrow p\mu^-\nu_\mu)}{dq^2} / |V_{ub}|^2 dq^2}{\int_{15 \text{ GeV}^2/c^2}^{q_{max}} \frac{d\Gamma(\Lambda_b \rightarrow p\mu^-\nu_\mu)}{dq^2} / |V_{ub}|^2 dq^2}
 \end{aligned}$$

- results in:

$$\mathcal{B}(\Lambda_b \rightarrow p\mu^-\nu_\mu) = (4.1 \pm 1.0) \times 10^{-4}$$

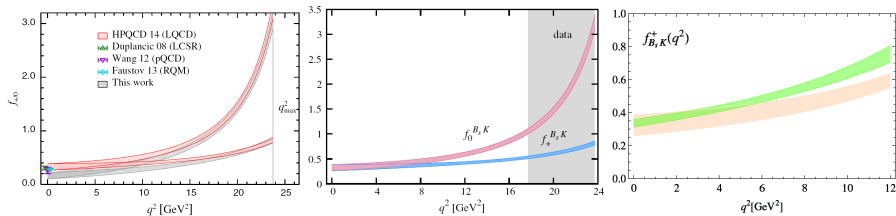
# $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ Selection

- apply stripping 21r0p1 cuts
- preselection cuts:
  - Bs mass cut =  $2500 < B_s\_MCORR < 7000$
  - Tight kaon PID cuts
  - Trigger:  
(Bs\_Hlt2SingleMuonDecision\_TOS ||Bs\_Hlt2TopoMu2BodyBBDTDecision\_TOS == 1)
- $J/\psi$  misID,  $\pi^0$  and  $K^*$  vetoes
- cut on charged isolation and SS BDT





# $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ Form factor calculations



Flynn

Bouchard

LCSR

$$f_{B_s K}^+(0) = 0.323(63)$$

$$f_{B_s K}^+(0) = 0.336 \pm 0.023$$

all three contain HPQCD Bouchard et al. prediction (middle)