

The Effective-Vector-Boson Approximation at the LHC

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Higgs Couplings
8th November 2017

Content

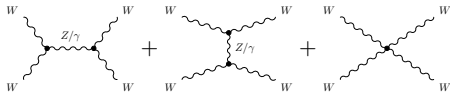
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- 2 Vector-Boson Scattering at the LHC
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Longitudinal W-Boson Scattering

The gauge-bosons W^\pm and Z obtain their **mass and longitudinal polarisation state** through EWSB.



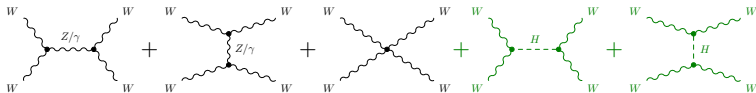
$$\mathcal{A}(W_L W_L \rightarrow W_L W_L) \propto -s - t$$

→ unitarity is violated!

Mechanism of **EWSB must restore unitarity** and regulate $\sigma(W_L W_L \rightarrow W_L W_L)$:

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$$\mathcal{A}(W_L W_L \rightarrow W_L W_L) \propto -s - t + \frac{s^2}{s - M_H^2} + \frac{t^2}{t - M_H^2}$$

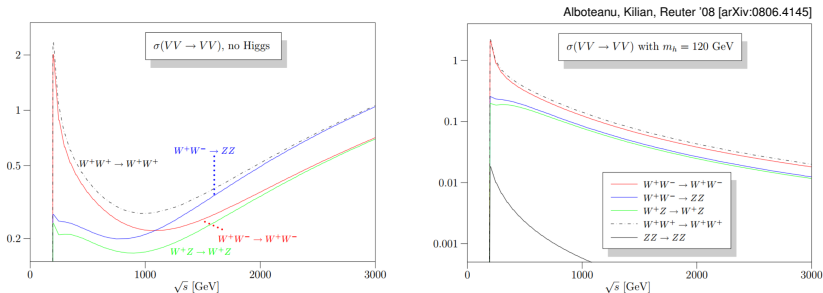
→ unitarity is violated!

Mechanism of EWSB must restore unitarity and regulate $\sigma(W_L W_L \rightarrow W_L W_L)$:

→ a light SM Higgs exactly cancels terms leading in energy

Unitarity Violation

If any or all couplings are slightly modified the **cancellation fails and unitarity is violated**.

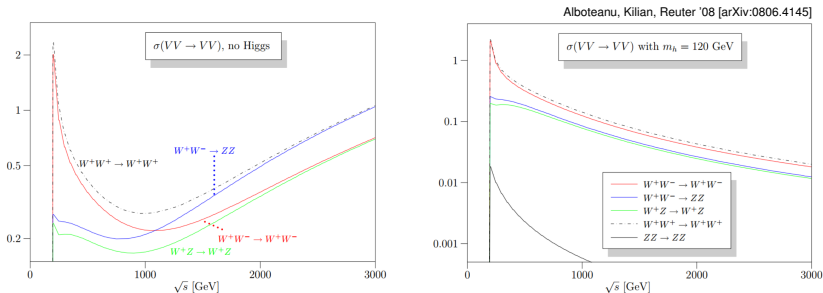


In order to restore **unitarity new interactions or particles** need to be introduced.

→ Any deviations from the SM represent **signals of new physics**.

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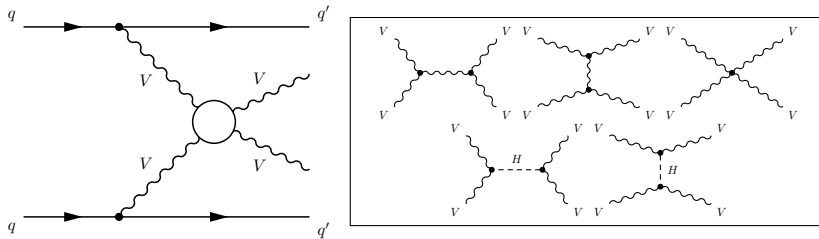
→ **VBS is a key tool in probing the mechanism of EWSB.**

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VBS at Hadron Colliders

VBS is only a **non-gauge-invariant subprocess** in the production of $VVjj$ final states.

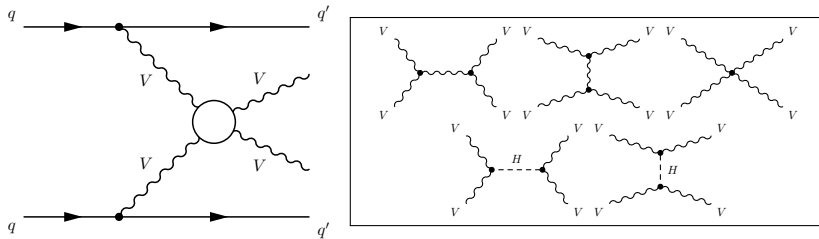


→ There are **two main types** of production modes at LO:

- **EW** $VVjj$ production: $\mathcal{O}(\alpha^6)$
- **QCD** $VVjj$ production: $\mathcal{O}(\alpha^4 \alpha_s^2)$

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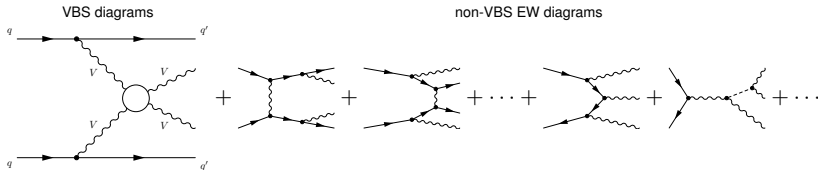


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- **EW** $VVjj$ production: $\mathcal{O}(\alpha^6)$
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- and interferences: $\mathcal{O}(\alpha^5\alpha_s)$ (colour and kinematically suppressed)
→ interference of both modes is negligible

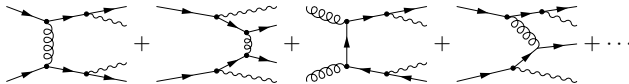
Production Modes

EW $VVjj$ production: $\mathcal{O}(\alpha^6)$



QCD $VVjj$ production: $\mathcal{O}(\alpha^4\alpha_s^2)$

gauge-invariantly separable: can be suppressed by cuts



Same-Sign VBS

Vest, Anger '15

final state	VV -channel	σ^{EW} [fb]	σ^{QCD} [fb]	$\sigma^{\text{EW}}/\sigma^{\text{QCD}}$
$l^\pm l^\pm \nu \nu' jj$	$W^\pm W^\pm$	19.5	18.8	$\sim 1 : 1$
$l^+ l^- \nu \nu' jj$	$W^\mp W^\pm, ZZ$	93.7	3192	$\sim 1 : 35$
$l^+ l^- l'^\pm \nu' jj$	$W^\pm Z$	30.2	687	$\sim 1 : 20$
$l^+ l^- l'^+ l'^- jj$	ZZ	1.5	106	$\sim 1 : 70$

most promising $VVjj$ channel in terms of VBS:

- same-sign $W^\pm W^\pm jj$ channel

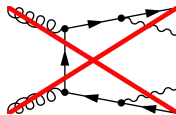
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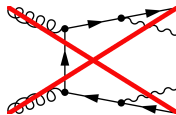
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most promising $VVjjj$ channel in terms of VBS:

- same-sign $W^\pm W^\pm jjj$ channel

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→ $l^\pm l^\pm \nu' \nu jjj$ final state is most sensitive to VBS measurements



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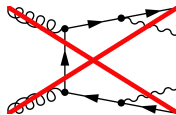
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However, VBS diagrams cannot gauge-invariantly separated from non-VBS EW diagrams!

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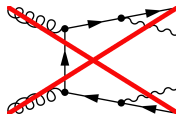
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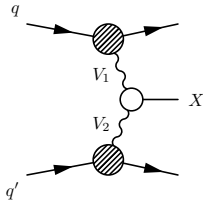
→ Are there kinematic regions in which the genuine VBS process is dominant?

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The Effective-Vector-Boson Approximation

In the EVBA the W-Boson is treated as **constituent of the quark** and assumed to be **on-shell**. Driven by **logarithmic enhancements** $\log^2(M_V^2/s)$ originating from collinear vector-boson emission off the quarks, in analogy to the **Weizsäcker-Williams approximation** of QED¹.

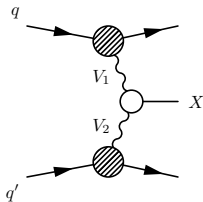


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Factorization into **probability densities** $P_{V_1|q}(z_1)$ and $P_{V_2|q'}(z_2)$ and a **hard scattering process** $\sigma_{V_1 V_2 \rightarrow X}(xs)$ at reduced CM energy \sqrt{xs} , with $x = z_1 z_2$.

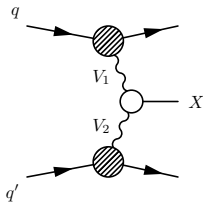
$$\sigma_{qq' \rightarrow X}(s) = \sum_{V_1, V_2} \int_{x_{\min}}^1 dx \int_{z_{\min}}^1 \frac{dz_1}{z_1} P_{V_1|q}(z_1) P_{V_2|q'}(x/z_1) \sigma_{V_1 V_2 \rightarrow X}(xs)$$

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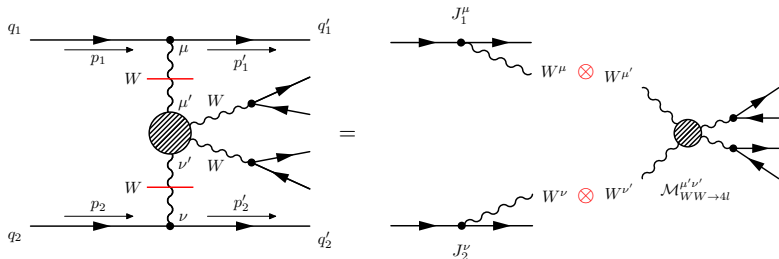
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However, naive convolution of single-vector-boson probabilities is not adequate to describe the two-vector-boson process sufficiently ².

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Factorisation of the Amplitude



The full amplitude reads

$$\mathcal{M}_{qq} = \sum_{\lambda_1, \lambda_2, \lambda_3, \lambda_4} \frac{(-1)^{\lambda_1 + \lambda_2}}{K_1 K_2 K_3 K_4} \mathcal{M}_{\lambda_1}^{\text{prod}} \mathcal{M}_{\lambda_2}^{\text{prod}} \times \mathcal{M}_{\lambda_1 \lambda_2 \lambda_3 \lambda_4}^{\text{VBS}} \times \mathcal{M}_{\lambda_3}^{\text{decay}} \mathcal{M}_{\lambda_4}^{\text{decay}},$$

where we have introduced the abbreviations

$$\begin{aligned} i\mathcal{M}_{\lambda_i}^{\text{prod}} &= J_i^\mu \varepsilon_{\lambda_i, \mu}^*, & K_i &= k_i^2 - M_W^2, & i &= 1, 2, \\ i\mathcal{M}_{\lambda_f}^{\text{decay}} &= J_f^\mu \varepsilon_{\lambda_f, \mu}, & K_f &= k_f^2 - M_W^2 + iM_W \Gamma_W, & f &= 3, 4. \end{aligned}$$

On-Shell Projection

In order to guarantee **gauge invariance** of the amplitude we need to consider **on-shell** W-boson scattering.

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Where the on-shell momenta are defined as follows

$$\begin{aligned} \text{VBS :} \quad & \tilde{k}_{12}^\mu = \frac{\sqrt{\tilde{s}}}{2} (1, 0, 0, \pm\beta), & \tilde{k}_{3/4}^\mu &= \frac{\sqrt{\tilde{s}}}{2} (1, \pm\beta \sin \tilde{\theta}, 0, \pm\beta \cos \tilde{\theta}), \\ \text{Decay :} \quad & \tilde{p}'_{3/4}{}^\mu = p'_{3/4}{}^\mu \frac{M_W^2}{2\tilde{k}_{3/4} \cdot p'_{3/4}}, & \tilde{p}_{3/4}^\mu &= \tilde{k}_{3/4}^\mu - \tilde{p}'_{3/4}{}^\mu, \end{aligned}$$

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$$\tilde{s} = 4 M_W^2 - t - u, \quad \beta = \sqrt{1 - 4M_W^2/\tilde{s}}, \quad \cos \tilde{\theta} = 1 + 2t/\tilde{s}\beta^2.$$

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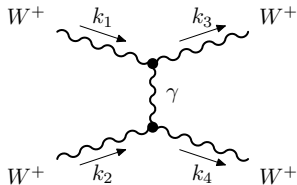
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Why do we keep t and u fixed? → Appearance of a photon pole!

The Photon Pole

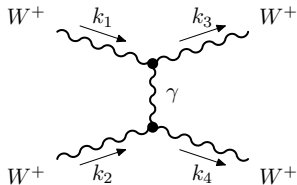


$$\begin{aligned} \widetilde{\mathcal{M}}^{\gamma,t} &\propto \frac{1}{\tilde{t}} & \tilde{t} &= -\frac{\tilde{s}\beta^2}{2}(1 - \cos\theta) \xrightarrow{\theta \rightarrow 0} 0, \\ \widetilde{\mathcal{M}}^{\gamma,u} &\propto \frac{1}{\tilde{u}} & \tilde{u} &= -\frac{\tilde{s}\beta^2}{2}(1 + \cos\theta) \xrightarrow{\theta \rightarrow \pi} 0 \end{aligned}$$

Physically a consequence of the of the infinite range of the Coulomb potential. Appears also in Møller-, Bhabha-, and in Rutherford scattering.

→ either cut on scattering angle θ or fix invariants t and u in the on-shell projection.

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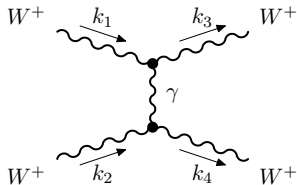
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Note: Photon pole lies outside the physical phase space of the full $2 \rightarrow 6$ process!

Numerical Results - Phase Space Cuts

We first use standard VBS cuts³:

- Jet recombination:

$$D = 0.7, \quad k_T \text{ algorithm.}$$

- Cuts on jets:

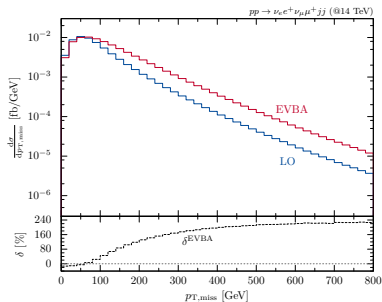
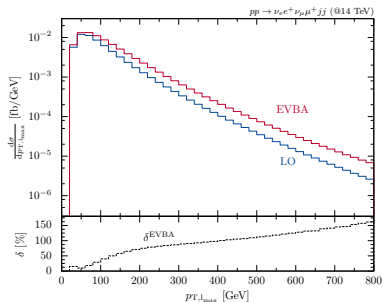
$$\begin{aligned} p_{T,j} &> 20 \text{ GeV}, & |y_j| &< 4.5, \\ M_{jj} &> 600 \text{ GeV}, & y_{j_1} \times y_{j_2} &< 0, \\ \Delta y_{jj} &> 4. \end{aligned}$$

- Cuts on leptons:

$$\begin{aligned} p_{T,l} &> 20 \text{ GeV}, & |y_l| &< 2.5, \\ \Delta R_{jl} &> 0.4, & y_{l_{\min}} &< y_l < y_{l_{\max}}, \\ \Delta R_{ll} &> 0.1. \end{aligned}$$

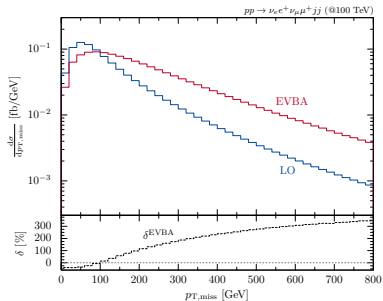
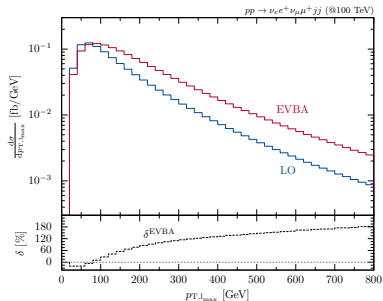
³Denner, Hosekova, Kallweit '12 [arXiv:1209.2389]

Numerical Results - EVBA I



\sqrt{s} [TeV]	σ_{LO} [fb]	σ_{EVBA} [fb]	δ^{EVBA}
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- Cuts on leptons:

$$\begin{aligned} p_{T,l} &> 20 \text{ GeV}, & |y_l| &< 2.5, \\ \Delta R_{jl} &> 0.4, & y_{j_{\min}} &< y_l < y_{j_{\max}}, \\ \Delta R_{ll} &> 0.1. \end{aligned}$$

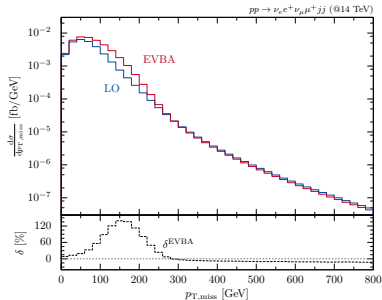
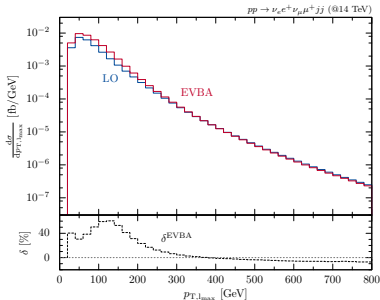
Numerical Results - Upper $p_{T,j}$ Cut

We now require $p_{T,j} < 150$ GeV.

\sqrt{s} [TeV]	σ_{LO} [fb]	σ_{EVBA} [fb]	δ^{EVBA}
14	0.579(1)	0.817(2)	41.1 %
100	4.81(2)	6.38(3)	32.6 %

Numerical Results - Upper $p_{T,j}$ Cut

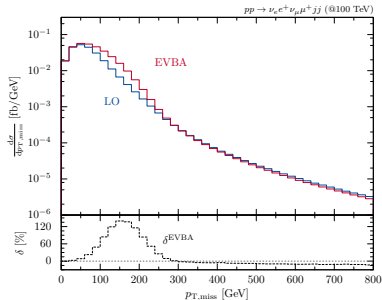
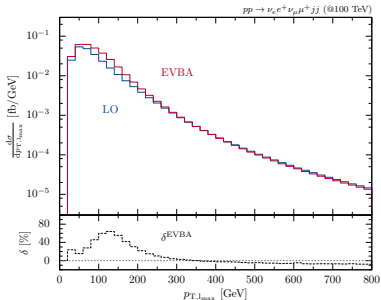
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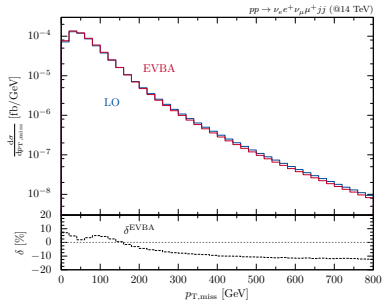
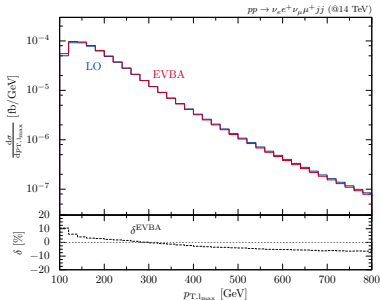
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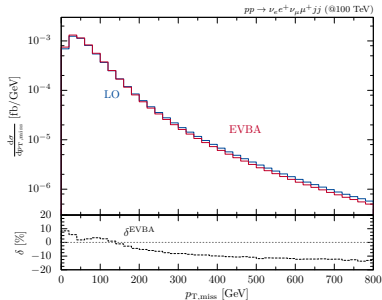
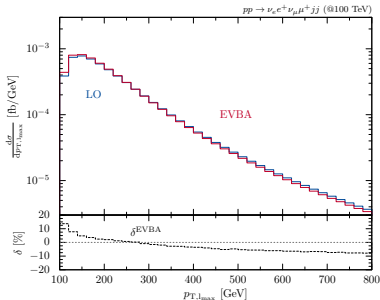
We now require $p_{T,j} < 100$ GeV and $p_{T,l} > 100$ GeV.



\sqrt{s} [TeV]	σ_{LO} [fb]	σ_{EVBA} [fb]	δ^{EVBA}
14	0.011584(4)	0.011985(3)	3.5 %
100	0.11433(6)	0.11772(5)	3.0 %

Numerical Results - Upper $p_{T,j}$ Cut

We now require $p_{T,j} < 100$ GeV and $p_{T,l} > 100$ GeV.



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- 2 Vector-Boson Scattering at the LHC
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- 4 Logarithmic Electroweak Corrections**
- 5 Conclusion

Logarithmic Electroweak Corrections

Typical one-loop Feynman diagrams that lead to [Sudakov logarithms](#):

$$\sum_{k=1}^n \sum_{l < k} \sum_{V_a = A, Z, W^\pm} \quad \text{Diagram: } \begin{array}{c} \text{---} k \\ \text{---} \text{---} \text{---} \\ \text{---} l \end{array}$$

The diagram shows a bubble diagram with two external lines labeled \$k\$ and \$l\$. The bubble is connected to the \$k\$ line at the top and the \$l\$ line at the bottom. A wavy line labeled \$V\$ connects the two vertices of the bubble.

For high energies, i.e. $s \gg M_W^2$, logarithms become dominant and are of significant size

$$\frac{\alpha}{4\pi s_W^2} \log^2 \frac{s}{M_W^2} \simeq 6.6\%, \quad \frac{\alpha}{4\pi s_W^2} \log \frac{s}{M_W^2} \simeq 1.3\%,$$

at $\sqrt{s} = 1 \text{ TeV}$. \rightarrow for VBS at the LHC we can approximate the EW corrections by considering only these logarithms!

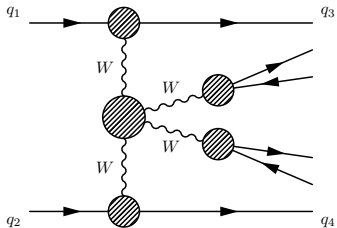
In LA the correction factorizes

$$\delta \mathcal{M}^{i_1 \dots i_n} = \mathcal{M}_0^{i'_1 \dots i'_n} \delta_{i'_1 i_1 \dots i'_n i_n},$$

and the correction factor can be decomposed

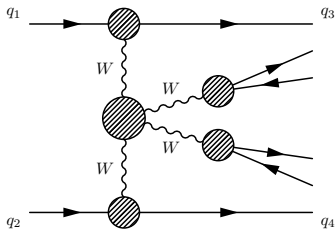
$$\delta = \underbrace{\delta^{\text{LSC}} + \delta^{\text{C}} + \delta^{\text{PR}}}_{= \delta^{\text{LL}}} + \underbrace{\delta^{\text{SSC}}}_{= \delta^{\text{NLL}}},$$

Radiative Corrections to VBS



- We neglect **non-factorizable** corrections.
- We neglect corrections to the **emission and decay** process.

Radiative Corrections to VBS



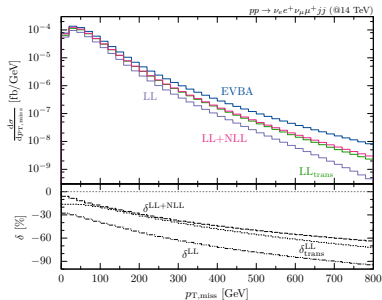
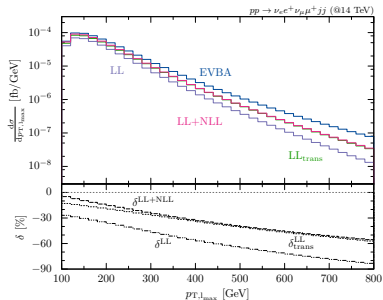
- We neglect **non-factorizable** corrections.
- We neglect corrections to the **emission and decay** process.

→ We consider **only corrections** to the $W^+W^+ \rightarrow W^+W^+$ subprocess.

Hence, using the EVBA the correction can be written as

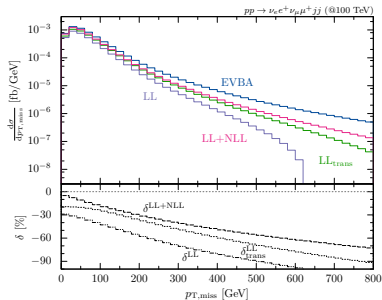
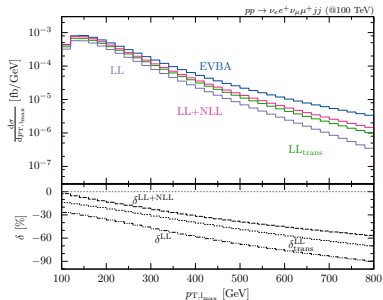
$$\delta\mathcal{M}_{qq}^{\text{EVBA}} = \sum_{\lambda_1, \lambda_2, \lambda_3, \lambda_4} \frac{(-1)^{\lambda_1 + \lambda_2}}{K_1 K_2 K_3 K_4} \mathcal{M}_{\lambda_1}^{\text{prod}} \mathcal{M}_{\lambda_2}^{\text{prod}} \times \delta\widetilde{\mathcal{M}}_{\lambda_1 \lambda_2 \lambda_3 \lambda_4}^{\text{VBS}} \times \widetilde{\mathcal{M}}_{\lambda_3}^{\text{decay}} \widetilde{\mathcal{M}}_{\lambda_4}^{\text{decay}}.$$

Numerical Results - EW Logarithms



\sqrt{s} [TeV]	$\delta^{LL_{trans}}$	δ^{LL}	δ^{LL+NLL}
14	-18.9 %	-35.1 %	-13.6 %
100	-23.8 %	-37.5 %	-13.8 %

Numerical Results - EW Logarithms



\sqrt{s} [TeV]	$\delta^{\text{LL+trans}}$	δ^{LL}	$\delta^{\text{LL+NLL}}$
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Conclusion

VBS in general

- Vector Boson Scattering is a key tool in probing the mechanism of EWSB.
- At the LHC all contributing processes need to be fully understood
→ kinematical cuts are required to suppress background contributions
- The EVBA may quantify the dominant region of VBS

EVBA

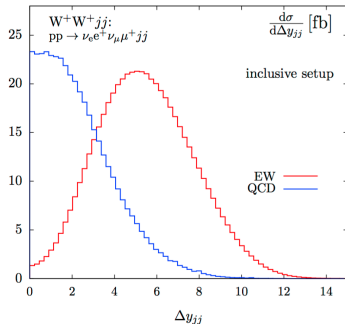
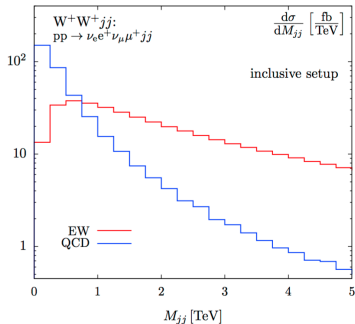
- The photon pole only appears as an artefact in a bad on-shell projection.
- For standard VBS cuts the approximation is not applicable as the collinearity of the W bosons is not ensured.
- If the collinearity is ensured the relative difference only amounts to $\sim 3.5\%$.
→ the EVBA yields an appropriate approximation in certain kinematic regions!

Logarithmic EW Corrections

- Both LL and NLL need to be taken into account.
- The NLO EW correction amounts to -13.6% , which is compatible with the literature.

Biedermann, Denner, Pellen 2017 [arXiv:1708.00268]

QCD Background Suppression Cuts



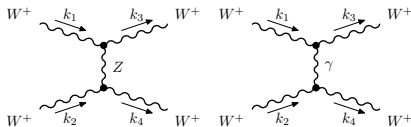
The SU(2) model

We consider a **non-Abelian SU(2) model** in which no photon field appears.

$$SU(2)_W \times U(1)_Y : D_\mu = \partial_\mu - ig I_W^i W_\mu^i + ig' \frac{Y}{2} B_\mu,$$

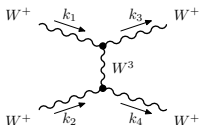
$$\downarrow \quad g' \rightarrow 0 \quad (g = g_{SM} = g_{SU(2)} = e/s_w)$$

$$SU(2)_W : D_\mu = \partial_\mu - ig I_W^i W_\mu^i.$$



$$\mathcal{M}^{Z,t} \propto \frac{c_W^2}{s_W^2} \frac{1}{t - M_Z^2}$$

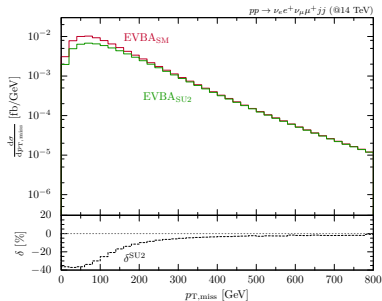
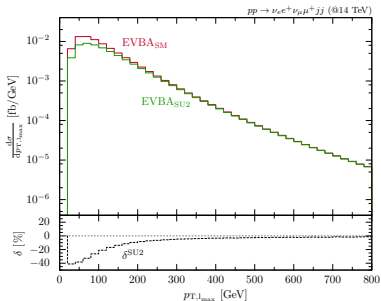
$$\mathcal{M}^{\gamma,t} \propto \frac{1}{t}$$



$$\mathcal{M}^{W^3,t} \propto \frac{1}{s_W^2} \frac{1}{t - M_W^2}$$

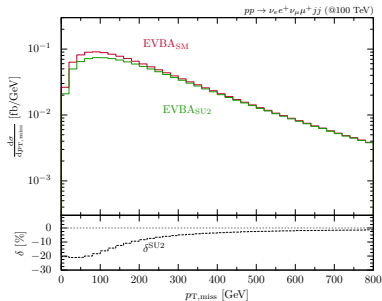
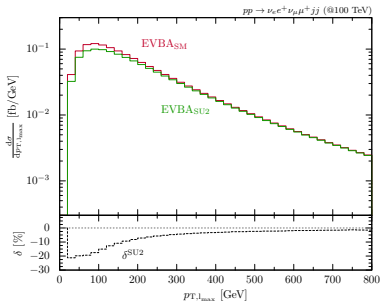
→ no photon diagrams → no photon pole!

Numerical Results - $SU(2)$ model



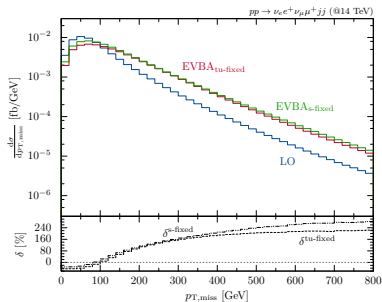
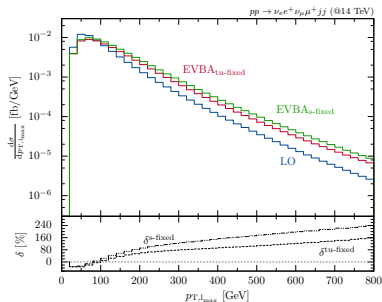
\sqrt{s} [TeV]	σ_{EVBA} [fb]	σ_{EVBA}^{SU2} [fb]	δ^{SU2}
14	1.6396(2)	1.2389(2)	-24.4 %
100	27.689(5)	24.713(5)	-10.7 %

Numerical Results - $SU(2)$ model



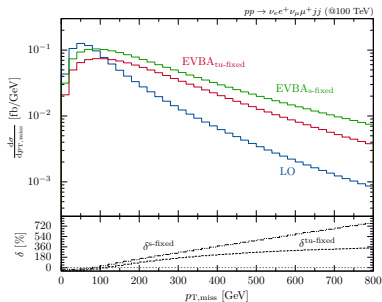
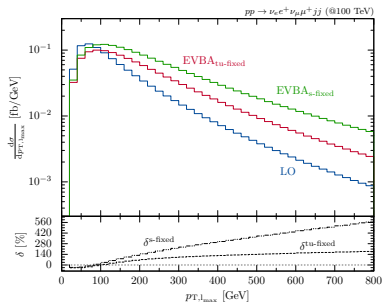
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Numerical Results - s fixed



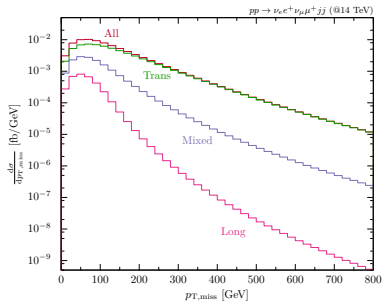
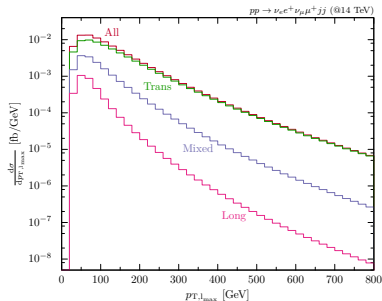
\sqrt{s} [TeV]	σ_{LO} [fb]	$\sigma_{EVBA}^{s-fixed}$ [fb]	$\sigma_{EVBA}^{tu-fixed}$ [fb]	$\delta^{s-fixed}$	$\delta^{tu-fixed}$
14	1.2240(2)	1.4042(2)	1.2389(2)	14.7 %	1.2 %
100	19.289(3)	36.247(5)	24.713(5)	87.9 %	28.2 %

Numerical Results - s fixed



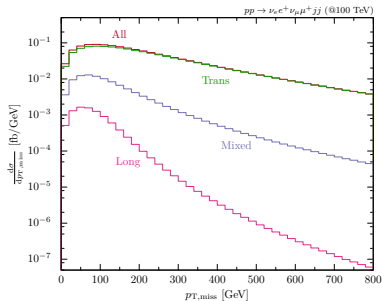
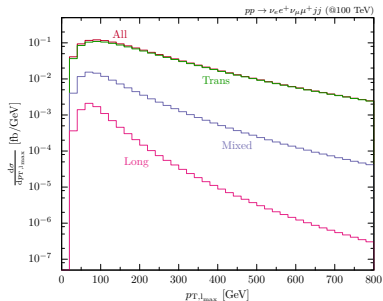
\sqrt{s} [TeV]	σ_{LO} [fb]	$\sigma_{\text{EVBA}}^{s\text{-fixed}}$ [fb]	$\sigma_{\text{EVBA}}^{tu\text{-fixed}}$ [fb]	$\delta^{s\text{-fixed}}$	$\delta^{tu\text{-fixed}}$
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Numerical Results - Helicity Configurations



\sqrt{s} [TeV]	σ_{EVBA} [fb]	$\sigma_{\text{EVBA}}^{\text{trans}}$ [fb]	$\sigma_{\text{EVBA}}^{\text{mixed}}$ [fb]	$\sigma_{\text{EVBA}}^{\text{long}}$ [fb]
14	1.6396(2)	1.2932(2)	0.32179(8)	0.06605(3)
100	27.689(5)	25.858(5)	2.0833(9)	0.1779(2)

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Complex-Shift Procedure

We set the W bosons **on-shell** by consistently **shifting** external momenta into the **complex plane**.

$$\tilde{p}_i^{\dot{A}B} = p_i^{\dot{A}} \tilde{p}_i^B, \quad \tilde{p}_i^B = p_i^B + \sum_{f=3}^4 z_{if} p_f^B, \quad i = 1, 2,$$

$$\tilde{p}_f^{\dot{A}B} = \tilde{p}_f^{\dot{A}} p_f^B, \quad \tilde{p}_f^{\dot{A}} = p_f^{\dot{A}} + \sum_{i=1}^2 z_{if} p_i^{\dot{A}}, \quad f = 3, 4,$$

Which is fixed by **4 on-shell conditions**

$$\begin{aligned} M_W^2 &= \tilde{k}_i^2 = (\tilde{p}_i - p'_i)^2 = -2\tilde{p}_i \cdot p'_i \\ &= -2p_i \cdot p'_i - \sum_{f=3}^4 z_{if} \langle p_i p'_i \rangle^* \langle p_f p'_i \rangle, \quad i = 1, 2, \end{aligned}$$

$$\begin{aligned} M_W^2 &= \tilde{k}_f^2 = (\tilde{p}_f + p'_f)^2 = 2\tilde{p}_f \cdot p'_f \\ &= 2p_f \cdot p'_f + \sum_{i=1}^2 z_{if} \langle p_i p'_f \rangle^* \langle p_f p'_f \rangle, \quad f = 3, 4. \end{aligned}$$

⇒ leads to inconsistent results which are off by several magnitudes or do not even converge.