
Quantum Field Theory 1 – Tutorial 8

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Problem 1: Slash notation

Using the slash notation $\not{p} = \partial_\mu \gamma^\mu$ introduced by Feynman, the Dirac equation reads

$$(i\not{p} - m)\psi = 0.$$

- a) For $\psi(x) = u(p)e^{-ipx}$ where $p^2 = m^2$, show that the Dirac equation in momentum space reads

$$(\not{p} - m)u(p) = 0. \quad (1)$$

- b) Using the Dirac algebra

$$\{\gamma^\mu, \gamma^\nu\} = 2\eta^{\mu\nu}\mathbb{1},$$

show that for arbitrary $\tilde{u}(p)$

$$u(p) = (\not{p} + m)\tilde{u}(p)$$

solves the Dirac equation (1) when $p^2 = m^2$.