

# Exotic Matter in Neutron Stars and Supernovae

Jürgen Schaffner-Bielich

Institute for Theoretical Physics and  
Heidelberg Graduate School for Fundamental Physics



RUPRECHT-KARLS-  
UNIVERSITÄT  
HEIDELBERG



Seminar, Physics Department

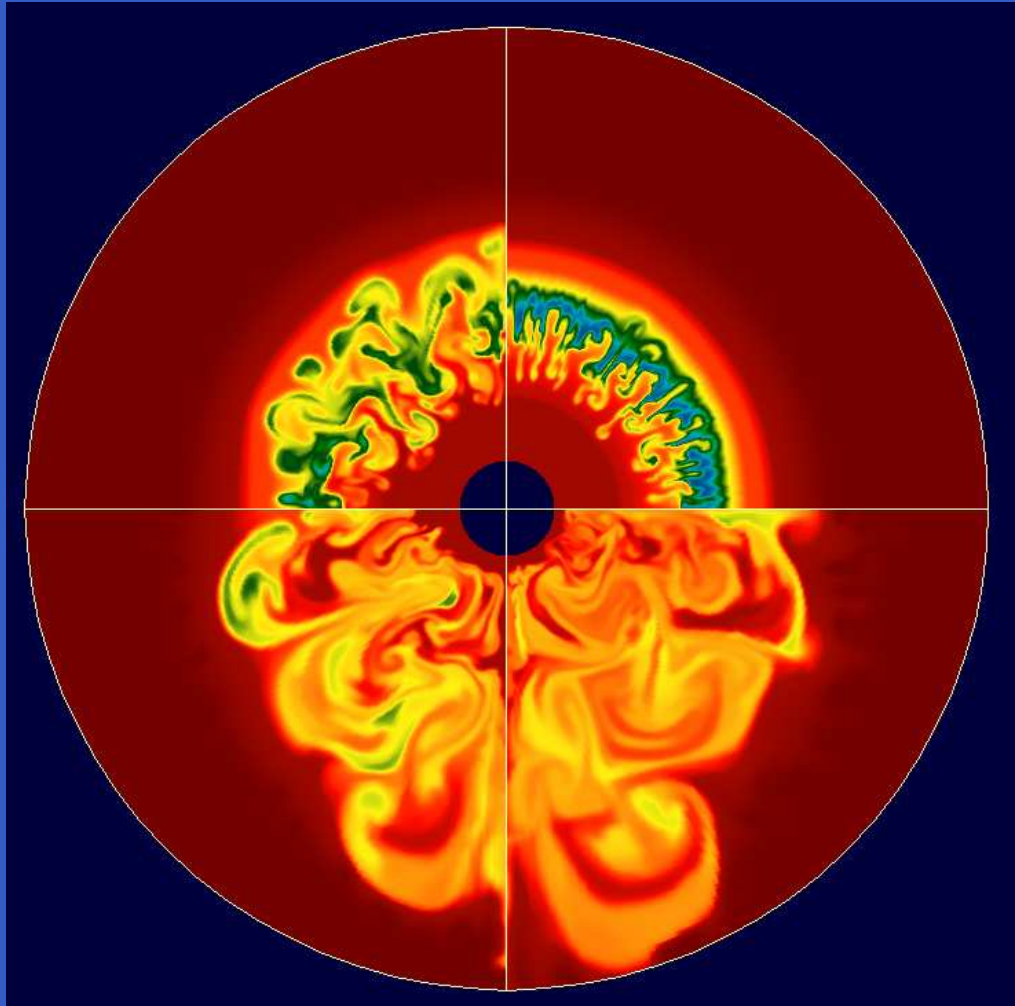
Goethe University, Frankfurt am Main, February 13, 2009

# Outline

- Observations of neutron stars
- Modelling neutron stars
- The FAIR connection:
  - Constraints on the maximum mass of neutron stars from heavy-ion data
  - QCD phase transition and neutron stars
  - QCD phase transition in supernovae
- Summary

# Observational Data of Neutron Stars

# Supernova Explosions



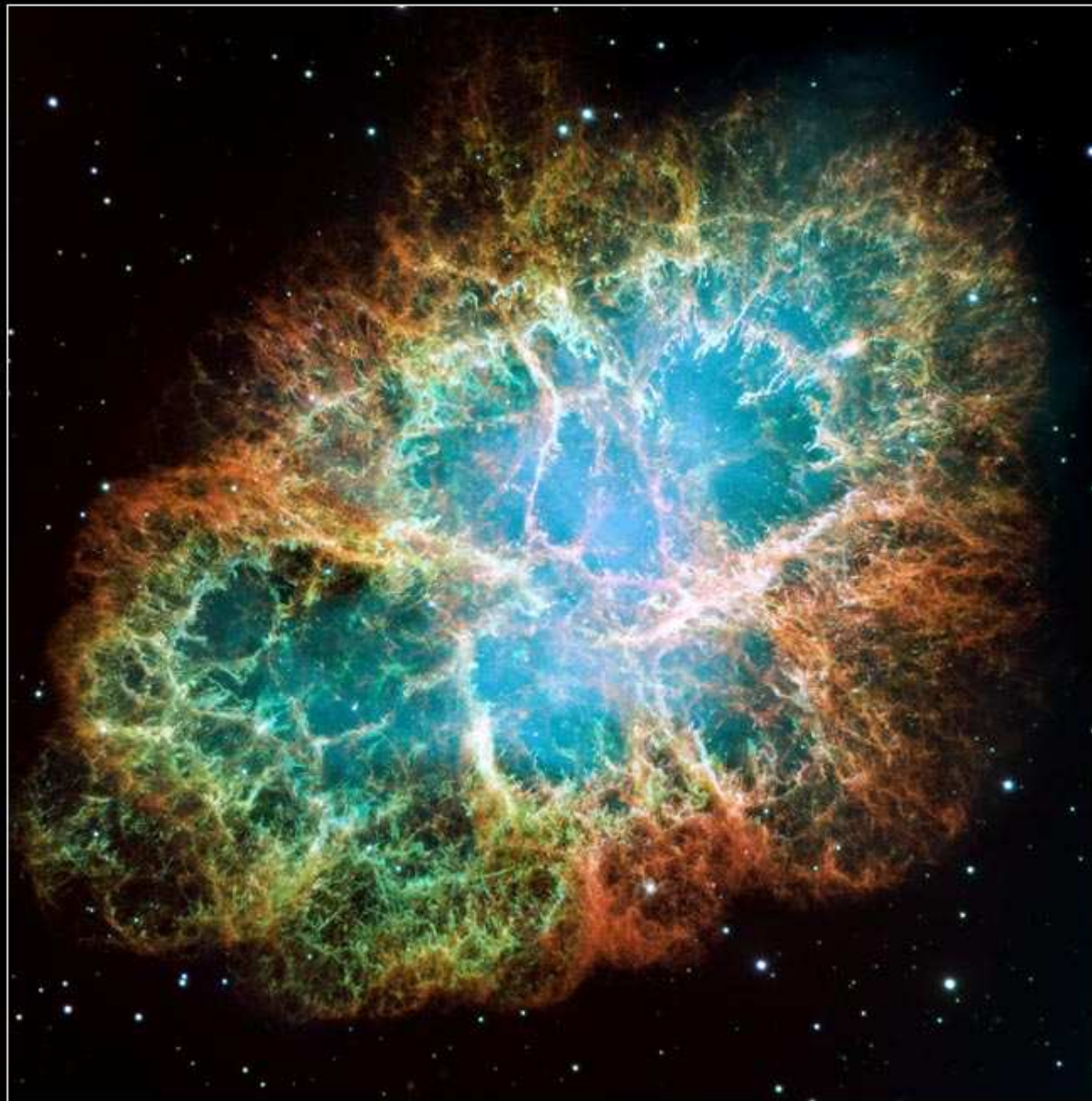
(supernova simulation by Janka et al.,  
MPA Garching)

- stars with a mass of more than 8 solar masses end in a (core collapse) supernova (type II)
- Supernova of AD 1054 was visible for three weeks during daytime (crab nebula)!
- supernovae are several thousand times brighter than a whole galaxy!
- last supernova explosion for the last 400 years in our local group: SN1987A
- most prominent candidate in the universe for producing the heavy elements (r-process)

# Neutron Stars

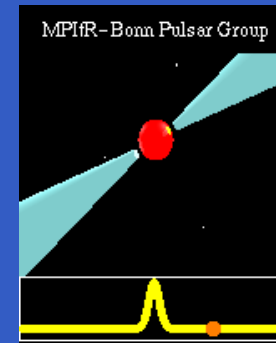
Crab Nebula ■ M1

HST ■ WFPC2



NASA, ESA, and J. Hester (Arizona State University)

STScI-PRC05-37



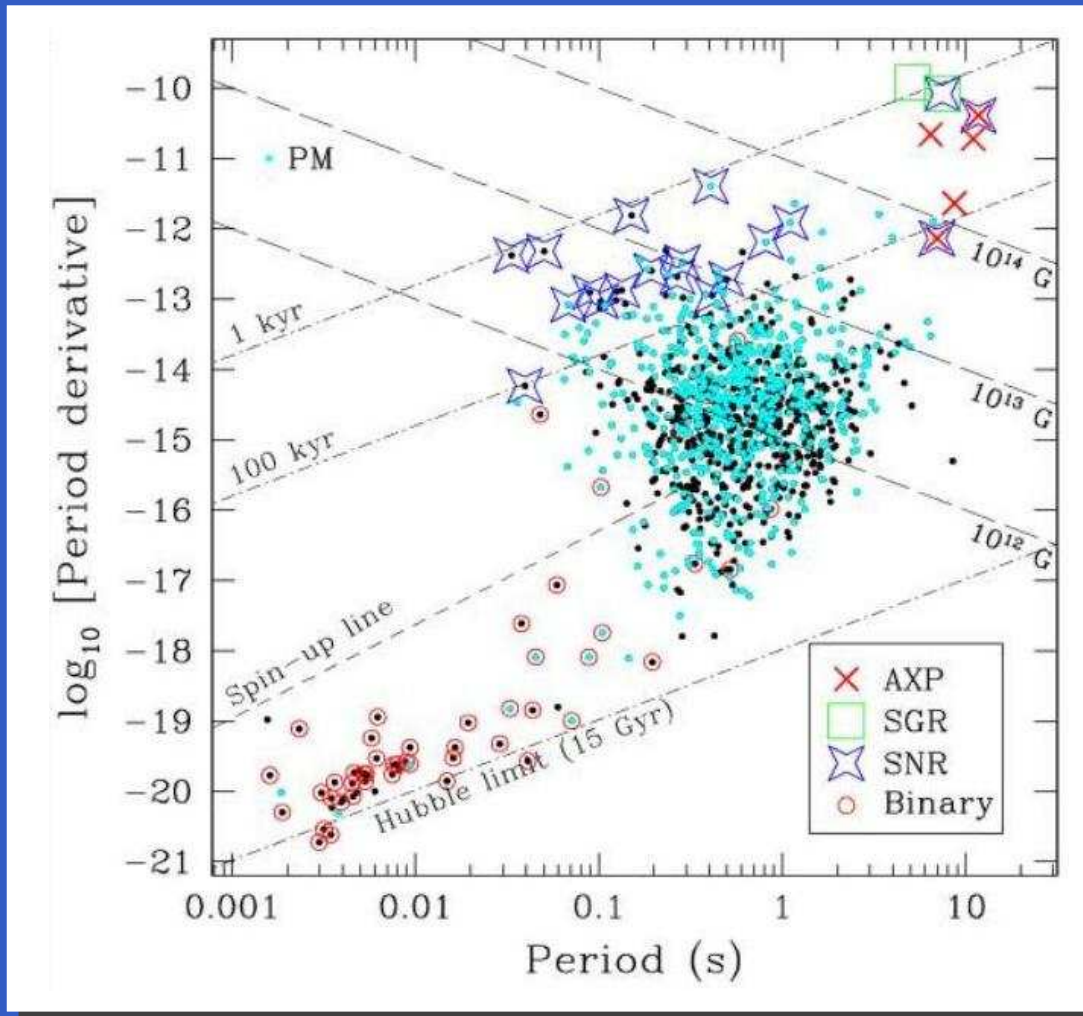
- produced in core collapse supernova explosions
- compact, massive objects: radius  $\approx 10$  km, mass  $1 - 2M_{\odot}$
- extreme densities, several times nuclear density:  $n \gg n_0 = 3 \cdot 10^{14}$  g/cm<sup>3</sup>
- in the middle of the crab nebula: a pulsar, a rotating neutron star!

Movie (seven still images in 11/2000–04/2001)

# The Sounds of Pulsars

- PSR B0329+54: typical pulsar with a period of 0.7145519 s (1.4 pulses per second)
- PSR B0833-45 (Vela pulsar): in Vela supernova remnant, period of 89 ms (11 pulses per second)
- PSR B0531+21 (crab pulsar): youngest known pulsar, in crab nebula (M1), period: 33 ms (30 pulses per second)
- PSR J0437-4715: recently discovered pulsar, period of 5.7 ms (174 pulses per second)
- PSR B1937+21: second fastest known pulsar with a period of 1.56 ms (642 pulses per second)

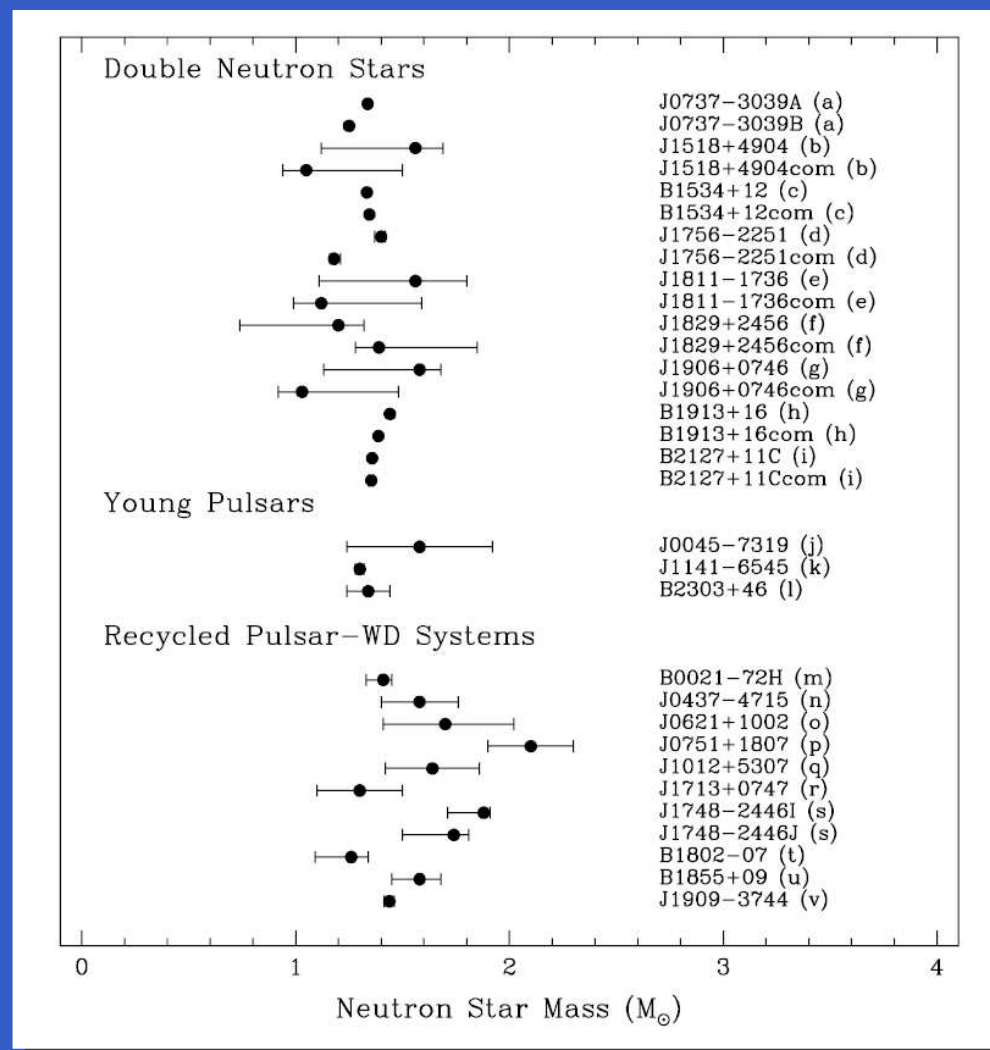
# The Pulsar Diagram



(ATNF pulsar catalog)

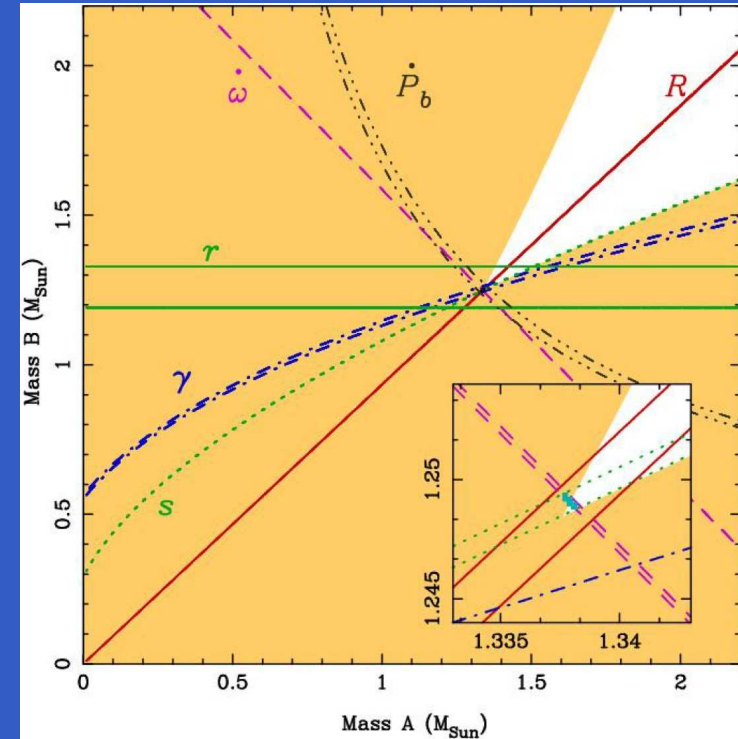
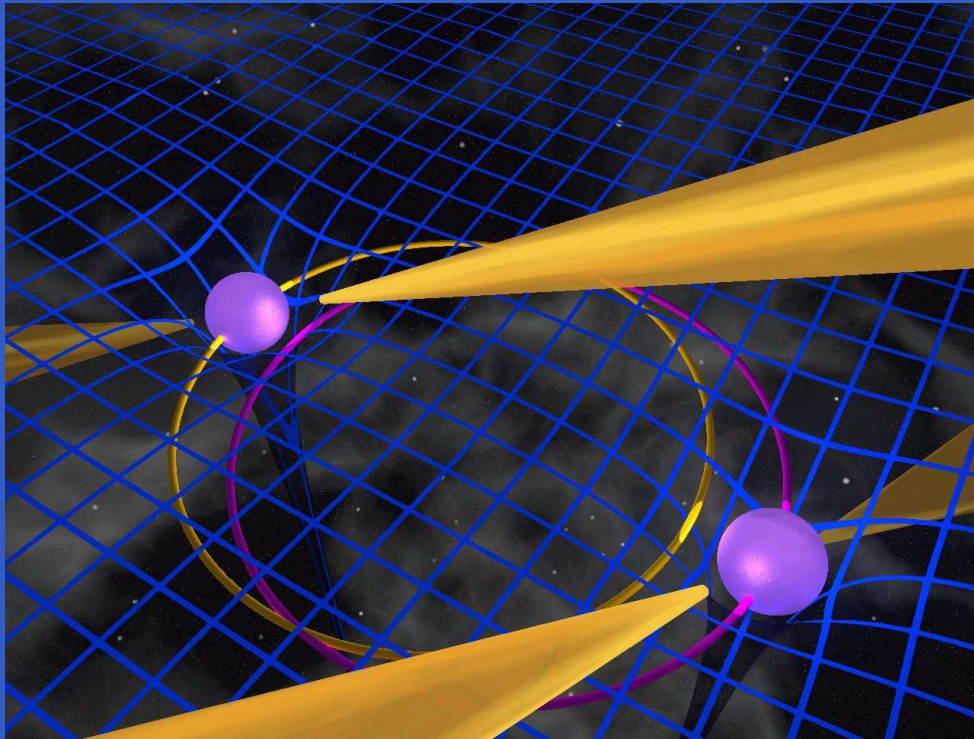
- the diagram for pulsars: period versus period change ( $P-\dot{P}$ )
- dipole model for pulsars:  
characteristic age:  $\tau = P/(2\dot{P})$   
and magnetic field  
 $B = 2 \cdot 10^{19} (P \cdot \dot{P})^{1/2}$  Gauss
- anomalous x-ray pulsars: AXP,  
soft-gamma ray repeaters:  
SGR, young pulsars in  
supernova remnants: SNR
- rapidly rotating pulsars (millisecond pulsars): mostly in binary systems (old recycled pulsars!)

# Masses of Pulsars (Stairs, 2006)



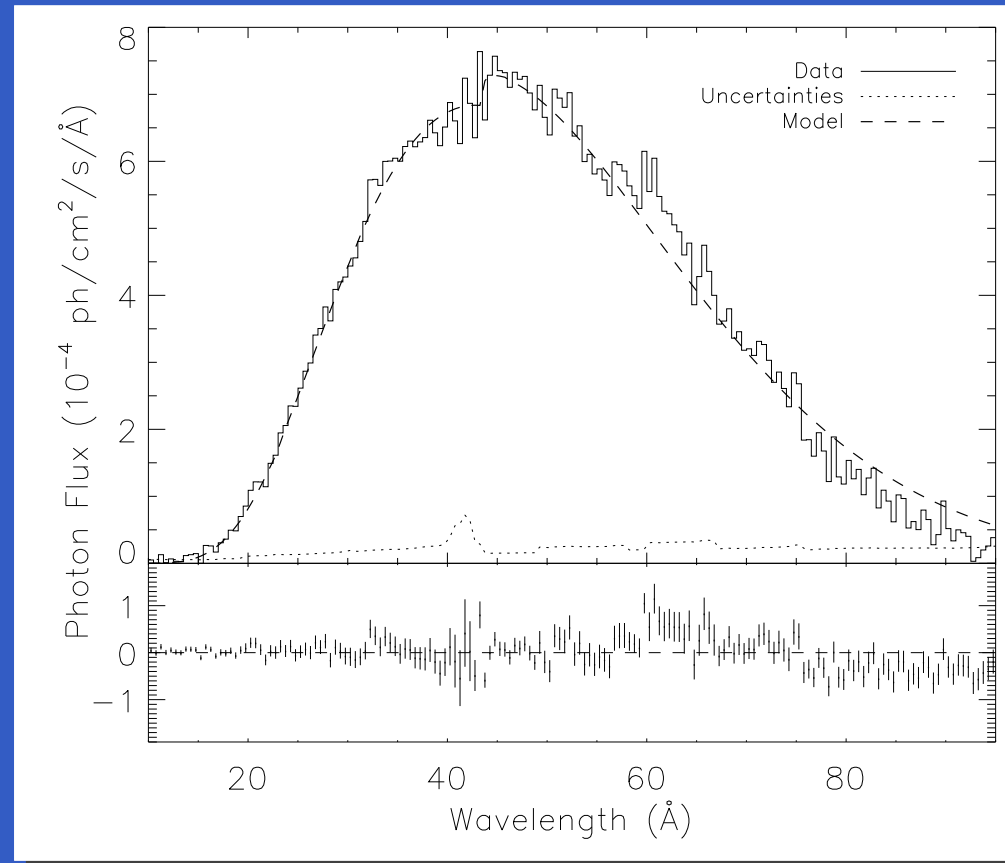
- more than 1700 pulsars known
- best determined mass:  
 $M = (1.4414 \pm 0.0002)M_{\odot}$   
for the Hulse-Taylor pulsar  
(Weisberg and Taylor, 2004)
- smallest known mass:  
 $M = (1.18 \pm 0.02)M_{\odot}$  for  
pulsar J1756-2251  
(Faulkner et al., 2005)
- PSR J0751+1807 corrected  
from  $M = 2.1 \pm 0.2M_{\odot}$  to  
 $M = 1.14 - 1.40M_{\odot}$   
(Nice et al. 2008)

# The Double Pulsar PSR J0737-3039



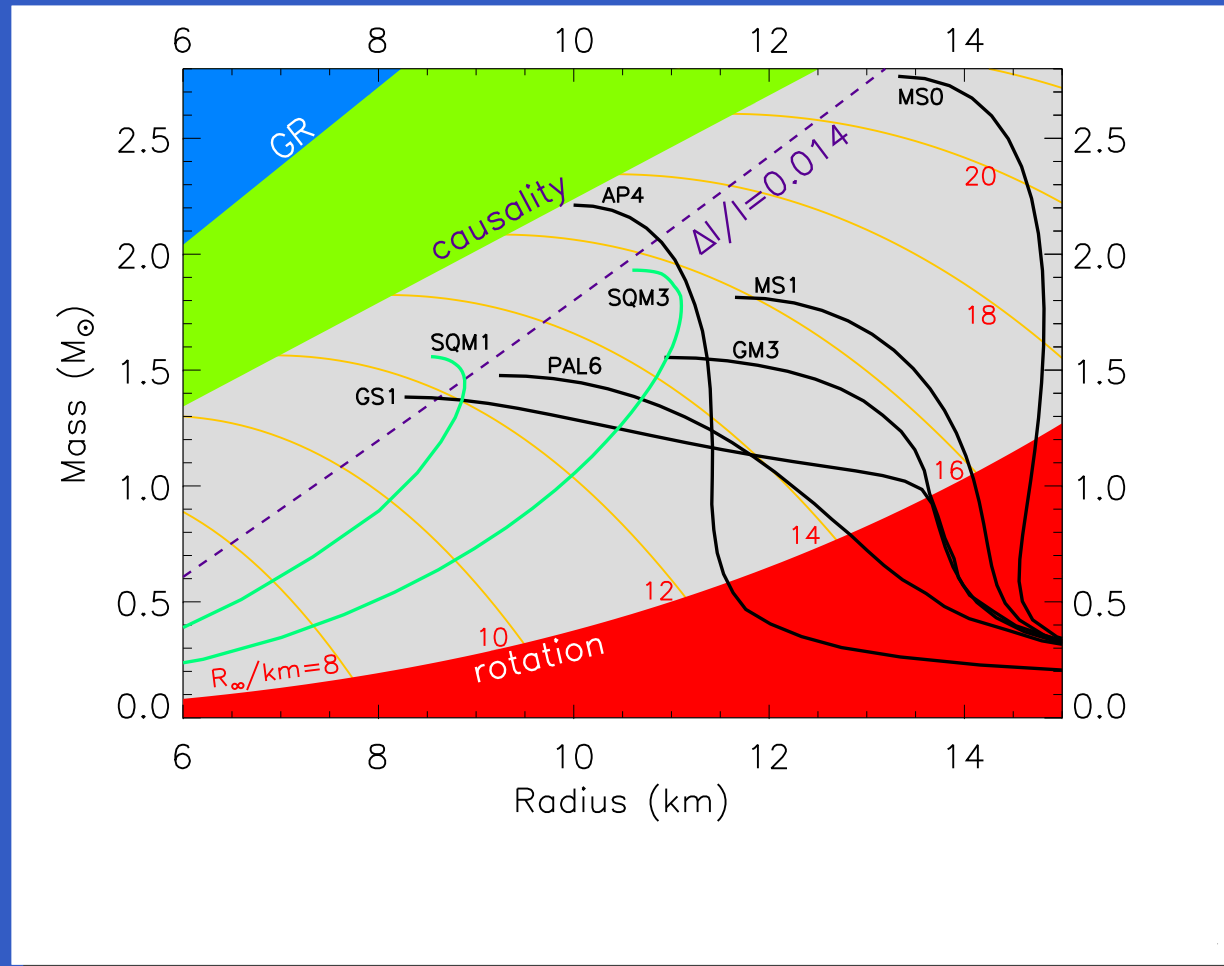
- sensational discovery of two pulsars orbiting each other (Lyne et al. 2004)
- measured five post-Keplerian parameters: Shapiro delay  $r$  and  $s$ , redshift  $\gamma$ , periastron advance  $\dot{\omega}$ , decrease in orbital period  $\dot{P}_b$  (Kramer et al. 2006)
- all in agreement with the prediction of GR to within 0.05% !
- fundamental tests of General Relativity in STRONG fields

# Isolated Neutron Star RX J1856 (Drake et al. (2002))



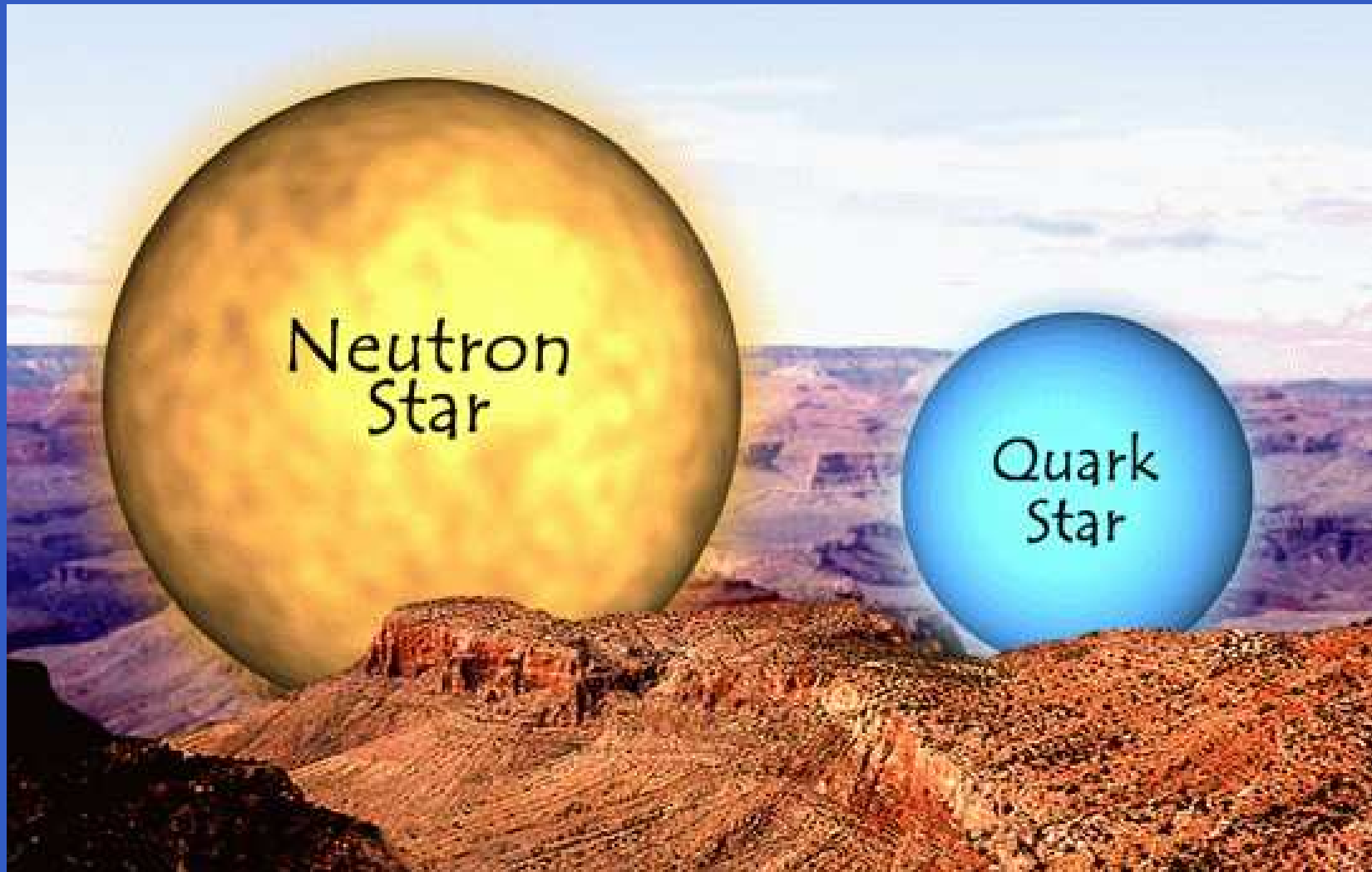
- closest known neutron star, parallax measurement with HST:  
 $D = 117 \pm 12$  pc (Lattimer and Wolter 2002),  $D = 140 \pm 40$  pc (van Kerkwijk and Kaplan 2004),  $D = 161 \pm 18$  pc (Kaplan 2007)
- perfect black-body spectrum, no spectral lines!
- for black-body emission (x-ray part only):  $T = 60$  eV and  $R_\infty = 4 - 8$  km!

# Constraints on the Mass–Radius Relation (Lattimer and Prakash (2004))



- spin rate from PSR B1937+21 of 641 Hz:  $R < 15.5$  km for  $M = 1.4M_{\odot}$
- Schwarzschild limit (GR):  $R > 2GM = R_s$
- causality limit for EoS:  $R > 3GM$
- only quark stars can have small radii!

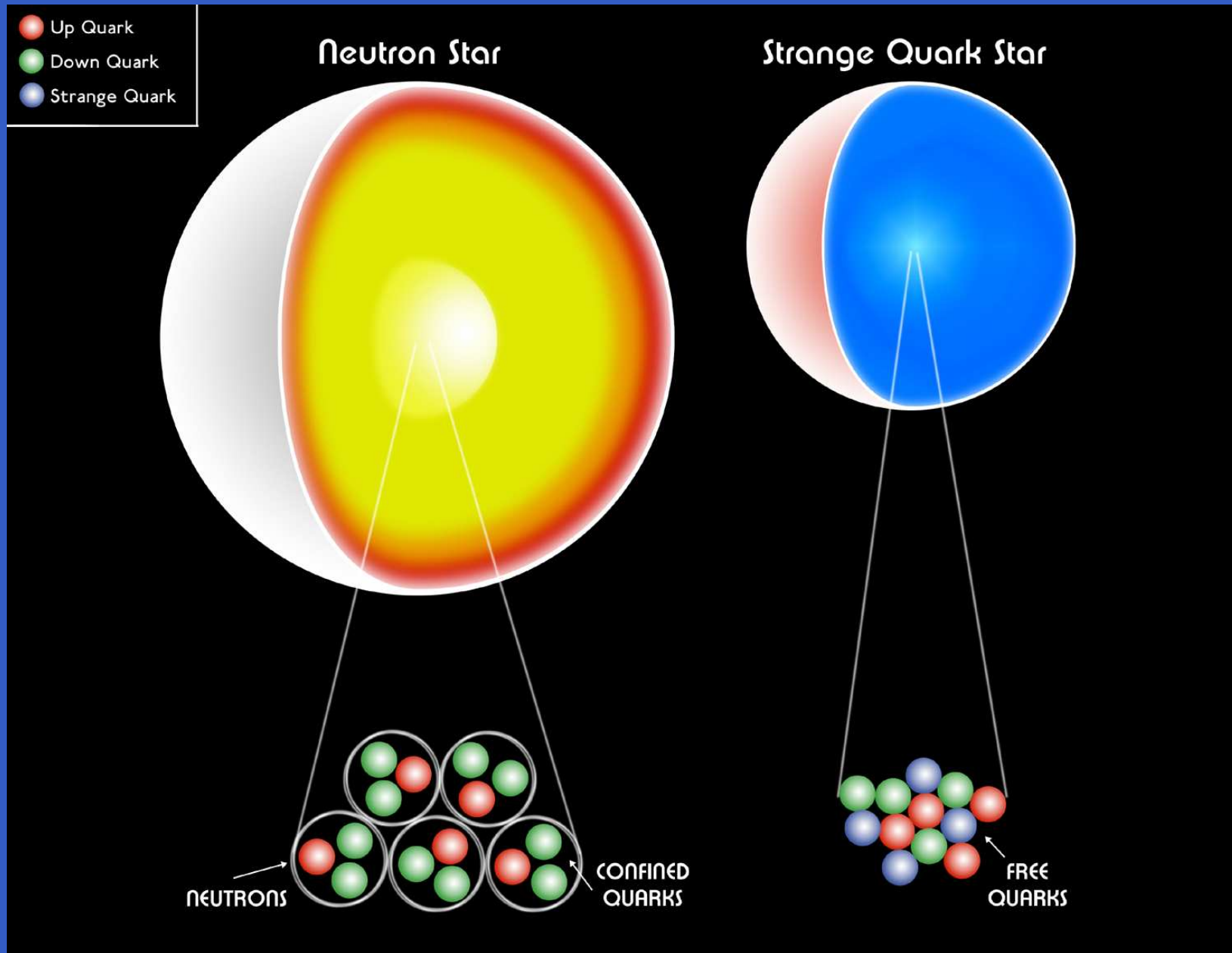
# A Quark Star? (NASA press release 2002)



NASA news release 02-082:

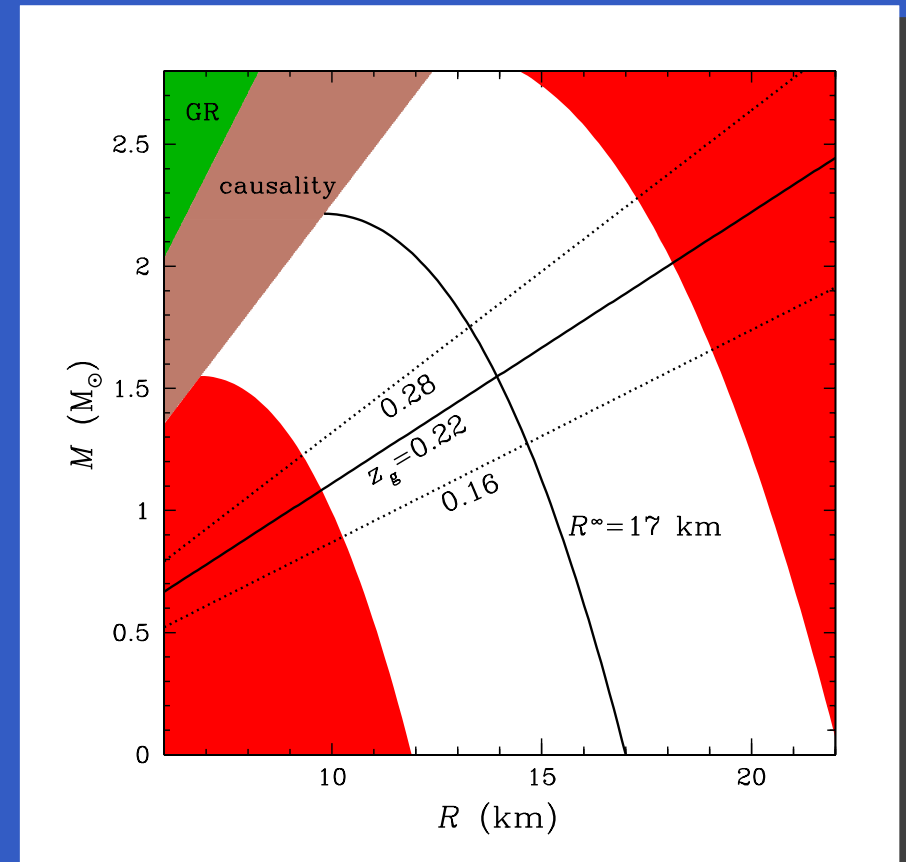
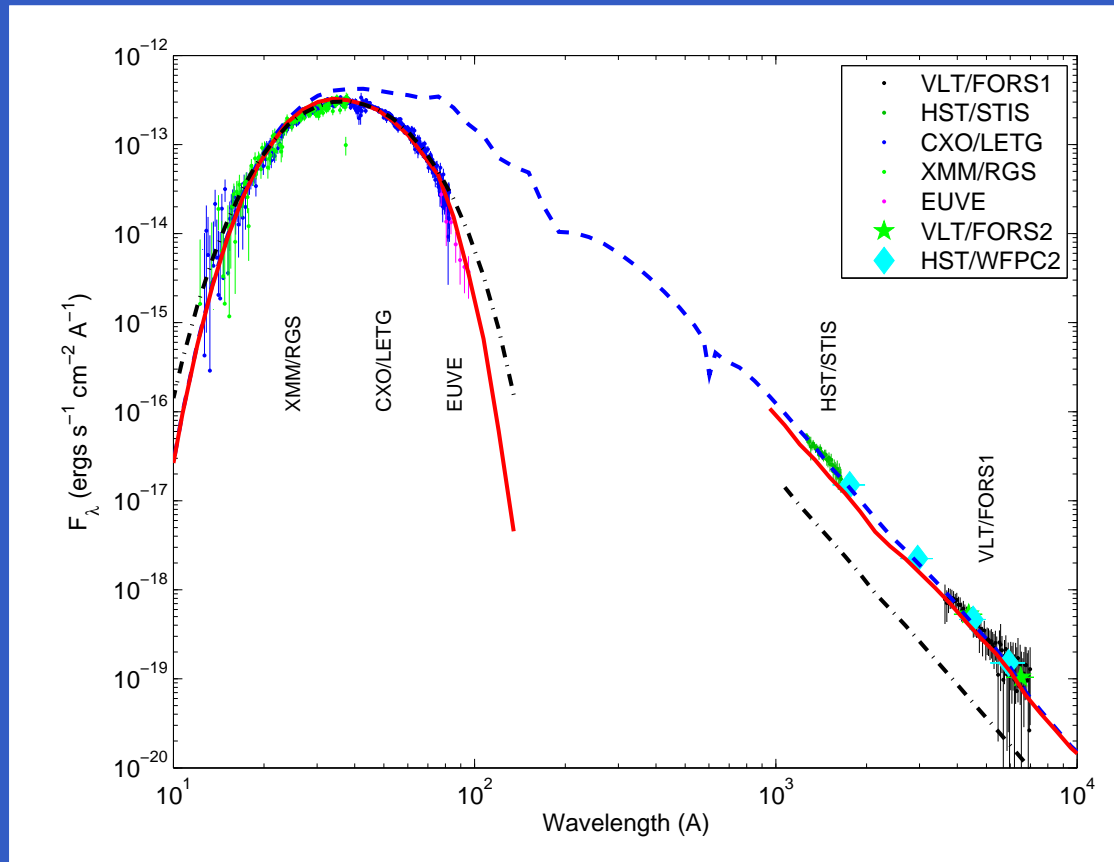
“Cosmic X-rays reveal evidence for new form of matter”  
— a quark star?

# Neutron Star versus Strange Quark Star



(Chandra X-Ray Center, 2002)

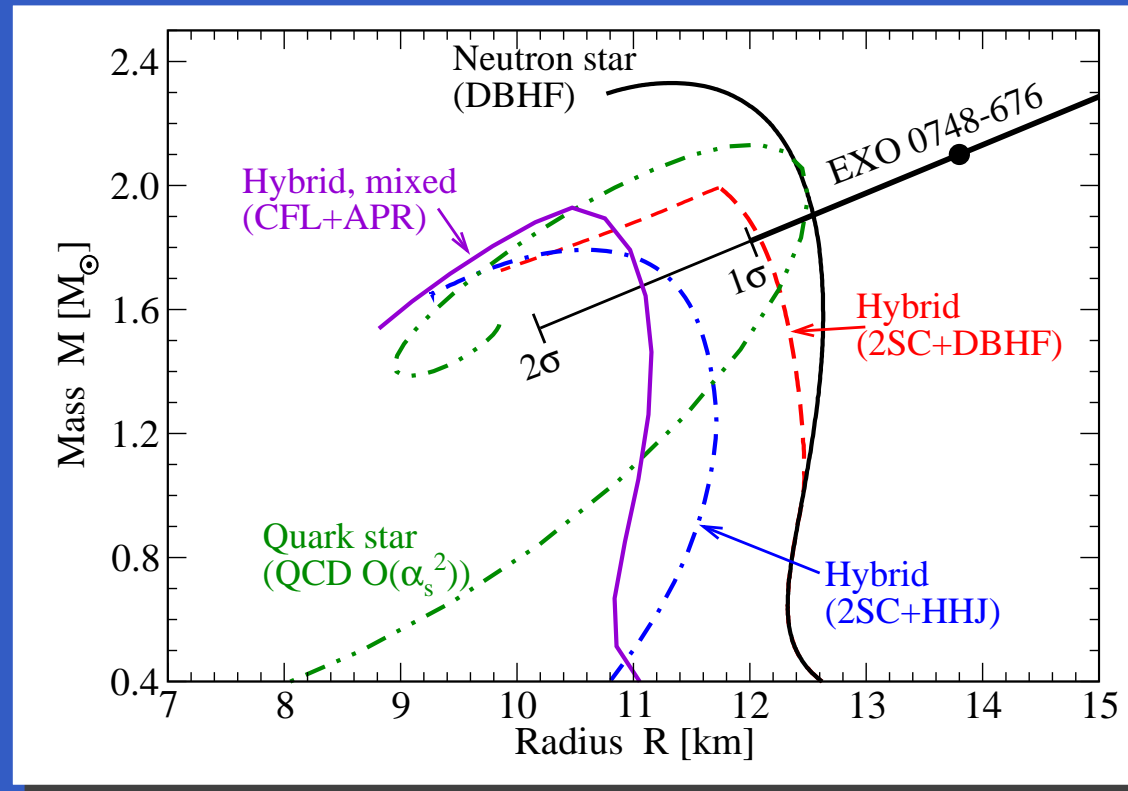
# RXJ 1856: Neutron Star or Quark Star? (Ho et al. (2007))



- two-temperature black-body fit implies a lower limit for radiation radius:  
 $R_\infty = R / \sqrt{1 - 2GM/R} \approx 17 \text{ km (d/140 pc)}$
- thin magnetized H-atmosphere on condensed iron core (Ho et al.):  
redshift  $z_g \approx 0.22$ :  $R \approx 14 \text{ km}$  and  $M \approx 1.55 M_\odot$
- not necessarily a quark star!



# X-Ray burster EXO 0748–676



- analysis of Özel (Nature 2006):  $M \geq 2.10 \pm 0.28M_{\odot}$  and  $R \geq 13.8 \pm 1.8$  km, claims: 'unconfined quarks do not exist at the center of neutron stars'!
- reply by Alford, Blaschke, Drago, Klähn, Pagliara, JSB (Nature 445, E7 (2007)): limits rule out soft equations of state, not quark stars or hybrid stars!
- multiwavelength analysis of Pearson et al. (2006): data more consistent with  $M = 1.35M_{\odot}$  than with  $M = 2.1M_{\odot}$

# Future: Square Kilometer Array (SKA)



- receiving surface of 1 million square kilometers
- 1 billion dollar international project
- potential to discover:
  - 10,000 to 20,000 new pulsars
  - up to 6,000 millisecond pulsars
  - at least 100 compact relativistic binaries!
- probing the equation of state at extreme limits!
- cosmic gravitational wave detector by using pulsars as clocks!
- design and location not fixed yet

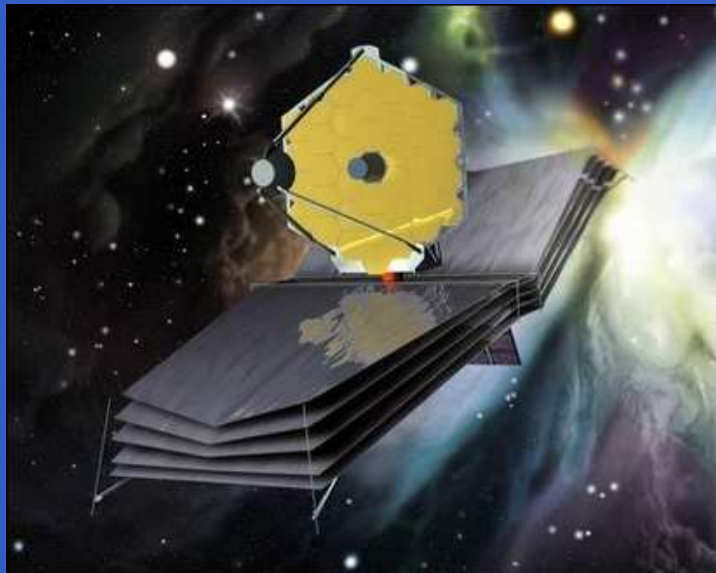
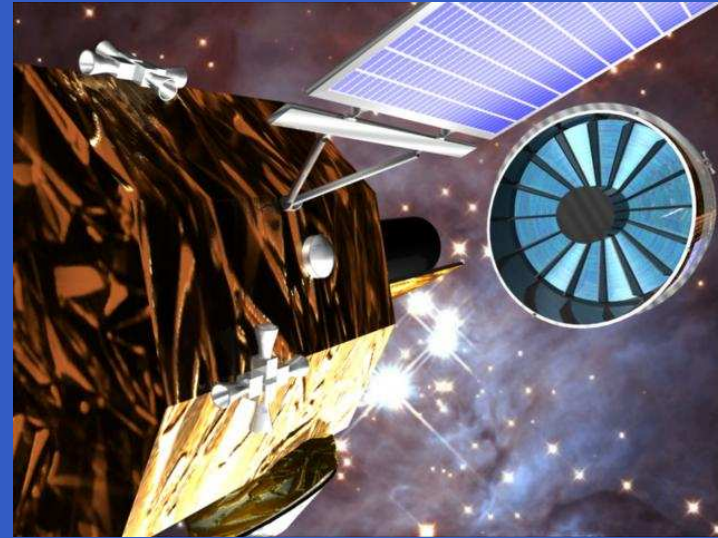
movie

# Future Telescopes and Detectors in Space

Constellation-X (Photo: NASA)



XEUS (Photo: ESA)

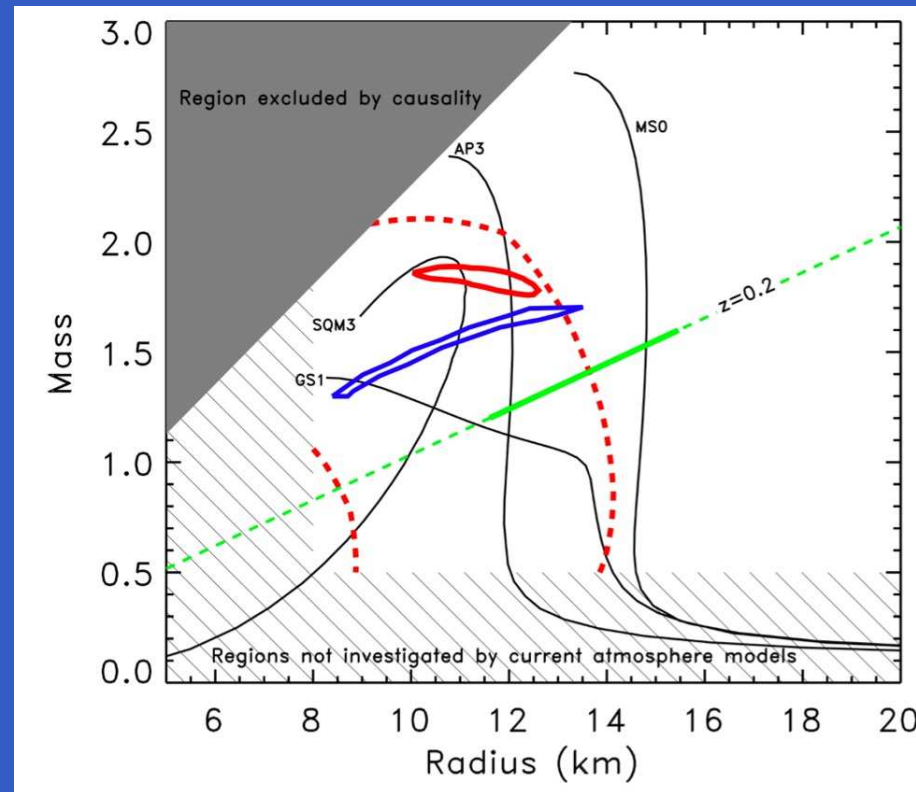


James Webb Space Telescope (Photo: ESA)



LISA (Photo: NASA)

# Probes Using the International X-Ray Observatory (IXO)

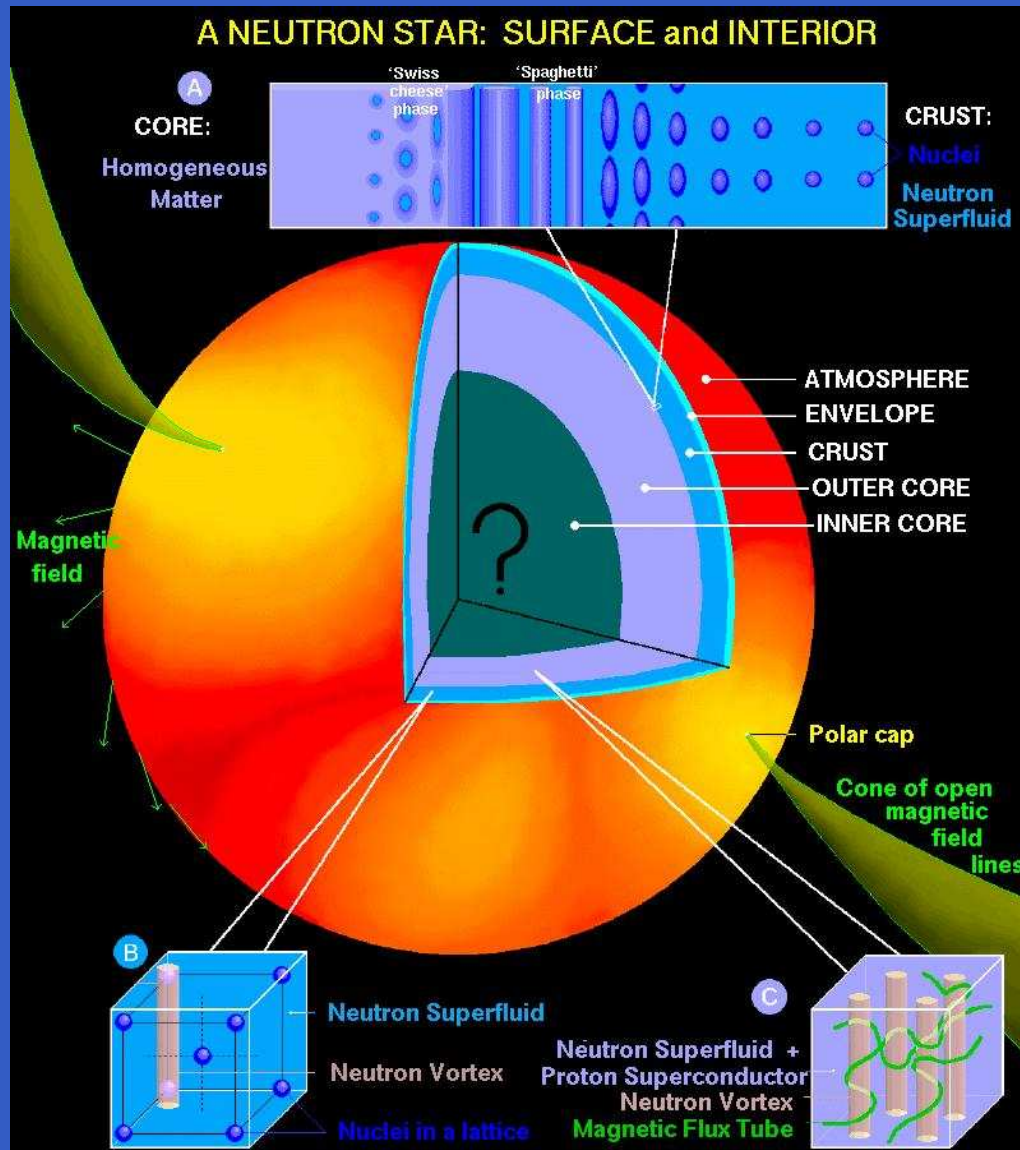


(Cackett et al., IXO Extreme States of Matter Working Group (2009))

- hydrogen atmosphere model fitting of quiescent neutron stars (red)
- waveform fitting of pulsations of accreting millisecond pulsar (spectral profile is modified from space-time warpage) (blue)
- X-ray bursts spectroscopy, gravitationally redshifted absorption lines (green)
- IXO can provide strong constraints on the mass-radius ratio

# Modelling the Neutron Star

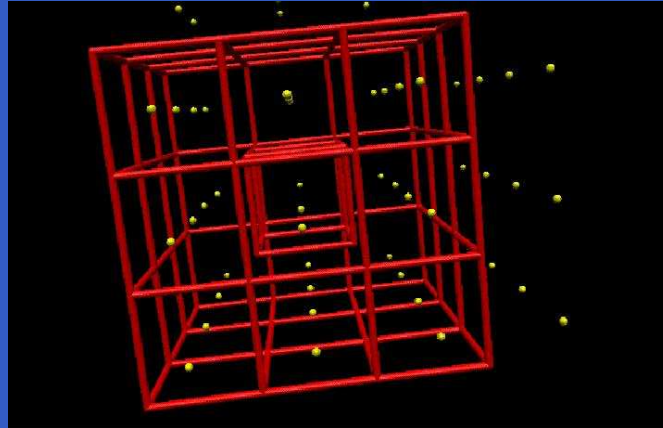
# Structure of Neutron Stars — the Crust (Dany Page)



- $n \leq 10^4 \text{ g/cm}^3$ :  
atmosphere  
(atoms)
- $n = 10^4 - 4 \cdot 10^{11} \text{ g/cm}^3$ :  
outer crust or envelope  
(free  $e^-$ , lattice of nuclei)
- $n = 4 \cdot 10^{11} - 10^{14} \text{ g/cm}^3$ :  
Inner crust  
(lattice of nuclei with free  
neutrons and  $e^-$ )

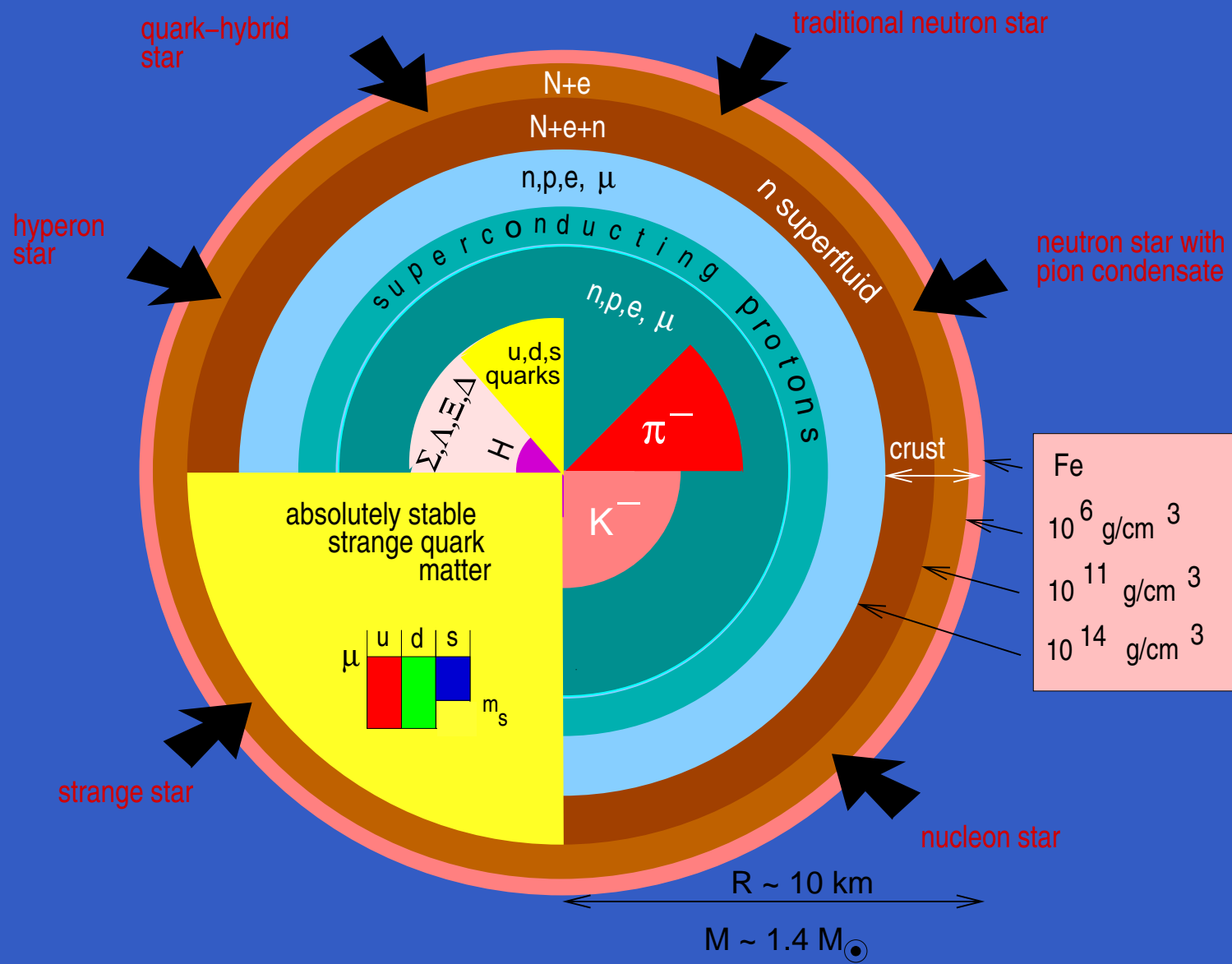
# Composition of the crust of a neutron star

lattice of nuclei surrounded by free electrons



- Wigner–Seitz–cell, lattice structure is bcc
- minimize  $E = E_{\text{nuclei}} + E_{\text{lattice}} + E_{\text{electrons}}$
- loop over all particle stable nuclei (up to 14.000)
- use atomic mass evaluation of 2003 by Audi, Wapstra, and Thibault
- extrapolate to the drip–line with various models
- $\implies$  sequence of nuclei  ${}^A Z$  as a function of density  
(Baym, Pethick, Sutherland 1971; Rüter, Hempel, JSB 2006)

# Structure of a Neutron Star — the Core (Fridolin Weber)



# Neutron Star Matter for a Free Gas

(Ambartsumyan and Saakyan, 1960)

Hadron	p,n	$\Sigma^-$	$\Lambda$	others
appears at:	$\ll n_0$	$4n_0$	$8n_0$	$> 20n_0$

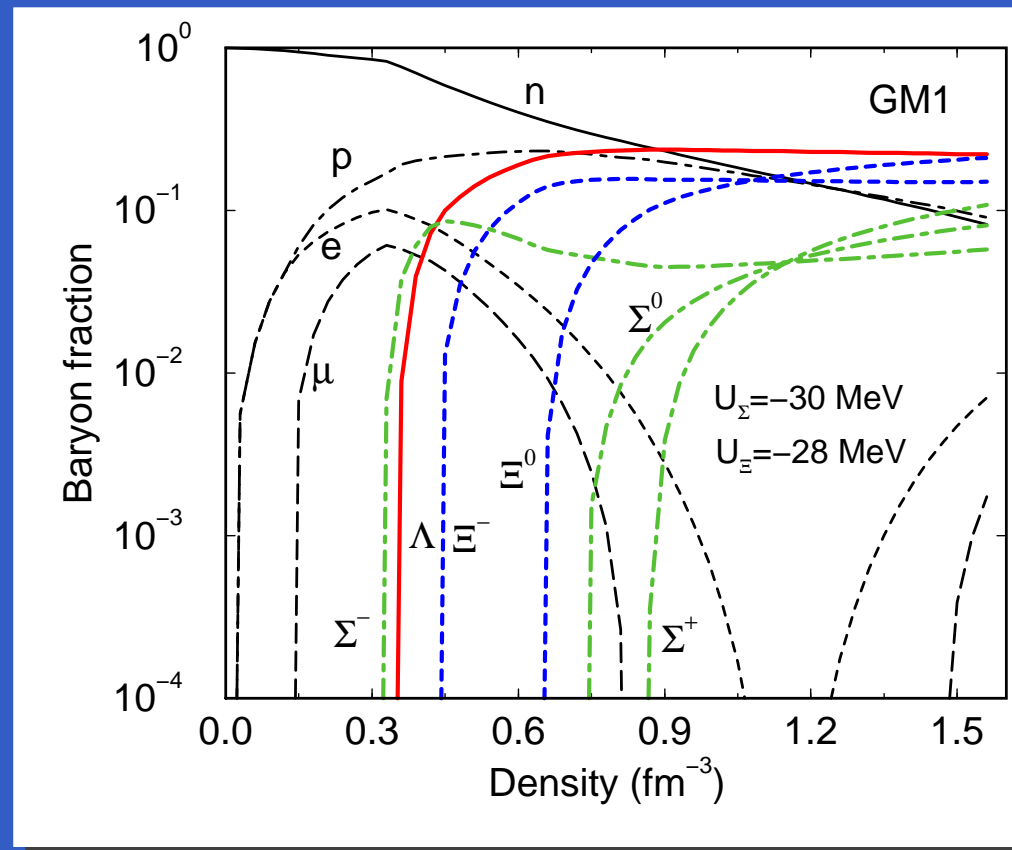
but the corresponding equation of state results in a maximum mass of only

$$M_{\max} \approx 0.7M_{\odot} < 1.44M_{\odot}$$

(Oppenheimer and Volkoff, 1939)

⇒ effects from strong interactions are essential to describe neutron stars!

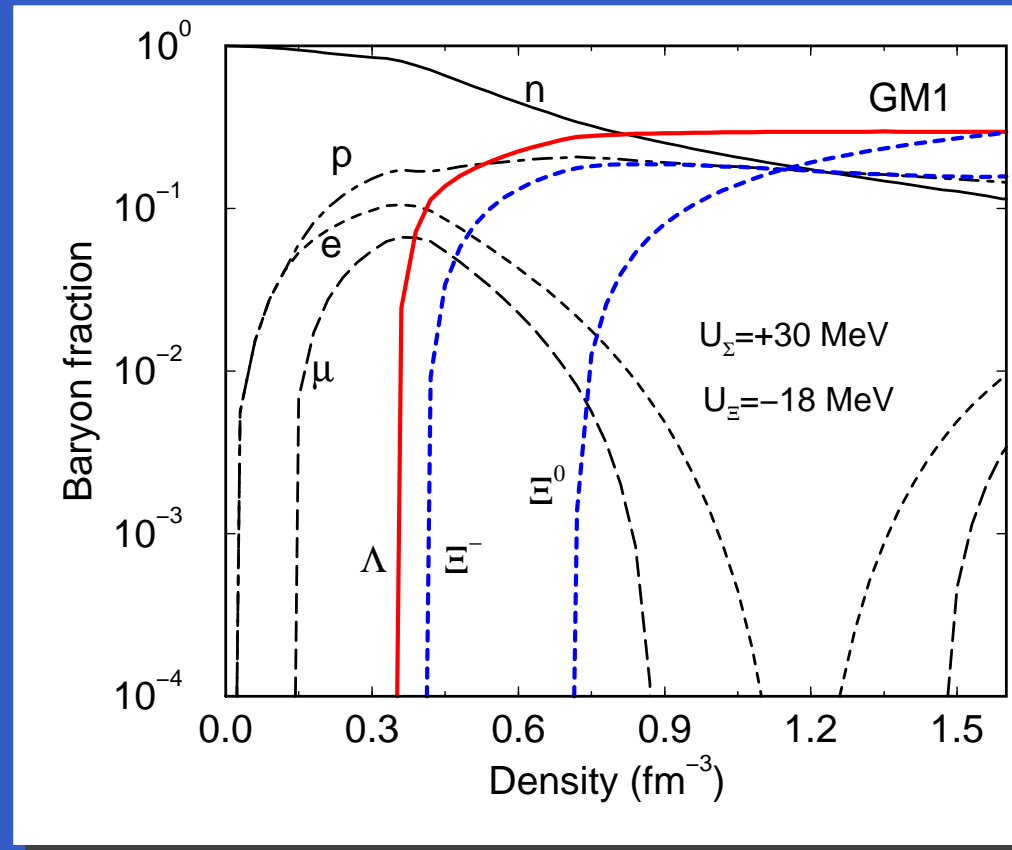
# Composition of Neutron Star Matter



(JS and Mishustin 1996)

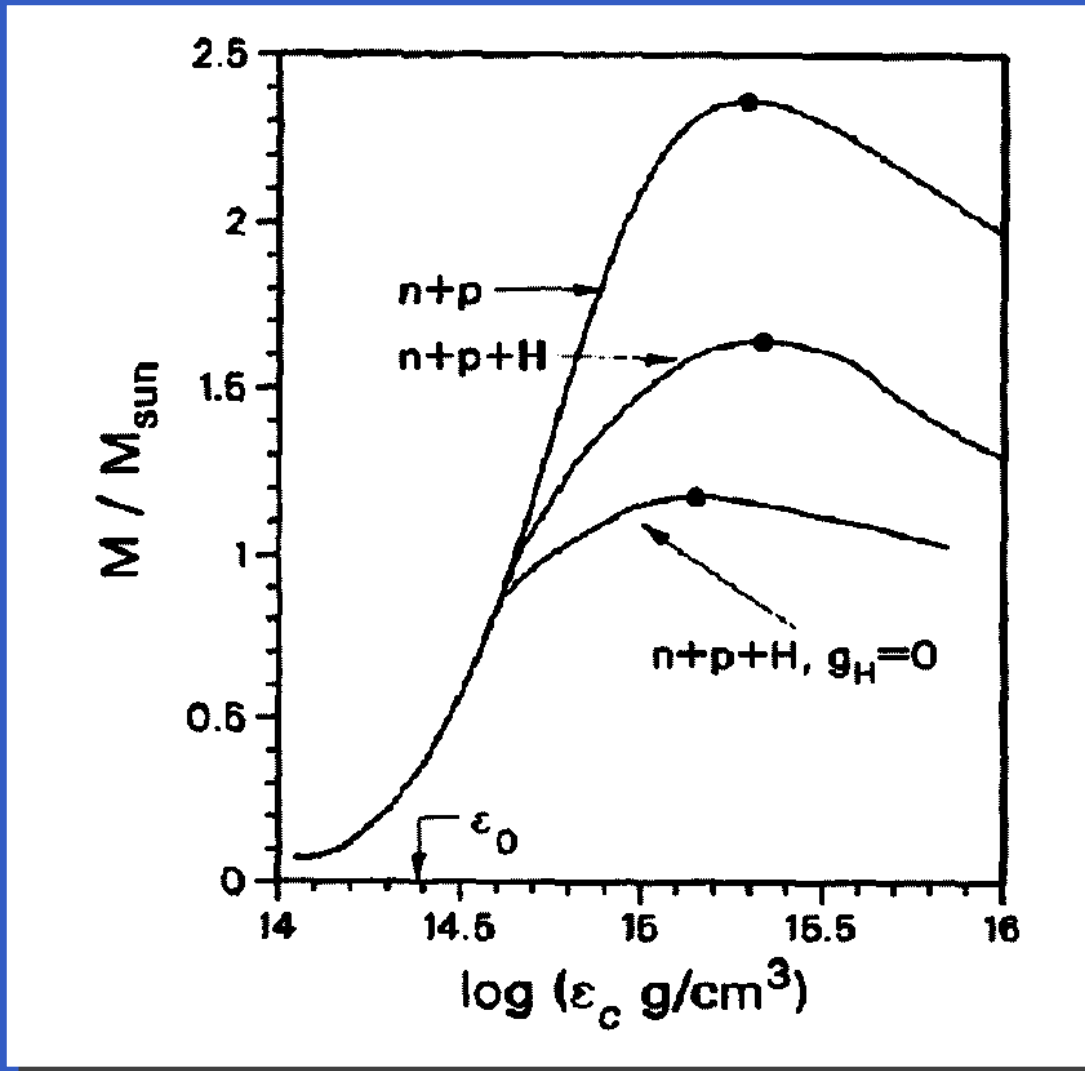
- hyperon potentials fixed to hypernuclear data
- attractive potential for  $\Sigma$ s and  $\Xi$ s
- $\Sigma^-$  appear shortly before  $\Lambda$ s around  $n = 2n_0$
- $\Lambda$ s present in matter at  $n = 2.5n_0$ ,  $\Xi^-$  before  $n = 3n_0$

# Composition of Neutron Star Matter



- $\Lambda$ s are present close to  $n = 2n_0$
- repulsive potential for  $\Sigma$ s:  $\Sigma$  hyperons do not appear at all!
- population is highly sensitive to the in-medium potential!

# Impact of hyperons on the maximum mass of neutron stars



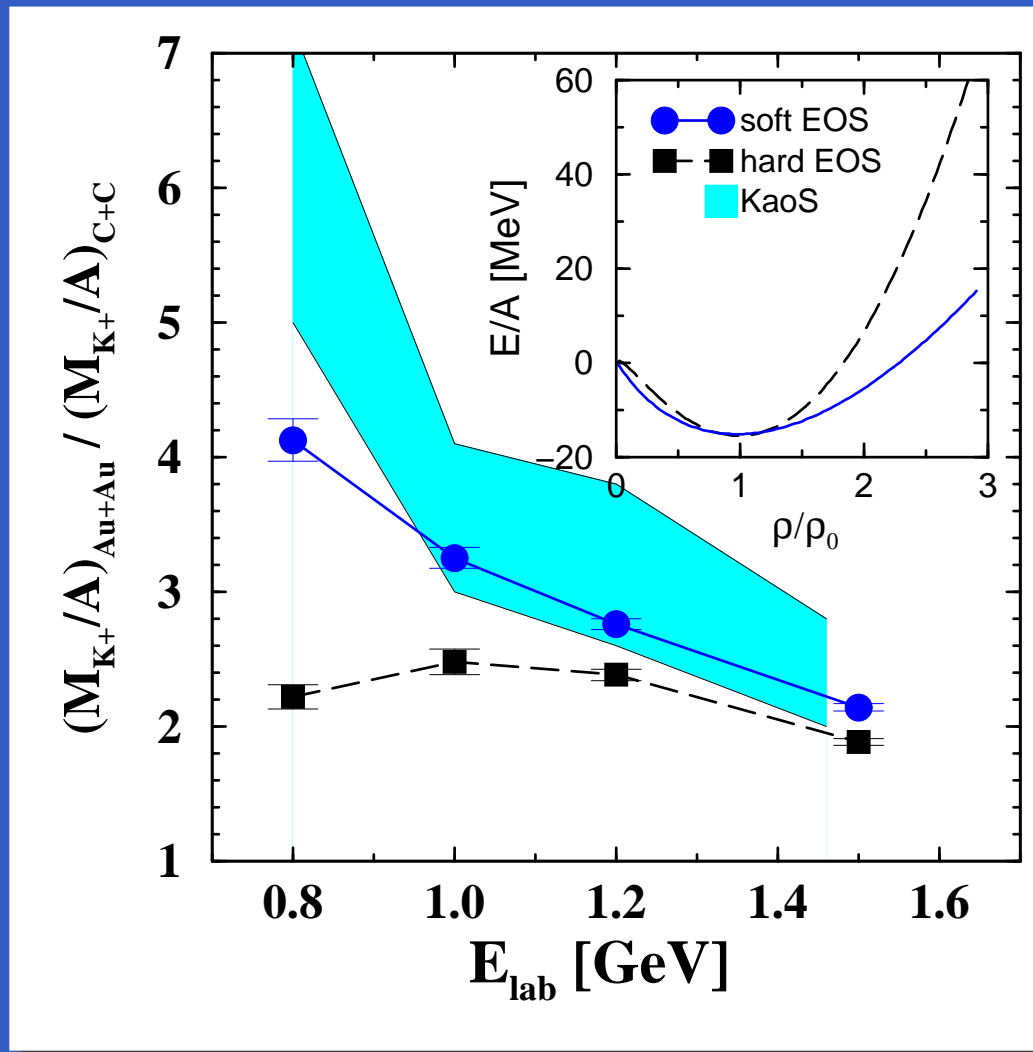
(Glendenning and Moszkowski 1991)

- neutron star with nucleons and leptons only:  
 $M \approx 2.3M_{\odot}$
- substantial decrease of the maximum mass due to hyperons!
- maximum mass for “giant hypernuclei”:  $M \approx 1.7M_{\odot}$
- noninteracting hyperons result in a too low mass:  
 $M < 1.4M_{\odot}$  !

# Constraint on the maximum mass of neutron stars from heavy-ion data

(Irina Sagert, JSB, Christian Sturm, 2009)

# Kaon production in heavy-ion collisions



Sturm et al. (KaoS collaboration), PRL 2001

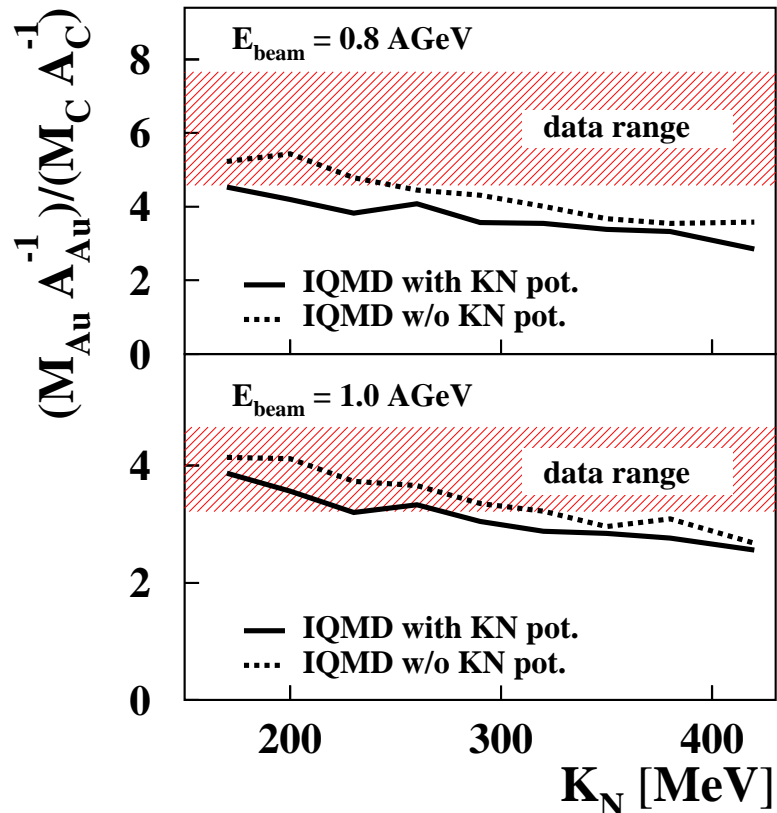
Fuchs, Faessler, Zabrodin, Zheng, PRL 2001

- Kaons produced by associated production:  
 $NN \rightarrow N\Lambda K, NN \rightarrow NNK\bar{K}$
- in-medium processes (rescattering):  $\pi N \rightarrow \Lambda K, \pi\Lambda \rightarrow N\bar{K}$
- nuclear matter is compressed up to  $3n_0!$
- long mean-free path of kaons: kaons can escape high density matter

# Confirmed KaoS data analysis: the nuclear EoS is soft!

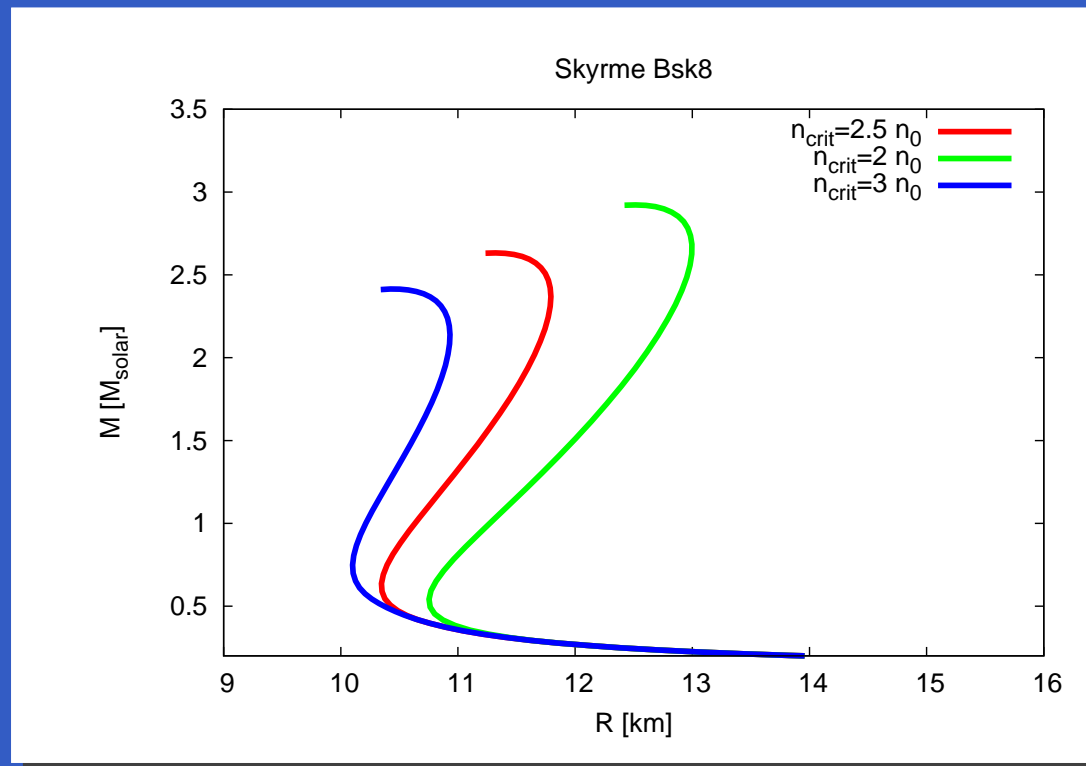
## The **KAO S** Collaboration

- kaon production ( $K^+$ ) in heavy-ion collisions at subthreshold energies
- double ratio: multiplicity per mass number for C+C collisions and Au+Au collisions at 0.8 AGeV and 1.0 AGeV (rather insensitive to input parameters)
- only calculations with a compression modulus of  $K_N \approx 200$  MeV can describe the data (Hartnack, Oeschler, Aichelin, PRL 2006; KaoS collaboration, 2007)



$\implies$  the nuclear equation of state is **SOFT!**

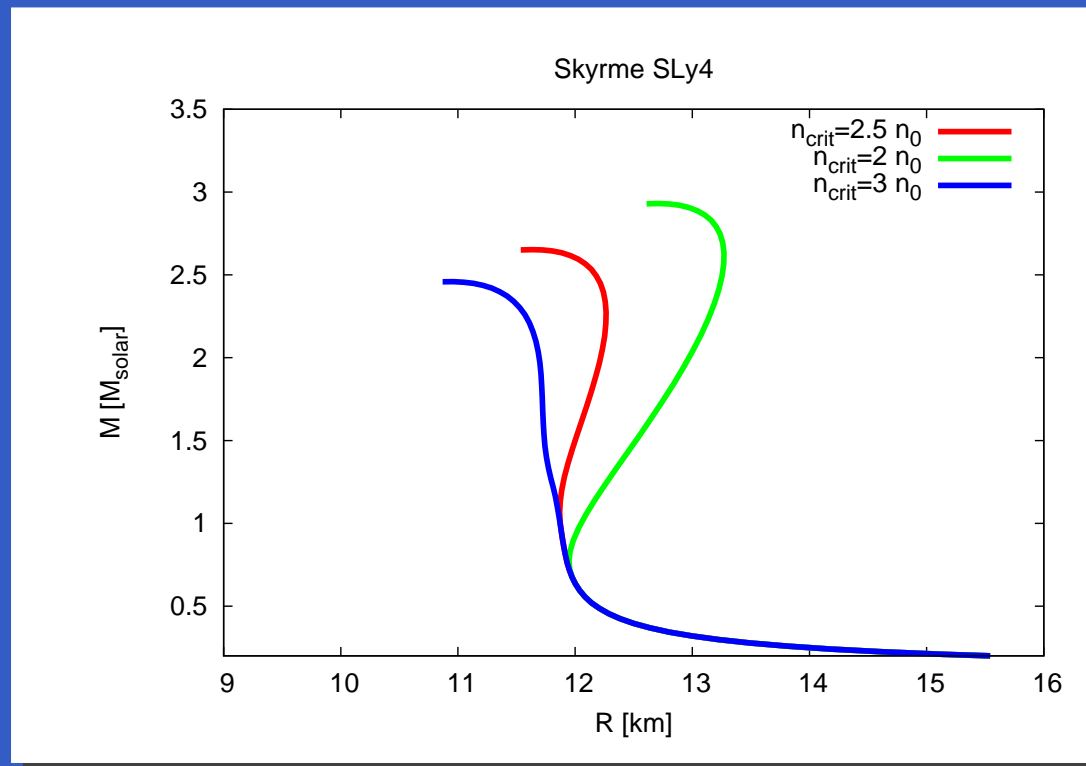
# Maximum Masses of Neutron Stars – Causality



(Irina Sagert)

- Skyrme parameter set BSK8: fitted to masses of all known nuclei
- above a fiducial density (determined from the data analysis of the KaoS data) transition to stiffest possible EoS
- causality argument:  $p = \epsilon - \epsilon_c$  above the fiducial density  $\epsilon_f$   
Rhoades, Ruffini (1974), Kalogera, Baym (1996):  $M_{\max} = 4.2M_{\odot}(\epsilon_0/\epsilon_f)^{1/2}$
- $\implies$  new upper mass limit of about  $2.7M_{\odot}$  from heavy-ion data!

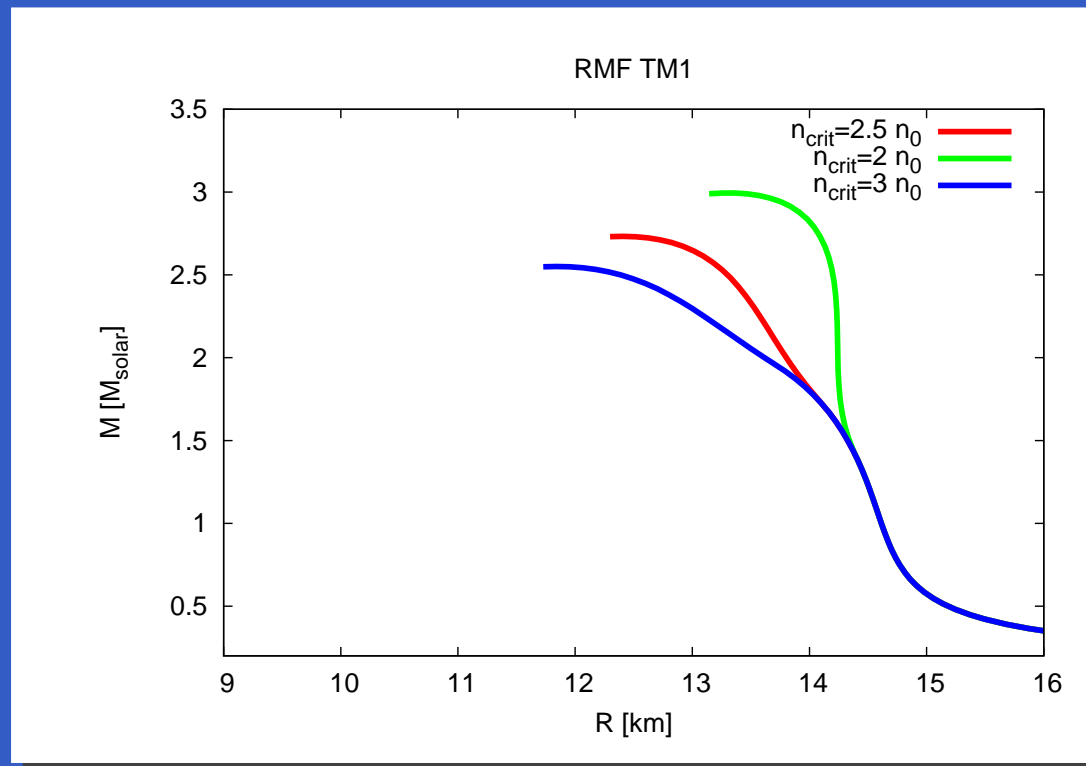
# Maximum Masses of Neutron Stars – Causality



(Irina Sagert)

- Skyrme parameter set Sly4: fitted to properties of spherical nuclei
- above a fiducial density (determined from the data analysis of the KaoS data) transition to stiffest possible EoS
- causality argument:  $p = \epsilon - \epsilon_c$  above the fiducial density  $\epsilon_f$   
Rhoades, Ruffini (1974), Kalogera, Baym (1996):  $M_{\text{max}} = 4.2M_{\odot}(\epsilon_0/\epsilon_f)^{1/2}$
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# Maximum Masses of Neutron Stars – Causality

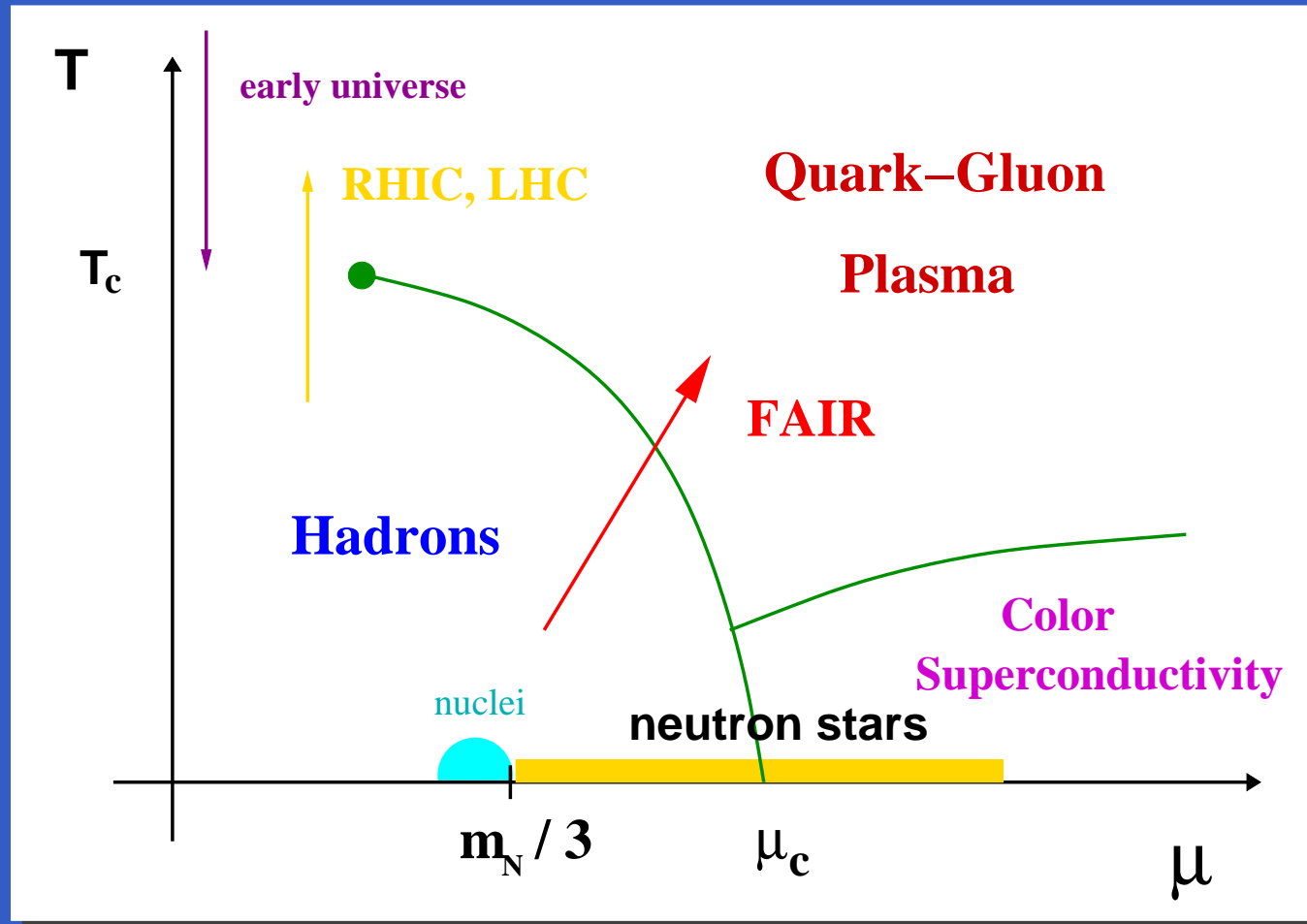


(Irina Sagert)

- RMF parameter set TM1: fitted to properties of spherical nuclei
- above a fiducial density (determined from the data analysis of the KaoS data) transition to stiffest possible EoS
- causality argument:  $p = \epsilon - \epsilon_c$  above the fiducial density  $\epsilon_f$   
Rhoades, Ruffini (1974), Kalogera, Baym (1996):  $M_{\text{max}} = 4.2 M_{\odot} (\epsilon_0 / \epsilon_f)^{1/2}$
- $\implies$  new upper mass limit of about  $2.8 M_{\odot}$  from heavy-ion data!

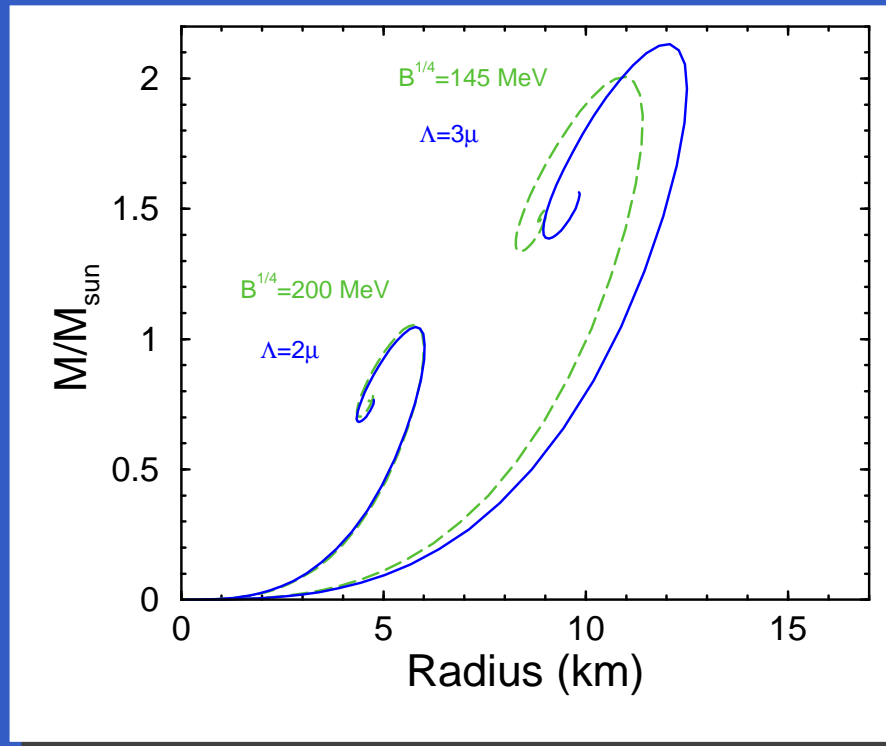
# QCD Phase Transition and Neutron Stars

# Phase Transitions in Quantum Chromodynamics QCD



- Early universe at zero density and high temperature
- neutron star matter at small temperature and high density
- first order phase transition at high density (not deconfinement)!
- probed by heavy-ion collisions at GSI, Darmstadt (FAIR!)

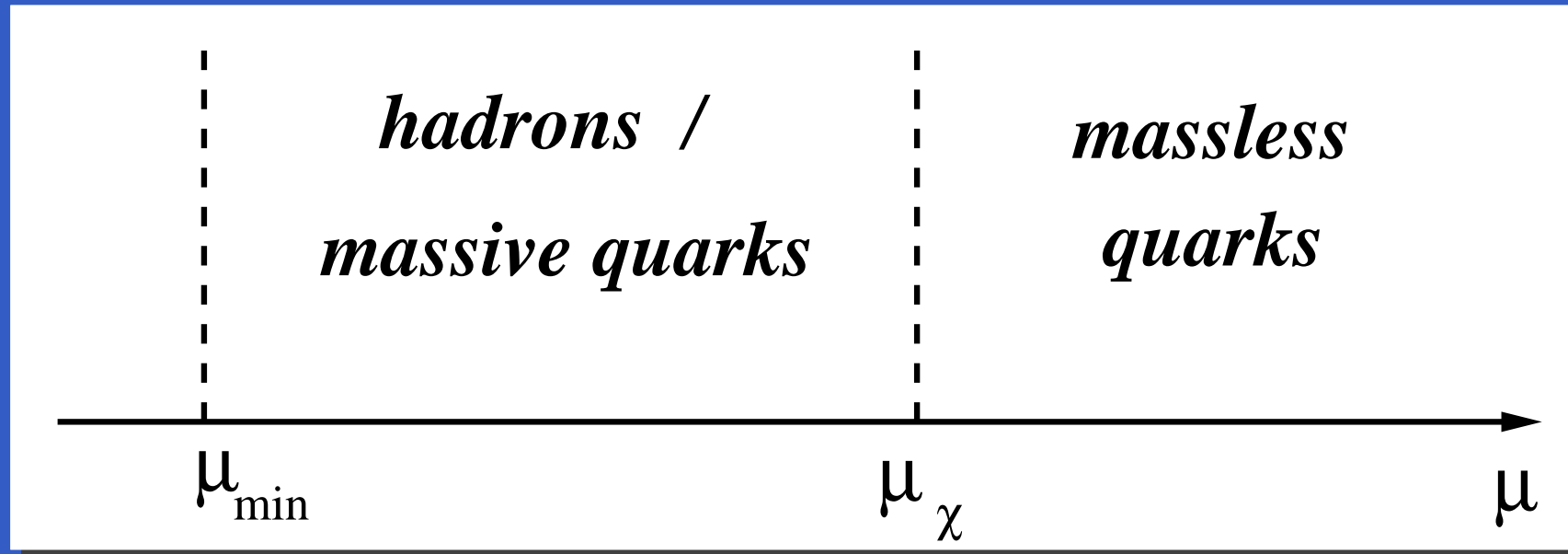
# Mass-radius and maximum density of pure quark stars



- green curves: MIT bag model
- blue curves: perturbative QCD calculations  
(Fraga, JSB, Pisarski 2001)

- case  $\Lambda = 2\mu$ :  $M_{\max} = 1.05 M_{\odot}$ ,  $R_{\max} = 5.8 \text{ km}$ ,  $n_{\max} = 15 n_0$
- case  $\Lambda = 3\mu$ :  $M_{\max} = 2.14 M_{\odot}$ ,  $R_{\max} = 12 \text{ km}$ ,  $n_{\max} = 5.1 n_0$
- other nonperturbative approaches: Schwinger–Dyson model (Blaschke et al.), massive quasiparticles (Peshier, Kämpfer, Soff), NJL model (Hanauske et al.), HDL (Andersen and Strickland), . . .
- note: pure quark stars can be very similar to ordinary neutron stars!

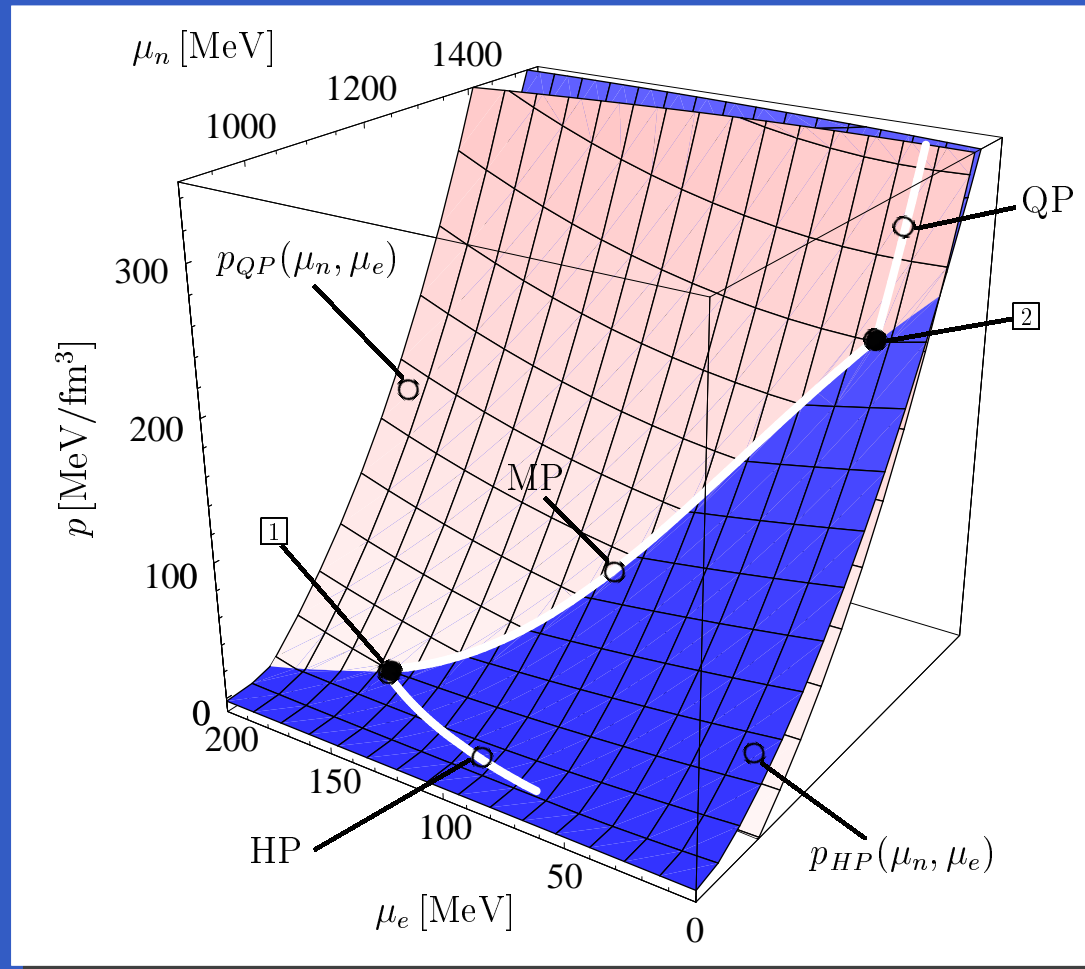
# Matching to low density EoS



Two possibilities for a first-order chiral phase transition:

- A weakly first-order chiral transition (or no true phase transition),  
⇒ one type of compact star (neutron star)
- A strongly first-order chiral transition  
⇒ two types of compact stars:  
a new stable solution with smaller masses and radii

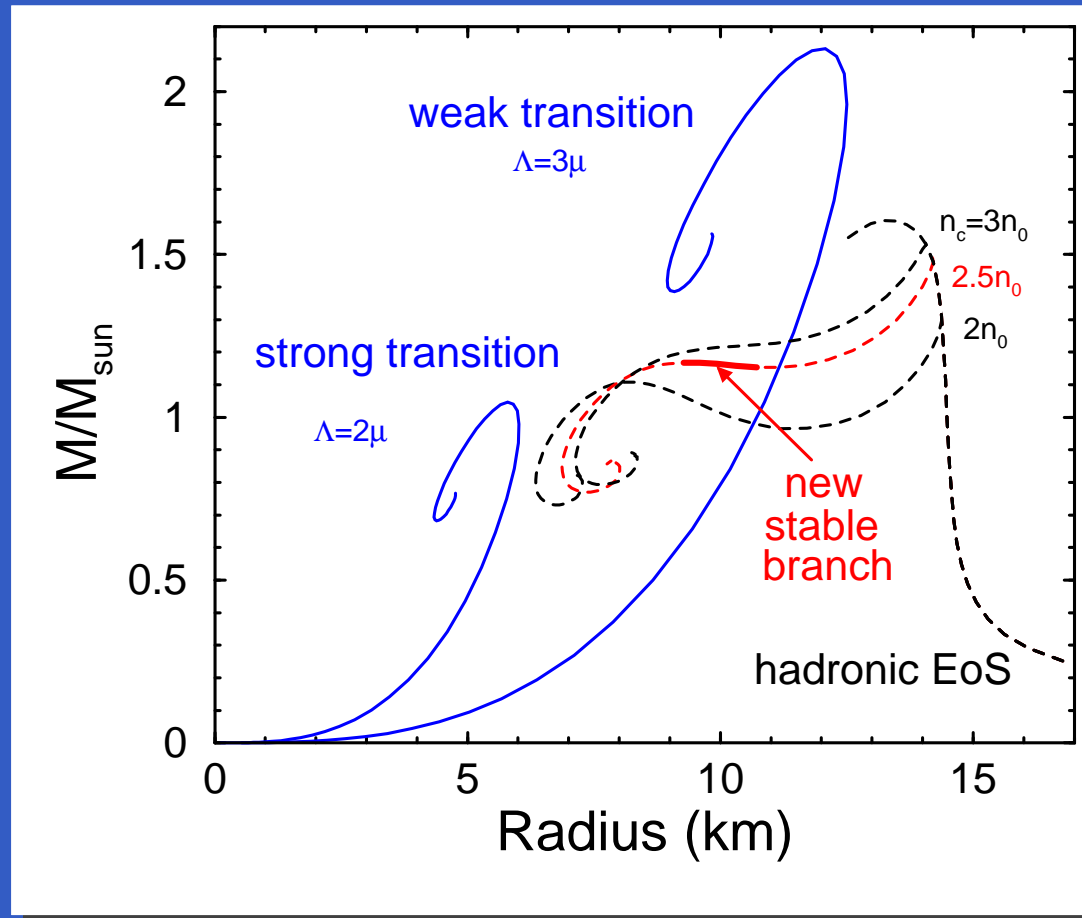
# Gibbs Phase Construction (Glendenning 1992)



(Schertler et al. (2000))

- two conserved charges in  $\beta$ -equilibrium: baryon number and charge!
- Gibbs criterium for phase equilibrium: equal pressure for equal chemical potentials  $P_I(\mu_B, \mu_e) = P_{II}(\mu_B, \mu_e)$
- globally charge neutral matter: mixed phase with charged bubbles forms!

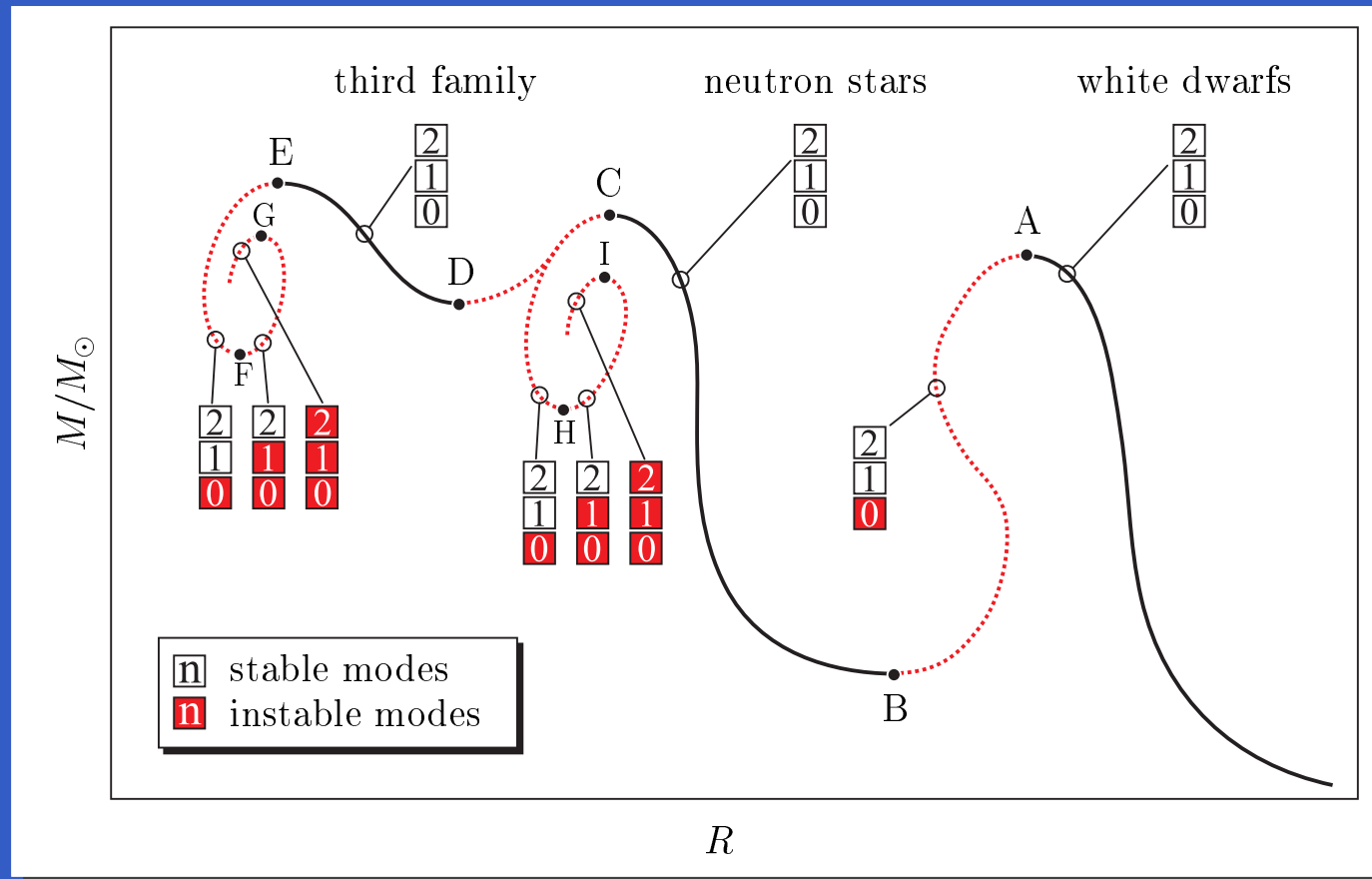
# Quark star twins? (Fraga, JSB, Pisarski 2001)



- Weak transition: ordinary neutron star with quark core (hybrid star)
- Strong transition: third class of compact stars possible with maximum masses  $M \sim 1 M_{\odot}$  and radii  $R \sim 6$  km
- Quark phase dominates ( $n \sim 15 n_0$  at the center), small hadronic mantle

# Third Family of Compact Stars (Gerlach 1968)

(Glendenning, Kettner 2000; Schertler, Greiner, JSB, Thoma 2000)

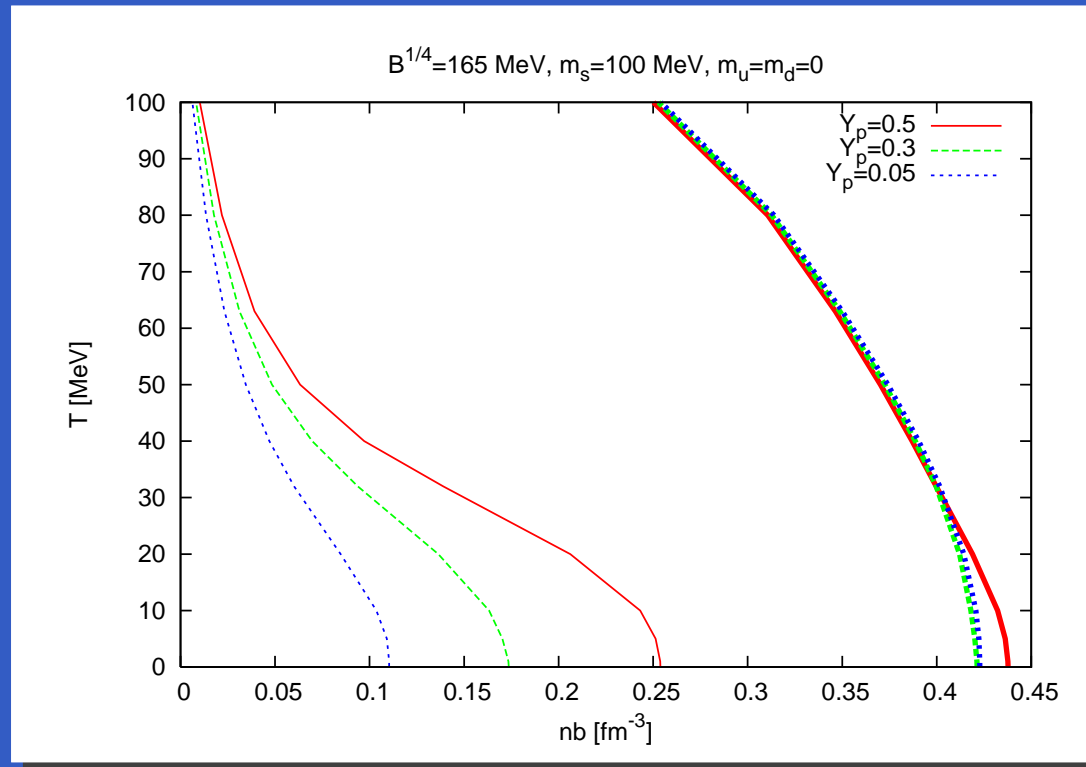


- third solution to the TOV equations besides white dwarfs and neutron stars, solution is stable!
- generates stars more compact than neutron stars!
- possible for any first order phase transition!

# QCD phase transition in supernovae

Irina Sagert, Matthias Hempel, Giuseppe Pagliara, JSB, Tobias Fischer, Anthony Mezzacappa, Friedel Thielemann, Matthias Liebendörfer, arXiv:0809.4225, PRL in press

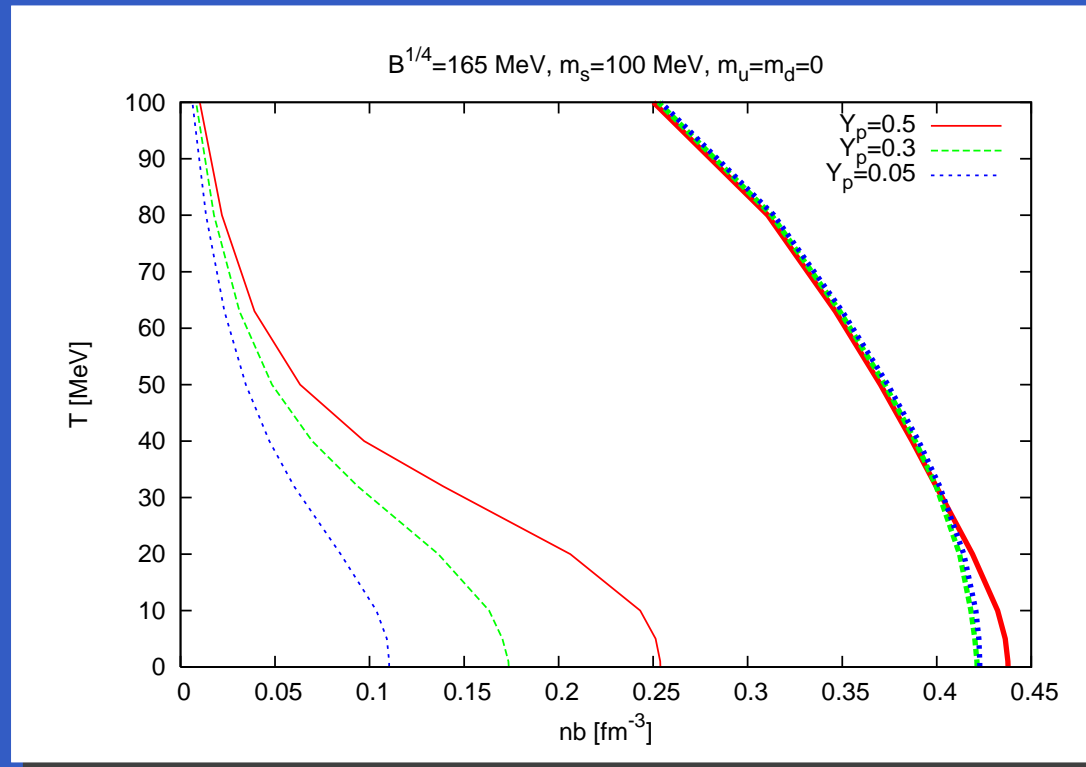
# Phase Transition to Quark Matter for Astros



(Irina Sagert and Giuseppe Pagliara)

- quark matter appears at low density due to  $\beta$ -equilibrium
- low critical density for low  $Y_p$  due to nuclear asymmetry energy
- quark matter favoured at finite temperature
- supernova matter at bounce:  $T = 10 - 20 \text{ MeV}$ ,  $Y_p = 0.2 - 0.3$ ,  $\epsilon \sim (1 - 1.5)\epsilon_0$

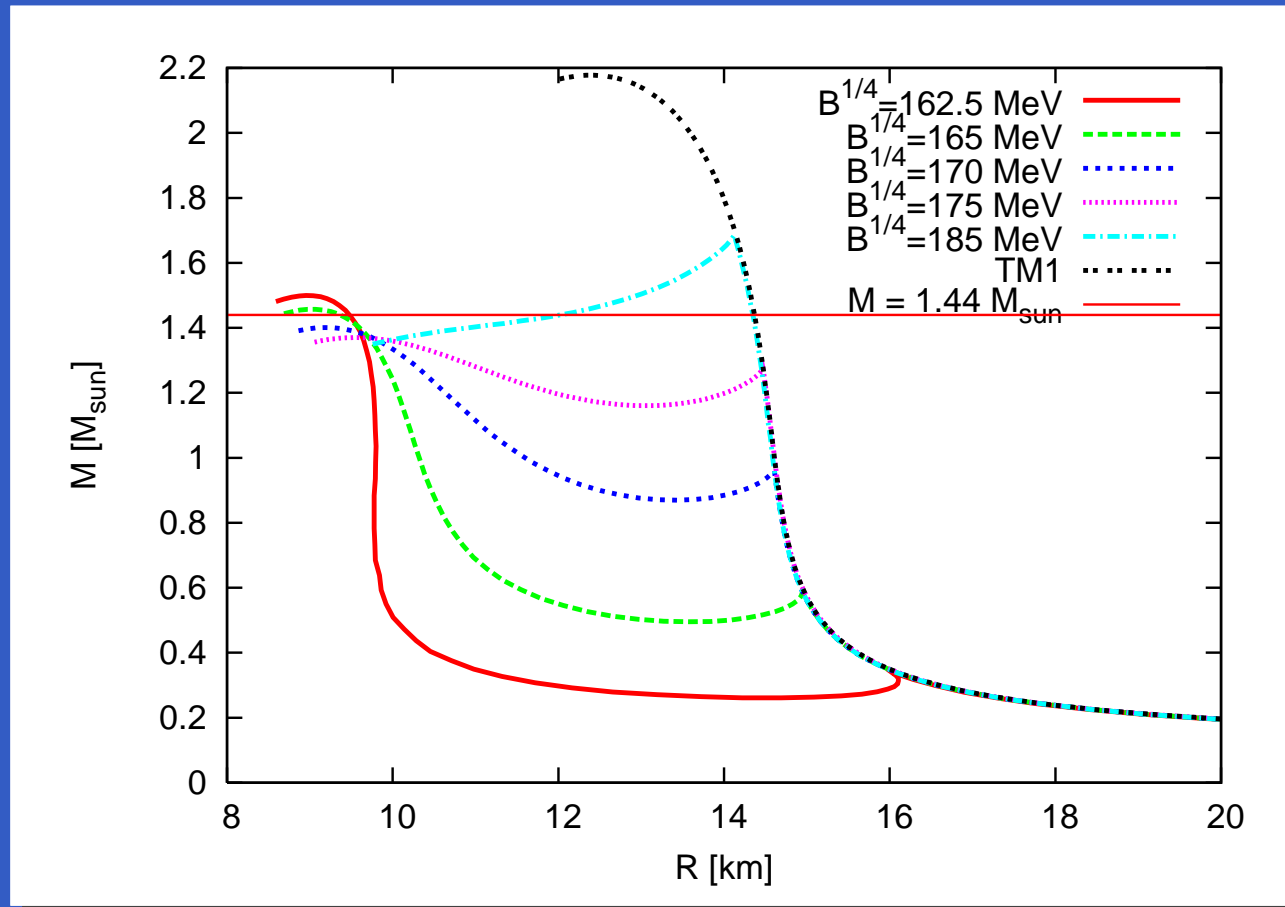
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- quark matter favoured at finite temperature
- supernova matter at bounce:  $T = 10 - 20$  MeV,  $Y_p = 0.2 - 0.3$ ,  $\epsilon \sim (1 - 1.5)\epsilon_0$
- production of quark matter in supernovae at bounce possible!

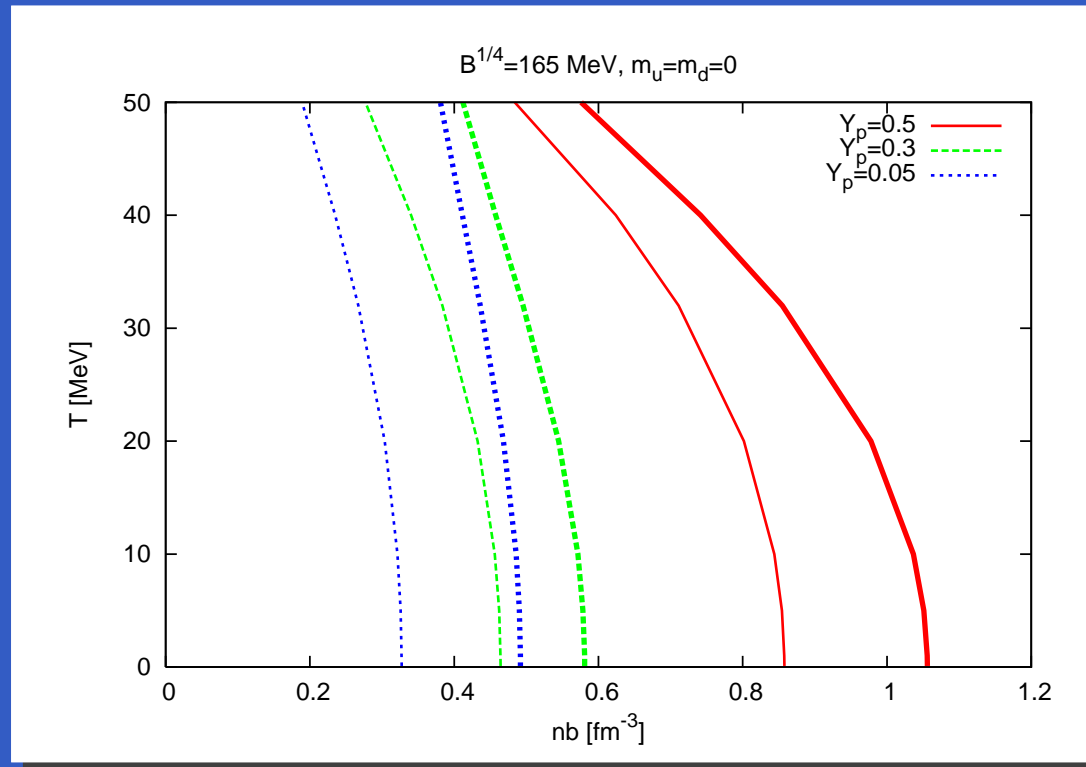
# Check: Mass-Radius Diagram of Cold Neutron Stars



(Irina Sagert and Giuseppe Pagliara)

- presence of quark matter can change drastically the mass-radius diagram
- third family of solution for certain bag constants
- maximum mass:  $1.56 M_{\odot}$  ( $B^{1/4} = 162$  MeV),  $1.5 M_{\odot}$  ( $B^{1/4} = 165$  MeV)

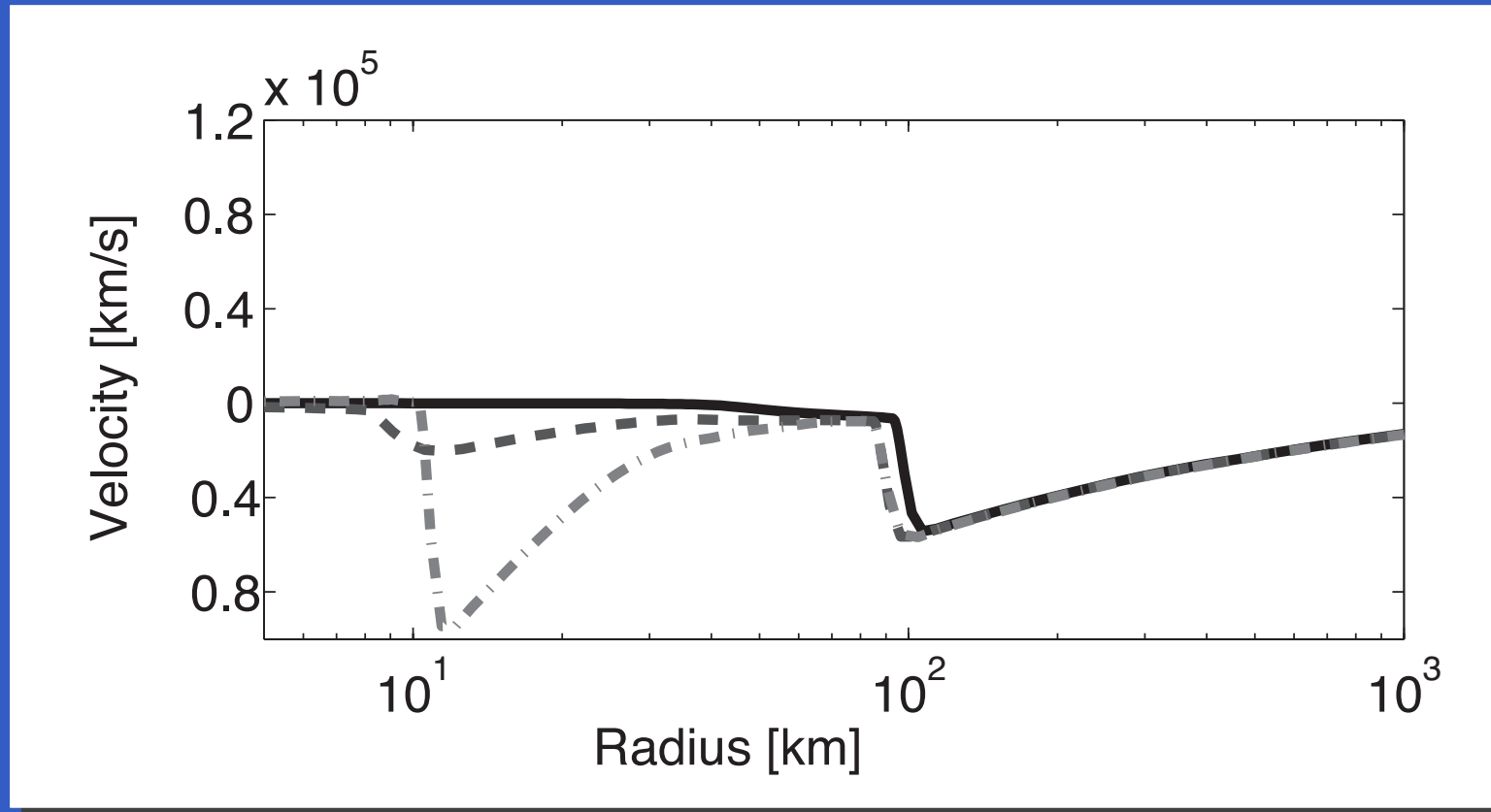
# Check: Phase Transition for Heavy-Ion Collisions



(Irina Sagert and Giuseppe Pagliara)

- no  $\beta$ -equilibrium (just up-/down-quark matter)
- large critical densities in particular for isospin-symmetric matter (proton fraction  $Y_p = 0.5$ )
- production of ud-quark matter unfavoured for HICs at small  $T$  and high density
- no contradiction with heavy-ion data!

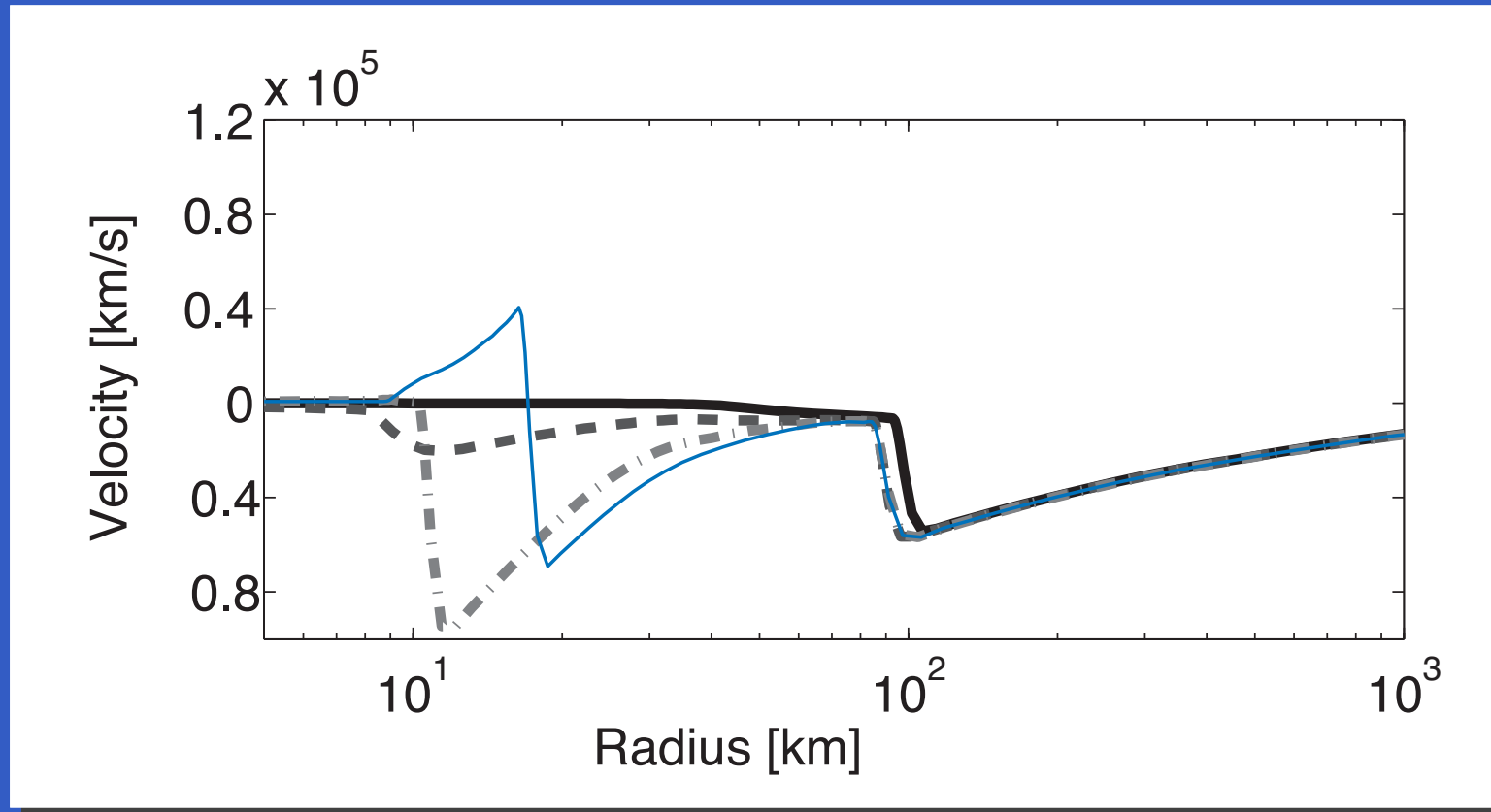
# Implications for Supernovae – Explosion!



(Sagert, Hempel, Pagliara, JSB, Fischer, Mezzacappa, Thielemann, Liebendörfer, 2008)

- velocity profile of a supernova for different times (around 250ms)
- formation of a core of pure quark matter produces a second shock wave

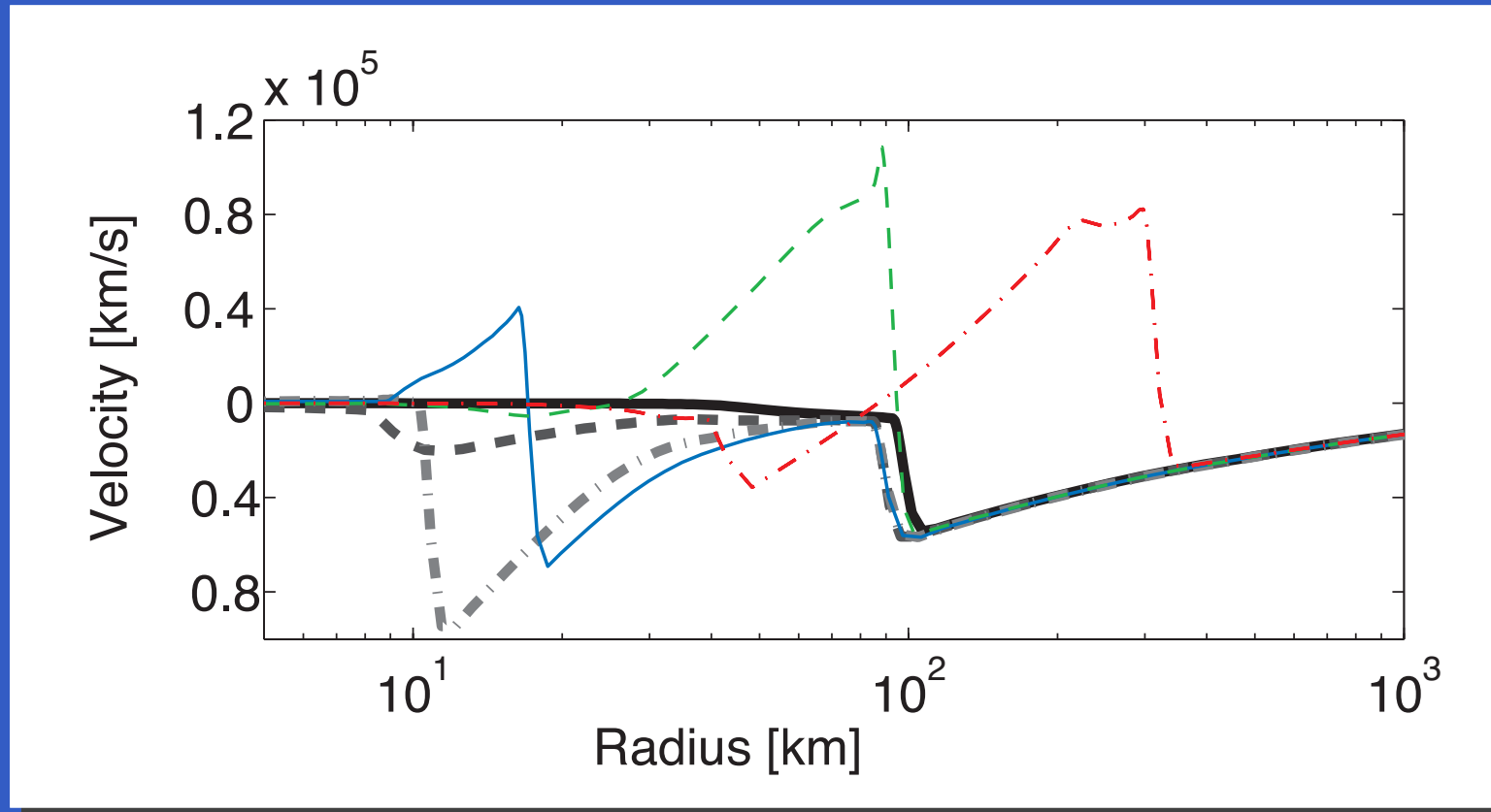
# Implications for Supernovae – Explosion!



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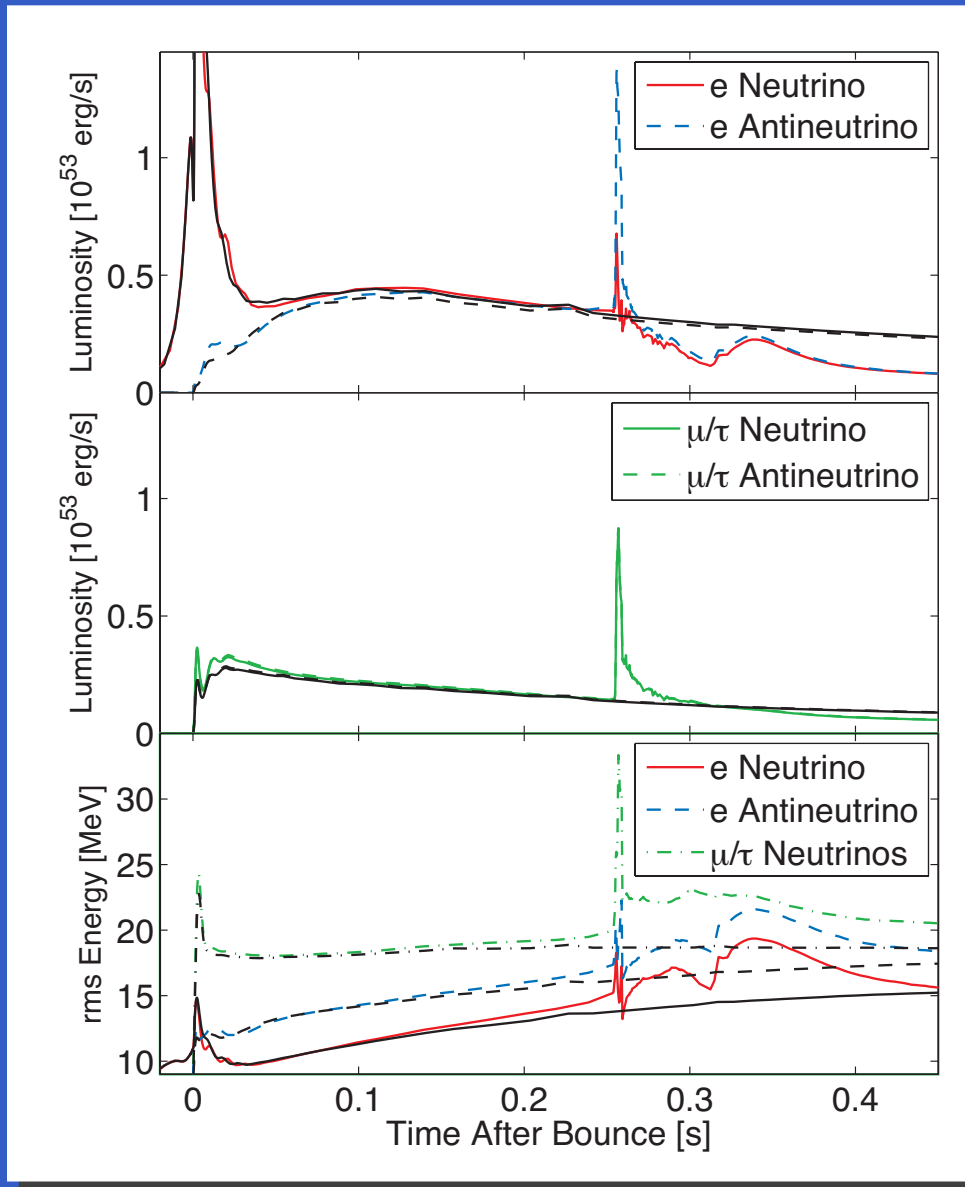
# Implications for Supernovae – Explosion!



(Sagert, Hempel, Pagliara, JSB, Fischer, Mezzacappa, Thielemann, Liebendörfer, 2008)

- velocity profile of a supernova for different times (around 250ms)
- formation of a core of pure quark matter produces a second shock wave
- leads to an explosion!

# Implications for Supernova – Neutrino-Signal!



(Sagert, Hempel, Pagliara, JSB, Fischer, Mezzacappa, Thielemann, Liebendörfer, 2008)

- temporal profile of the emitted neutrinos out of the supernova
- thick lines: without, thin lines: with a phase transition
- pronounced second peak of anti-neutrinos due to the formation of quark matter
- peak location and height determined by the critical density and strength of the QCD phase transition!!

# Summary

- heavy-ion data constrains the maximum mass of neutron stars to be less than  $2.7M_{\odot}$
- quark matter can be present in the core of neutron stars and can lead to a new family of compact stars
- quark matter can be formed in supernovae, even shortly after the first bounce
  - leads to an explosion (with enough explosion energy in the shock)
  - forms a second peak in the (anti-)neutrino signal
  - implications for gravitational wave signal?
  - and r-process nucleosynthesis?
- a FAIR chance for exploring exotic matter on Earth and in the sky

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(full supernova equation of state)
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(EoS from heavy ion physics, SN EoS, proto-neutron stars)
- Rainer Stiele (starts his PhD 03/2009 in HD)  
(interacting dark matter in the early universe)