

# The Structure of Neutron Stars

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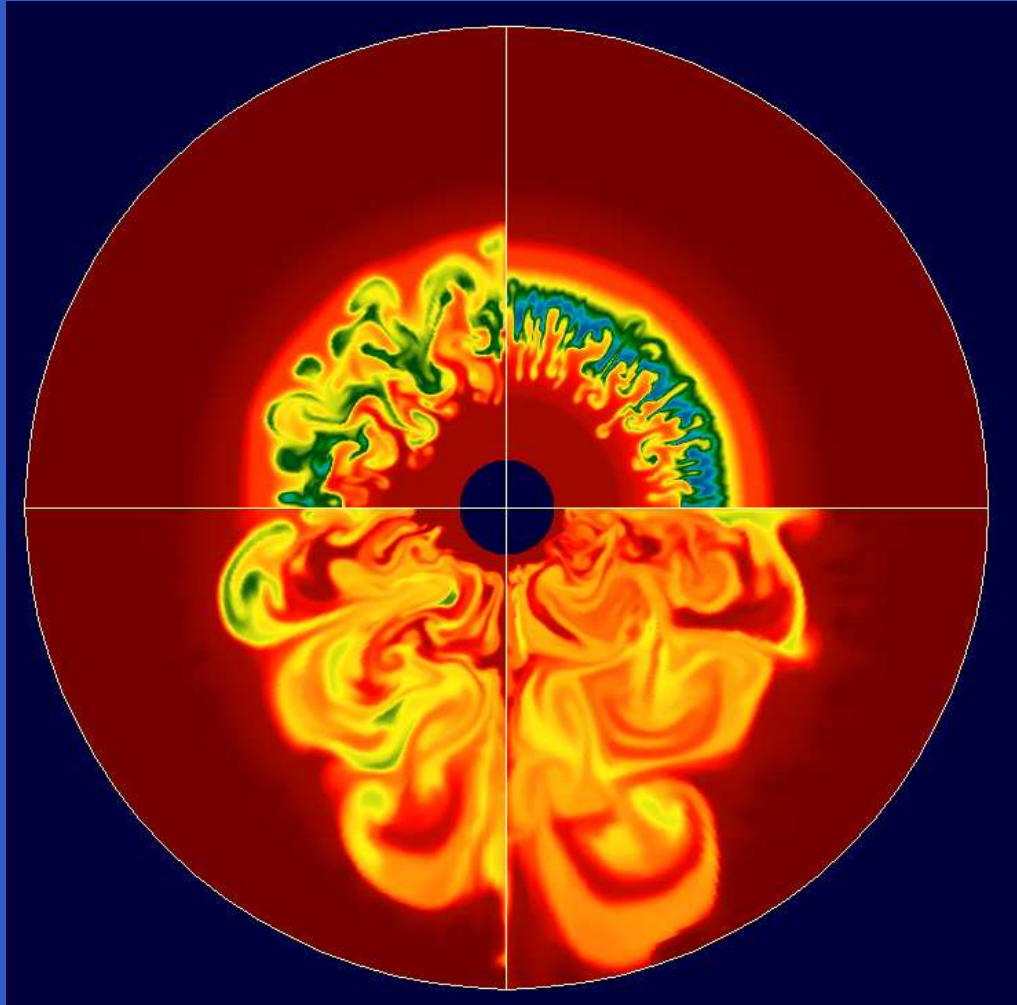
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Theoretisch-Physikalisches Kolloquium  
Heidelberg, 16.12.2008

# Introduction

# Supernova Explosions



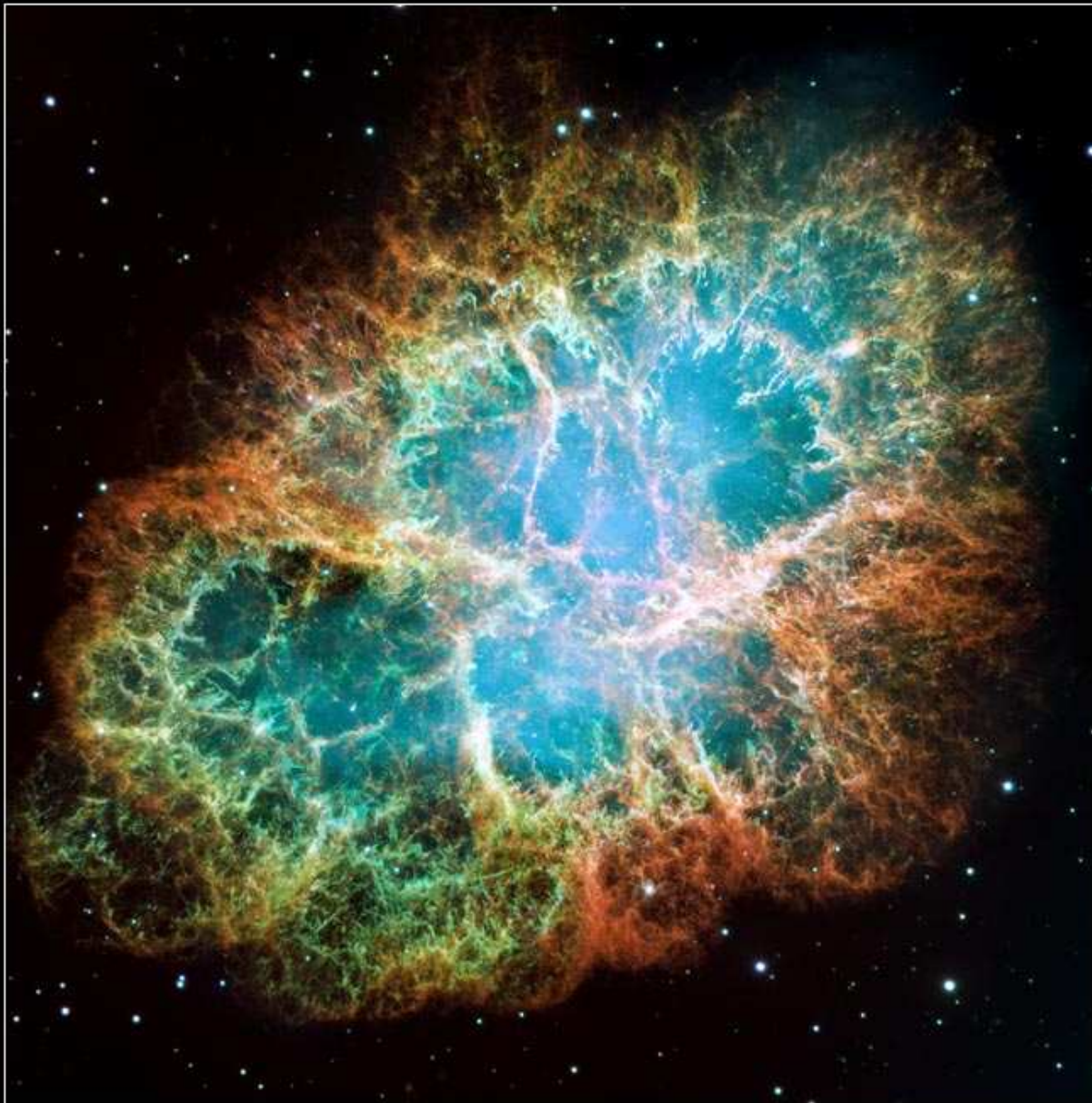
- stars with a mass of more than 8 solar masses end in a (core collapse) supernova (type II)
- Supernova of AD 1054 was visible for three weeks during daytime (crab nebula)!
- supernovae are several thousand times brighter than a whole galaxy!
- last supernova explosion for the last 400 years in our local group: SN1987A
- most prominent candidate in the universe for producing the heavy elements (r-process)

Animation of a supernova explosion (Chandra, NASA)

# Neutron Stars

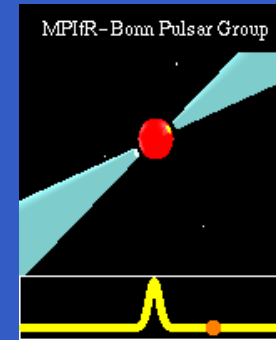
Crab Nebula ■ M1

HST ■ WFPC2



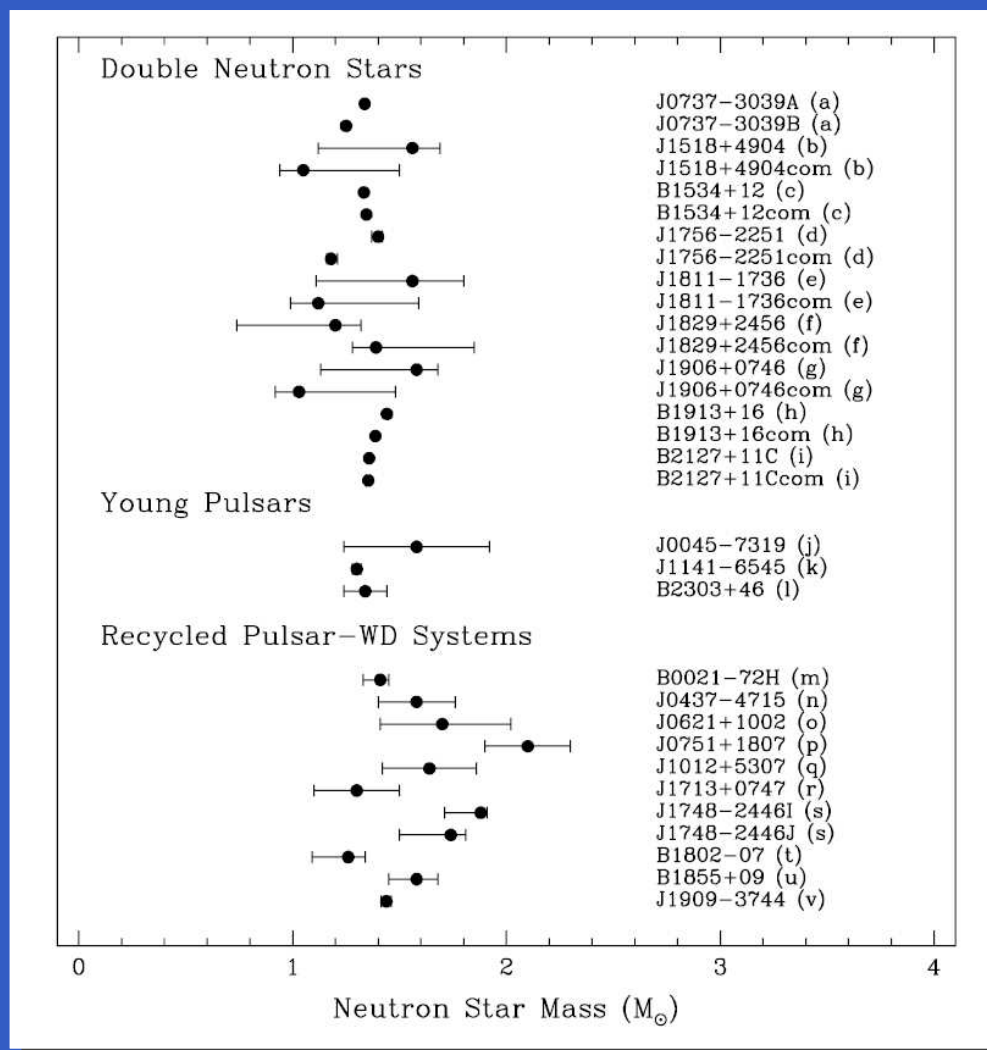
NASA, ESA, and J. Hester (Arizona State University)

STScI-PRC05-37



- produced in core collapse supernova explosions
- compact, massive objects: radius  $\approx 10$  km, mass  $1 - 2M_{\odot}$
- extreme densities, several times nuclear density:  $n \gg n_0 = 3 \cdot 10^{14} \text{ g/cm}^3$
- in the middle of the crab nebula: a pulsar, a rotating neutron star!

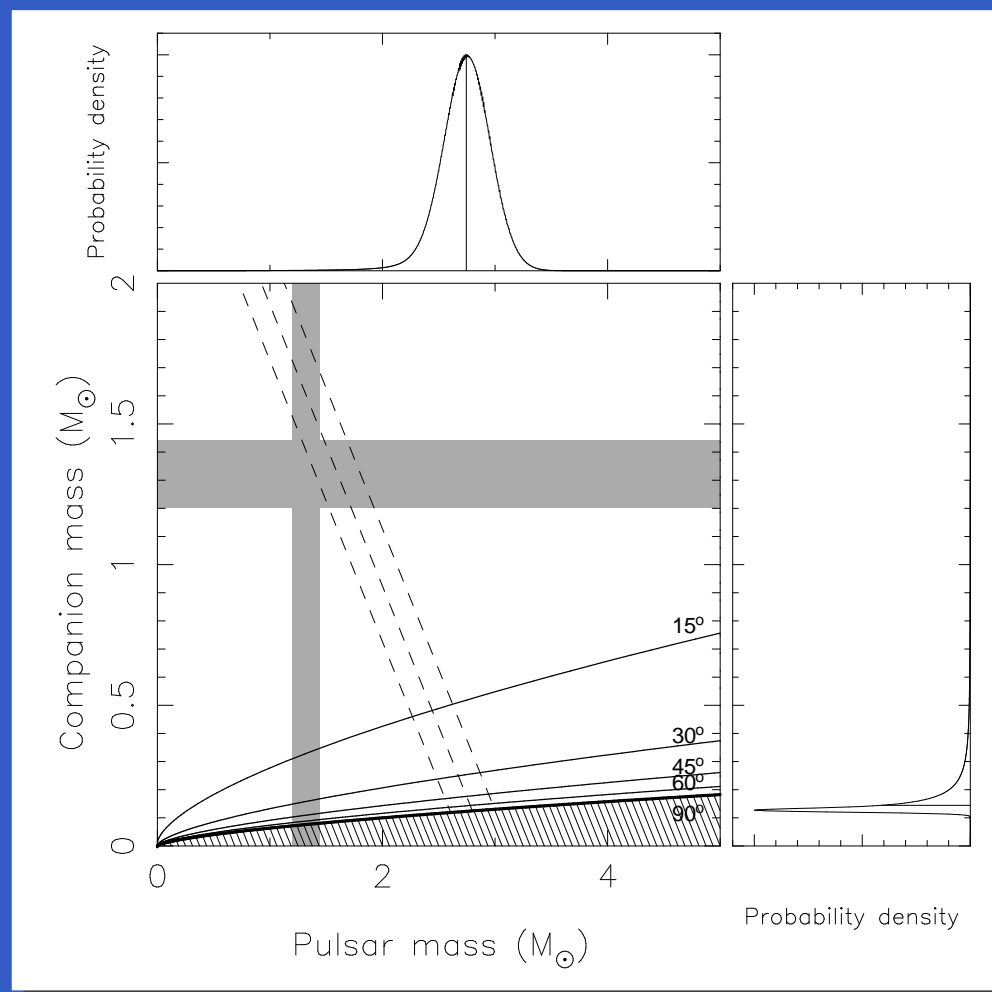
# Masses of Pulsars (Stairs, 2006)



- more than 1600 pulsars known
- best determined mass:  
 $M = (1.4414 \pm 0.0002)M_{\odot}$   
for the Hulse-Taylor pulsar  
(Weisberg and Taylor, 2004)
- smallest known mass:  
 $M = (1.18 \pm 0.02)M_{\odot}$  for  
pulsar J1756-2251 (Faulkner  
et al., 2005)
- PSR J0751+1807 corrected  
from  $M = 2.1 \pm 0.2M_{\odot}$  to  
 $M = 1.14 - 1.40M_{\odot}$  (Nice et  
al. 2008)

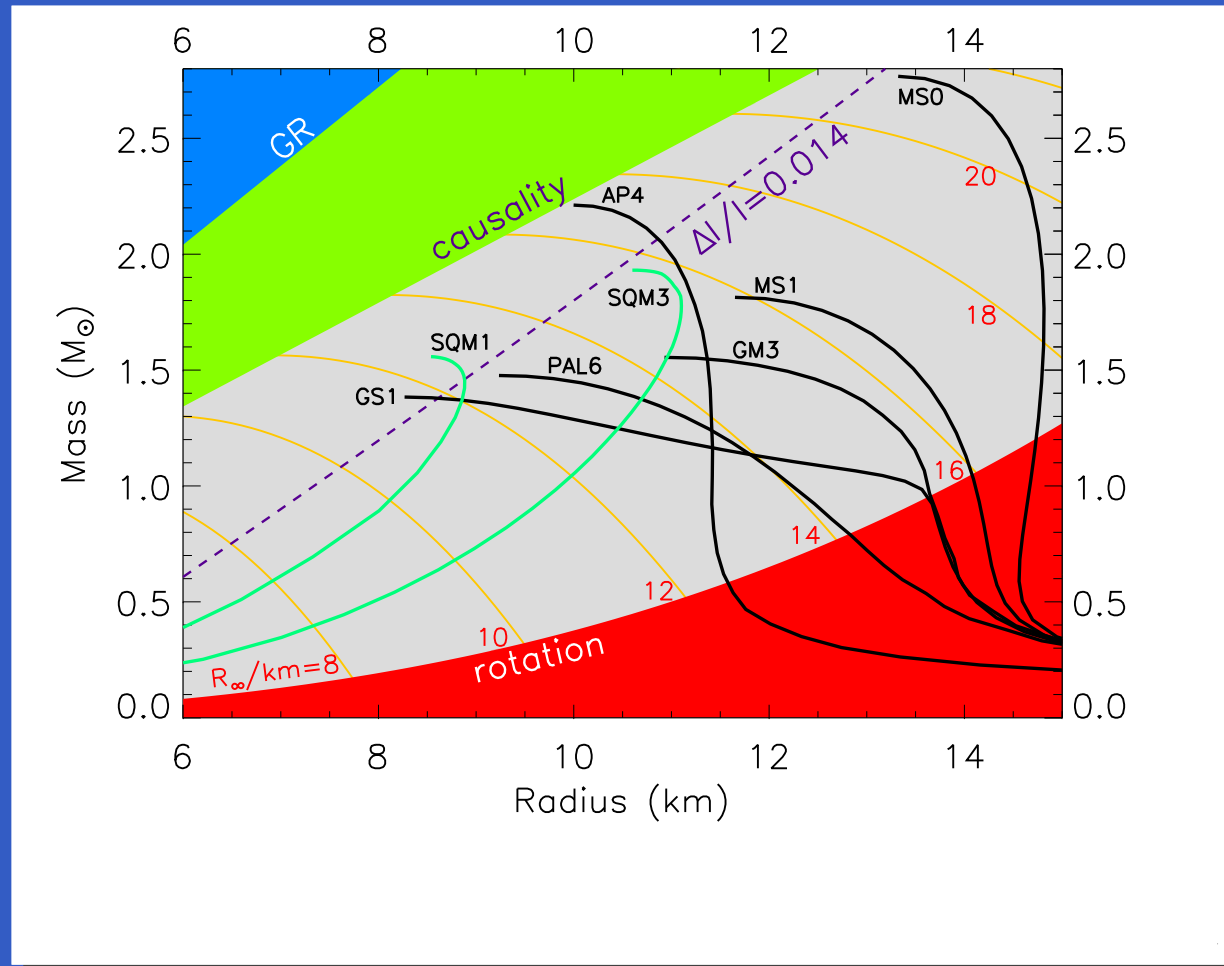
# Supermassive Pulsar in Globular Cluster?

(Freire et al., arXiv:0711.0925v2 (2007))



- measurement of periastron advance of the pulsar PSR J1748-2021B
- inclination angle  $i$  of orbital plane unknown
- statistical analysis (for angle  $i$ ):  
 $M = 2.74 \pm 0.21 M_{\odot}$  ( $1\sigma$ ) and  
 $M > 2.0 M_{\odot}$  (99% c.l.)
- two neutron stars with  $M \sim 1.4 M_{\odot}$  possible for  $i = 4 - 5$  degrees
- measurement of a second GR effect needed to draw a firm conclusions! Beware! not a real measurement!
- mass would be at variance with heavy-ion data (Sagert et al. in preparation)

# Constraints on the Mass–Radius Relation (Lattimer and Prakash (2004))



- spin rate from PSR B1937+21 of 641 Hz:  $R < 15.5$  km for  $M = 1.4M_{\odot}$
- observed giant glitch from Vela pulsar: moment of inertia changes by 1.4%
- Schwarzschild limit (GR):  $R > 2GM = R_s$
- causality limit for EoS:  $R > 3GM$

# How To Measure Masses AND Radii of Compact Stars

- mass from binary systems (pulsar with a companion star)
- radius and mass from thermal emission, for a blackbody:

$$F_{\infty} = \frac{L_{\infty}}{4\pi d^2} = \sigma_{\text{SB}} T_{\text{eff},\infty}^4 \left( \frac{R_{\infty}}{d} \right)^2$$

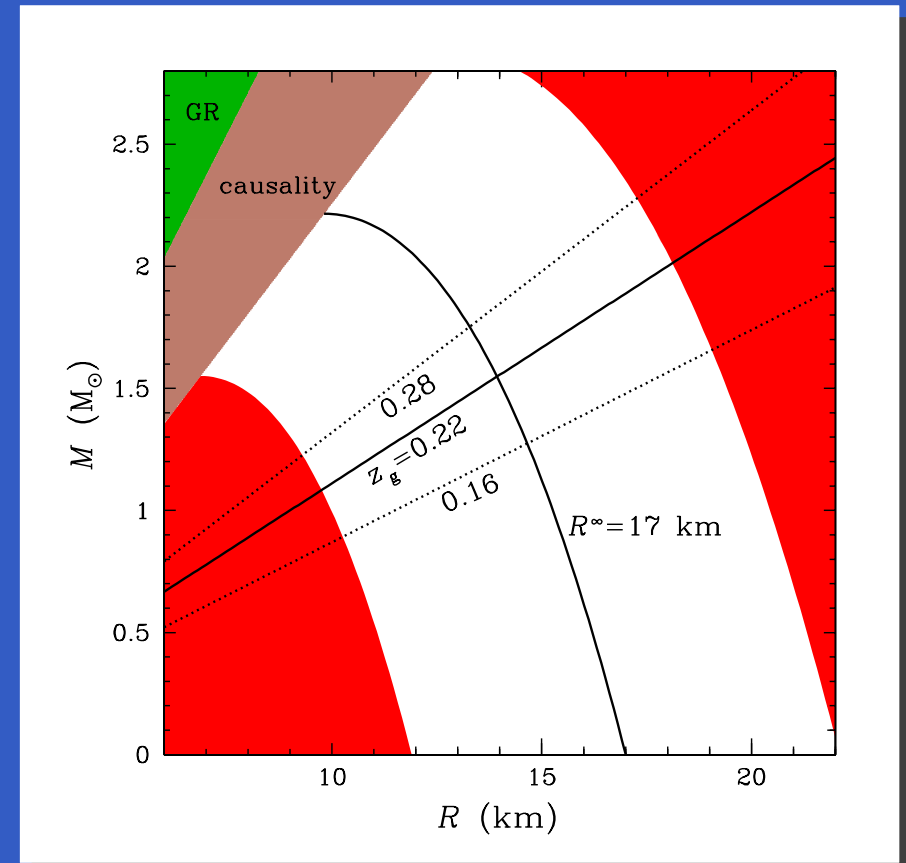
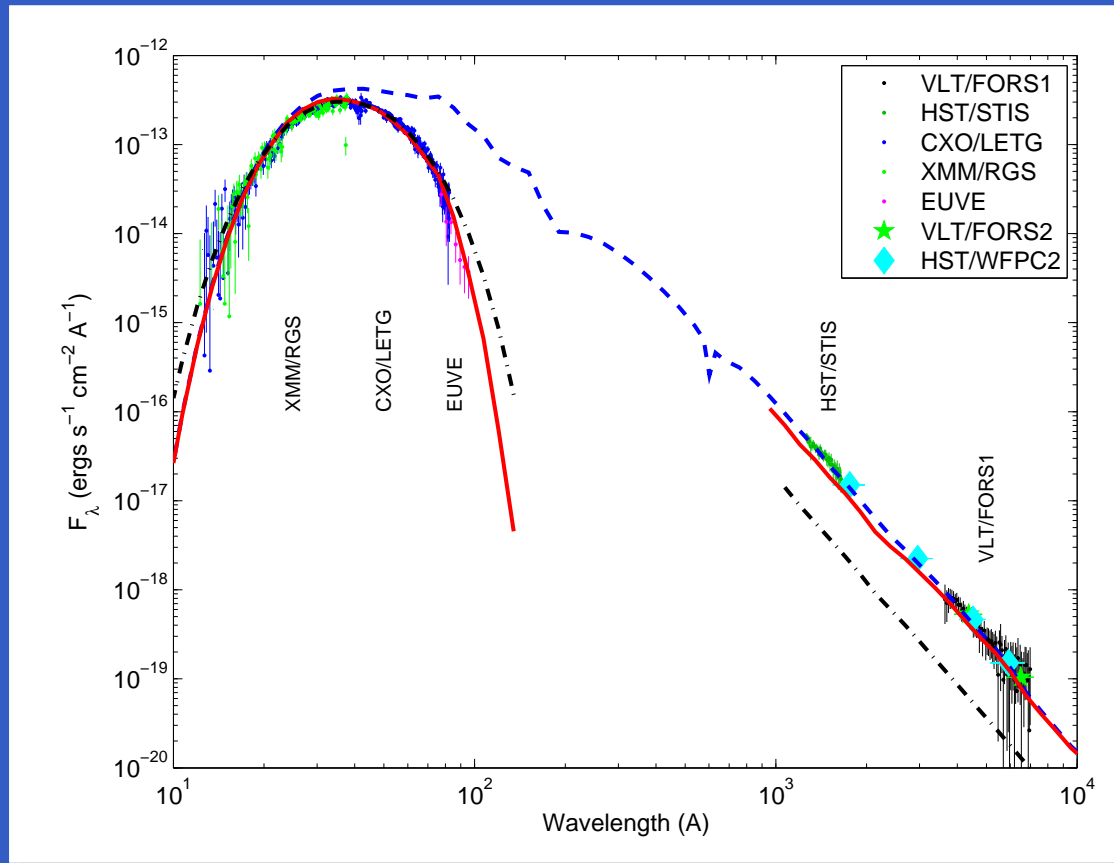
with  $T_{\text{eff},\infty} = T_{\text{eff}}/(1+z)$  and  $R_{\infty} = R/(1+z)$

- redshift:

$$1+z = \left( 1 - \frac{2GM}{R} \right)^{-1/2}$$

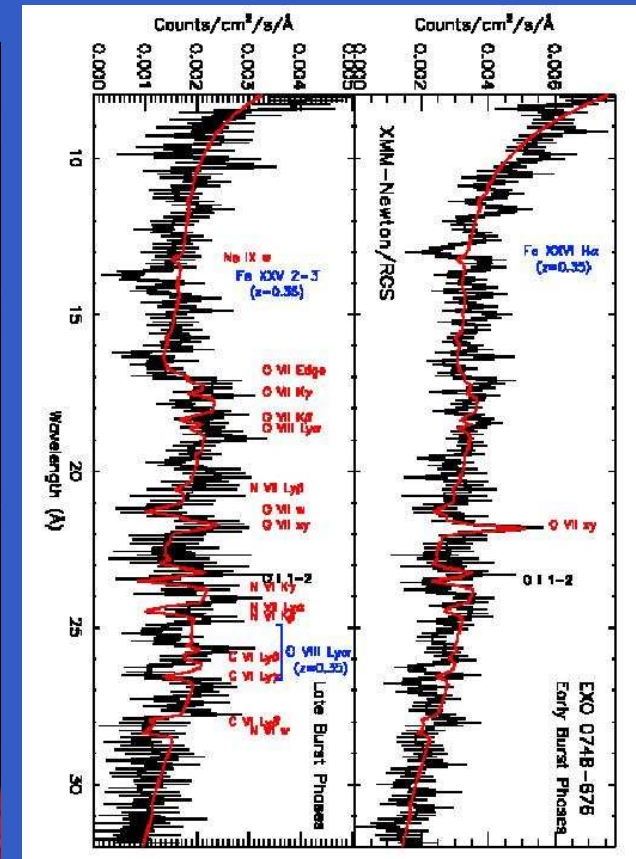
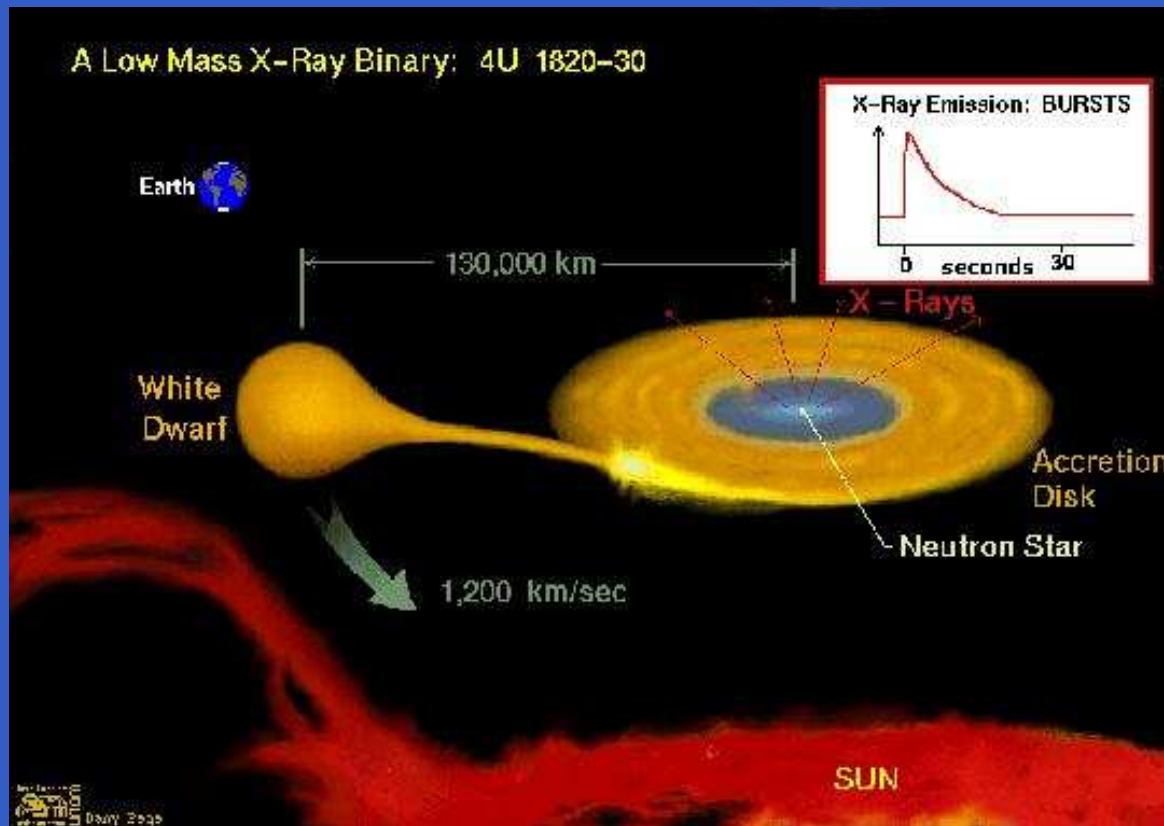
- need to know distance and effective temperature to get  $R_{\infty}$
- radius measured depends on true mass and radius of the star
- additional constraint from redshift measurement from e.g. redshifted spectral lines fixes mass and radius uniquely

# RXJ 1856: Neutron Star or Quark Star? (Trümper et al. (2003), Ho et al. (2003))



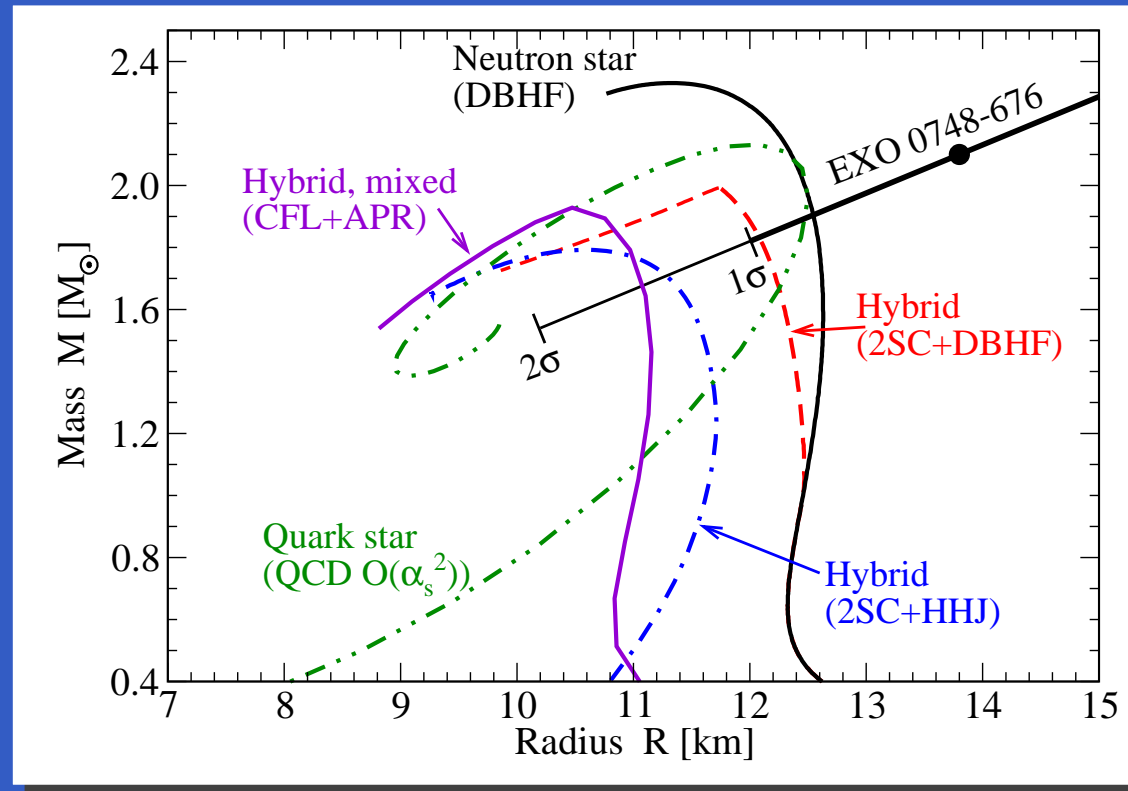
- two-component blackbody: small soft temperature, so as not to spoil the x-ray
- this implies a rather LARGE radius so that the optical flux is right!
- lower limit for radiation radius:  $R_\infty = R / \sqrt{1 - 2GM/R} = 17 \text{ km}$  ( $d/140 \text{ pc}$ )
- redshift  $z_g \approx 0.22$ :  $R \approx 14 \text{ km}$  and  $M \approx 1.55 M_\odot$
- largest uncertainty in distance  $d$

# X-Ray burster



- binary systems of a neutron star with an ordinary star
- accreting material on the neutron star ignites nuclear burning
- explosion on the surface of the neutron star: x-ray burst
- red shifted spectral lines measured!  
( $z = 0.35 \rightarrow M/M_{\odot} = 1.5 (R/10 \text{ km})$ ) (Cottam, Paerels, Mendez (2002))

# X-Ray burster EXO 0748–676: the EoS is hard!

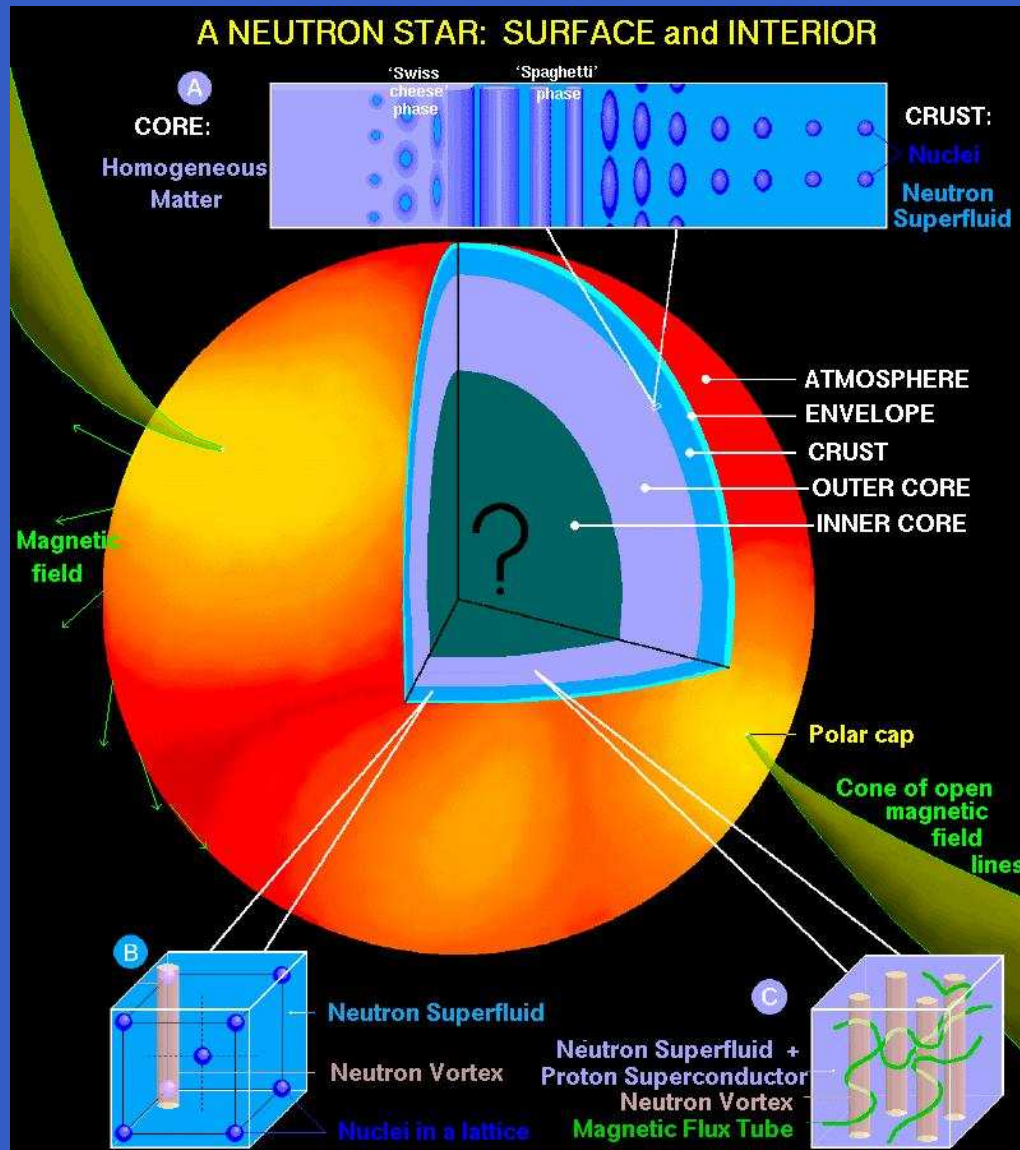


- analysis of Özel (Nature 2006):  $M \geq 2.10 \pm 0.28M_{\odot}$  and  $R \geq 13.8 \pm 1.8$  km, claims: 'unconfined quarks do not exist at the center of neutron stars'!
- reply by Alford, Blaschke, Drago, Klähn, Pagliara, JSB (Nature 445, E7 (2007)): limits rule out soft equations of state, not quark stars or hybrid stars!

⇒ the nuclear equation of state (EoS) would be hard

# Modelling the Neutron Star

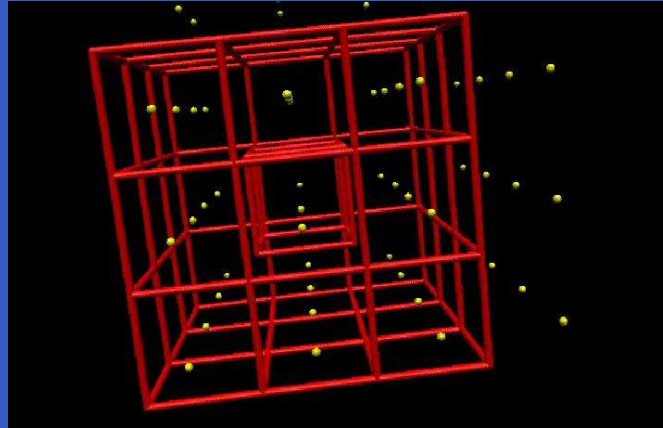
# Structure of Neutron Stars — the Crust (Dany Page)



- $n \leq 10^4 \text{ g/cm}^3$ :  
atmosphere  
(atoms)
- $n = 10^4 - 4 \cdot 10^{11} \text{ g/cm}^3$ :  
outer crust or envelope  
(free  $e^-$ , lattice of nuclei)
- $n = 4 \cdot 10^{11} - 10^{14} \text{ g/cm}^3$ :  
Inner crust  
(lattice of nuclei with free  
neutrons and  $e^-$ )

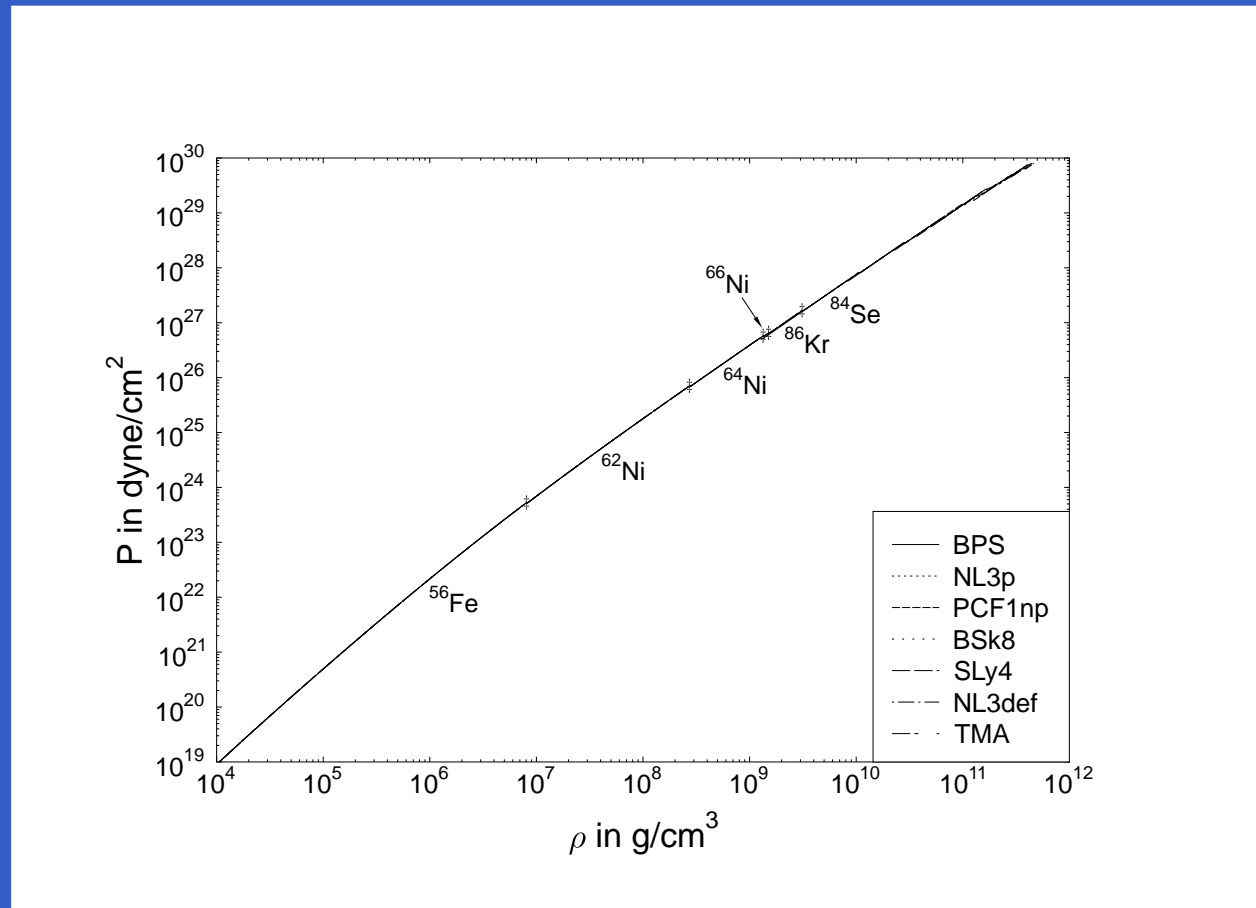
# Composition of the crust of a neutron star

lattice of nuclei surrounded by free electrons



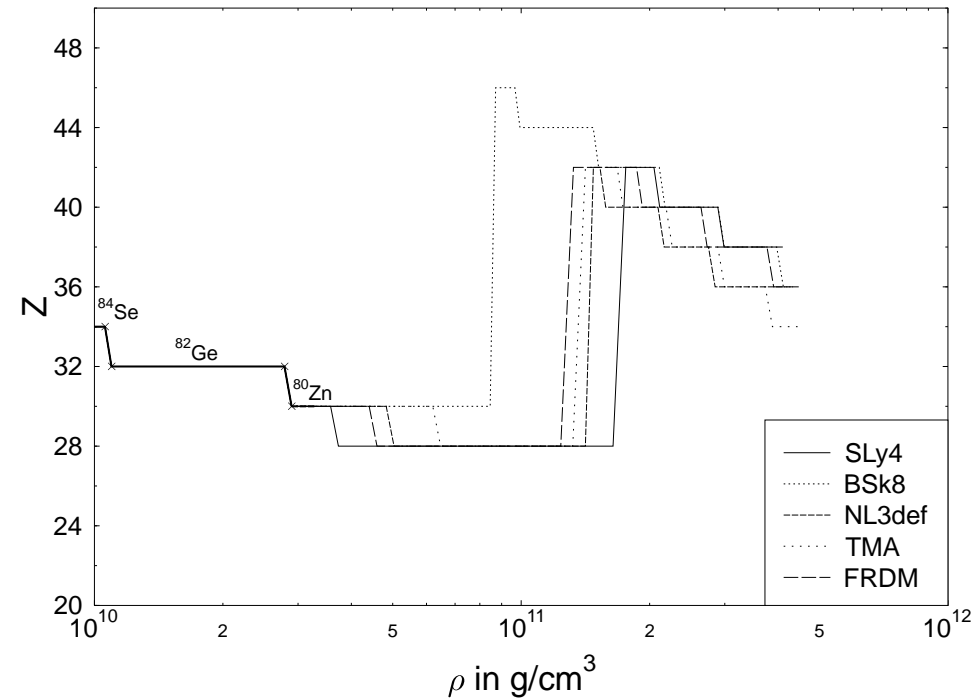
- Wigner–Seitz–cell, lattice structure is bcc
- minimize  $E = E_{\text{nuclei}} + E_{\text{lattice}} + E_{\text{electrons}}$
- loop over all particle stable nuclei (up to 14.000)
- use atomic mass evaluation of 2003 by Audi, Wapstra, and Thibault
- extrapolate to the drip–line with various models
- $\implies$  sequence of nuclei  ${}^A_Z$  as a function of density

# Sequence to the Dripline (Hempel, Rüter, JSB 2005)



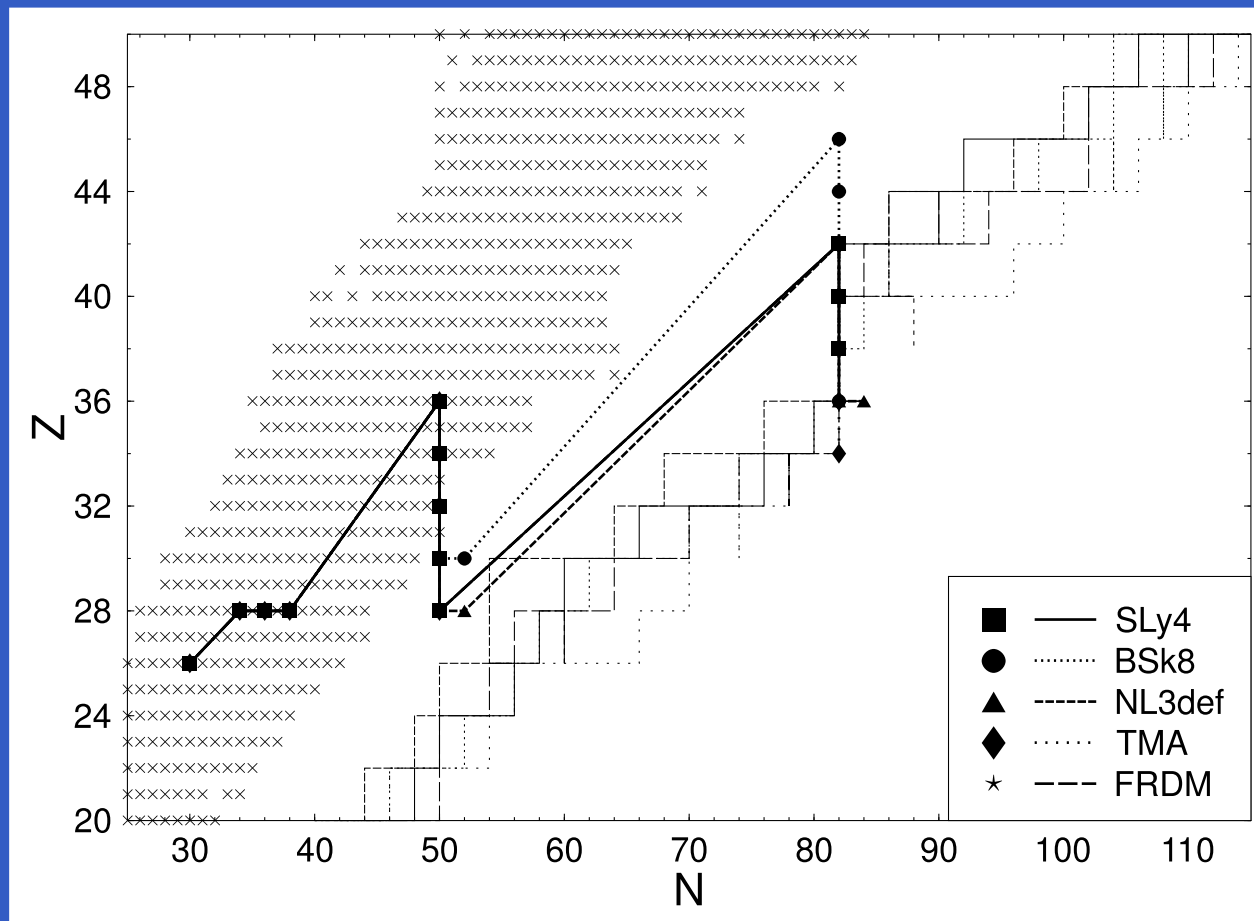
- outer crust starts with iron ( $^{56}\text{Fe}$ ) up to  $\rho \approx 10^7 \text{ g/cm}^3$
- continues along nickel isotopes ( $Z = 28$ ), then Kr, Se ( $N = 50$ )
- initial sequence at low densities independent of parameter set (data)!
- equation of state (nearly) independent of parameter set!

# Sequence to the Dripline II (Hempel, Ruster, JSB 2005)



- selection of state-of-the-art mass tables (deformed calculations)
- initial sequence of nuclei: Se, Ge, Zn (data)
- overall narrow range in  $Z$
- neutron drip around  $5 \cdot 10^{11}$   $\text{g/cm}^3$

# Nuclei in the crust (Hempel, Rüter, JSB 2005)



- sequence of nuclei: along  $N = 50$  then along  $N = 82$  with  $Z = 46 - 34$
- common endpoint around  $N = 82$  and  $Z = 36$  (!)
- common location of the dripline at  $N = 82$  (!)
- updates classic work of Baym, Pethick, Sutherland from 1971!



# Neutron Star Matter for a Free Gas

(Ambartsumyan and Saakyan, 1960)

Hadron	p,n	$\Sigma^-$	$\Lambda$	others
appears at:	$\ll n_0$	$4n_0$	$8n_0$	$> 20n_0$

but the corresponding equation of state results in a maximum mass of only

$$M_{\max} \approx 0.7M_{\odot} < 1.44M_{\odot}$$

(Oppenheimer and Volkoff, 1939)

⇒ effects from strong interactions are essential to describe neutron stars!

# Baryon–Baryon Interactions

$N\Lambda$ : attractive  $\rightarrow$   $\Lambda$ -hypernuclei for  $A = 3 - 209$   
 $U_\Lambda = -30$  MeV at  $n = n_0$

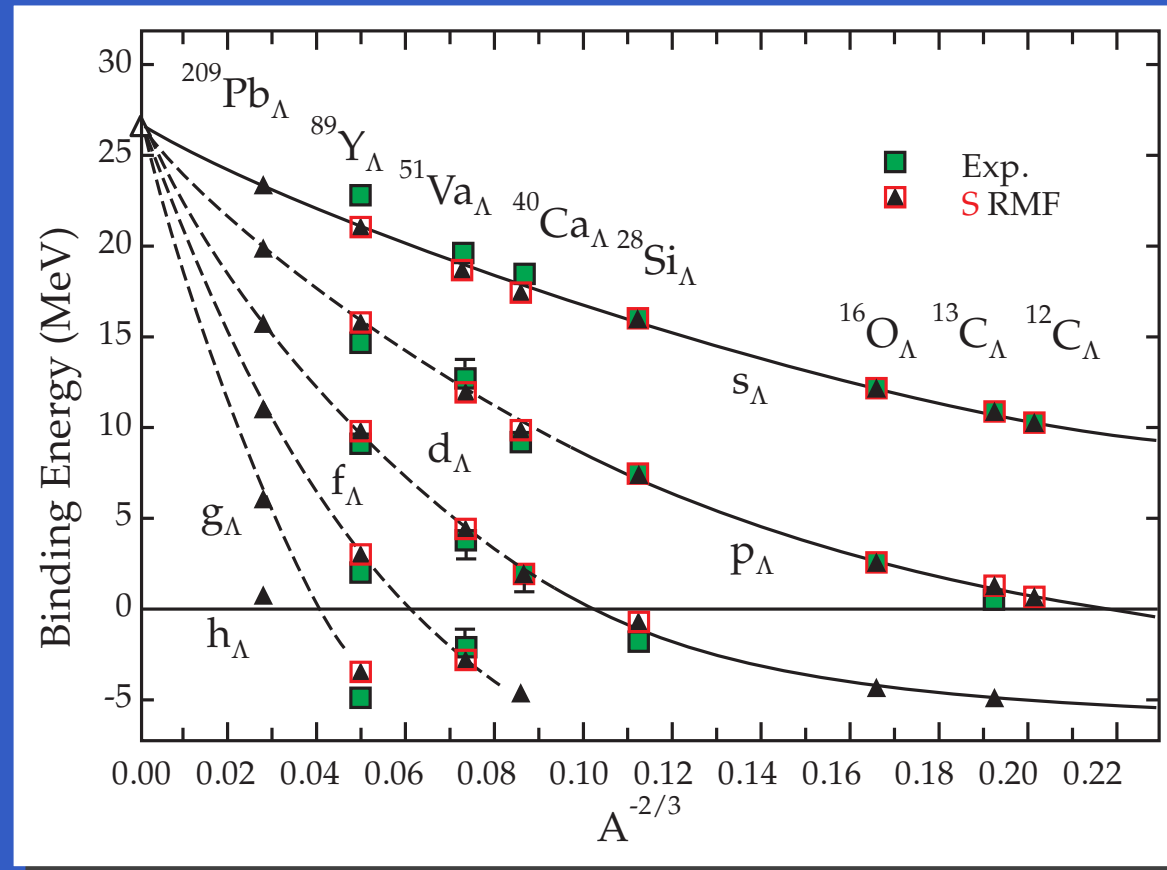
$N\Sigma$ :  ${}^4_\Sigma\text{He}$  hypernucleus bound by isospin forces  
 $\Sigma^-$  atoms: potential is repulsive

$N\Xi$ : attractive  $\rightarrow$  7  $\Xi$  hypernuclear events  
 $U_\Xi = -28$  MeV at  $n = n_0$   
quasi-free production of  $\Xi$ :  $U_\Xi = -18$  MeV

$\Lambda\Lambda$ : attractive  $\rightarrow$  5  $\Lambda\Lambda$  hypernuclear measurements  
more attractive than  $N\Lambda$ ?

$YY$ :  $Y = \Lambda, \Sigma, \Xi$ , unknown!

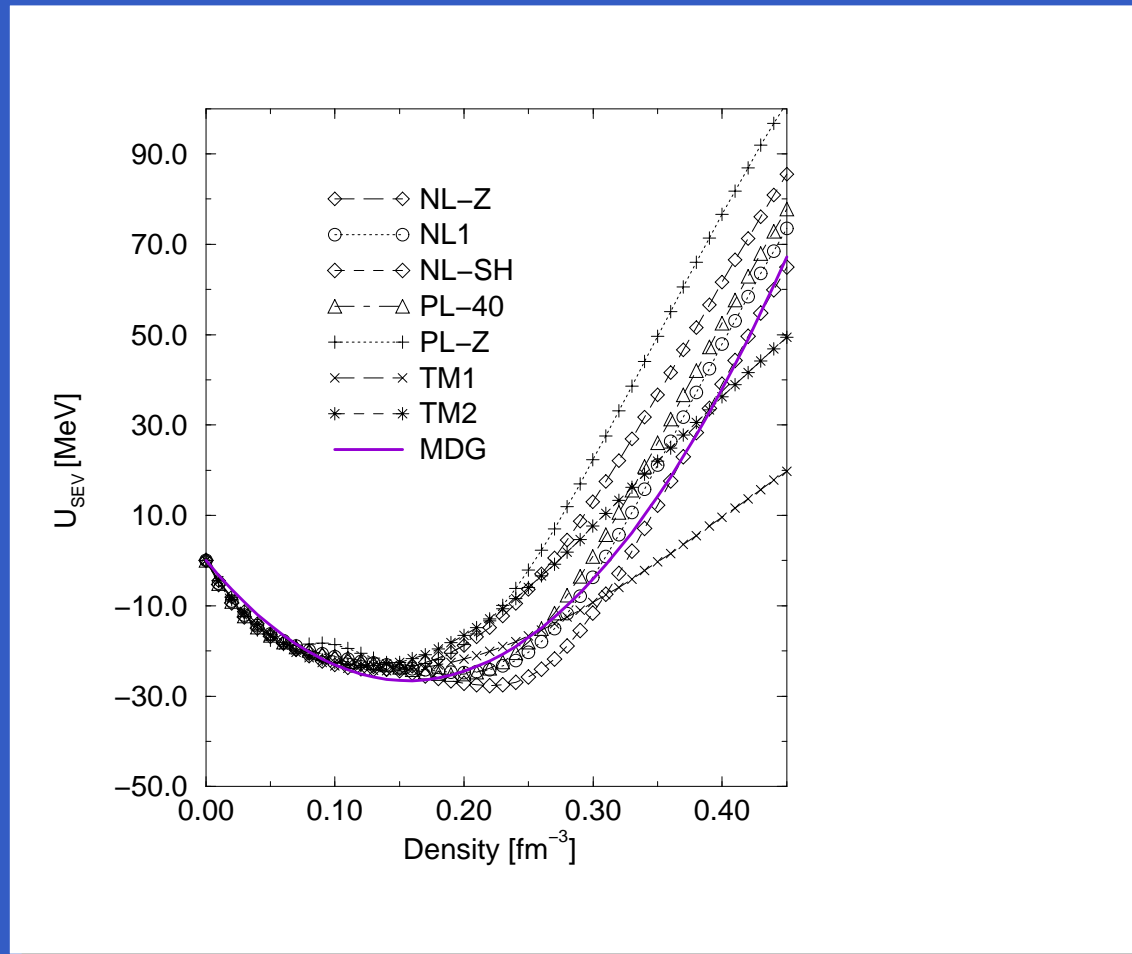
# $\Lambda$ Single-Particle Energies



(Rufa, JS, Maruhn, Stöcker, Greiner, Reinhard (1990))

- measured in  $(\pi^+, K^+)$  reactions
- spin-orbit splitting smaller than experimental resolution
- fit to single particle energies:  $U_\Lambda = -27 \text{ MeV}$  for  $A \rightarrow \infty$

# $\Lambda$ potential in nuclear matter (JSB, Bondorf, Mishustin 1997)



- hyperon potential in various (relativistic) parameterizations
- hyperon potential becomes repulsive above  $2n_0$
- compatible with hypernuclear data, three-body interactions for hyperons (MDG: Millener, Dover, Gal 1988)

# $\Lambda\Lambda$ Hypernuclei

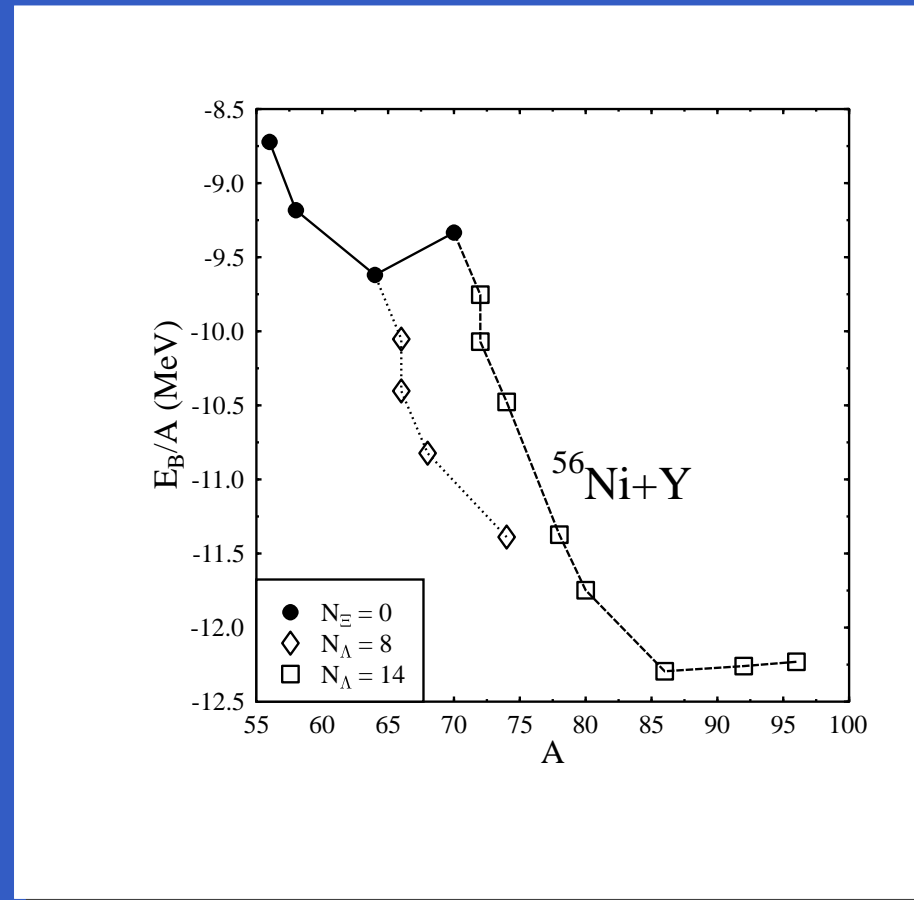
two  $\Lambda$ s bound in a nucleus, produced by  $\Xi^-$  capture



- $\Lambda\Lambda$  interaction is attractive
- no strong decay to the H-dibaryon seen

$$\Lambda + \Lambda \rightarrow H \rightsquigarrow m_H > 2m_\Lambda - B_{\Lambda\Lambda} \sim 2220 \text{ MeV}$$

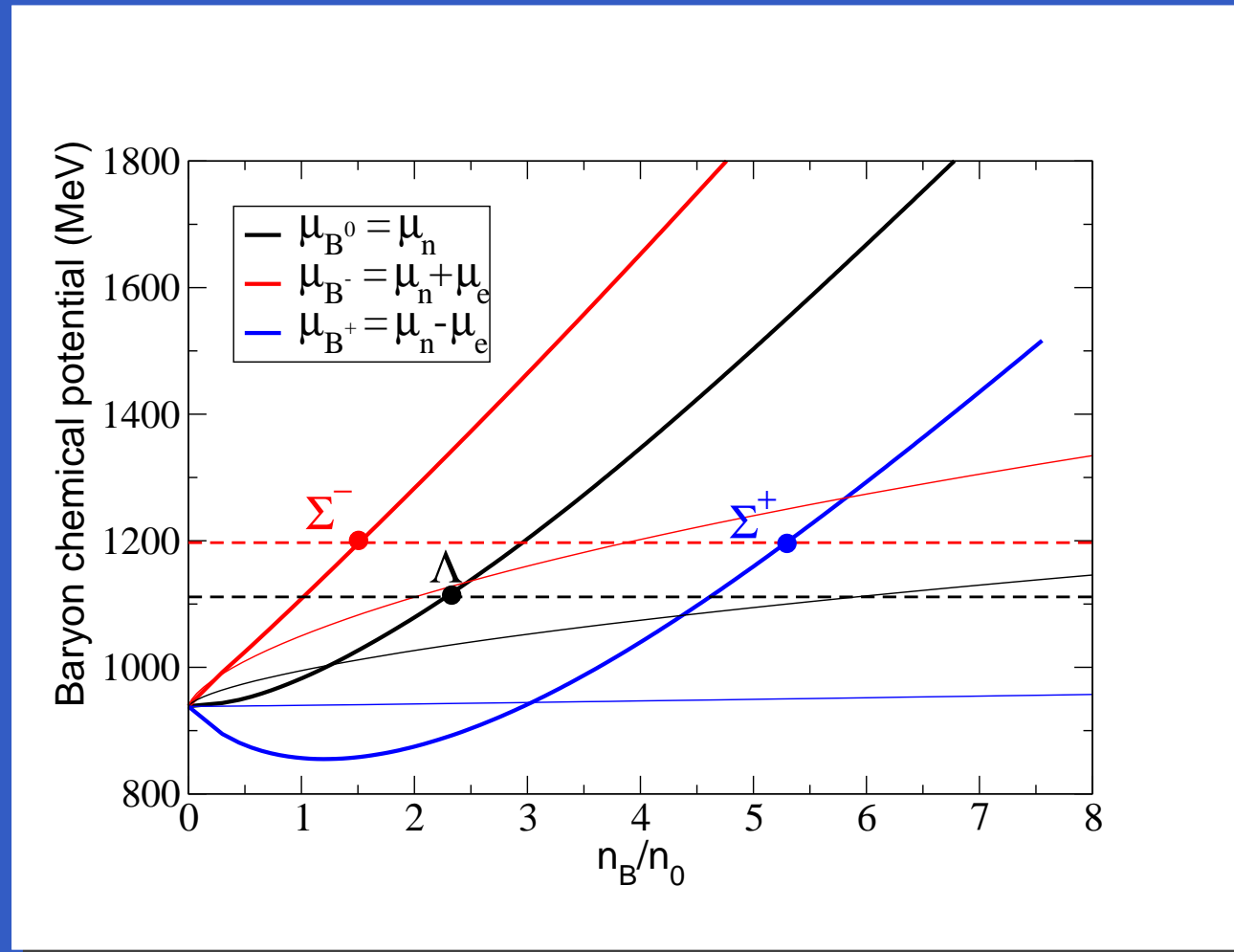
# Systems of Nucleons and Hyperons



(JS, Dover, Gal, Greiner, Stöcker (1993))

- Pauli-blocking of the reactions:  $\Lambda + \Lambda \leftrightarrow \Xi + N$ ,  $Q \approx -25$  MeV
- $\Sigma$ s are not stable:  $\Sigma + N \rightarrow \Lambda + N$ ,  $Q \approx -80$  MeV
- nuclear binding energy with  $\Lambda$ s and  $\Xi$ s increases to  $E/A = -12$  MeV!

# At which density do new particles appear? (Page and Reddy (2006))



- hyperons appear, when its in-medium energy equals its chemical potential:

$$\mu(Y) = \omega(Y) = m_Y + U_Y(n)$$

- thin lines: no potential, thick lines: with mean-field potential

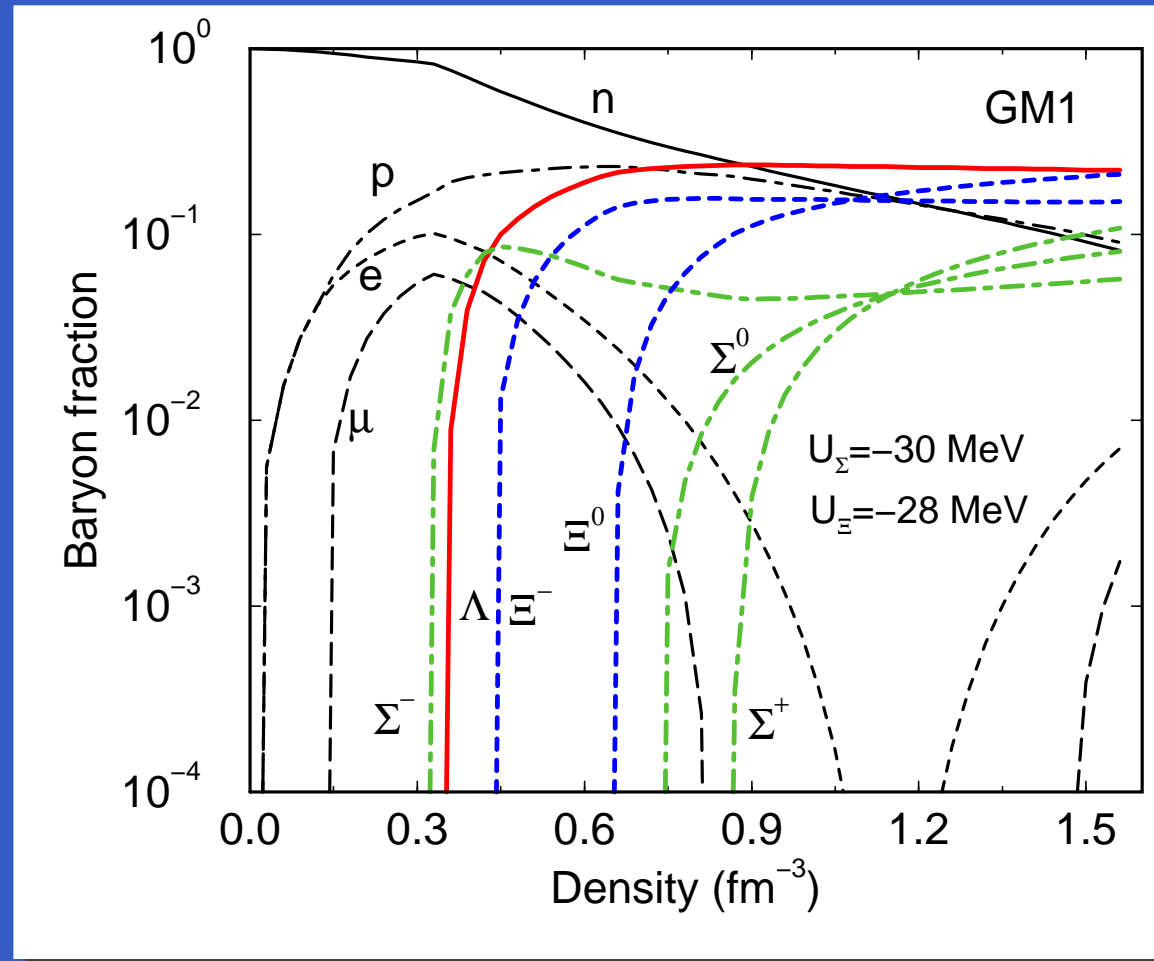
# Neutron Star Matter and Hyperons

Hyperons appear at  $n \approx 2n_0$ !

- nonrelativistic potential model (Balberg and Gal, 1997)
- quark-meson coupling model (Pal et al., 1999)
- relativistic mean-field models (Glendenning, 1985; Knorren, Prakash, Ellis, 1995; JS and Mishustin, 1996)
- relativistic Hartree-Fock (Huber, Weber, Weigel, Schaab, 1998)
- Brueckner-Hartree-Fock (Baldo, Burgio, Schulze, 2000; Vidana et al., 2000)
- chiral effective Lagrangian's (Hanuske et al., 2000)
- density-dependent hadron field theory (Hofmann, Keil, Lenske, 2001)
- RG approach alias  $V_{\text{low}k}$  (Djapo, Schäfer, Wambach, 2008)

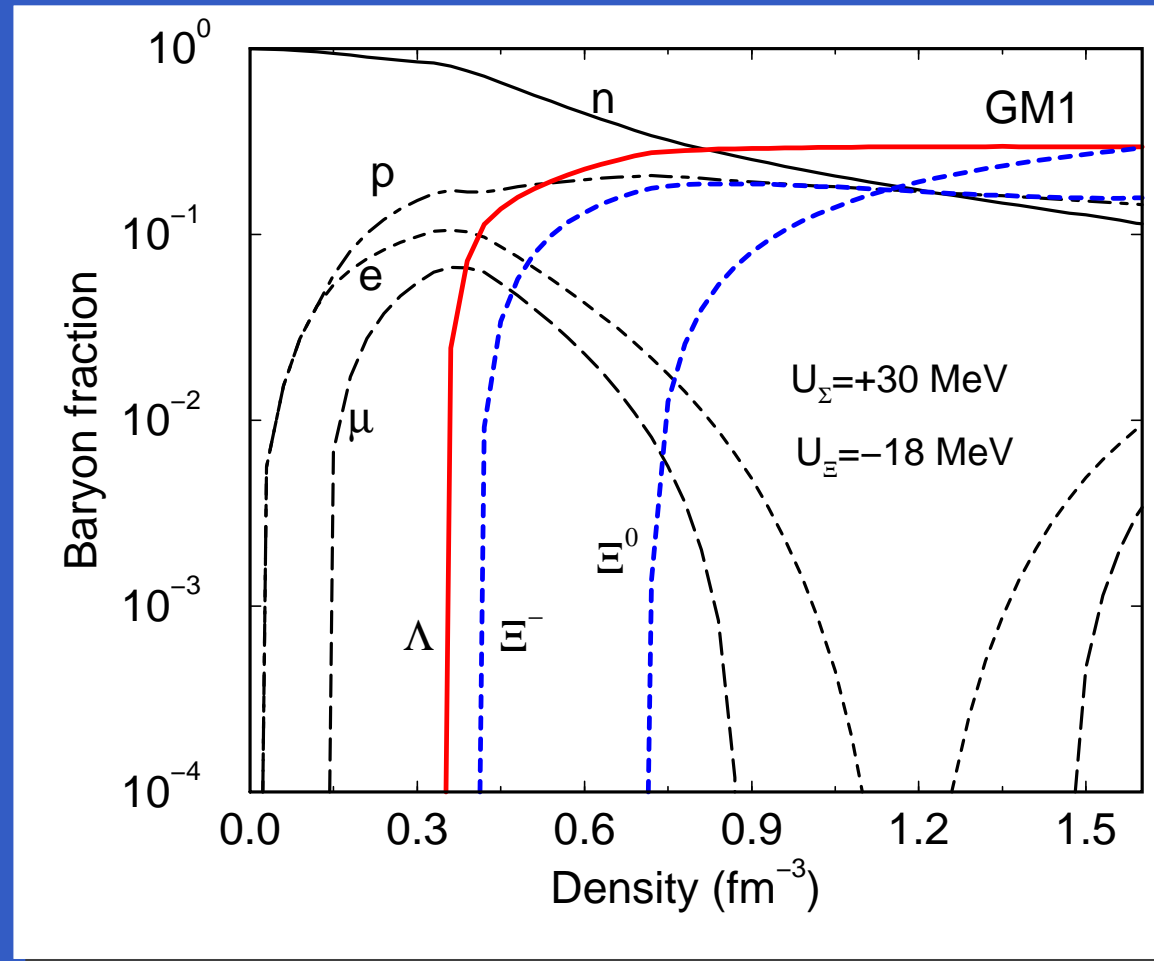
⇒ neutron stars are strange !!!

# Composition of Neutron Star Matter



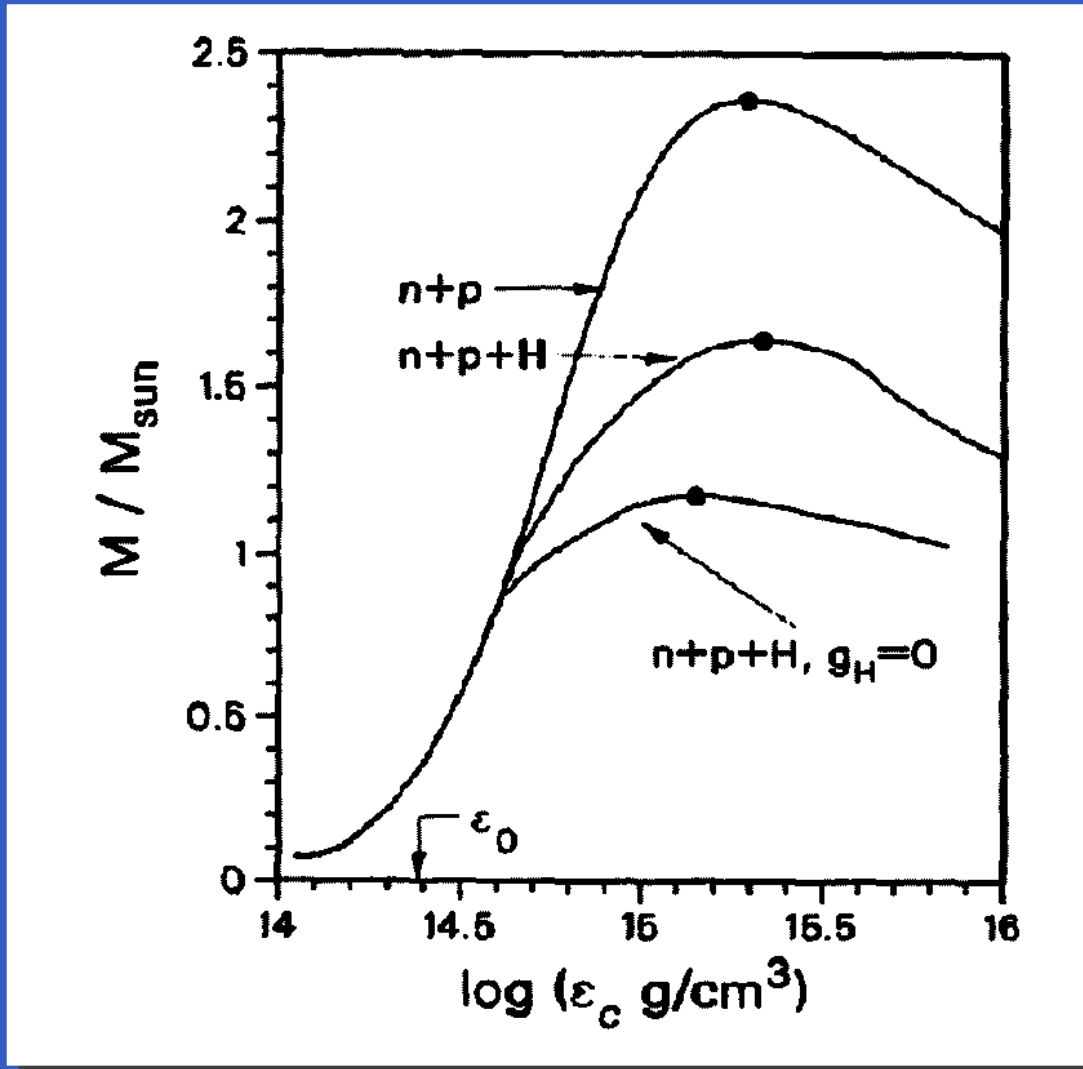
- attractive potential for  $\Sigma$ s and  $\Xi$ s
- $\Sigma^-$  appear shortly before  $\Lambda$ s around  $n = 2n_0$
- $\Lambda$ s present in matter at  $n = 2.5n_0$ ,  $\Xi^-$  before  $n = 3n_0$

# Composition of Neutron Star Matter



- $\Lambda$ s are present close to  $n = 2n_0$
- repulsive potential for  $\Sigma$ s:  $\Sigma$  hyperons do not appear at all!
- population is highly sensitive to the in-medium potential!

# Impact of hyperons on the maximum mass of neutron stars



(Glendenning and Moszkowski 1991)

- neutron star with nucleons and leptons only:  
 $M \approx 2.3 M_{\odot}$
- substantial decrease of the maximum mass due to hyperons!
- maximum mass for “giant hypernuclei”:  $M \approx 1.7 M_{\odot}$
- noninteracting hyperons result in a too low mass:  
 $M < 1.4 M_{\odot}$  !

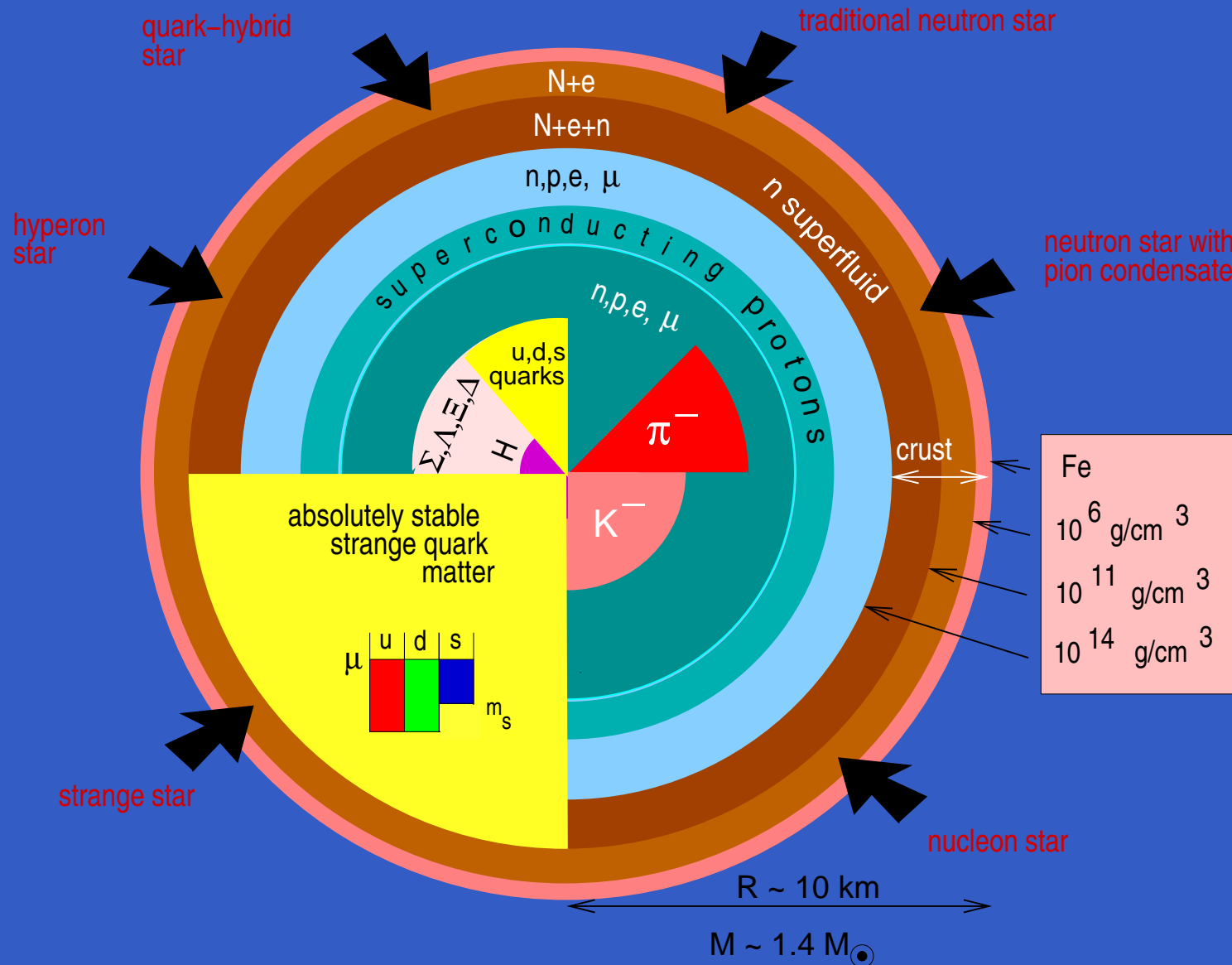
# Modern many-body approaches to neutron stars

## beyond mean-field . . .

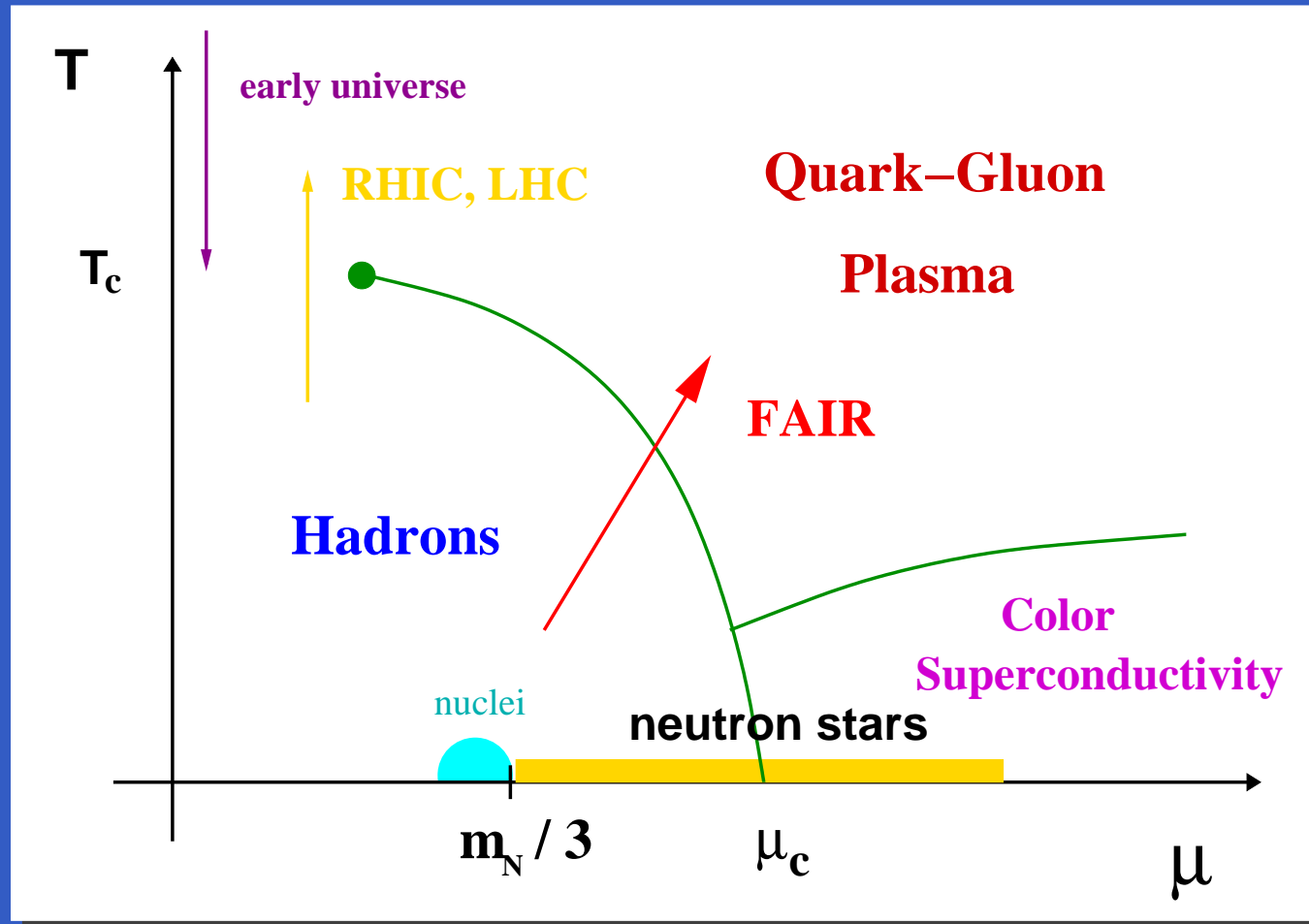
- Relativistic Hartree-Fock (Huber et al. 1998):  
 $M_{\max} = 1.3 - 1.6 M_{\odot}$  depending on hyperon coupling strength
- Brueckner-Hartree-Fock: using Nijmegen soft-core YN potential
- Vidana et al. (2000):  $M_{\max} = 1.47 M_{\odot}$  (NN and YN interactions),  
 $M_{\max} = 1.34 M_{\odot}$  (NN, NY, YY interactions)
- Baldo et al. (2000):  $M_{\max} = 1.26 M_{\odot}$  including three-body forces
- Djapo, Schäfer, Wambach (2008):  $M_{\max} = 0.8 - 1.3 M_{\odot}$  (RG approach)
- too soft EoS, too low masses!
- three-body force for hyperons? momentum dependence?  
typically  $p = 300 - 600$  MeV

# Quark Matter in Neutron Stars

# Structure of a Neutron Star — the Core (Fridolin Weber)

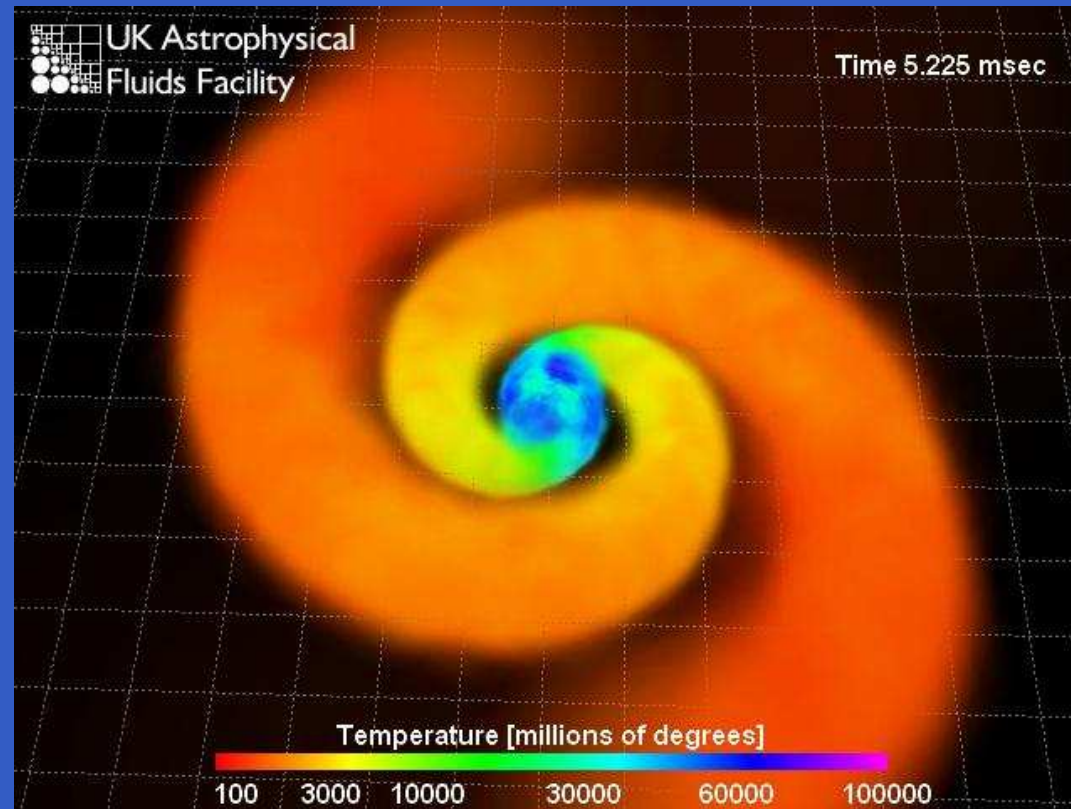


# Phase Transitions in Quantum Chromodynamics QCD



- Early universe at zero density and high temperature
- neutron star matter at small temperature and high density
- first order phase transition at high density (not deconfinement)!
- probed by heavy-ion collisions at GSI, Darmstadt (FAIR!)

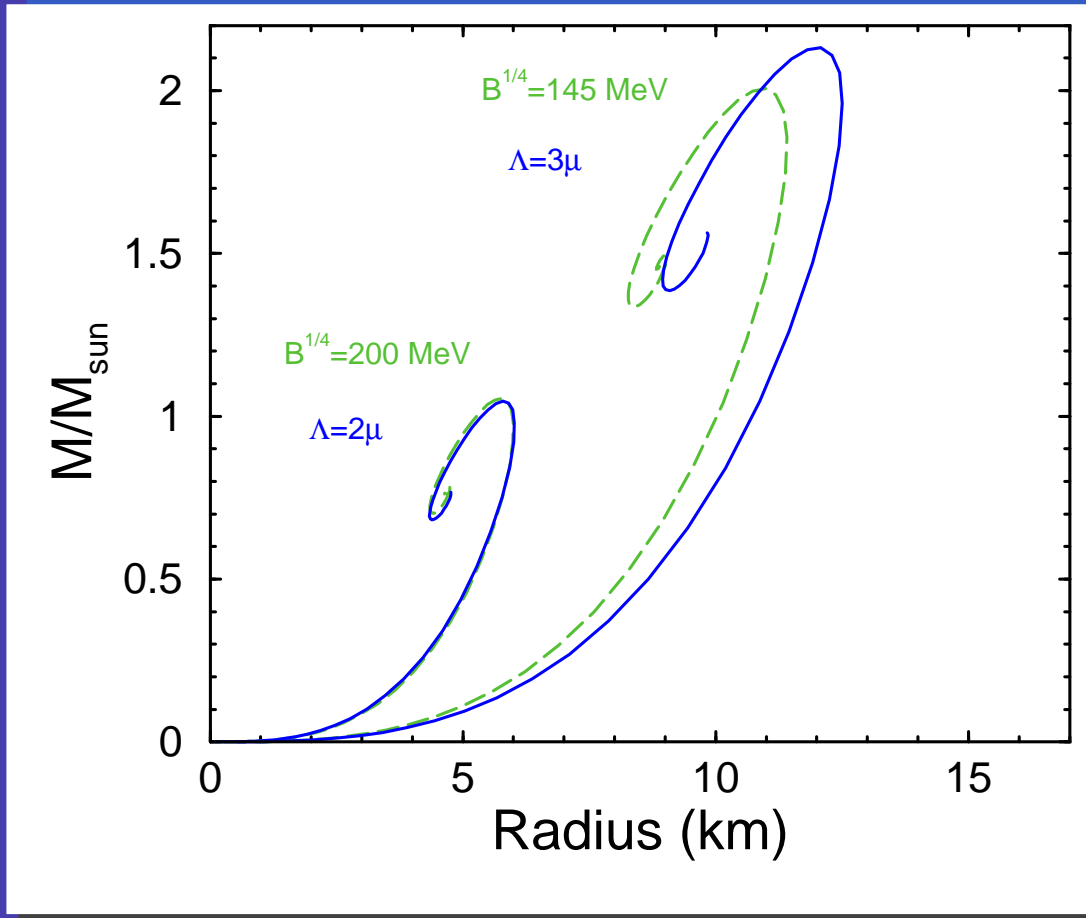
# Nuclear EoS in Astrophysics



- supernovae simulations:  $T = 1\text{--}50 \text{ MeV}$ ,  $n = 10^{-10}\text{--}2n_0$
- proto-neutron star:  $T = 1\text{--}50 \text{ MeV}$ ,  $n = 10^{-3}\text{--}10n_0$
- global properties of neutron stars:  $T = 0$ ,  $n = 10^{-3}\text{--}10n_0$
- neutron star mergers:  $T = 0\text{--}100 \text{ MeV}$ ,  $n = 10^{-10}\text{--}10n_0$



# Mass-radius and maximum density of pure quark stars



- green curves: MIT bag model
- blue curves: perturbative QCD calculations  
(Fraga, JSB, Pisarski 2001)

- case  $\Lambda = 2\mu$ :  $M_{\max} = 1.05 M_{\odot}$ ,  $R_{\max} = 5.8$  km,  $n_{\max} = 15 n_0$
- case  $\Lambda = 3\mu$ :  $M_{\max} = 2.14 M_{\odot}$ ,  $R_{\max} = 12$  km,  $n_{\max} = 5.1 n_0$
- other nonperturbative approaches: Schwinger–Dyson model (Blaschke et al.), massive quasiparticles (Peshier, Kämpfer, Soff), NJL model (Hanauske et al.), HDL (Andersen and Strickland), ...

# A Simple Model of Dense QCD

- star made of a gas of **u**, **d** and **s** quarks
- interaction taken into account perturbatively up to  $\alpha_s^2$ ;  $\alpha_s = g^2/4\pi$
- $\alpha_s$  runs according to the renormalization group equation ( $u = \ln(\bar{\Lambda}^2/\Lambda_{\overline{\text{MS}}}^2)$ ):

$$\alpha_s(\bar{\Lambda}) = \frac{4\pi}{\beta_0 u} \left[ 1 - \frac{2\beta_1}{\beta_0^2} \frac{\ln(u)}{u} + \frac{4\beta_1^2}{\beta_0^4 u^2} \left( \left( \ln(u) - \frac{1}{2} \right)^2 + \frac{\beta_2\beta_0}{8\beta_1^2} - \frac{5}{4} \right) \right]$$

- Particle Data Group:  $\alpha_s(2 \text{ GeV}) = 0.3089 \longrightarrow \Lambda_{\overline{\text{MS}}} = 365 \text{ MeV}$  for  $N_f = 3$
- No bag constant is introduced!
- star temperature  $\ll$  typical chemical potentials  $\longrightarrow$  zero temperature
- $m_s = 100 \text{ MeV} \ll \mu_{\min} = m_N/3 \longrightarrow$  three flavor massless quarks
- charge neutrality and  $\beta$  equilibrium:  $\mu_s = \mu_d = \mu_u \equiv \mu$

# Equation of State in pQCD

The thermodynamic potential (Freedman and McLerran (1978))

$$\Omega(\mu) = -\frac{N_f \mu^4}{4\pi^2} \left\{ 1 - 2 \left( \frac{\alpha_s}{\pi} \right) - \left[ G + N_f \ln \frac{\alpha_s}{\pi} + \left( 11 - \frac{2}{3} N_f \right) \ln \frac{\bar{\Lambda}}{\mu} \right] \left( \frac{\alpha_s}{\pi} \right)^2 \right\}$$

$G$  is scheme dependent and in  $\overline{\text{MS}}$  scheme:

$$G = G_0 - 0.536 N_f + N_f \ln N_f, \quad G_0 = 10.73 \pm 0.13$$

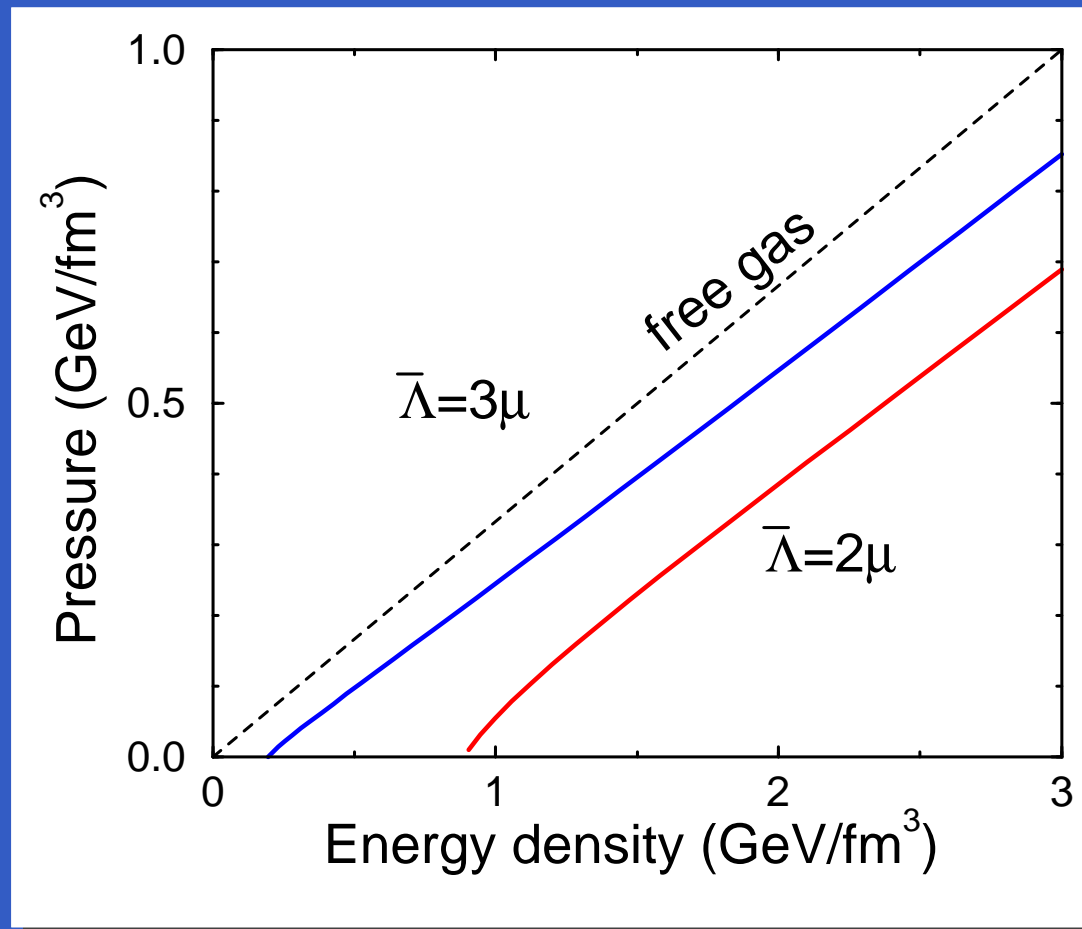
From  $\Omega(\mu)$  we have

pressure:  $p(\mu) = -\Omega(\mu)$

number density:  $n(\mu) = (\partial p / \partial \mu)$

energy density:  $\epsilon = -p + \mu n$

# Equation of State in pQCD



Nearly linear behavior of the pressure with the energy density

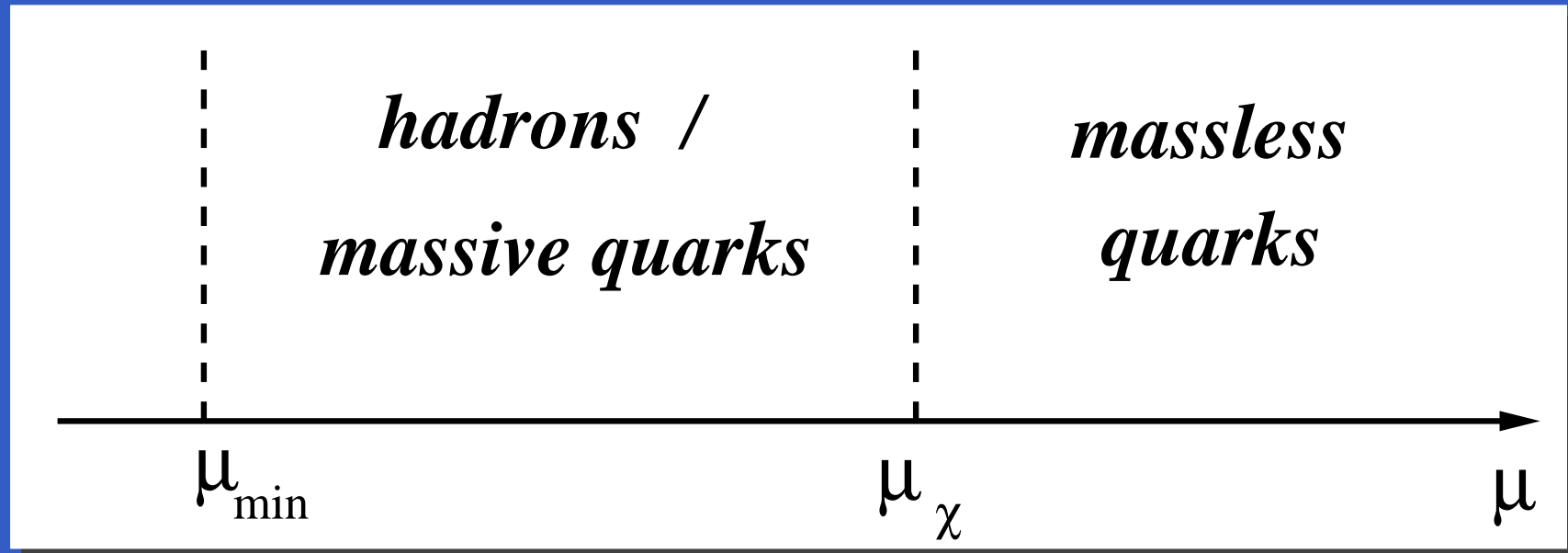
⇒ approximation with an effective nonideal bag model:

$$\Omega(\mu) = -\frac{N_f}{4\pi^2} a_{\text{eff}} \mu^4 + B_{\text{eff}}$$

case 2:  $B_{\text{eff}}^{1/4} = 199 \text{ MeV}$ ,  $a_{\text{eff}} = 0.628$  ( $\leq 4\%$ )

case 3:  $B_{\text{eff}}^{1/4} = 140 \text{ MeV}$ ,  $a_{\text{eff}} = 0.626$  ( $\leq 2\%$ )

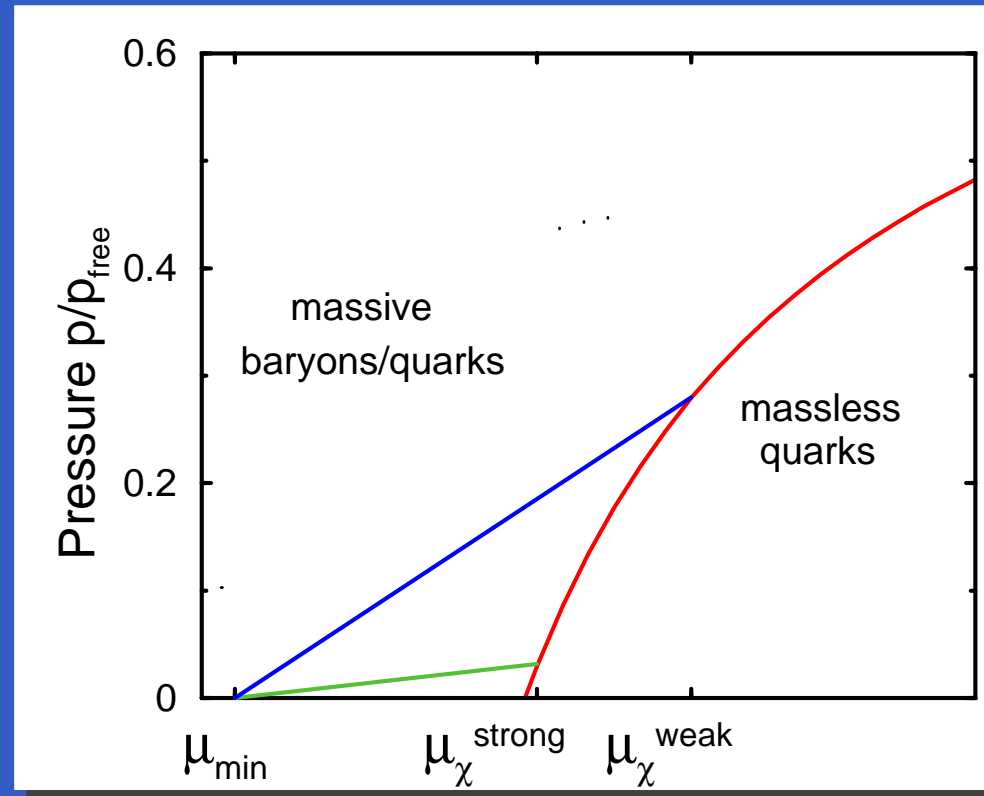
# A Model For Cold And Dense QCD



Two possibilities for a first-order chiral phase transition:

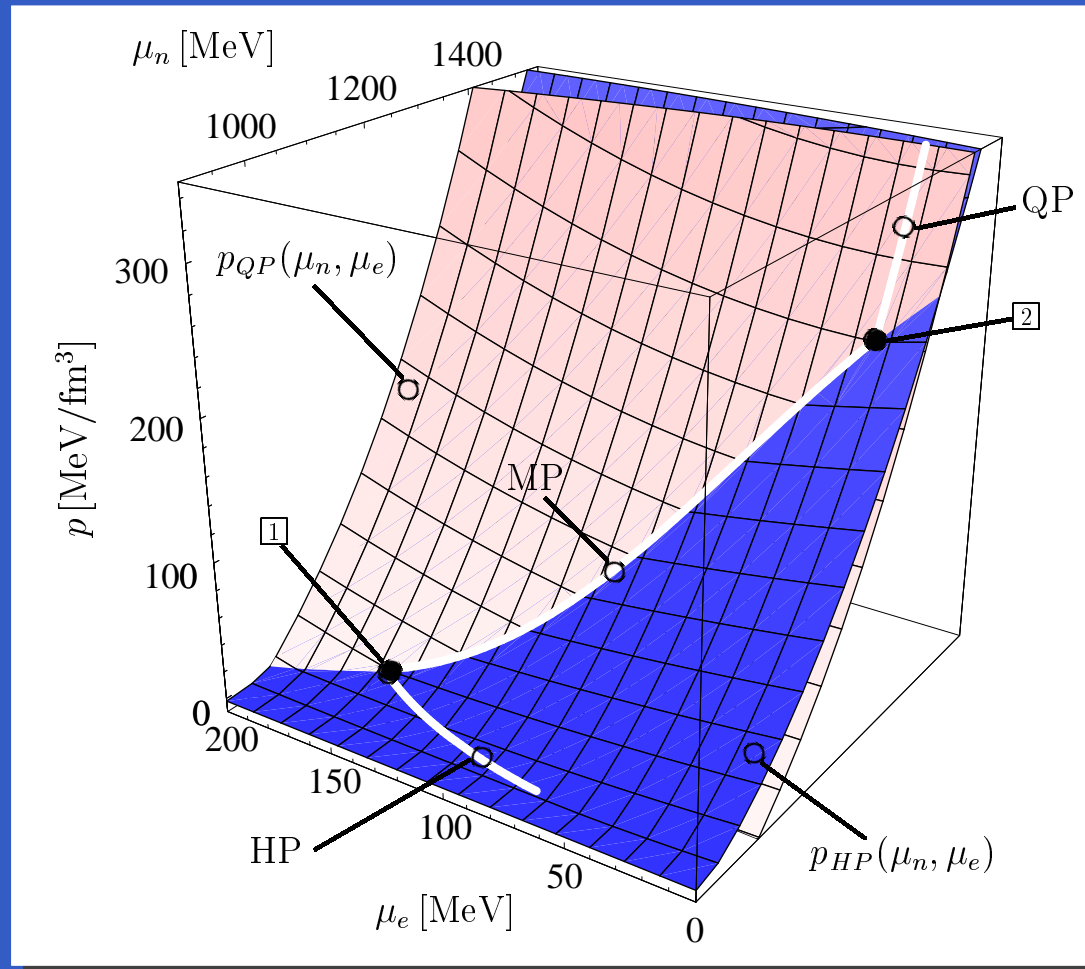
- A weakly first-order chiral transition (or no true phase transition),  
⇒ one type of compact star (neutron star)
- A strongly first-order chiral transition  
⇒ two types of compact stars:  
a new stable solution with smaller masses and radii

# Matching the two phases: two possible scenarios



- Weak: phase transition is weakly first order or a crossover  $\rightarrow$  pressure in massive phase rises strongly
- Strong: transition is strongly first order  $\rightarrow$  pressure rises slowly with  $\mu$
- asymmetric matter up to  $\sim 2n_0$ : suggest a slow rise with density!

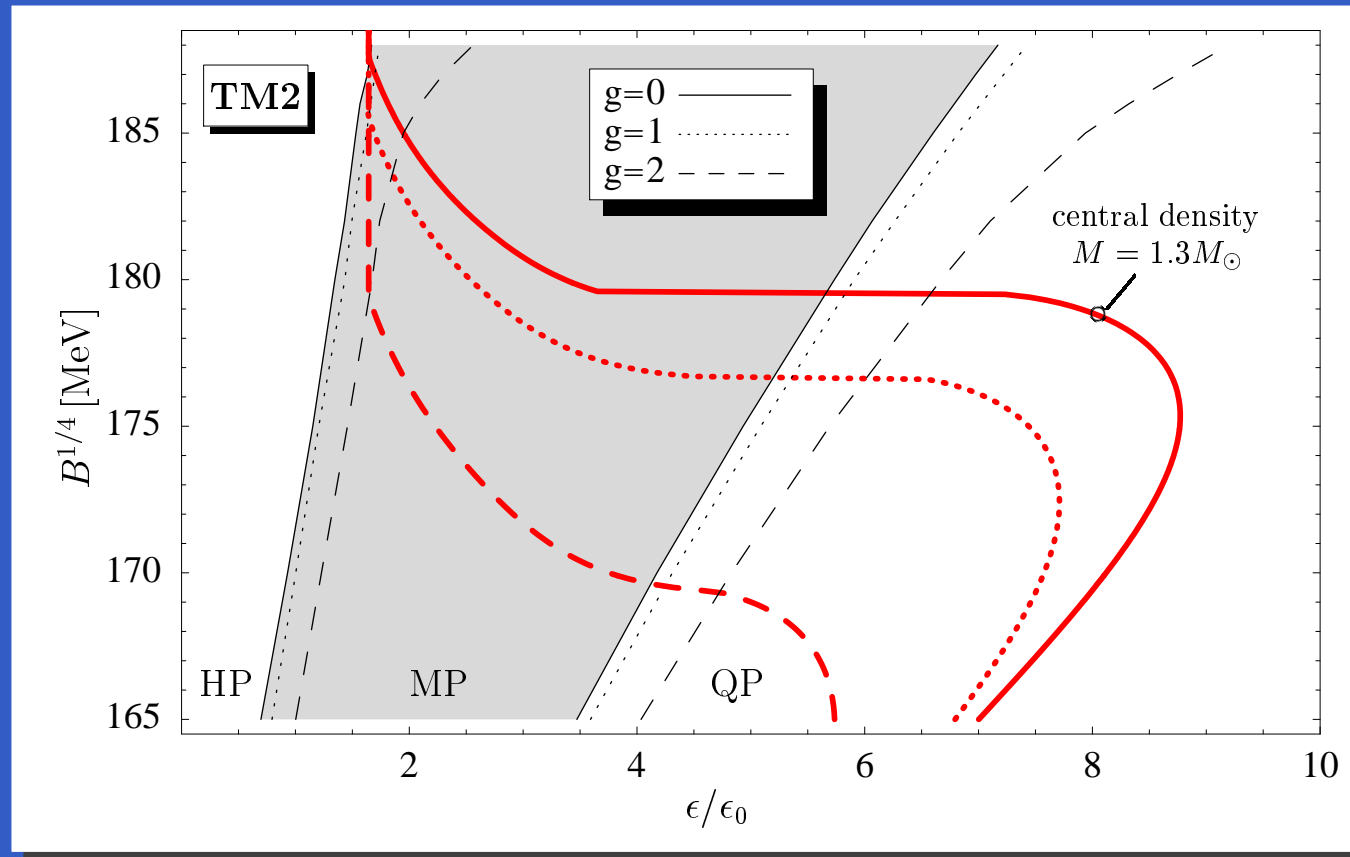
# Gibbs Phase Construction (Glendenning (1992))



(Schertler et al. (2000))

- two conserved charges in  $\beta$ -equilibrium: baryon number and charge!
- Gibbs criterion for phase equilibrium: equal pressure for equal chemical potentials  $P_I(\mu_B, \mu_e) = P_{II}(\mu_B, \mu_e)$
- globally charge neutral matter: mixed phase with charged bubbles forms!

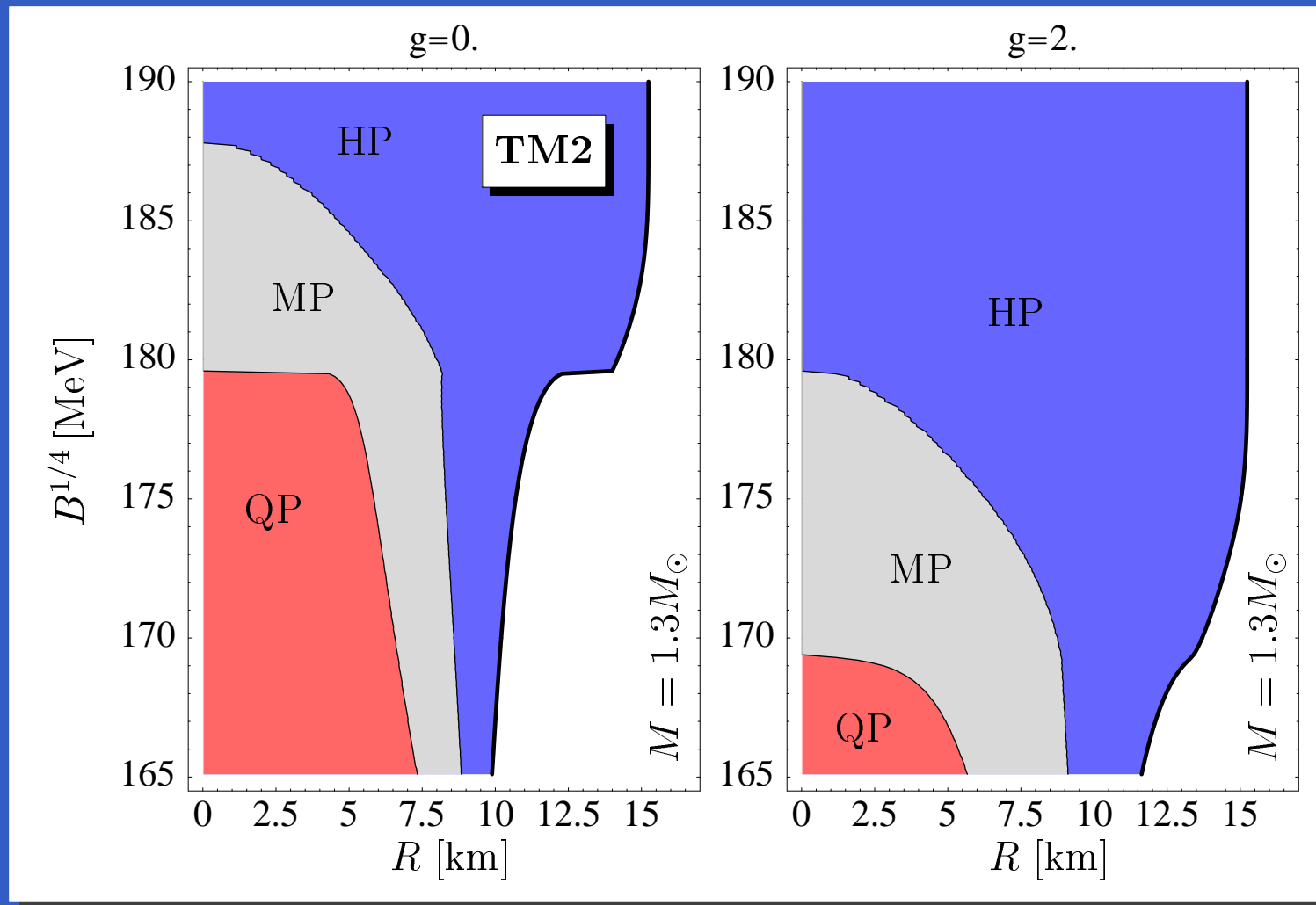
# Quark Matter in Cold Neutron Stars



(Schertler, C. Greiner, JSB, Thoma (2000))

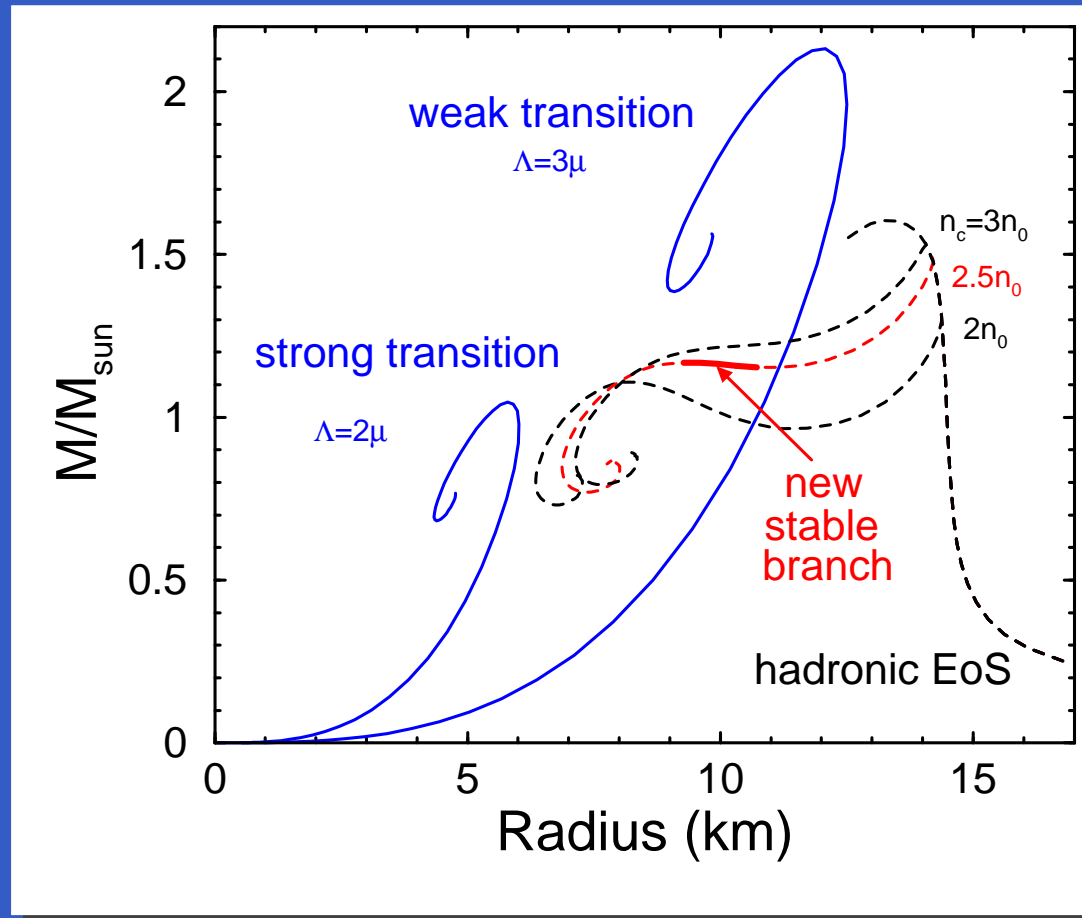
- phase transition to quark matter in the MIT bag model
- onset of mixed phase appears between  $(1 - 2)n_0$  even for large values of the bag constant
- sufficiently high densities reached in the core for a  $1.3M_{\odot}$  neutron star to have quark matter

# Hybrid Stars (Schertler et al. (2000))



- hybrid star: consists of hadronic and quark matter
- three phases possible: hadronic, mixed phase and pure quark phase
- composition depends crucially on the parameters as the bag constant  $B$  (and on the mass!)

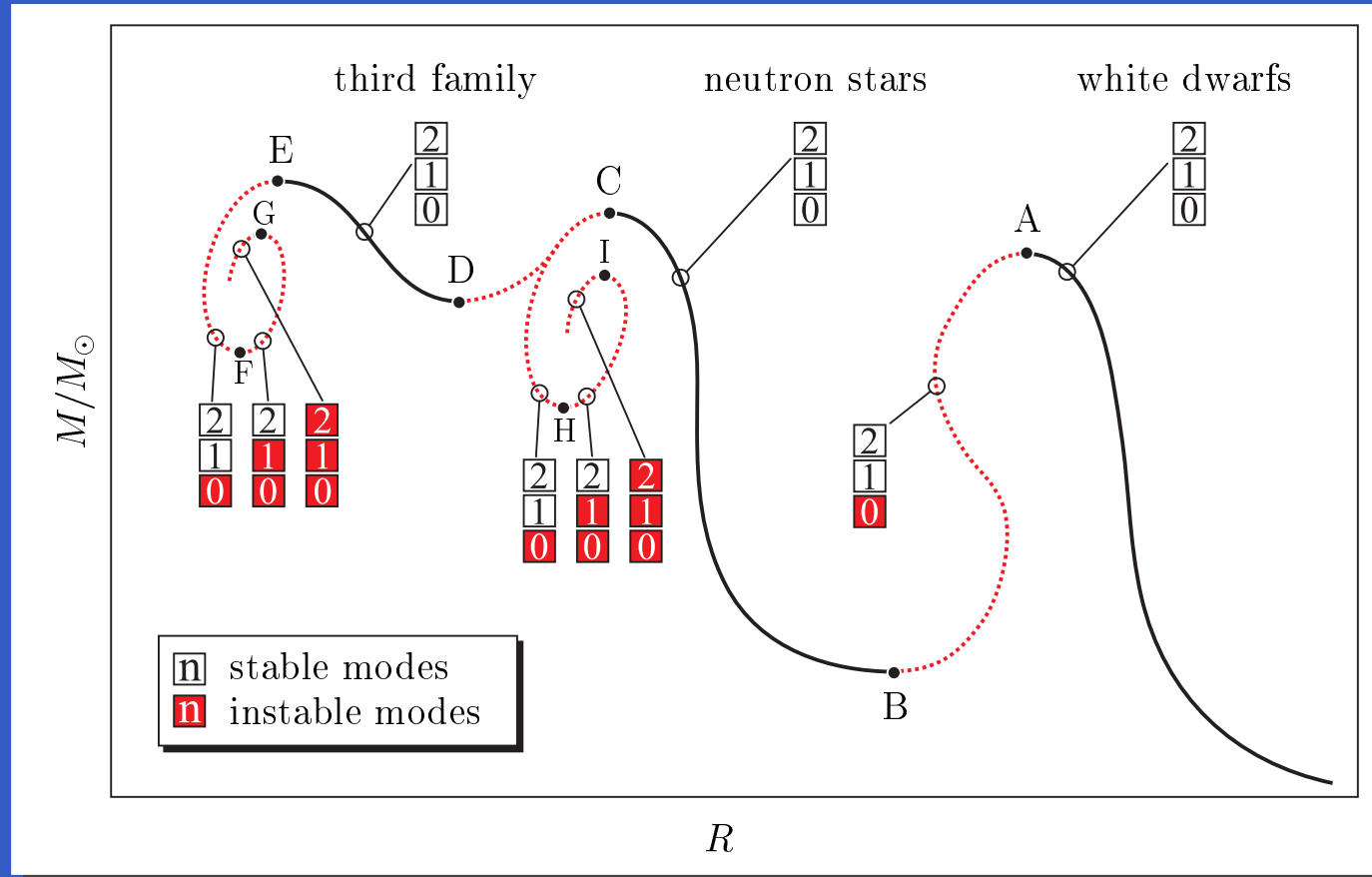
# Quark star twins? (Fraga, JSB, Pisarski (2001))



- Weak transition: ordinary neutron star with quark core (hybrid star)
- Strong transition: third class of compact stars possible with maximum masses  $M \sim 1 M_{\odot}$  and radii  $R \sim 6$  km
- Quark phase dominates ( $n \sim 15 n_0$  at the center), small hadronic mantle

# Third Family of Compact Stars (Gerlach 1968)

(Glendenning, Kettner 2000; Schertler, Greiner, JSB, Thoma 2000)



- third solution to the TOV equations besides white dwarfs and neutron stars, solution is stable!
- generates stars more compact than neutron stars!
- possible for any first order phase transition!

# Signals for a Third Family/Phase Transition?

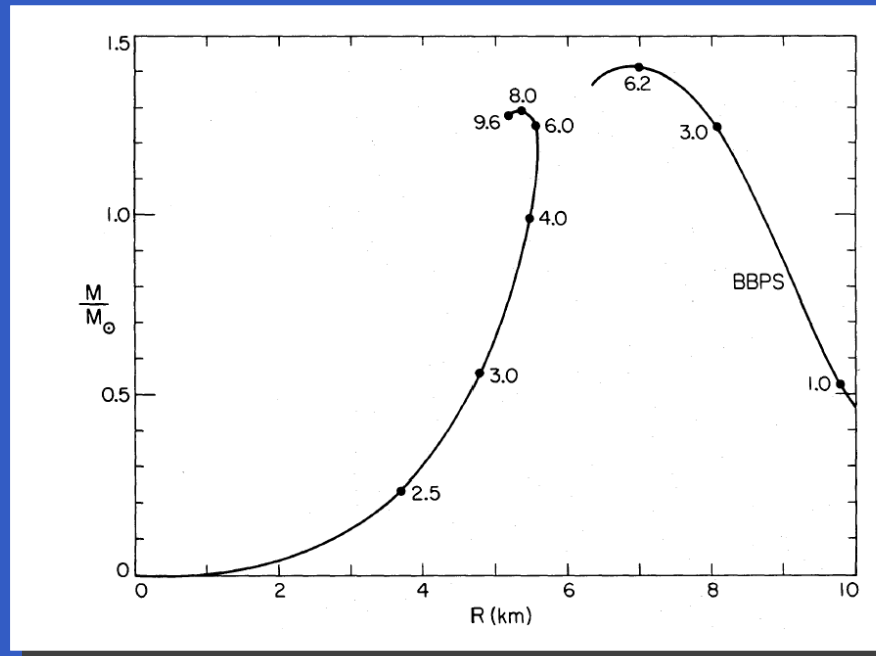
- mass-radius relation: rising twins (Schertler et al., 2000)
- spontaneous spin-up of pulsars (Glendenning, Pei, Weber, 1997)
- delayed collapse of a proto-neutron star to a black hole (Thorsson, Prakash, Lattimer, 1994)
- bimodal distribution of pulsar kick velocities (Bombaci and Popov, 2004)
- collapse of a neutron star to the third family? (gravitational waves,  $\gamma$ -rays, neutrinos)
- secondary shock wave in supernova explosions?
- gravitational waves from colliding neutron stars?

# Difference between quark stars, hybrid stars, etc?

- hybrid stars: neutron stars mixed with quark matter in the core
- quark star twins: special hybrid stars with a pure quark matter core
- strange stars or selfbound stars: consists of stable quark matter only, purely hypothetical!!!

# Hypothetical Selfbound Star versus Ordinary Neutron Star

(Hartle, Sawyer, Scalapino (1975!))



## selfbound stars:

- vanishing pressure at a finite energy density
- mass-radius relation starts at the origin (ignoring a possible crust)
- arbitrarily small masses and radii possible

## neutron stars:

- bound by gravity, finite pressure for all energy density
- mass-radius relation starts at large radii
- minimum neutron star mass:  
 $M \sim 0.1M_{\odot}$  with  $R \sim 200$  km

# Signals for Strange Stars?

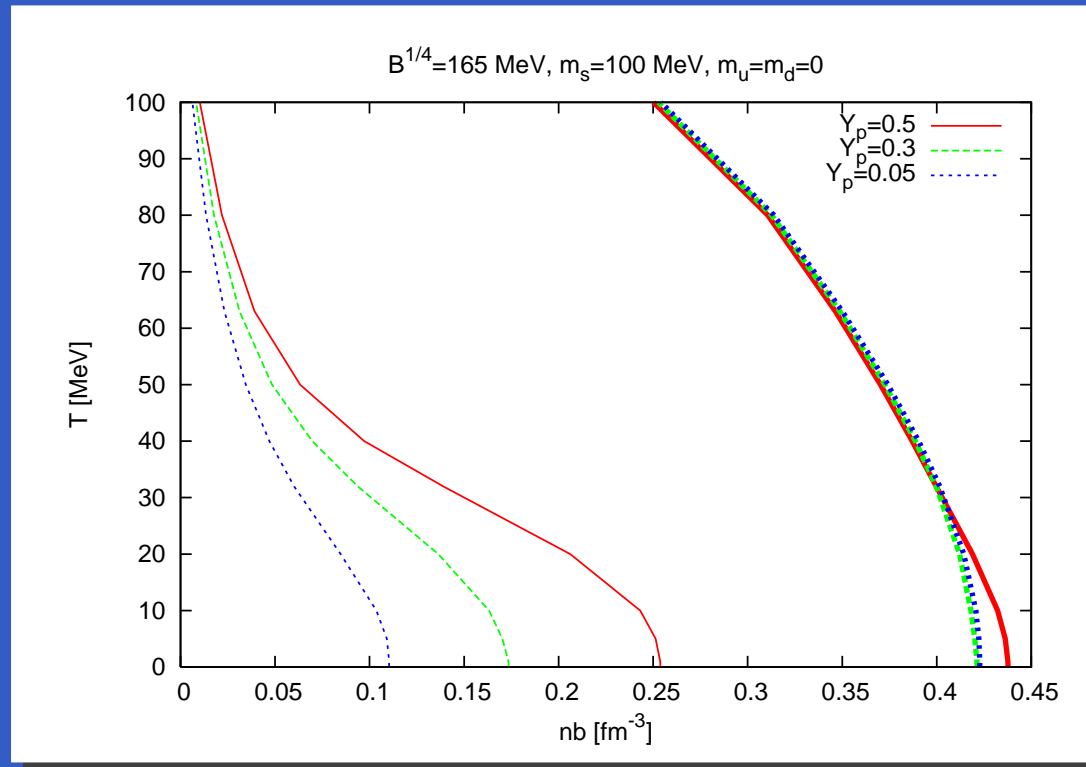
similar masses and radii, cooling, surface (crust), ... but look for

- extremely small mass, small radius stars (includes strangelets!)
- strange dwarfs: small and light white dwarfs with a strange star core (Glendenning, Kettner, Weber, 1995)
- super-Eddington luminosity from bare, hot strange stars (Page and Usov, 2002)
- conversion of neutron stars to strange stars (explosive events!)
- ...

# Summary

- equation of state (EoS) determines the maximum mass and its radius
- in-medium potentials of hadrons determine the population
- new hadronic degrees of freedoms normally soften the EoS!
- but quark matter can also stiffen the EoS!
- strong chiral phase transition leads to a third family of compact stars
- implications for mass-radius relation, cooling, neutrino emission, gravitational waves emission
- and for supernovae!

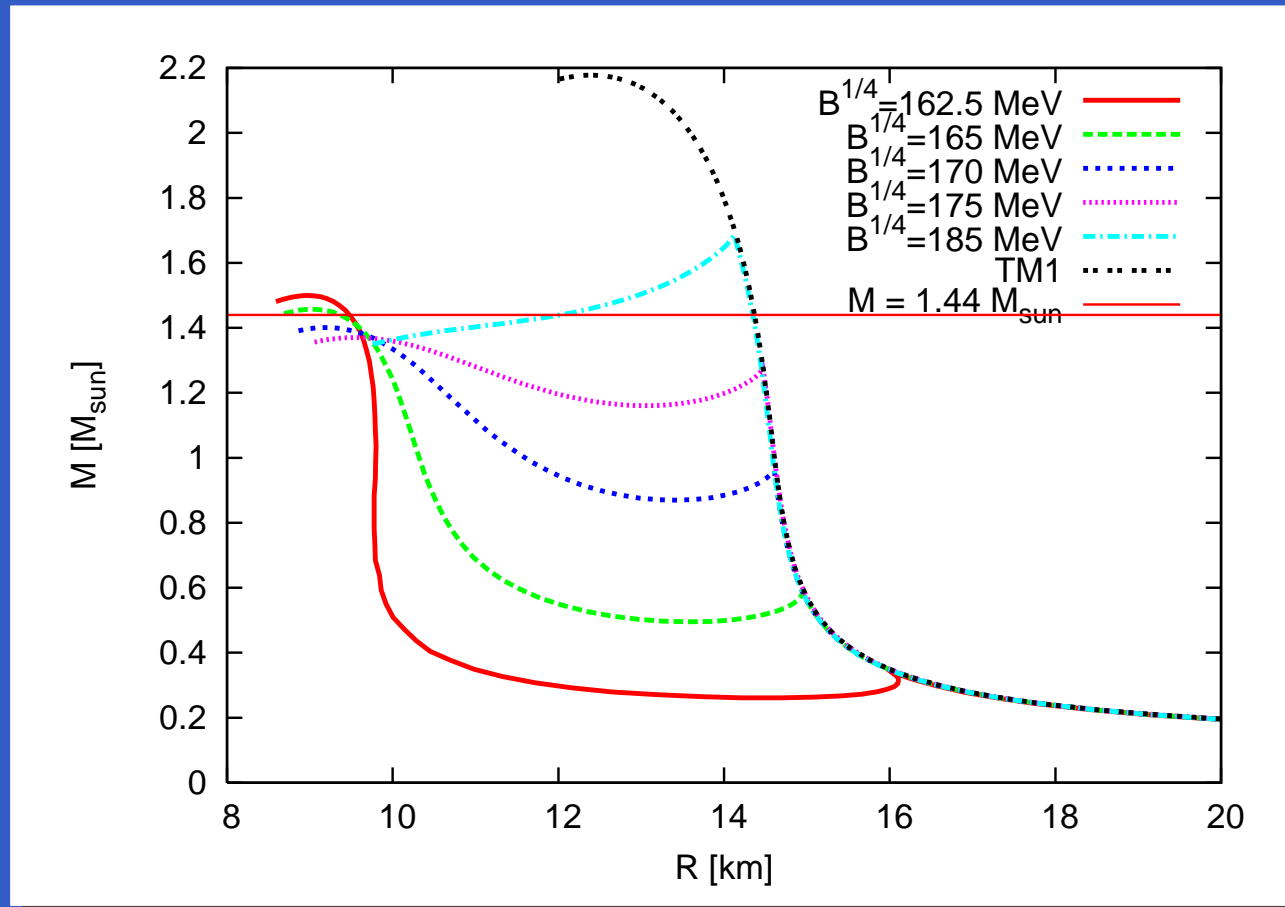
# Phase Transition to Quark Matter for Astros



(Irina Sagert and Giuseppe Pagliara)

- start of the mixed phase at quite low densities due to  $\beta$ -equilibrium, strange quark matter is more stable than nucleon matter (using RMF model TMA)
- even lower critical densities for isospin-asymmetric matter (low proton fraction  $Y_p$ ) due to asymmetry energy for nucleons
- quark matter favored in hot matter due to the QCD phase diagram
- production of quark matter in supernovae at bounce possible!

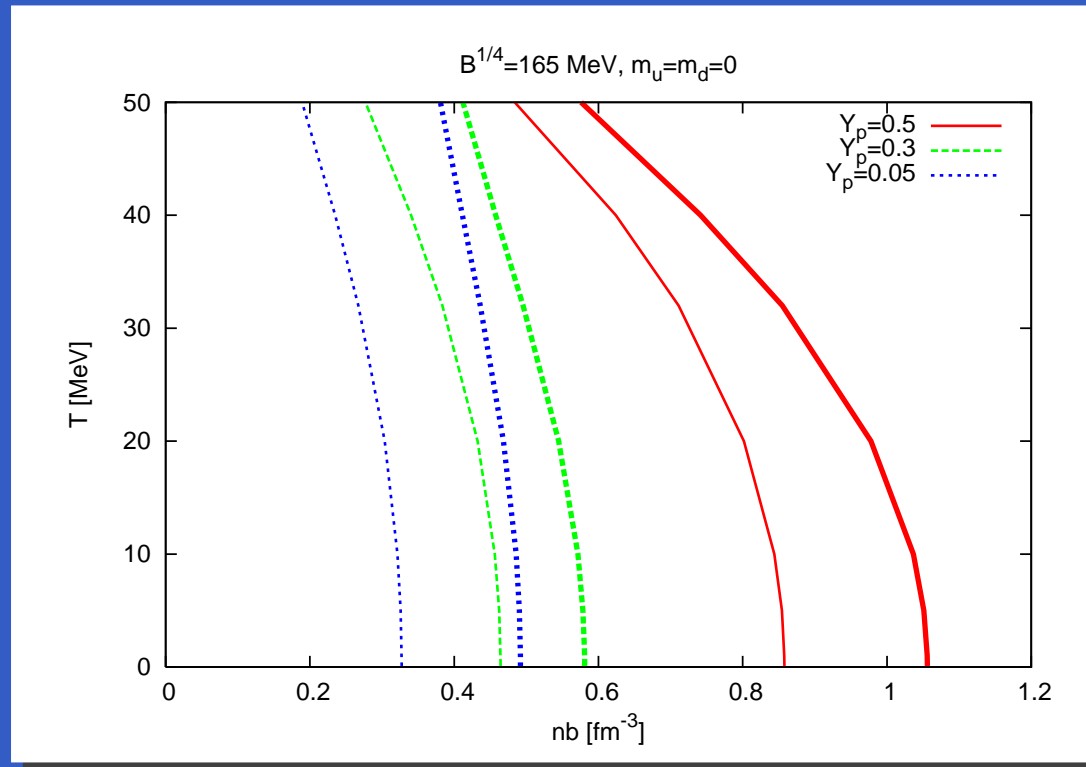
# Check: Mass-Radius Diagram of Cold Neutron Stars



(Irina Sagert and Giuseppe Pagliara)

- presence of quark matter can change drastically the mass-radius diagram
- third family of solution for certain bag constants
- maximum mass:  $1.56 M_{\odot}$  ( $B^{1/4} = 162$  MeV),  $1.5 M_{\odot}$  ( $B^{1/4} = 165$  MeV)

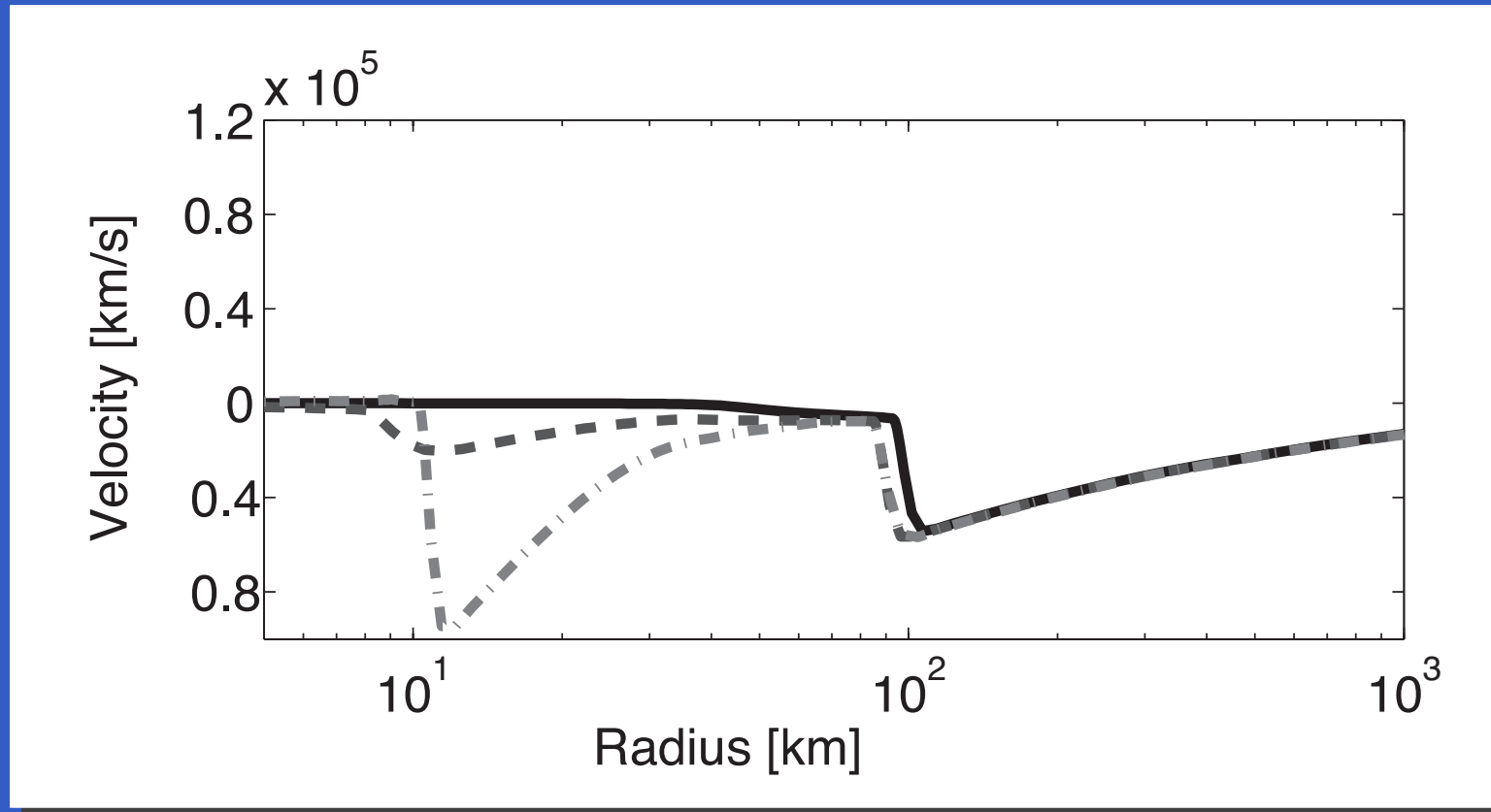
# Check: Phase Transition for Heavy-Ion Collisions



(Irina Sagert and Giuseppe Pagliara)

- no  $\beta$ -equilibrium (just up-/down-quark matter)
- large critical densities in particular for isospin-symmetric matter (proton fraction  $Y_p = 0.5$ )
- production of ud-quark matter unfavoured for HICs at small  $T$  and high density
- no contradiction with heavy-ion data!

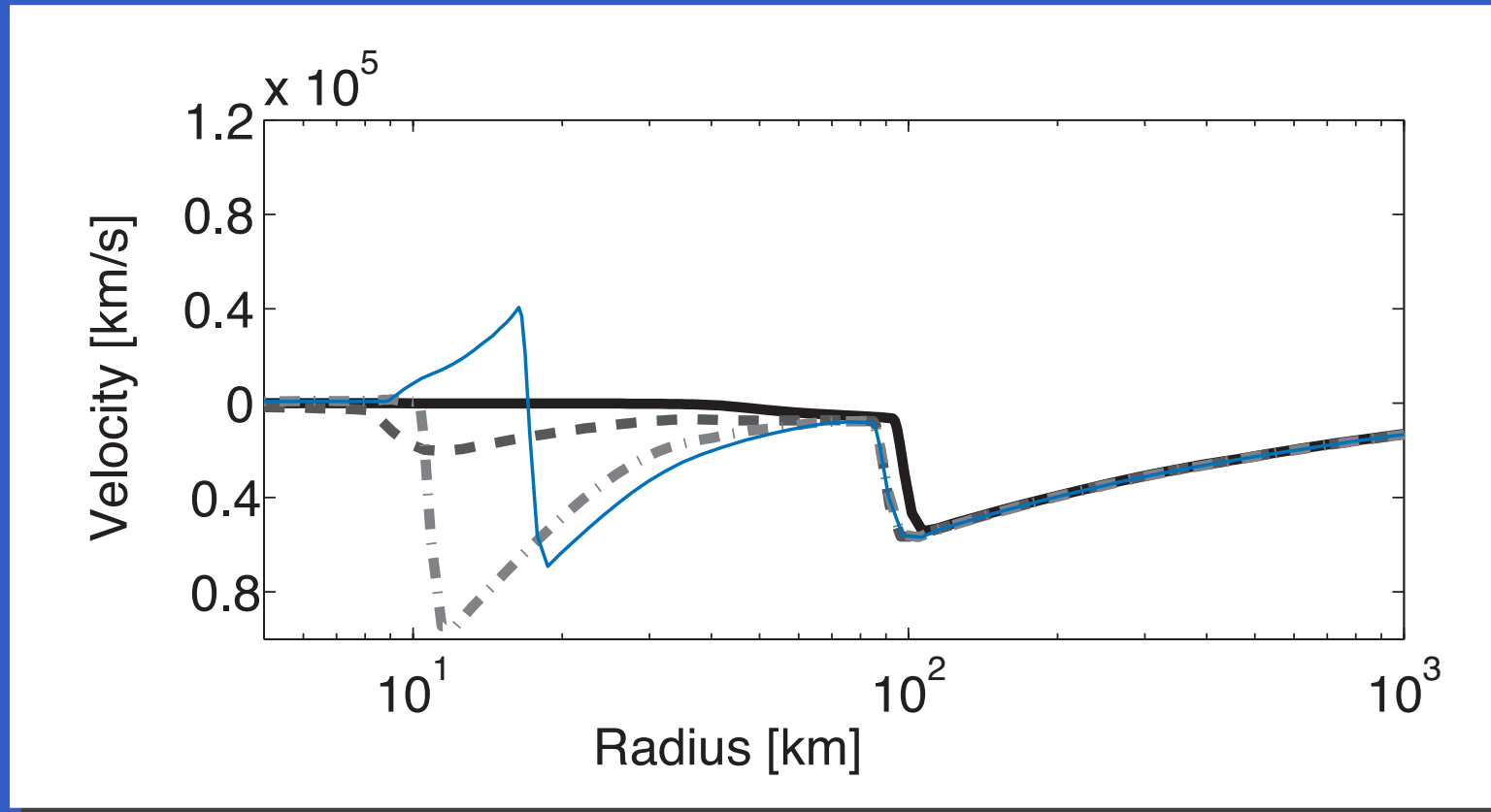
# Implications for Supernovae – Explosion!



(Sagert, Hempel, Pagliara, JSB, Fischer, Mezzacappa, Thielemann, Liebendörfer, 2008)

- velocity profile of a supernova for different times (around 250ms)
- formation of a core of pure quark matter produces a second shock wave

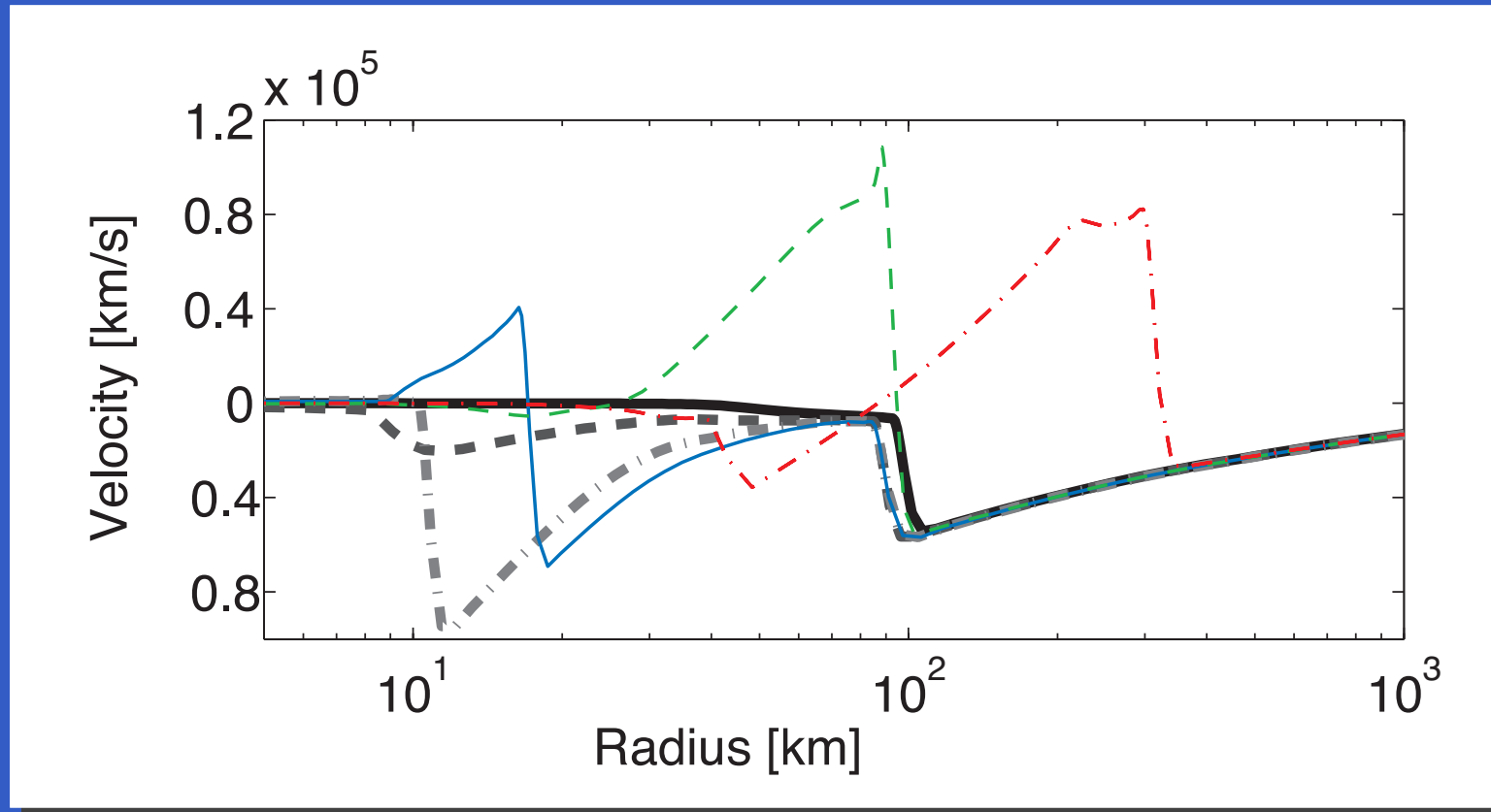
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- velocity profile of a supernova for different times (around 250ms)
- formation of a core of pure quark matter produces a second shock wave
- leads to a successful explosion!

# Successful Supernova Explosion – Parameter dependence

Prog.	B	$t_{pb}$	$M_Q$	$M_{mixed}$	$M_{PN S}$	$E_{expl}$
[M ]	[MeV]	[ms]	[M ]	[M ]	[M ]	[ $10^{51}$ erg]
10	162	255	0.850	0.508	1.440	0.44
<b>10</b>	<b>165</b>	448	1.198	0.161	1.478	<b>1.64</b>
15	162	209	1.146	0.320	1.608	0.42
15	165	330 <sup>a</sup>	1.496	0.116	1.700	unknown <sup>b</sup>

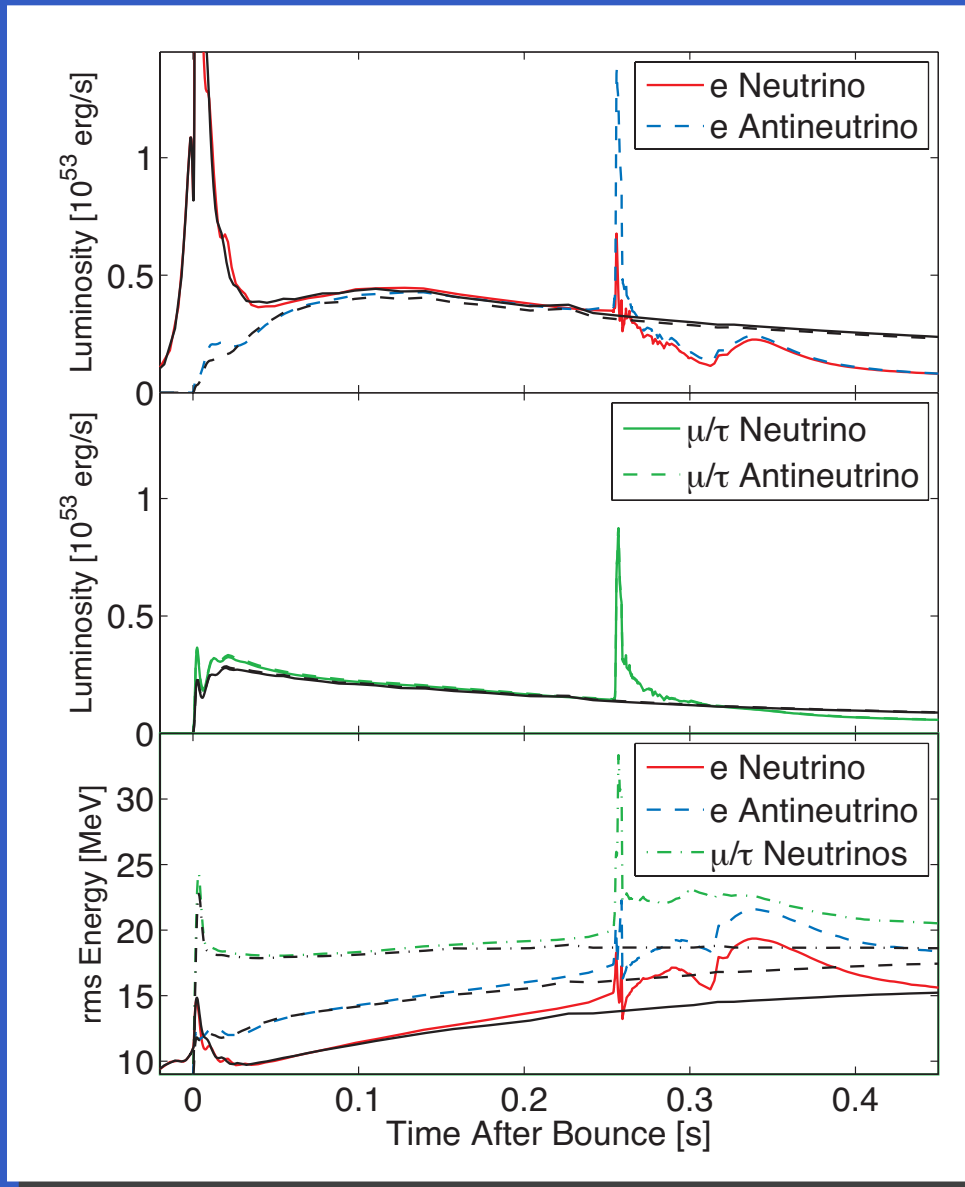
<sup>a</sup> moment of black hole formation

<sup>b</sup> black hole formation before positive explosion energy is achieved

(Sagert, Hempel, Pagliara, JSB, Fischer, Mezzacappa, Thielemann, Liebendörfer, 2008)

- supernova simulation runs for different parameters
- appearance of the quark core at  $t_{pb} = 200$  to 500 ms
- results ( $t_{pb}$ , baryonic mass and explosion energy) are significantly sensitive to the location of the QCD phase transition (bag constant)
- heavier progenitor masses can lead to the formation of a black hole

# Implications for Supernova – Neutrino-Signal!



(Sagert, Hempel, Pagliara, JSB, Fischer, Mezzacappa, Thielemann, Liebendörfer, 2008)

- temporal profile of the emitted neutrinos out of the supernova
- thick lines: without, thin lines: with a phase transition
- pronounced second peak of anti-neutrinos due to the formation of quark matter
- peak location and height determined by the critical density and strength of the QCD phase transition!!

# Thanks to:

my research group in Heidelberg:

- Dr. Giuseppe Pagliara  
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- Dr. Basil Sa'd  
(r-mode instability, gravitational wave emission, csc phases)
- Dipl.-Phys. Till Boeckel  
(QCD phase transition in the early universe)
- Dipl.-Phys. Matthias Hempel  
(low density SN EoS, NSE) (03/09)
- Dipl.-Phys. Irina Sagert  
(EoS from heavy ions, SN EoS, proto-neutron stars)
- Rainer Stiele  
(interacting dark matter in the early universe) (03/09)