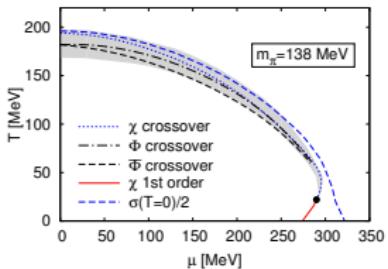


On the Phase Structure and Thermodynamics of QCD

Tina Katharina Herbst

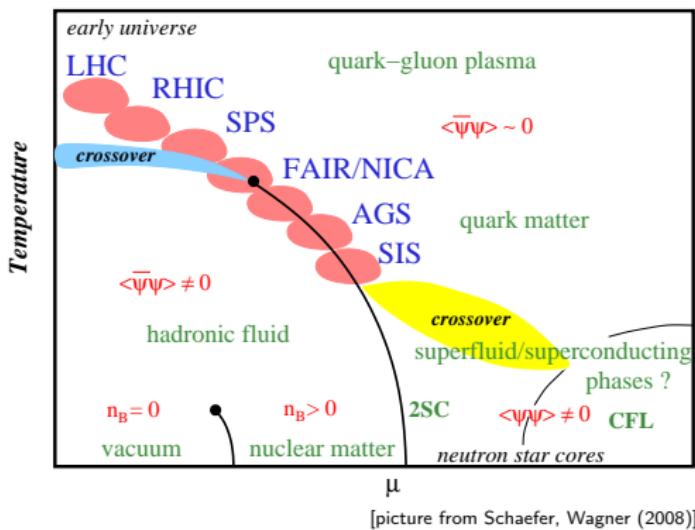
In Collaboration with J. M. Pawłowski and B.-J. Schaefer



*Delta Meeting 2013
Heidelberg, Germany
January 11th - 12th, 2013*



Expected QCD Phase Structure & Open Questions:



- ▶ Chiral and Deconfinement Transitions:
 - ▷ Coincidence at $\mu > 0$?
 - ▷ Quarkyonic Phase ?
- ▶ Critical Endpoint:
 - ▷ Existence ?
 - ▷ Location ?
 - ▷ Properties ?
 - ▷ Additional CEPs ?
- ▶ Additional Phases ?
- ▶ Beyond Mean-Field Approximation: Impact of Fluctuations ?
- ▶ ...



Talk Outline

1 From QCD to Polyakov-Loop Extended Chiral Models

2 Mass Sensitivity of the Phase Structure

3 Thermodynamics

4 Conclusions



From QCD
to
**Polyakov-Loop Extended
Chiral Models**



FRG Flow for 2-Flavour QCD

Including **Fluctuations** by the Functional Renormalisation Group

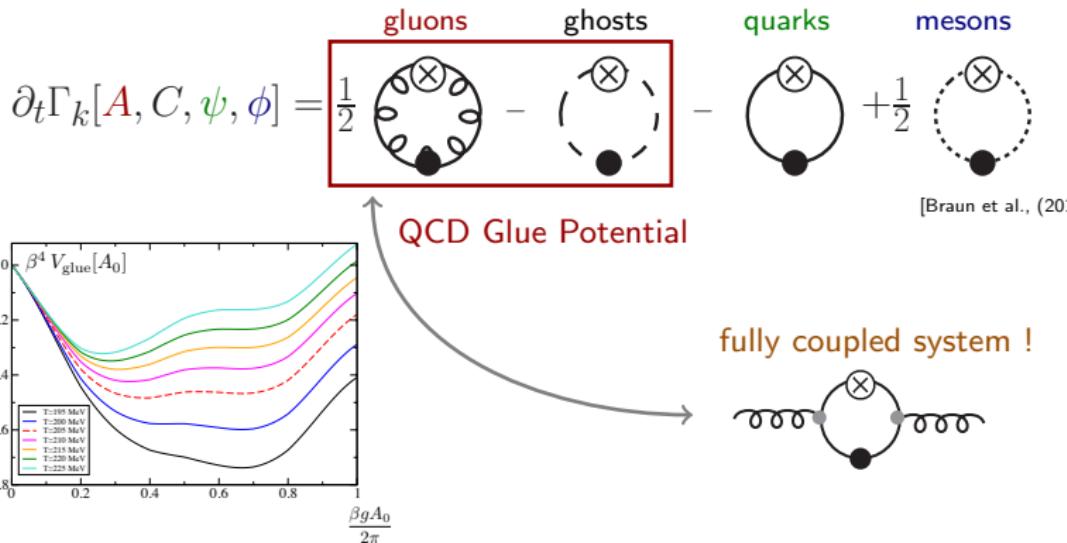
$$\partial_t \Gamma_k[A, C, \psi, \phi] = \frac{1}{2} \text{gluons} - \text{ghosts} - \text{quarks} + \frac{1}{2} \text{mesons}$$

[Braun et al., (2011)]



FRG Flow for 2-Flavour QCD

Including **Fluctuations** by the Functional Renormalisation Group



[Haas, Stiele, Braun, Pawłowski,

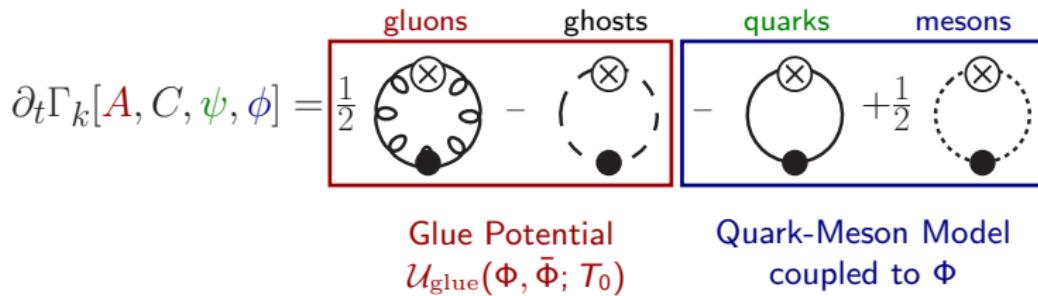
Schaffner-Bielich in prep.]



A Low-Energy Effective Description

Integrate out **gluon** degrees of freedom

[more](#)



Polyakov–Quark–Meson Model

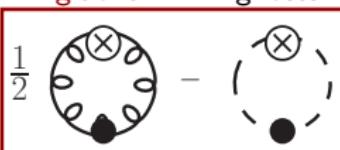
$$\begin{aligned} \mathcal{L}_{\text{PQM}} = & \bar{q} [\not{D}(\Phi) + h(\sigma + i\gamma_5 \vec{\tau} \vec{\pi}) + \mu \gamma_0] q + \frac{1}{2} (\partial_\mu \sigma)^2 + \frac{1}{2} (\partial_\mu \vec{\pi})^2 \\ & + U(\sigma, \vec{\pi}) + \mathcal{U}(\Phi, \bar{\Phi}; T_0) \end{aligned}$$



A Low-Energy Effective Description

Usually: Polyakov-loop potential fitted to Yang-Mills lattice data

[e.g. Ratti, Thaler, Weise (2006)]

$$\partial_t \Gamma_k[A, C] = \frac{1}{2} \left(\text{gluons} - \text{ghosts} \right)$$


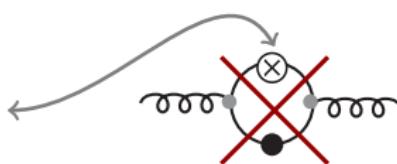
Polyakov-Loop Potential
 $\mathcal{U}_{\text{YM}}(\Phi, \bar{\Phi}; T_0)$



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Polyakov-Loop Potential
 $\mathcal{U}_{\text{YM}}(\Phi, \bar{\Phi}; T_0)$

Include the Matter Backreaction

$$T_0(N_f, T, \mu) = T_\tau e^{-\frac{1}{\alpha_0 b(N_f, T, \mu)}}$$

account for the
Silver-Blaze Property

$$b(N_f, T, \mu) = \frac{11N_c - 2N_f}{6\pi} - b_\mu \frac{\mu^2}{(\hat{\gamma} T_\tau)^2} \Theta_T(\mu - m_q)$$

more

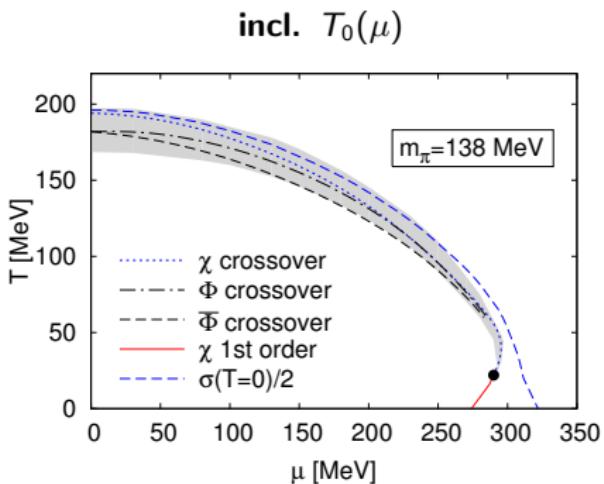
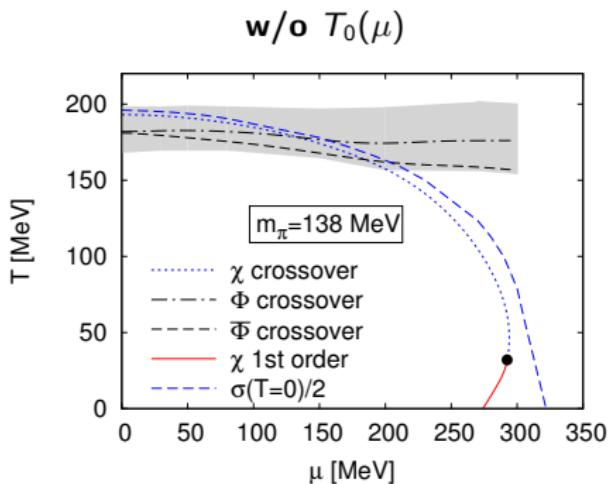


Mass Sensitivity of the Phase Structure



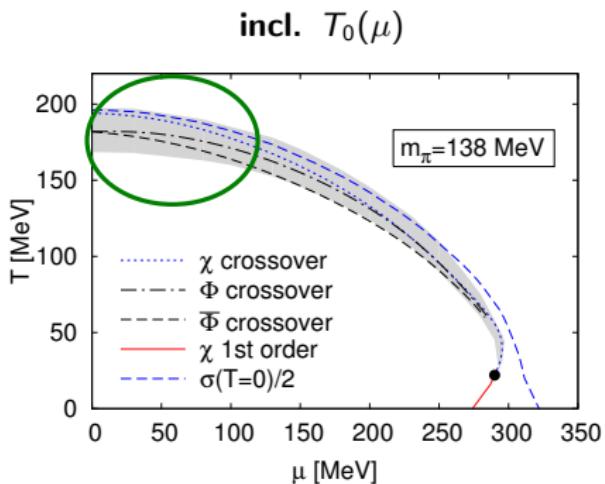
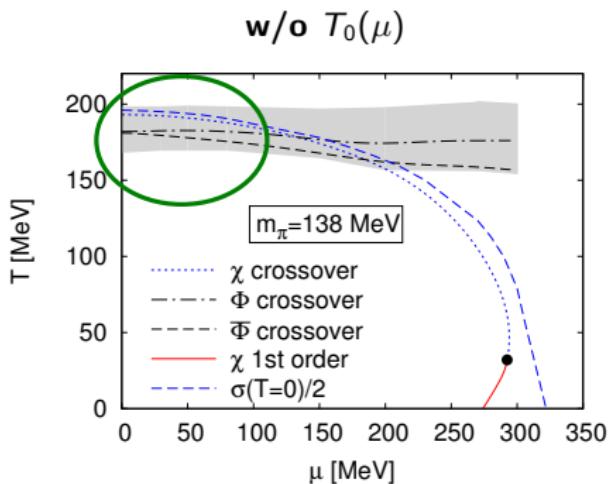
Physical Masses $m_\pi = 138$ MeV

[TKH, Pawlowski, Schaefer, (2010, 2012)]



Physical Masses $m_\pi = 138$ MeV

[TKH, Pawłowski, Schaefer, (2010, 2012)]



Curvature: $\kappa = -0.1434(39)$

- ▷ 2-flavour DSE: $\kappa = -0.23$ (HTL)
 $\kappa = -0.37$ (w/o HTL)
- ▷ (2+1)-flavour lattice: $\kappa = -0.059(2)(4)$

$\kappa = -0.2889(47)$

[Fischer, Luecker, (2012)]

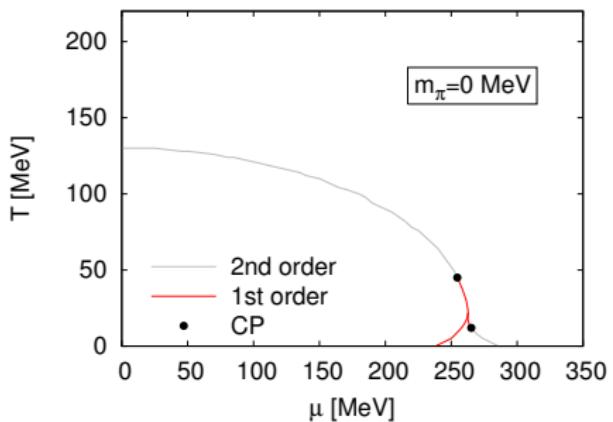
[Kaczmarek et al., (2011)]



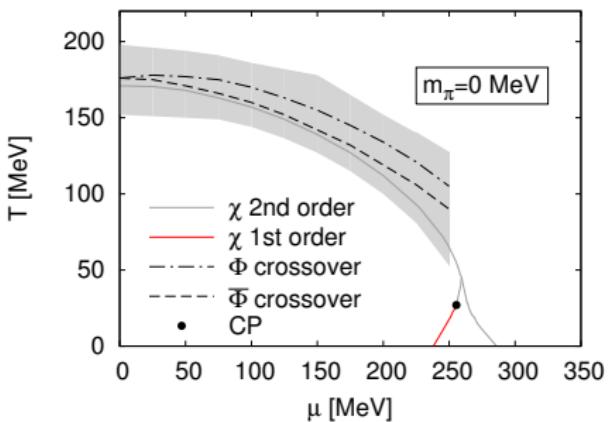
Chiral Limit $m_\pi = 0$ MeV

[TKH, Pawlowski, Schaefer in prep.]

QM

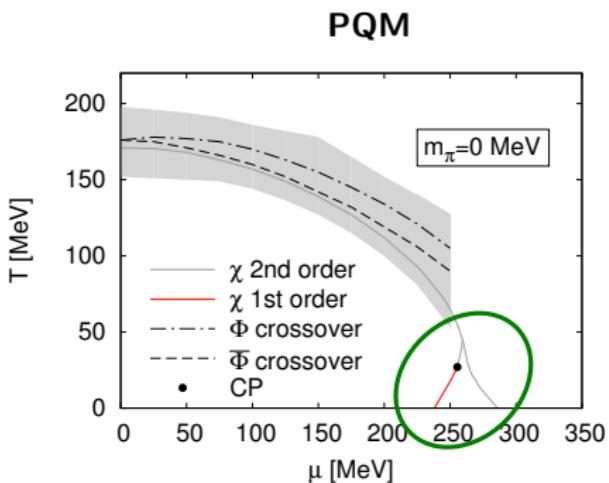
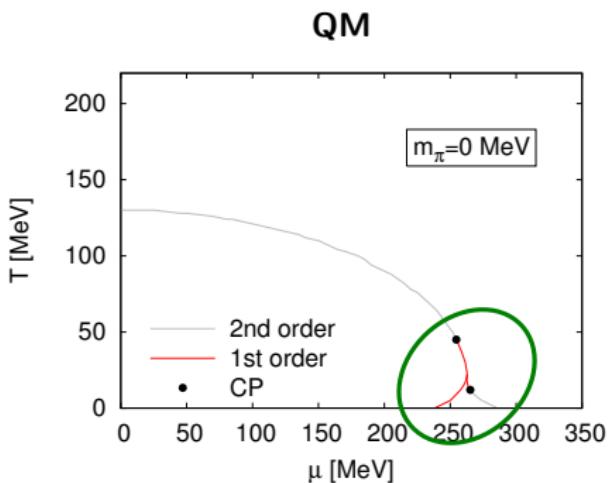


PQM



Chiral Limit $m_\pi = 0$ MeV

[TKH, Pawlowski, Schaefer in prep.]

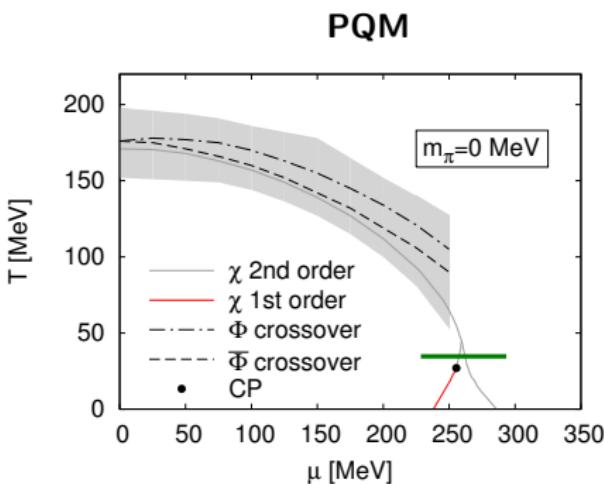
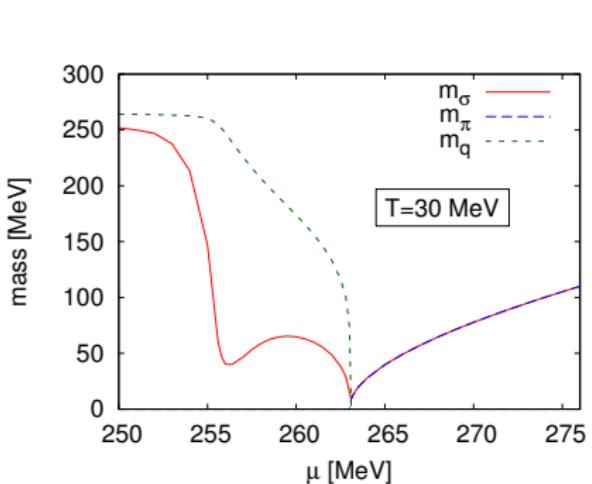


- ▶ 2 CEPs in QM, only 1 in PQM
- ▶ Splitting in the chiral transition line



Chiral Limit $m_\pi = 0$ MeV

[TKH, Pawlowski, Schaefer in prep.]

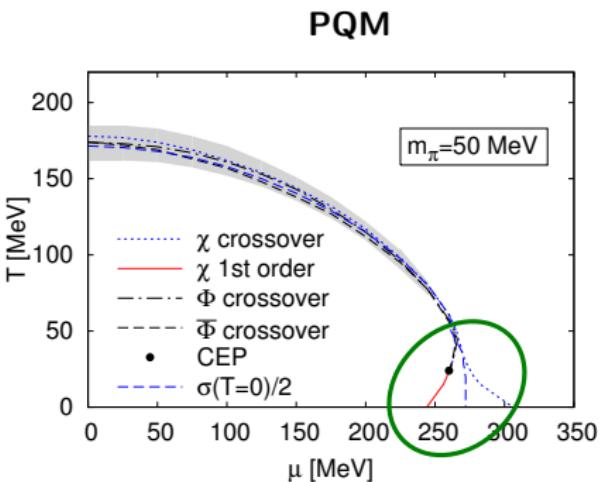
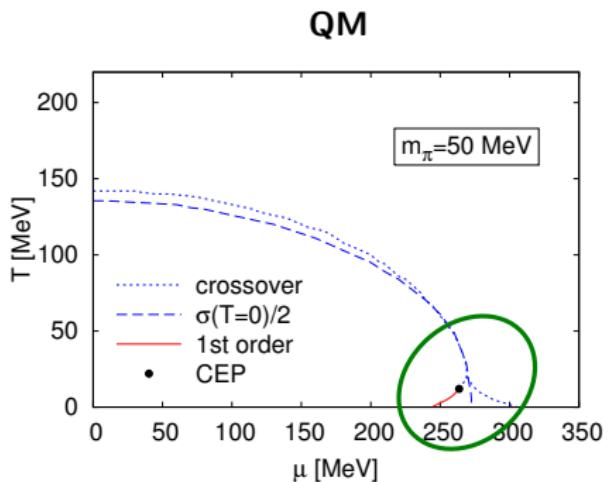


- ▶ 2 CEPs in QM, only 1 in PQM
- ▶ Splitting in the chiral transition line
- ▶ Splitting also seen in sigma-meson mass



Small Masses $m_\pi = 50$ MeV

[TKH, Pawlowski, Schaefer in prep.]



- ▶ Splitting persists
- ▶ only 1 CEP in QM & PQM
- ▶ outer transition branch weakened with increasing m_π

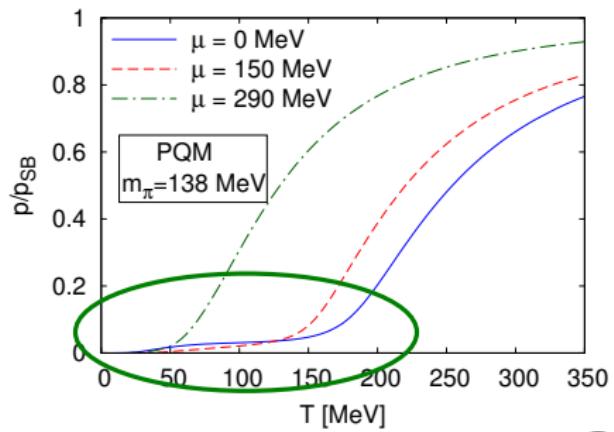
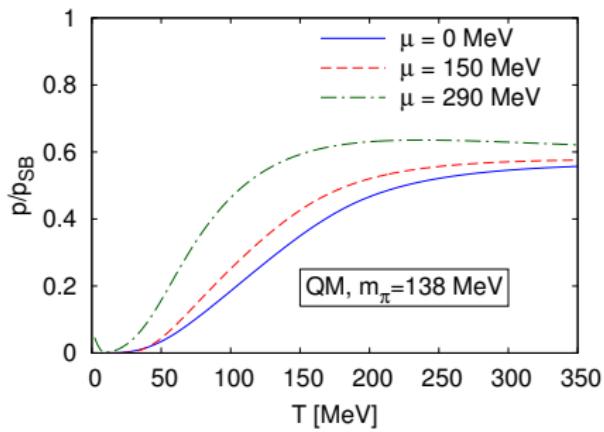
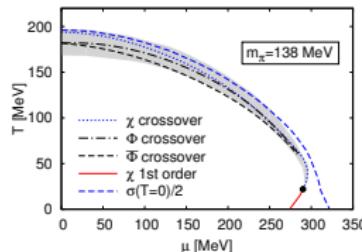
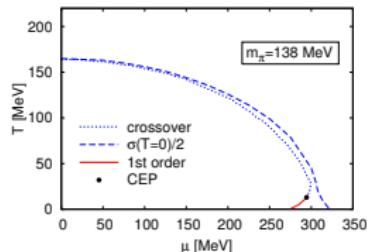


Thermodynamics



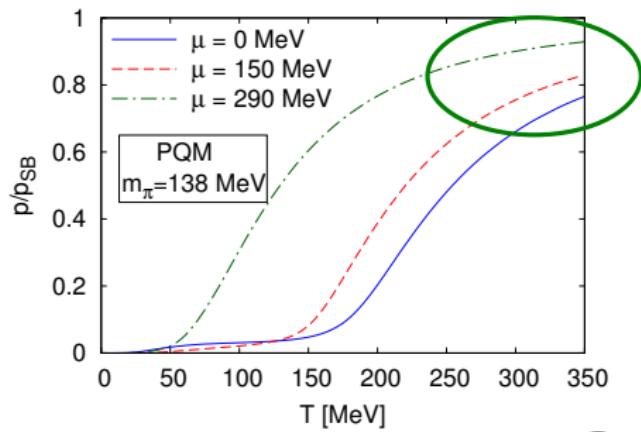
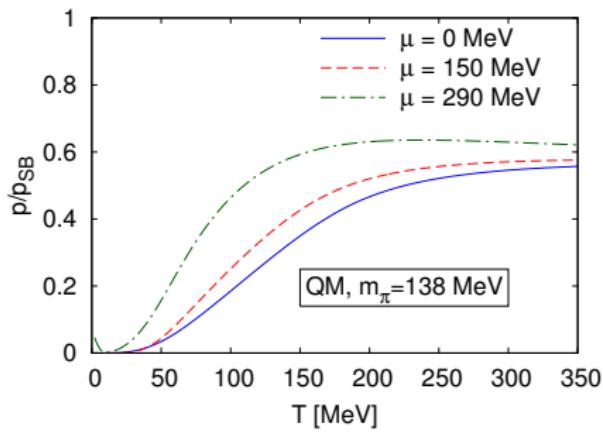
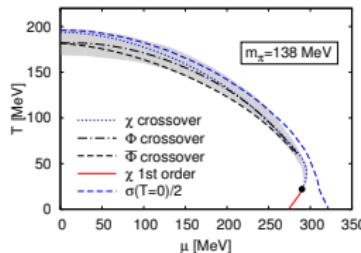
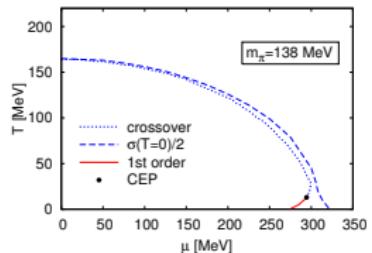
Pressure at the Physical Mass Point

[TKH, Pawlowski, Schaefer in prep.]



Pressure at the Physical Mass Point

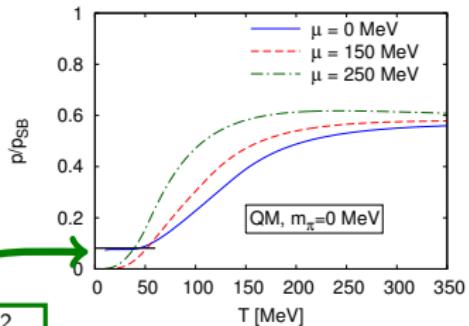
[TKH, Pawlowski, Schaefer in prep.]



Pressure at Smaller Masses

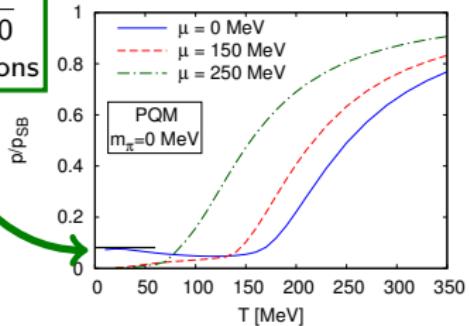
[TKH, Pawlowski, Schaefer in prep.]

$m_\pi = 0 \text{ MeV}$

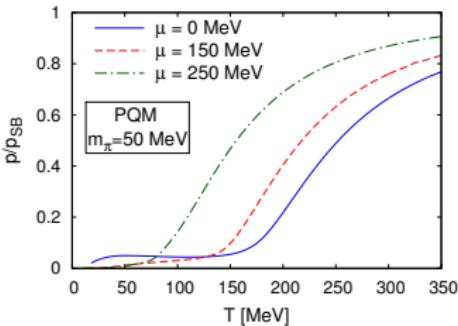
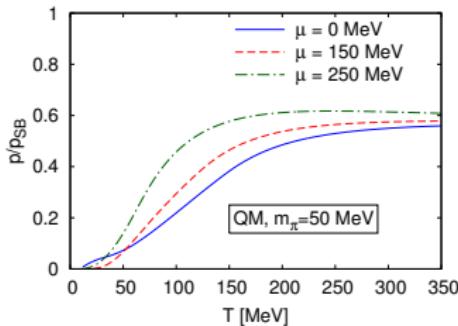


$$\frac{p}{T^4} = 3 \frac{\pi^2}{90}$$

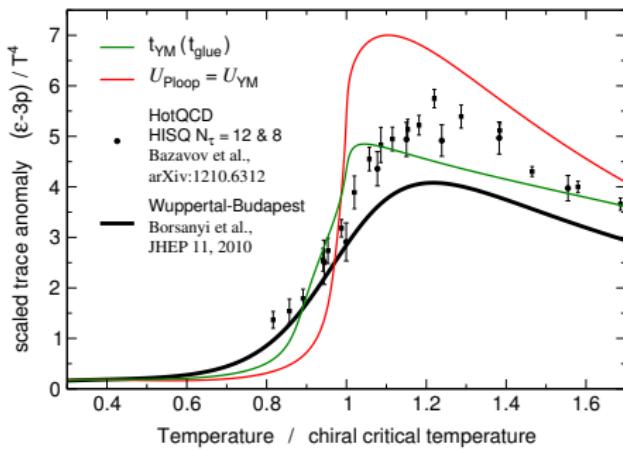
massless pions



$m_\pi = 50 \text{ MeV}$



Interaction Measure at $\mu = 0$

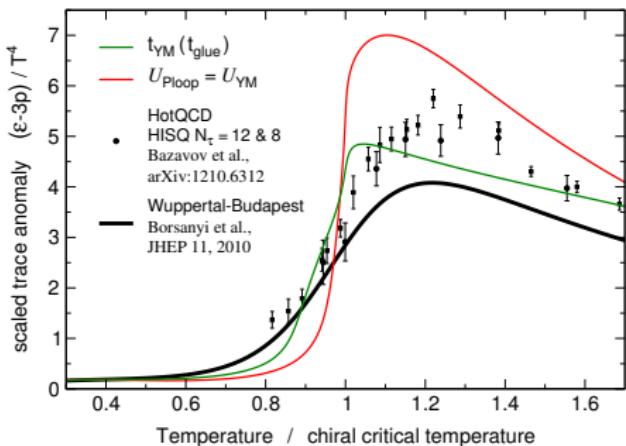


solid coloured lines:
 $(2+1)$ -flavour PQM in MFA
 [Haas, Stiele, Braun, Pawłowski, Schaffner-Bielich in prep.]

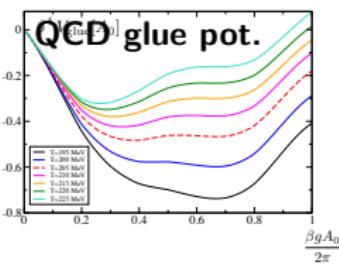
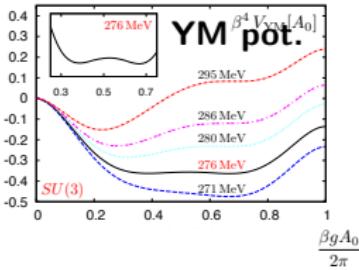
red: standard Polyakov-loop potential U_{YM}
green: augmented Polyakov-loop potential using QCD input:



Interaction Measure at $\mu = 0$



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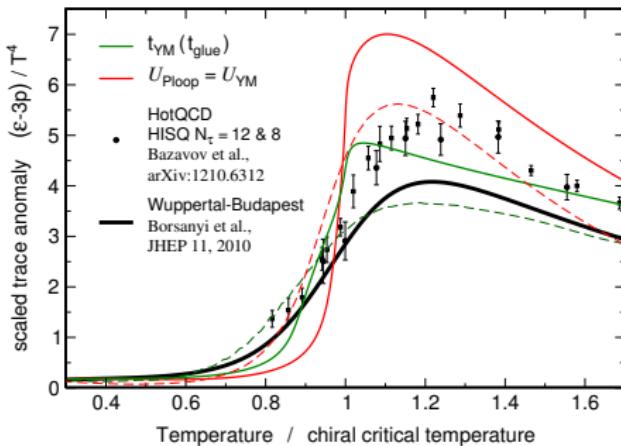
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$$\mathcal{U}_{glue}(T) = \mathcal{U}_{YM}(T_{YM}(T))$$



Interaction Measure at $\mu = 0$

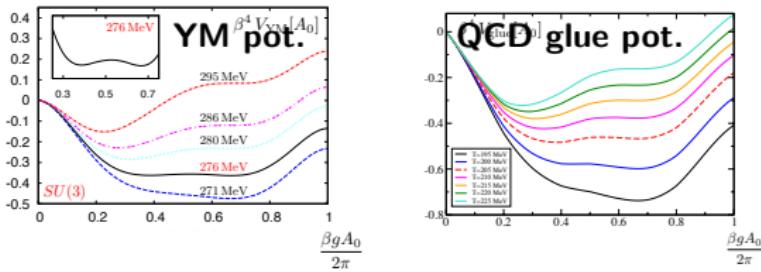


solid coloured lines:
(2+1)-flavour PQM in MFA
[Haas, Stiele, Braun, Pawłowski, Schaffner-Bielich in prep.]

dashed lines: 2-flavour PQM with FRG [(2+1)-flavour: work in progress]
[TKH, Stiele, Pawłowski, Schaefer in prep.]

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$$\mathcal{U}_{glue}(T) = \mathcal{U}_{YM}(T_{YM}(T))$$



Summary & Outlook

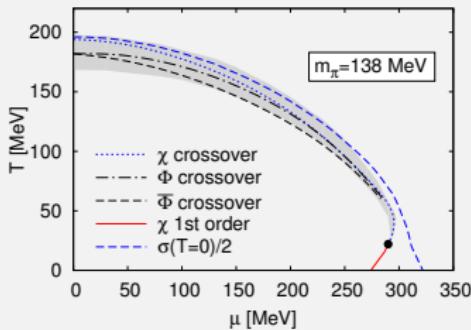
QCD Phase Structure and TD via 2-flavour PQM truncation

- ▶ Important Feature: Matter Backreaction to Gluonic Sector

$$T_0 \rightarrow T_0(N_f, T, \mu)$$

- ▶ Modifications of the Phase Structure

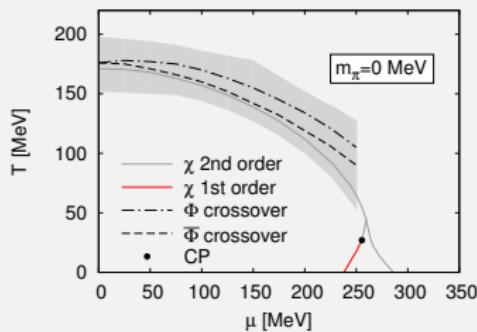
- ▷ **fluctuations** push CEP downwards
- ▷ no CEP for $\mu/T < 1$
- ▷ $T_0(\mu)$: chiral and deconfinement transitions coincide
- ▷ \sim **quarkyonic** phase shrinks



Summary & Outlook

QCD Phase Structure and TD via 2-flavour PQM truncation

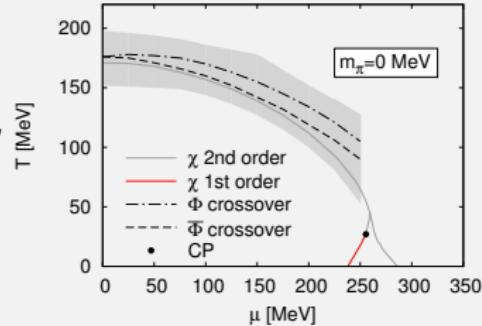
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Summary & Outlook

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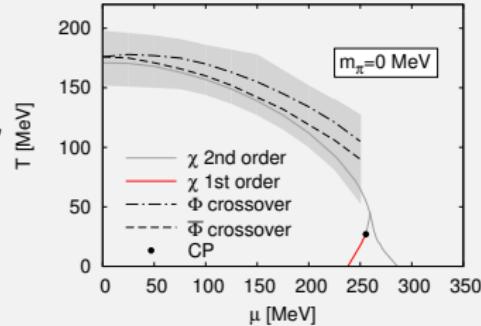
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Summary & Outlook

QCD Phase Structure and TD via 2-flavour PQM truncation

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 - ▷ splitting in chiral transition at small T weakened for physical m_π
- ▶ QCD input to Polyakov-loop potential
 - ▷ good agreement with lattice results for, e.g., the interaction measure
- ▶ high μ /low T region
 - ▷ baryons not included here
- ▶ Next step: (2+1)-flavours beyond MFA



Backup I: The Polyakov–Quark-Meson Model

Polyakov–Quark-Meson Truncation

$$\Gamma_k = \int d^4x \left\{ \bar{q} (\not{D} + \mu \gamma_0 + ih(\sigma + i\gamma_5 \vec{\pi} \cdot \vec{\pi})) q + \frac{1}{2} (\partial_\mu \phi)^2 + \Omega_k[\sigma, \vec{\pi}, \Phi, \bar{\Phi}] \right\}$$

at initial scale Λ : $\Omega_\Lambda[\sigma, \vec{\pi}, \Phi, \bar{\Phi}] = \mathcal{U}(\Phi, \bar{\Phi}) + U(\sigma, \vec{\pi}) + \Omega_\Lambda^\infty[\sigma, \vec{\pi}, \Phi, \bar{\Phi}]$

$\phi = (\sigma, \vec{\pi}) \dots$ meson field ($N_f = 2$)

$g \dots$ gauge coupling

$\not{D}(\Phi) = \gamma_\mu \partial_\mu - ig\gamma_0 A_0(\Phi)$

$h \dots$ Yukawa coupling

► Polynomial Polyakov-Loop Potential

$$\frac{\mathcal{U}(\Phi, \bar{\Phi}; T_0)}{T^4} = -\frac{b_2(T; T_0)}{2} \Phi \bar{\Phi} - \frac{b_3}{6} (\Phi^3 + \bar{\Phi}^3) + \frac{b_4}{4} (\Phi \bar{\Phi})^2$$

► Ω_Λ^∞ : T & μ dependent initial condition

◀ back



Backup II: $T_0(N_f, T, \mu)$

[Schaefer, Pawłowski, Wambach (2007)]

- ▶ $T_0 \longleftrightarrow \Lambda_{QCD}$

[TKH, Pawłowski, Schaefer (2011)]

- ▶ perturbative 1-loop estimate:

$$\beta(\alpha) = -b(N_f) \alpha^2 + \mathcal{O}(\alpha^3)$$

- ▶ $\mu \neq 0$: HDL/HTL

$$b(N_f) \rightarrow b(N_f, \mu)$$

- ▷ at $T=0$: Silver-Blaze Property

$$\Gamma(T=0, \mu) \sim \Theta(\mu - m_q)$$

- ▷ at $T > 0$: $\Theta(\mu - m_q) \rightarrow \Theta_T(\mu - m_q)$

- ▷ $b(N_f, \mu) \rightarrow b(N_f, T, \mu)$

$$T_0(N_f, T, \mu) = T_\tau e^{-1/(\alpha_0 b(N_f, T, \mu))}$$

◀ back

