Particle spectra in Models of New Physics

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NAWI Graz

Natural Sciences



Der Wissenschaftsfonds

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- Ws W^a_{μ} W
- Higgs h_i (h)
- No QED: Ws and Zs are degenerate
- Couplings g, v, λ and some numbers f^{abc} and t_a^{ij}

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- Global SU(2) Higgs custodial (flavor) symmetry
 - Acts as right-transformation on the Higgs field only $W^a_\mu \rightarrow W^a_\mu \rightarrow W^a_\mu$ $h_i \rightarrow h_i + a^{ij} h_j + b^{ij} h_j^*$

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- Mass spectrum?
- Why does perturbation theory work?

[Fröhlich et al. PLB 80 Maas'12, Maas & Mufti'13]

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 - Fröhlich-Morchio-Strocchi (FMS) mechanism
 - Perturbative tool to calculate bound state masses
- Deeply-bound relativistic state
 - Mass defect~constituent mass
 - Cannot be described with quantum mechanics

[Fröhlich et al. PLB 80 Maas'12, Maas & Mufti'13]

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- Also confirmed in lattice calculations

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- Photons
 - QED similar but simpler

[Maas'12]



Collision of bound states



Collision of bound states - 'constituent' particles



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- 750 GeV: excitation of the 0⁺ state? perhaps pure SM!



• Description of impact?



[Maas'12

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Maas'12

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- Fragmentation 100% efficient like for quarks

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 - Observed in experiment
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Effective mass



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- Positivity violation for QCD-like region at long times
- FMS mechanism works well throughout Higgs region
 - For scalar difficult if unstable

[Maas, Mufti'13]



FMS mechanism does not work everywhere



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- Contradiction to perturbation theory for some range?
 - No light Higgs, BEH effect suppressed at weak coupling

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[Maas,'15, Maas & Pedro'16]

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- All other states expand to scattering states
- Validity: Requires non-perturbative check
- Discrete factor groups could yield doubling

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- Enlarged custodial group
- BEH Effect FMS mechanism applicable
 - In a suitable basis, all condensates contained in a single doublet
 - Yields again perturbative spectrum

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- Size of fluctuations needs to be checked non-perturbatively!

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 - ... or something else?

Test for GUTs

[Maas, '15, Toerek & Maas '15 Maas & Toerek, unpublished]



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- No hint of massless physical state (yet?)
 - Check of FMS prediction requires more statistics

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 - Vectors must be lighter
 - Behavior not yet seen for strong interactions
 - Usually: Scalars and pseudoscalars

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- Can be used to test theories
 - Check for low-mass states
- Theories without BEH effect challenging

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