

Big bang or freeze ?



## *NATURE* | NEWS

Cosmologist claims Universe may not be expanding  
**Particles' changing masses could explain why  
distant galaxies appear to be rushing away.**

**Jon Cartwright**      16 July 2013



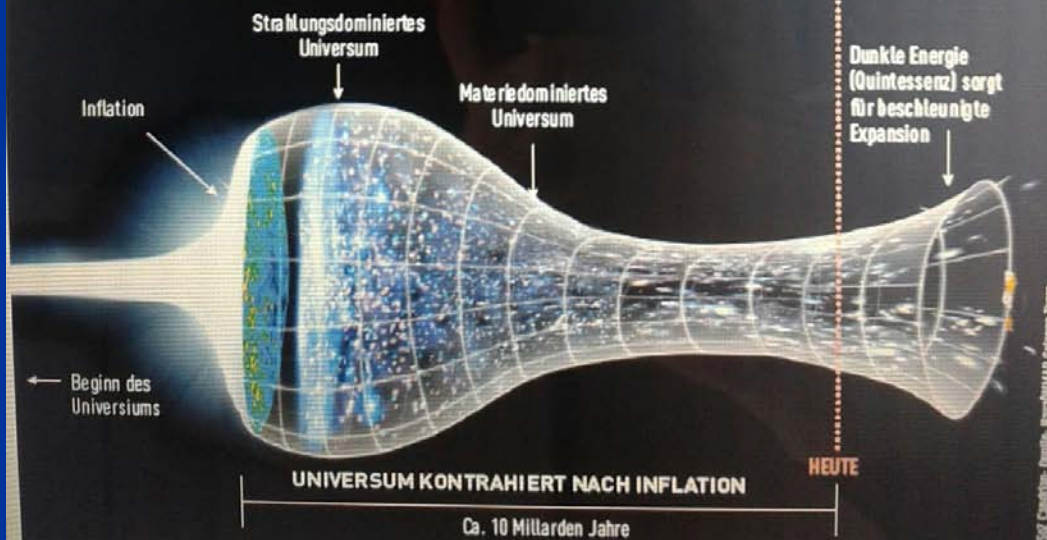
German physicist stops  
Universe

25.07.2013

## Klassisches Bild der Kosmologie



## Model von Wetterich



Sonntagszeitung  
Zürich  
Laukenmann

**The Universe is shrinking**

The Universe is shrinking ...

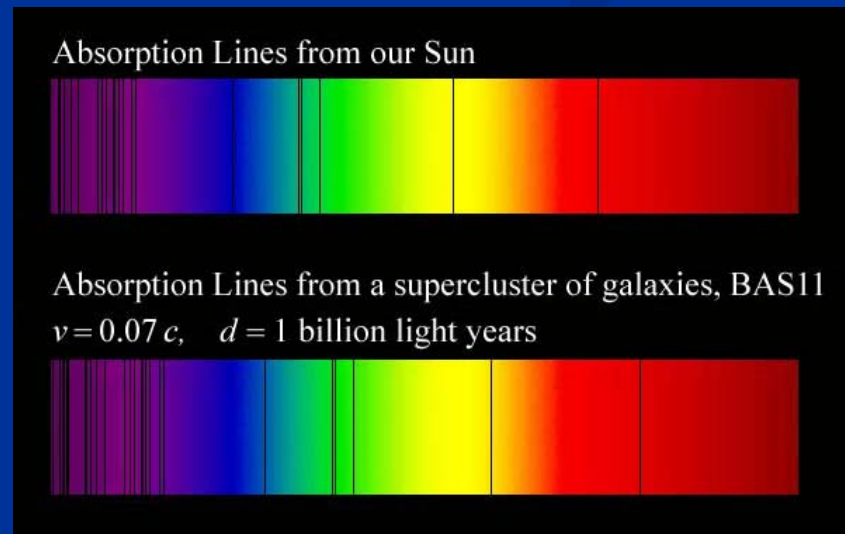
while Planck mass and particle  
masses are increasing



# Redshift

instead of redshift due to expansion :

smaller frequencies have been emitted in the past, because electron mass was smaller !



# What is increasing ?

Ratio of distance between galaxies  
over size of atoms !

atom size constant : expanding geometry

alternative : shrinking size of atoms

general idea not new : Hoyle, Narlikar,...

# Different pictures of cosmology

- same physical content can be described by different pictures
- related by field – redefinitions ,  
e.g. Weyl scaling , conformal scaling of metric
- which picture is usefull ?



# Cosmological scalar field ( cosmon )

- scalar field is crucial ingredient
- particle masses proportional to scalar field – similar to Higgs field
- particle masses increase because value of scalar field increases
- scalar field plays important role in cosmology
- cosmon : pseudo Goldstone boson of spontaneously broken scale symmetry

# Cosmon inflation

Unified picture of inflation and  
dynamical dark energy

Cosmon and inflaton are the same  
scalar field

# Quintessence

Dynamical dark energy ,  
generated by scalar field (cosmon )

C.Wetterich,Nucl.Phys.B302(1988)668, 24.9.87

P.J.E.Peebles,B.Ratra,ApJ.Lett.325(1988)L17, 20.10.87

**Prediction :**

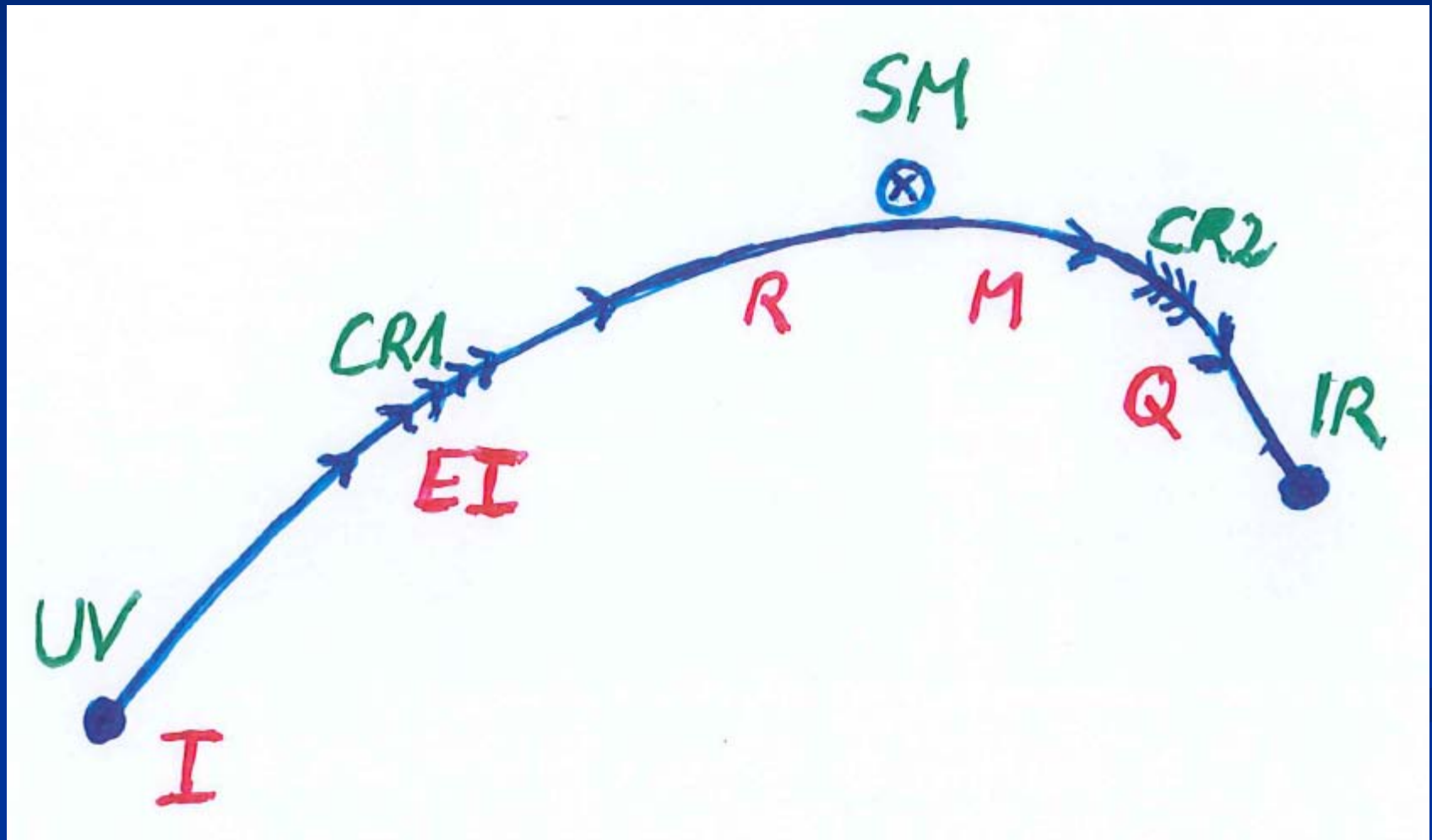
**homogeneous dark energy  
influences recent cosmology**

**- of same order as dark matter -**

Original models do not fit the present observations  
.... modifications  
( different growth of neutrino mass )

scalar field may be  
important feature of  
quantum gravity

# Crossover in quantum gravity





# Approximate scale symmetry near fixed points

- UV : approximate scale invariance of primordial fluctuation spectrum from inflation
- IR : almost massless pseudo-Goldstone boson (cosmon) responsible for dynamical Dark Energy

# Variable Gravity

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

scale invariant for  $\mu = 0$  and  $B$  const.

quantum effects : flow equation for kineticial

$$\mu \frac{\partial B}{\partial \mu} = \frac{\kappa \sigma B^2}{\sigma + \kappa B}$$

# Variable Gravity

- Scalar field coupled to gravity
- Effective Planck mass depends on scalar field
- Simple quadratic scalar potential involves intrinsic mass  $\mu$
- Nucleon and electron mass proportional to dynamical Planck mass
- Neutrino mass has different dependence on scalar field

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

# No tiny dimensionless parameters ( except gauge hierarchy )

- one mass scale  $\mu = 2 \cdot 10^{-33} \text{ eV}$

- one time scale  $\mu^{-1} = 10^{10} \text{ yr}$

- Planck mass does not appear

- Planck mass grows large dynamically

# Infrared fixed point

■  $\mu \rightarrow 0$

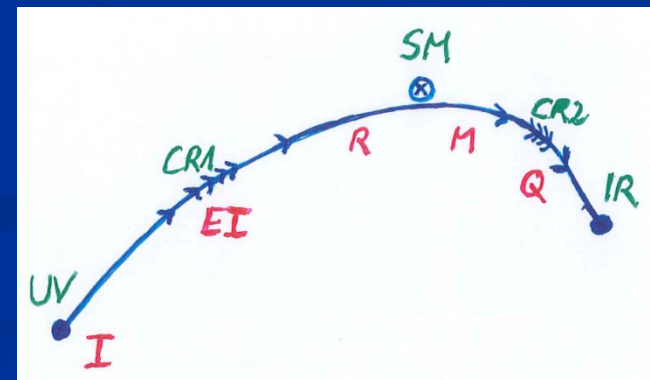
■  $B \rightarrow 0$

$$\mu \partial_\mu B = \kappa B^2 \quad \text{for} \quad B \rightarrow 0$$

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

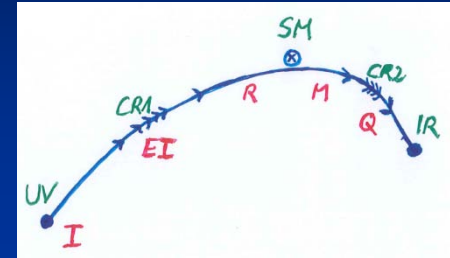
■ no intrinsic mass scale

■ scale symmetry



# Ultraviolet fixed point

■  $\mu \rightarrow \infty$



■ kinetic diverges

$$B = b \left( \frac{\mu}{\chi} \right)^{\sigma} = \left( \frac{m}{\chi} \right)^{\sigma}$$

■ scale symmetry with anomalous dimension  $\sigma$

$$g_{\mu\nu} \rightarrow \alpha^2 g_{\mu\nu} , \quad \chi \rightarrow \alpha^{-\frac{2}{2-\sigma}} \chi$$



# Renormalized field at UV fixed point

$$\chi_R = b^{\frac{1}{2}} \left(1 - \frac{\sigma}{2}\right)^{-1} \mu^{\frac{\sigma}{2}} \chi^{1-\frac{\sigma}{2}}$$

$$1 < \sigma < 2$$

$$\Gamma_{UV} = \int_x \sqrt{g} \left\{ \frac{1}{2} \partial^\mu \chi_R \partial_\mu \chi_R - \frac{1}{2} C R^2 + D R^{\mu\nu} R_{\mu\nu} \right\}$$

no mass  
scale

$$\Delta\Gamma_{UV} = \int_x \sqrt{g} E \left( \mu^2 - \frac{R}{2} \right) \mu^{-\frac{2\sigma}{2-\sigma}} \chi_R^{\frac{4}{2-\sigma}},$$

deviation from  
fixed point  
vanishes for

$$E = b^{-\frac{2}{2-\sigma}} \left(1 - \frac{\sigma}{2}\right)^{\frac{4}{2-\sigma}}$$

$$\mu \rightarrow \infty$$

# Asymptotic safety

if UV fixed point exists :

*quantum gravity is  
non-perturbatively renormalizable !*

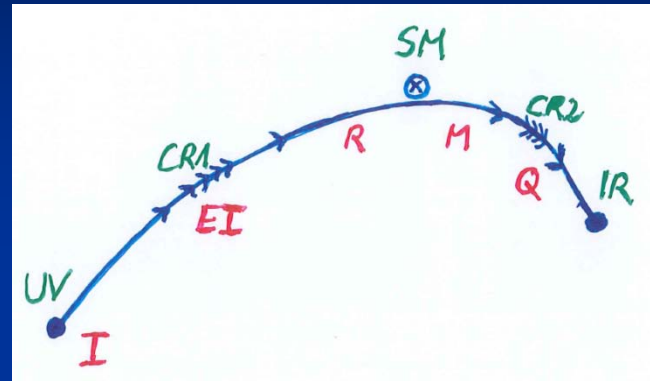
S. Weinberg , M. Reuter

# Quantum scale symmetry

- quantum fluctuations violate scale symmetry
- running dimensionless couplings
- at fixed points , scale symmetry is exact !

# Crossover between two fixed points

$$\mu \frac{\partial B}{\partial \mu} = \frac{\kappa \sigma B^2}{\sigma + \kappa B}$$



$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[ \ln \left( \frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left( \frac{\chi}{m} \right)$$

m : scale of crossover

can be exponentially larger than intrinsic scale  $\mu$

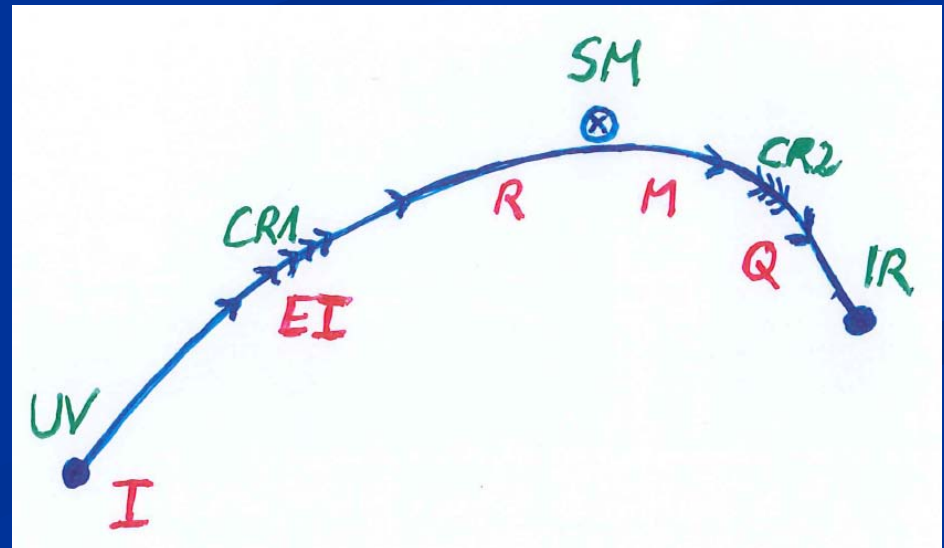
# Origin of mass

- UV fixed point : scale symmetry unbroken  
all particles are massless
- IR fixed point : scale symmetry spontaneously broken,  
massive particles , massless dilaton
- crossover : explicit mass scale  $\mu$  or  $m$  important
- SM fixed point : approximate scale symmetry spontaneously broken, massive particles , almost massless cosmon, tiny cosmon potential

# Cosmological solution : crossover from UV to IR fixed point

- Dimensionless functions as  $B$   
depend only on ratio  $\mu/\chi$ .
- IR:  $\mu \rightarrow 0$  ,  $\chi \rightarrow \infty$
- UV:  $\mu \rightarrow \infty$  ,  $\chi \rightarrow 0$

Cosmology makes  
crossover between  
fixed points by  
variation of  $\chi$ .





# Simplicity

simple description of **all** cosmological epochs

natural incorporation of Dark Energy :

- inflation
- Early Dark Energy
- present Dark Energy dominated epoch

# Model is compatible with present observations

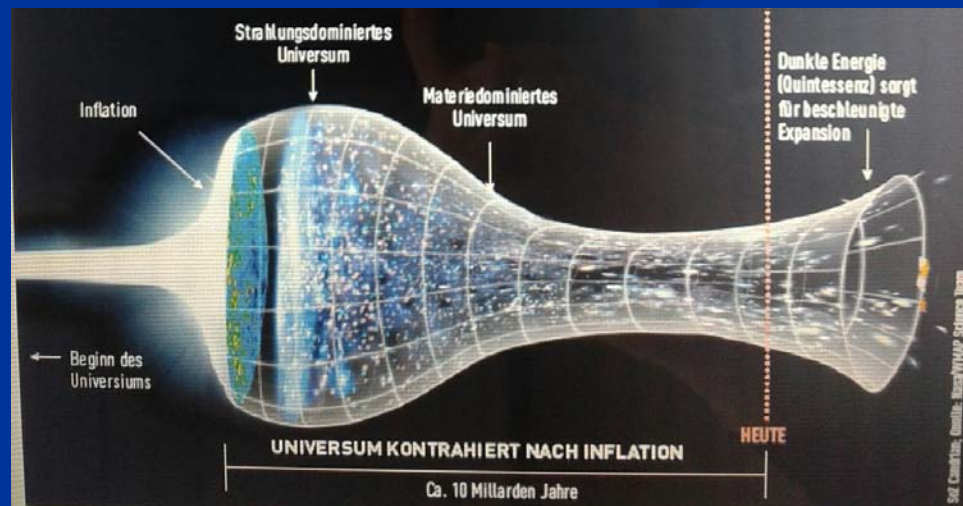
Together with variation of neutrino mass over  
electron mass during second stage of crossover :  
model is compatible with all present observations

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[ \ln \left( \frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left( \frac{\chi}{m} \right)$$

# Expansion

- Inflation : Universe expands
- Radiation : Universe shrinks
- Matter : Universe shrinks
- Dark Energy : Universe expands



# Hot plasma ?

- Temperature in radiation dominated Universe :  
 $T \sim \chi^{1/2}$  **smaller** than today
- Ratio temperature / particle mass :  
 $T / m_p \sim \chi^{-1/2}$  **larger** than today
- $T/m_p$  counts ! This ratio decreases with time.
- Nucleosynthesis , CMB emission as in standard cosmology !

# Infinite past : slow inflation

$\sigma = 2$  : field equations

$$\ddot{\chi} + \left( 3H + \frac{1}{2} \frac{\dot{\chi}}{\chi} \right) \dot{\chi} = \frac{2\mu^2 \chi^2}{m}$$

$$H = \sqrt{\frac{\mu^2}{3} + \frac{m\dot{\chi}^2}{6\chi^3}} - \frac{\dot{\chi}}{\chi}$$

solution

$$H = \frac{\mu}{\sqrt{3}}, \quad \chi = \frac{3^{\frac{1}{4}} m}{2\sqrt{\mu}} (t_c - t)^{-\frac{1}{2}}$$

# Eternal Universe

- solution valid back to the infinite past in physical time



# Slow Universe

$$H = \frac{\mu}{\sqrt{3}}, \quad \chi = \frac{3^{\frac{1}{4}} m}{2\sqrt{\mu}} (t_c - t)^{-\frac{1}{2}}$$

$$\mu = 2 \cdot 10^{-33} \text{ eV}$$

Expansion or shrinking always slow ,  
characteristic time scale of the order of the age of the  
Universe :  $t_{\text{ch}} \sim \mu^{-1} \sim 10 \text{ billion years} !$   
Hubble parameter of the order of **present** Hubble  
parameter for all times , including inflation and big bang !  
Slow increase of particle masses !

# Spectrum of primordial density fluctuations

tensor  
amplitude

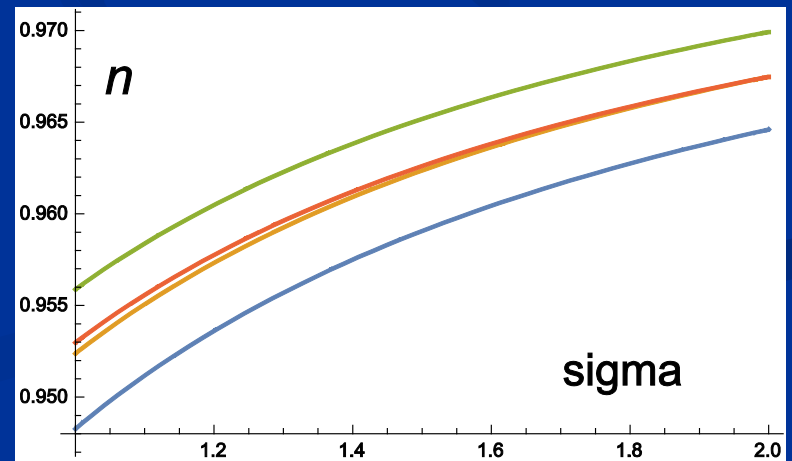
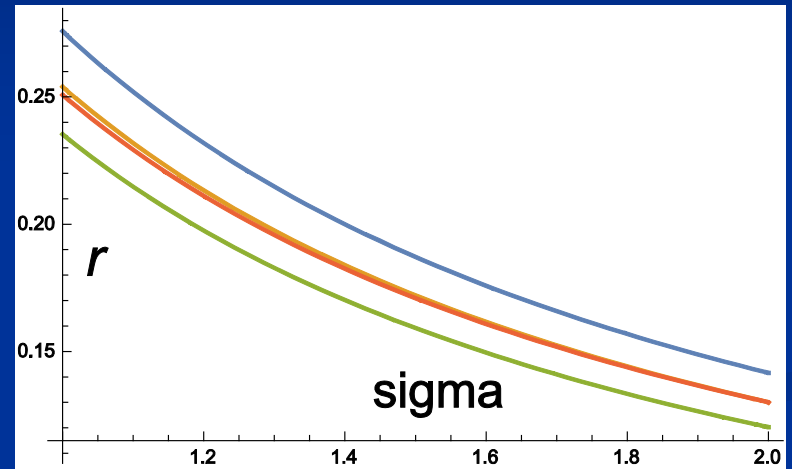
$$r = \frac{32}{B(N)}$$

rather large !

spectral  
index

$$1 - n = \frac{r}{8} \left( 1 + \frac{1}{2} \sigma(N) \right)$$

$$\sigma = - \frac{\partial \ln B}{\partial \ln \chi} \Big|_{B=2\sigma N+6}$$



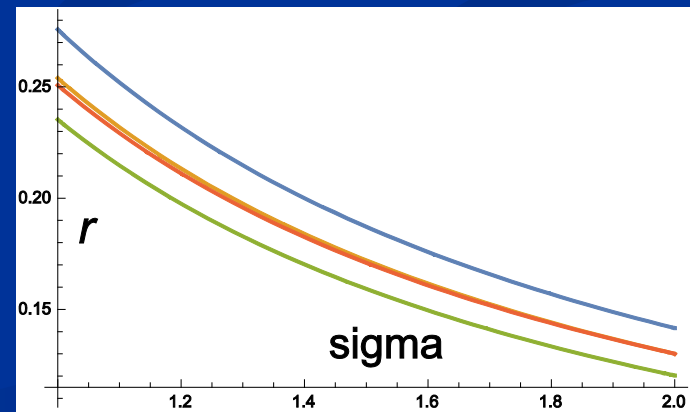
# Anomalous dimension determines spectrum of primordial fluctuations

$$r = \frac{0.26}{\sigma}$$

$$n = 1 - \frac{0.065}{\sigma} \cdot \left(1 + \frac{\sigma - 2}{4}\right)$$

$$\sigma = 2$$

$$r = 0.13, \quad n = 0.967$$



# Amplitude of density fluctuations

small because of logarithmic running  
near UV fixed point !

$$\mathcal{A} = \frac{(N + 3)^3}{4} e^{-2c_t}$$

$$c_t = \ln \left( \frac{m}{\mu} \right) = 14.1.$$

$$\frac{m}{\mu} = \frac{(N + 3)^{\frac{3}{2}}}{2\sqrt{\mathcal{A}}} = 1.32 \cdot 10^6 \left( \frac{N}{60} \right)^{\frac{3}{2}}$$

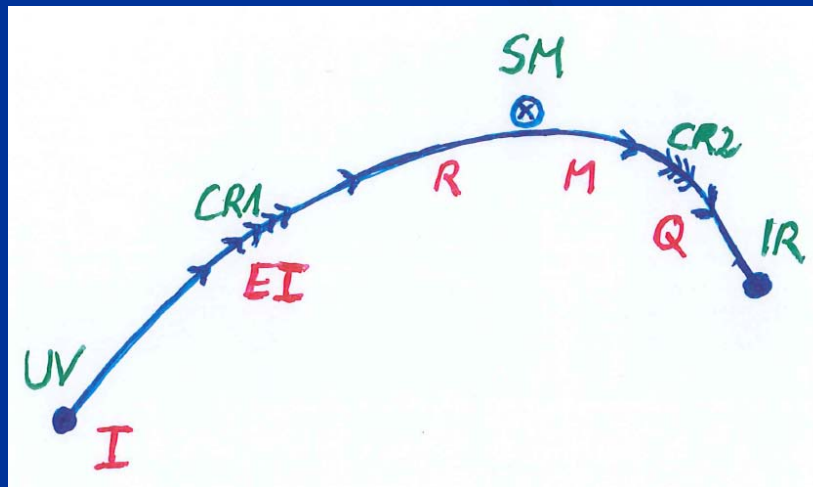
$N$  : number of e – foldings at horizon crossing

# First step of crossover ends inflation

- induced by crossover in B

$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[ \ln \left( \frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left( \frac{\chi}{m} \right)$$

- after crossover B changes only very slowly



# Scaling solutions near SM fixed point

( approximation for constant B )

$$H = b\mu \ , \ \chi = \chi_0 \exp(c\mu t).$$

Different scaling solutions for  
radiation domination and  
matter domination

# Radiation domination

$$c = \frac{2}{\sqrt{K+6}}$$

$$b = -\frac{c}{2}$$

**Universe  
shrinks !**

$$T_{00} = \rho = \bar{\rho} \mu^2 \chi^2$$

$$\bar{\rho}_r = -3 \frac{K+5}{K+6}$$

$$\mathbf{K = B - 6}$$

solution exists for  $B < 1$  or  $K < -5$

$$S = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \frac{1}{2} K(\chi) \partial^\mu \chi \partial_\mu \chi + V(\chi) \right\}$$

$$H = b\mu, \quad \chi = \chi_0 \exp(c\mu t)$$

# Varying particle masses near SM fixed point

- All particle masses are proportional to  $\chi$ .  
( scale symmetry )
- Ratios of particle masses remain constant.
- Compatibility with observational bounds on time dependence of particle mass ratios.



# cosmon coupling to matter

$$K(\ddot{\chi} + 3H\dot{\chi}) + \frac{1}{2} \frac{\partial K}{\partial \chi} \dot{\chi}^2 = -\frac{\partial V}{\partial \chi} + \frac{1}{2} \frac{\partial F}{\partial \chi} R + q_\chi$$

$$q_\chi = -(\rho - 3p)/\chi$$

$$F = \chi^2$$

# Matter domination

$$c = \sqrt{\frac{2}{K+6}},$$

$$b = -\frac{1}{3}\sqrt{\frac{2}{K+6}} = -\frac{1}{3}c,$$

**Universe shrinks !**

$$T_{00} = \rho = \bar{\rho}\mu^2\chi^2,$$

solution exists for

$$B < 4/3, \quad K < -14/3$$

$$\bar{\rho}_m = -\frac{2(3K+14)}{3(K+6)}$$

$$K = B - 6$$

# Early Dark Energy

Energy density in radiation increases ,  
proportional to cosmon potential

$$T_{00} = \rho = \bar{\rho} \mu^2 \chi^2, \quad V(\chi) = \mu^2 \chi^2,$$

fraction in early dark energy

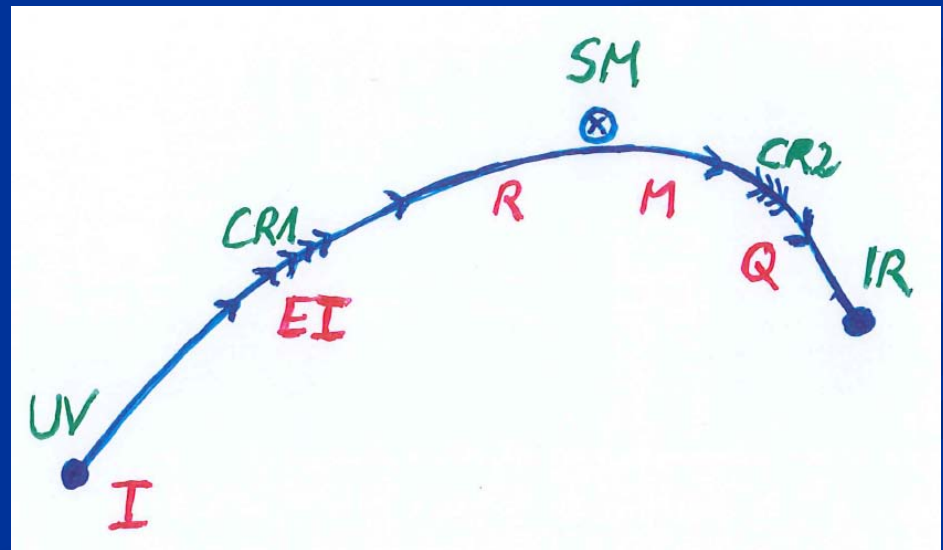
$$\Omega_h = \frac{\rho_h}{\rho_r + \rho_h} = \frac{nB(\chi)}{4}$$

or m

observation requires  **$B < 0.02$**  ( at CMB emission )

# Second crossover

- from SM to IR
- in sector of SM-singlets
- affects neutrino masses first



# Varying particle masses at onset of second crossover

- All particle masses **except neutrinos** are proportional to  $\chi$ .
- Ratios of particle masses remain constant.
- Compatibility with observational bounds on time dependence of particle mass ratios.
- Neutrino masses show stronger increase with  $\chi$ , such that **ratio neutrino mass over electron mass grows**.

# Dark Energy domination

neutrino masses scale  
differently from electron mass

$$\left. \frac{\partial \ln m_\nu}{\partial \ln \chi} \right|_{\text{today}} = 2\tilde{\gamma} + 1$$



$$m_\nu = \bar{c}_\nu \chi^{2\tilde{\gamma}+1}$$

$$\chi q_\chi = -(2\tilde{\gamma} + 1)(\rho_\nu - 3p_\nu)$$

new scaling solution. not yet reached.  
at present : transition period

$$\frac{\rho_\nu}{\chi^2} = \bar{\rho}_\nu \mu^2$$

$$b = \frac{1}{3}(2\tilde{\gamma} - 1)c$$

# connection between dark energy and neutrino properties

$$[\rho_h(t_0)]^{\frac{1}{4}} = 1.27 \left( \frac{\gamma m_\nu(t_0)}{eV} \right)^{\frac{1}{4}} 10^{-3} eV$$

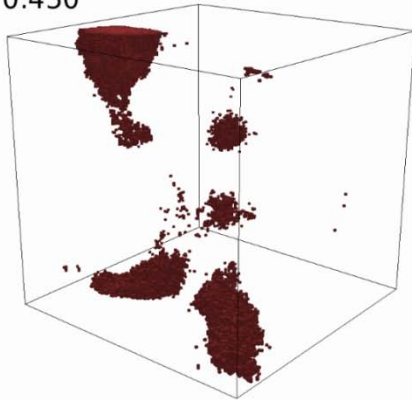
present dark energy density given by neutrino mass

present equation  
of state given by  
neutrino mass !

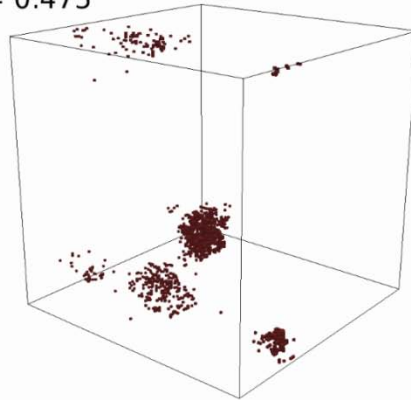
$$w_0 \approx -1 + \frac{m_\nu(t_0)}{12eV}$$

# Oscillating neutrino lumps

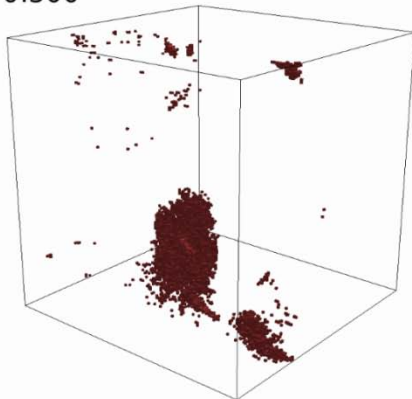
$a = 0.450$



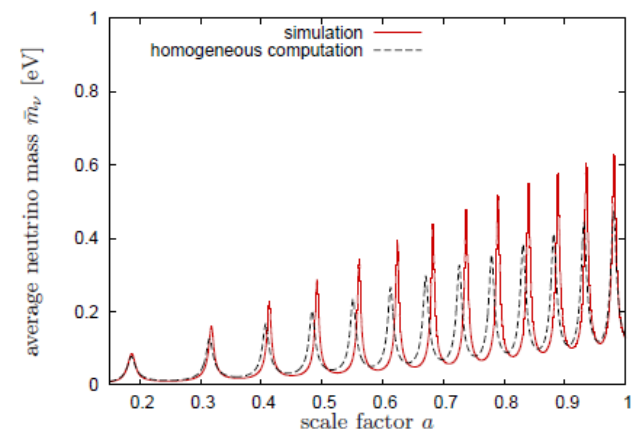
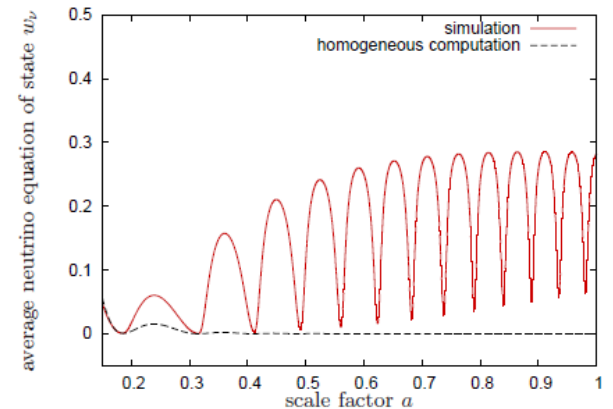
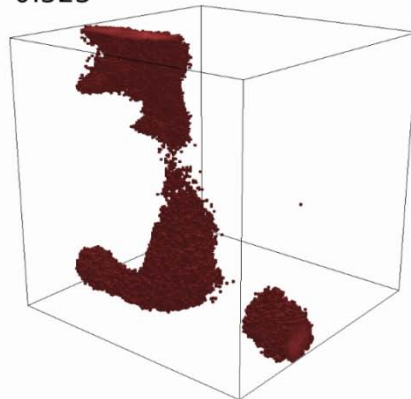
$a = 0.475$



$a = 0.500$



$a = 0.525$

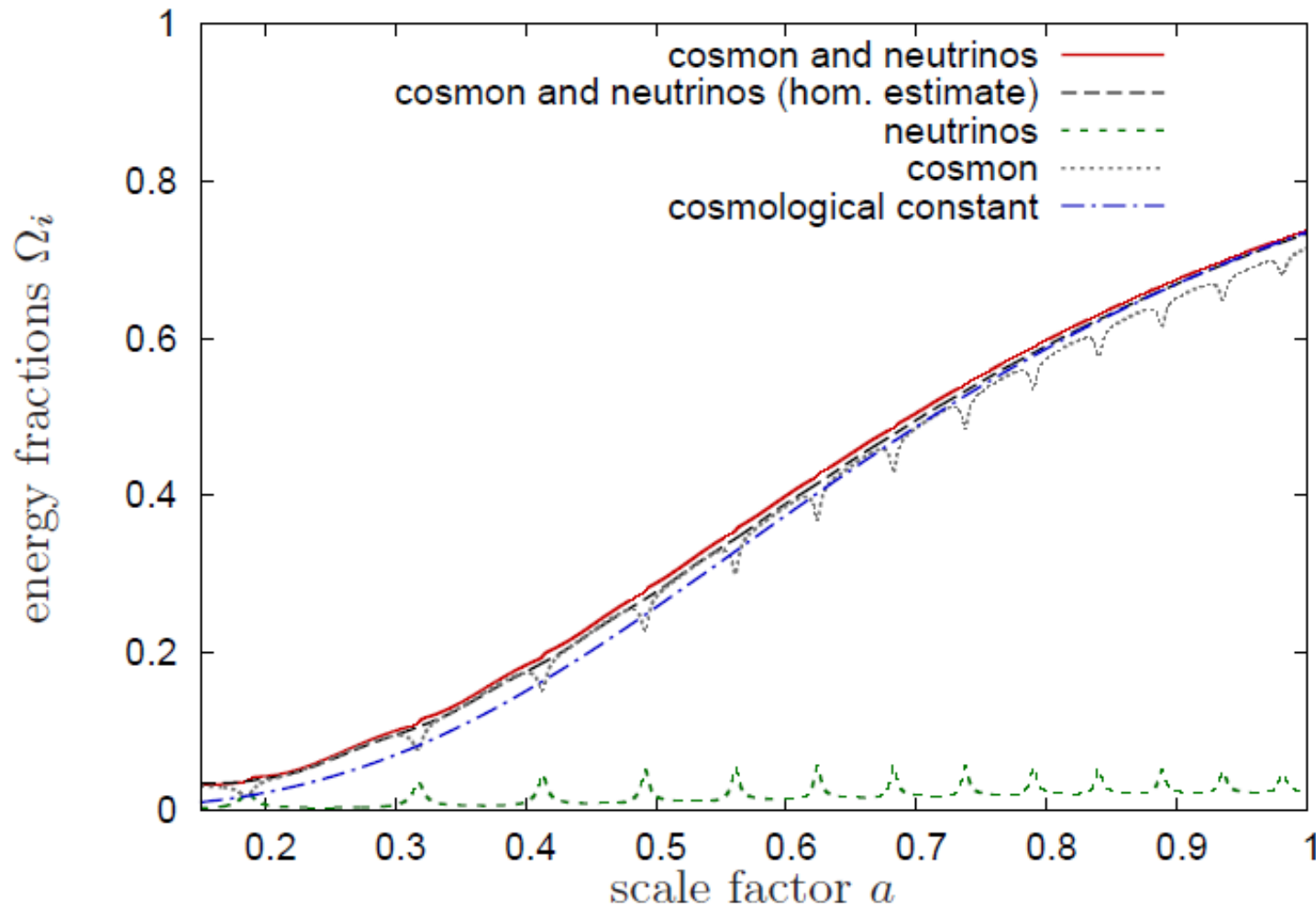


Y. Ayaita, M. Weber, ...

Ayaita, Baldi, Fuehrer,  
Puchwein, ...



# Evolution of dark energy similar to $\Lambda$ CDM



# Compatibility with observations

- Realistic inflation model:  
 $n = 0.976$  ,  $r = 0.13$
- Almost same prediction for radiation, matter, and Dark Energy domination as  $\Lambda$ CDM
- Presence of small fraction of Early Dark Energy
- Large neutrino lumps

# Einstein frame

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu} \ , \ \varphi = \frac{2M}{\alpha} \ln \left( \frac{\chi}{\mu} \right)$$

$$\Gamma = \int_x \sqrt{g'} \left\{ -\frac{1}{2} M^2 R' + V'(\varphi) + \frac{1}{2} k^2(\varphi) \partial^\mu \varphi \partial_\mu \varphi \right\}$$

$$V'(\varphi) = M^4 \exp \left( -\frac{\alpha \varphi}{M} \right)$$

$$k^2 = \frac{\alpha^2 B}{4}$$

# Einstein frame

- Weyl scaling maps variable gravity model to Universe with fixed masses and standard expansion history.
- Standard gravity coupled to scalar field.
- Only neutrino masses are growing.

# conclusions

- crossover in quantum gravity is reflected in crossover in cosmology
- quantum gravity becomes testable by cosmology
- quantum gravity plays a role not only for primordial cosmology
- crossover scenario explains different cosmological epochs
- simple model is compatible with present observations
- no more parameters than  $\Lambda$ CDM : tests possible

## conclusions (2)

- Variable gravity cosmologies can give a simple and realistic description of Universe
- Compatible with tests of equivalence principle and bounds on variation of fundamental couplings if nucleon and electron masses are proportional to variable Planck mass
- Different cosmological dependence of neutrino mass can explain why Universe makes a transition to Dark Energy domination **now**
- **characteristic signal : neutrino lumps**

The background is a solid dark blue color. On the right side, there are several thick, wavy, light blue lines that flow from the top towards the bottom, creating a sense of movement and depth.

end

# Scaling of particle masses

mass of electron or nucleon is proportional to variable Planck mass  $\chi$  !

effective potential for Higgs doublet  $h$

$$\tilde{V}_h = \frac{1}{2} \lambda_h (\tilde{h}^\dagger \tilde{h} - \epsilon_h \chi^2)^2$$