The background of the slide is a deep-field astronomical image, likely from the Hubble Space Telescope. It shows a vast field of galaxies and distant stars against a black background. The galaxies are of various shapes and sizes, some appearing as bright, diffuse clouds of light, while others are more compact and point-like. The stars are small, bright points of light, some with visible diffraction patterns. The overall scene is a dense, colorful mosaic of cosmic objects.

# Quantum gravity, Dark Energy, and the Origin of the Universe

The background of the slide is a deep-field astronomical image, likely from the Hubble Space Telescope. It shows a dense field of galaxies at various distances and orientations. Some galaxies are bright and clear, while others are faint and blurry. The colors range from yellow and orange to blue and purple, representing different types of galaxies and the light they emit. The overall effect is a sense of vastness and the scale of the universe.

Expanding Universe or  
shrinking atoms ?

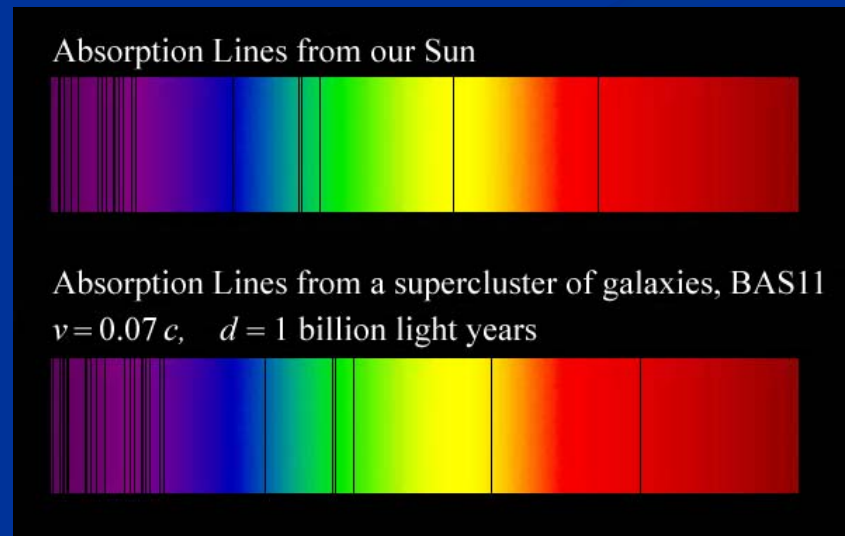
A deep-field astronomical image, likely from the Hubble Space Telescope, showing a vast field of galaxies and distant stars. The galaxies are of various shapes and sizes, including spiral, elliptical, and irregular forms, scattered across a black background. The text "Hot big bang or freeze ?" is overlaid in the center in a yellow, serif font.

Hot big bang or freeze ?

# Do we know that the Universe expands ?

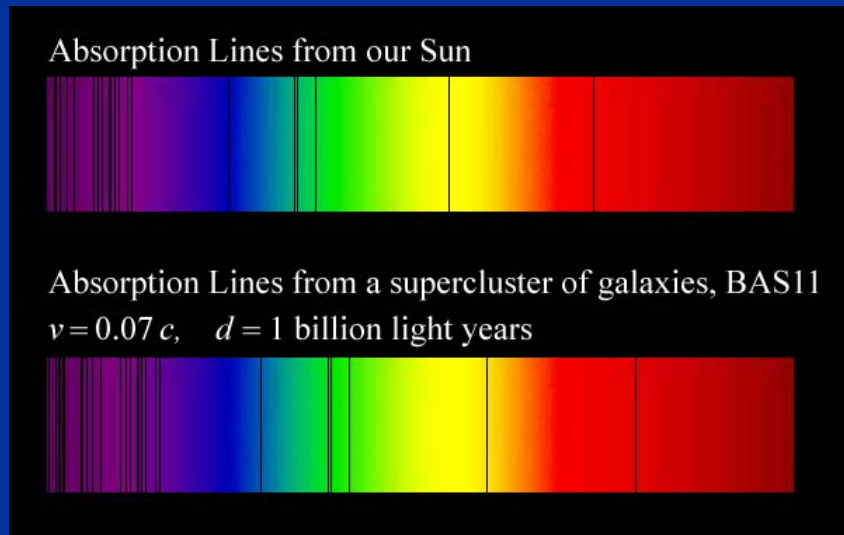
instead of redshift due to expansion :

smaller frequencies have been emitted in the past,  
because electron mass was smaller !



# Why do we see redshift of photons emitted in the distant past ?

photons are more red because they have been **emitted** with longer wavelength



frequency  $\sim$  mass

wavelength  $\sim$   
atoms size

# What is increasing ?

Ratio of distance between galaxies  
over size of atoms !

atom size constant : expanding geometry

alternative : shrinking size of atoms

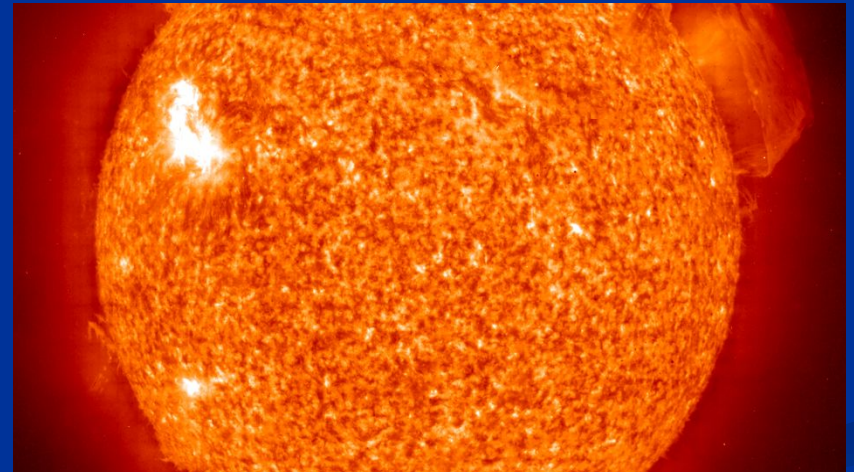
# How can particle masses change with time ?

- Particle masses are proportional to scalar field  $\chi$  .  
Similar to Higgs field.
- Scalar field varies with time.
- Ratios of particle masses are independent of  $\chi$  and therefore remain constant.
- Compatibility with observational bounds on time dependence of particle mass ratios.
- Dimensionless couplings are independent of  $\chi$  .

Do we know that the temperature was higher in the early Universe than now ?

Cosmic microwave radiation , nucleosynthesis

instead of  
higher temperature :  
smaller particle masses



# Hot plasma ?

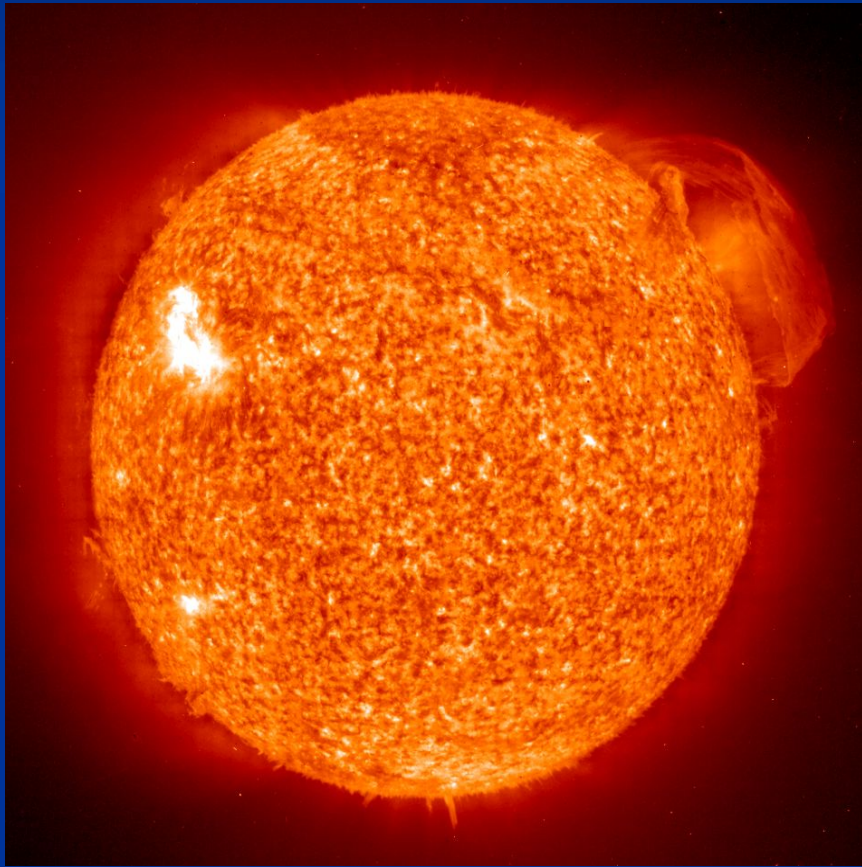
- Temperature in radiation dominated Universe :  
 $T \sim \chi^{1/2}$  **smaller** than today
- Ratio temperature / particle mass :  
 $T / m_p \sim \chi^{-1/2}$  **larger** than today
- $T/m_p$  counts ! This ratio decreases with time.
- Nucleosynthesis , CMB emission as in standard cosmology !

# Freeze Universe

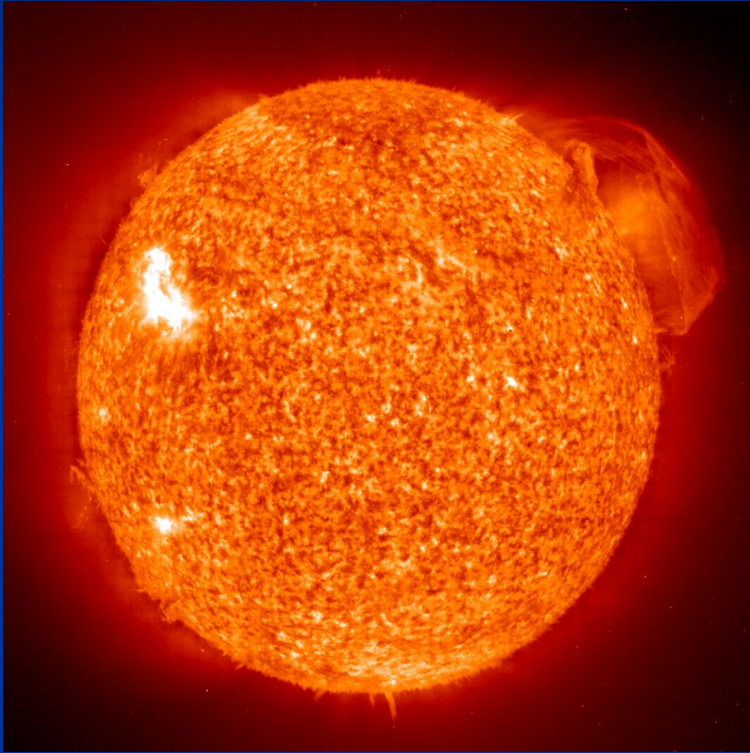
*The Universe may have started very cold,  
and only later heat up.*

*Freeze picture of the Universe*

# Big bang or freeze ?



# Big bang or freeze ?



freeze picture :  
only rods for measurements  
( masses ) are different !



*Big bang is not wrong,*

*but alternative pictures exist !*

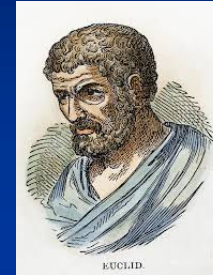
# Field relativity :

## different pictures of cosmology

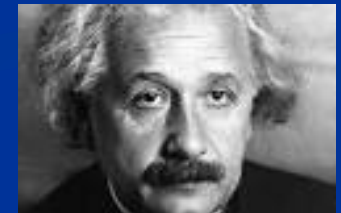
- same physical content can be described by different pictures
- related by field – redefinitions ,  
e.g. Weyl scaling , conformal scaling of metric
- observables cannot depend on choice of fields
- metric is one of the fields
- which picture is usefull ?

# Relativity of geometry

- Euclid ... Newton : space and time are absolute



- Special relativity : space and time depend on observer
- General relativity : space-time is influenced by matter ( including radiation )  
geometry is independent of coordinates  
geometry is observable
- Field relativity : geometry is relative



*Space-time is a description  
of correlations between “matter”.*

*Observables cannot depend on choice of  
fields used to describe them.*

*Different pictures for geometry exist.*

# Why should you care about the freeze picture of the Universe ?

*Some aspects are understood easier :*

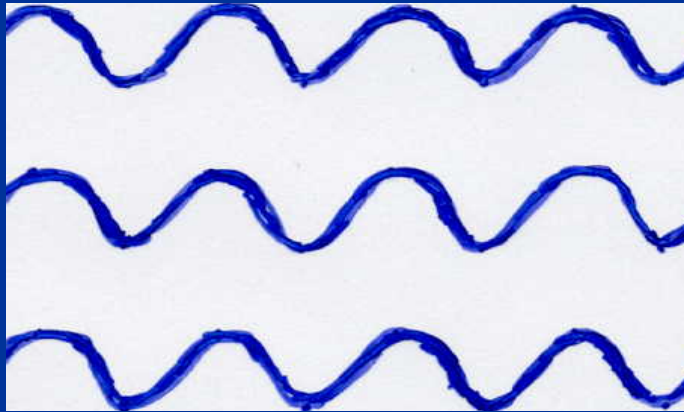
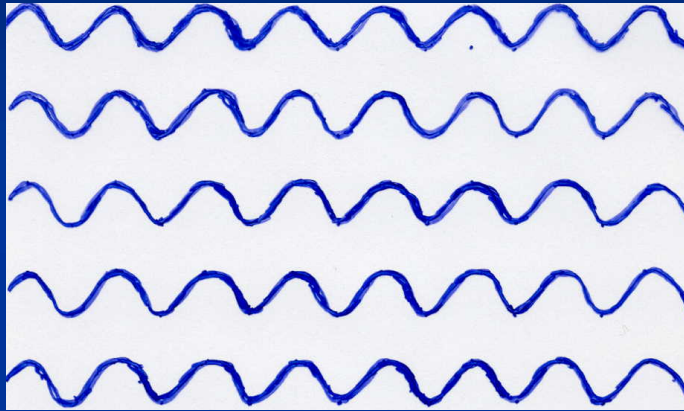
- Beginning of Universe
- Role of scale symmetry
- Range of impact of quantum gravity

# preview

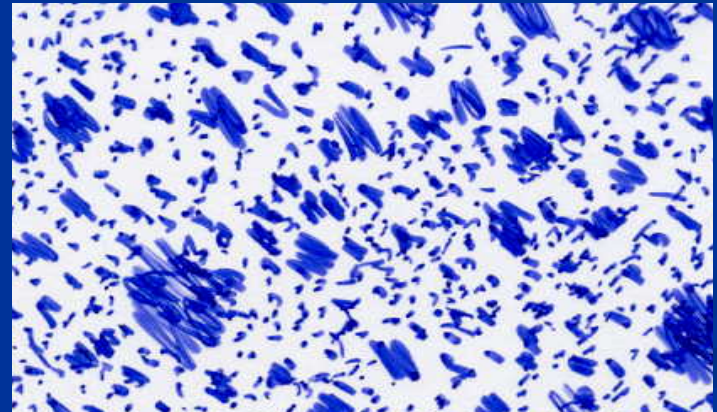
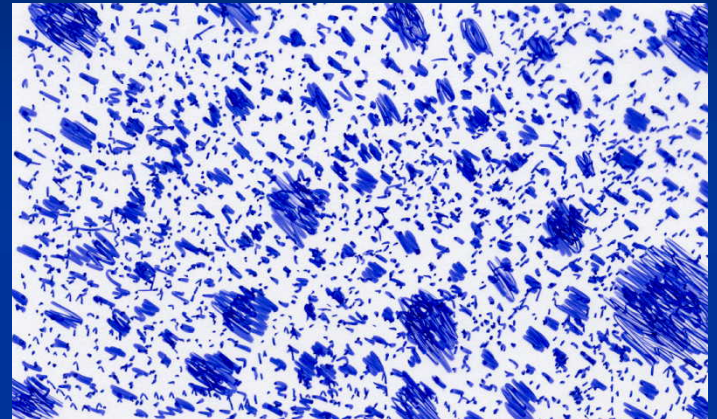
- Big bang singularity is artefact of inappropriate choice of field variables – no physical singularity
- Quantum gravity may be observable in dynamics of present Universe

# quantum gravity – the role of scale symmetry

# Scale symmetry



no scale symmetry



scale symmetry

# Scale symmetry

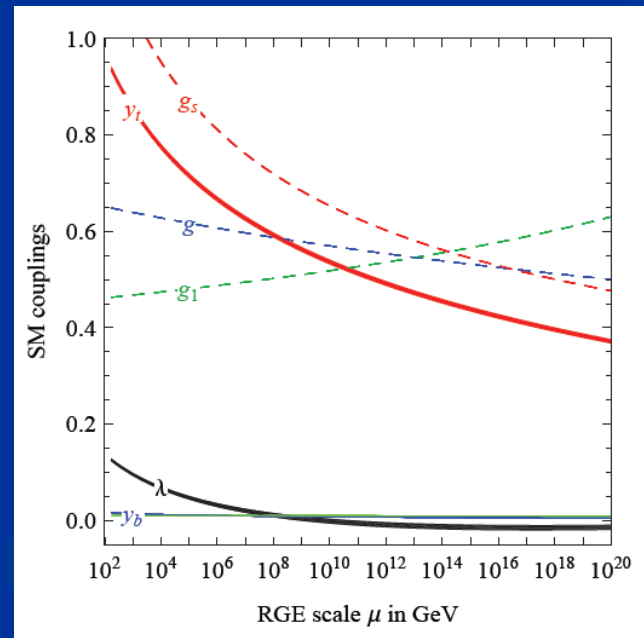
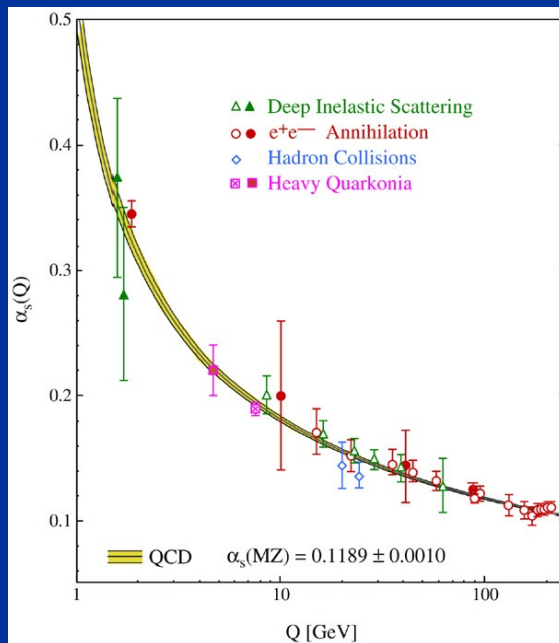
No parameter with dimension of length or mass is present.

Then invariance under dilatations or global scale transformations is realized.

Continuous global symmetry

# Fluctuations induce running couplings

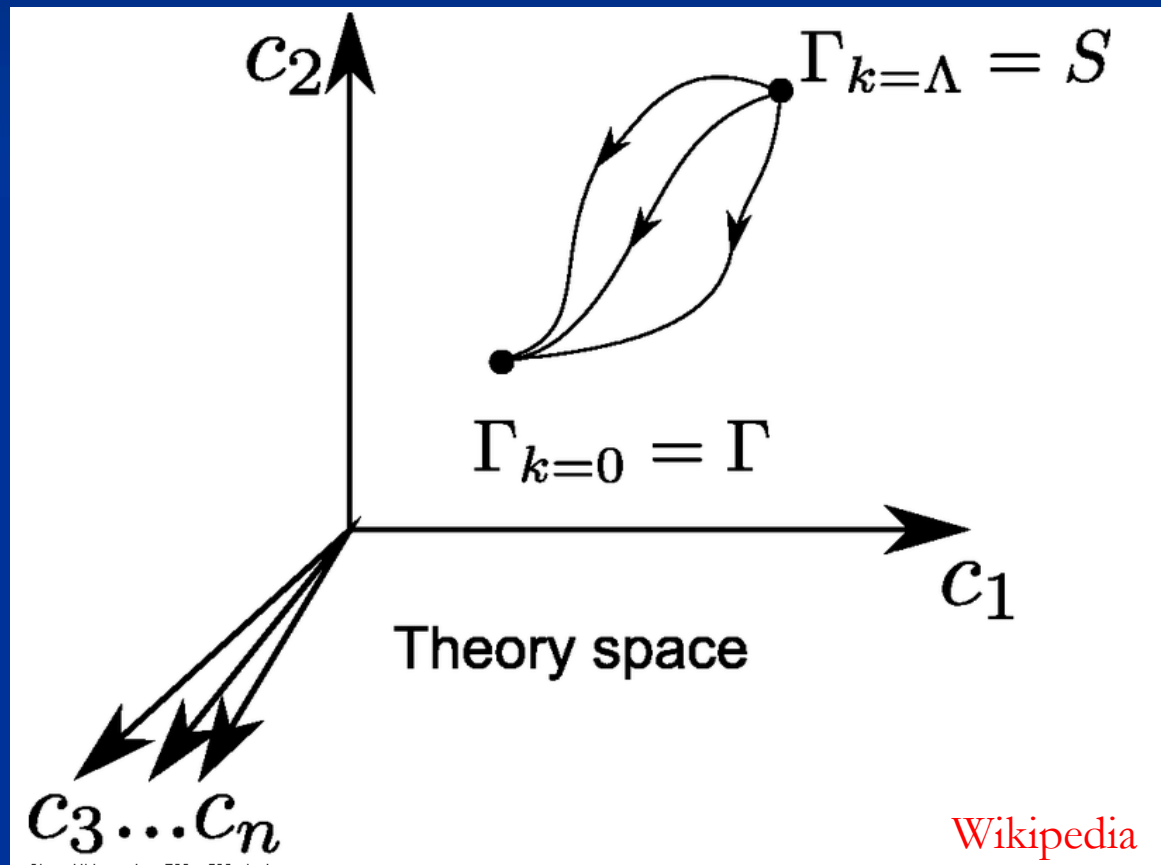
- violation of scale symmetry
- well known in QCD or standard model



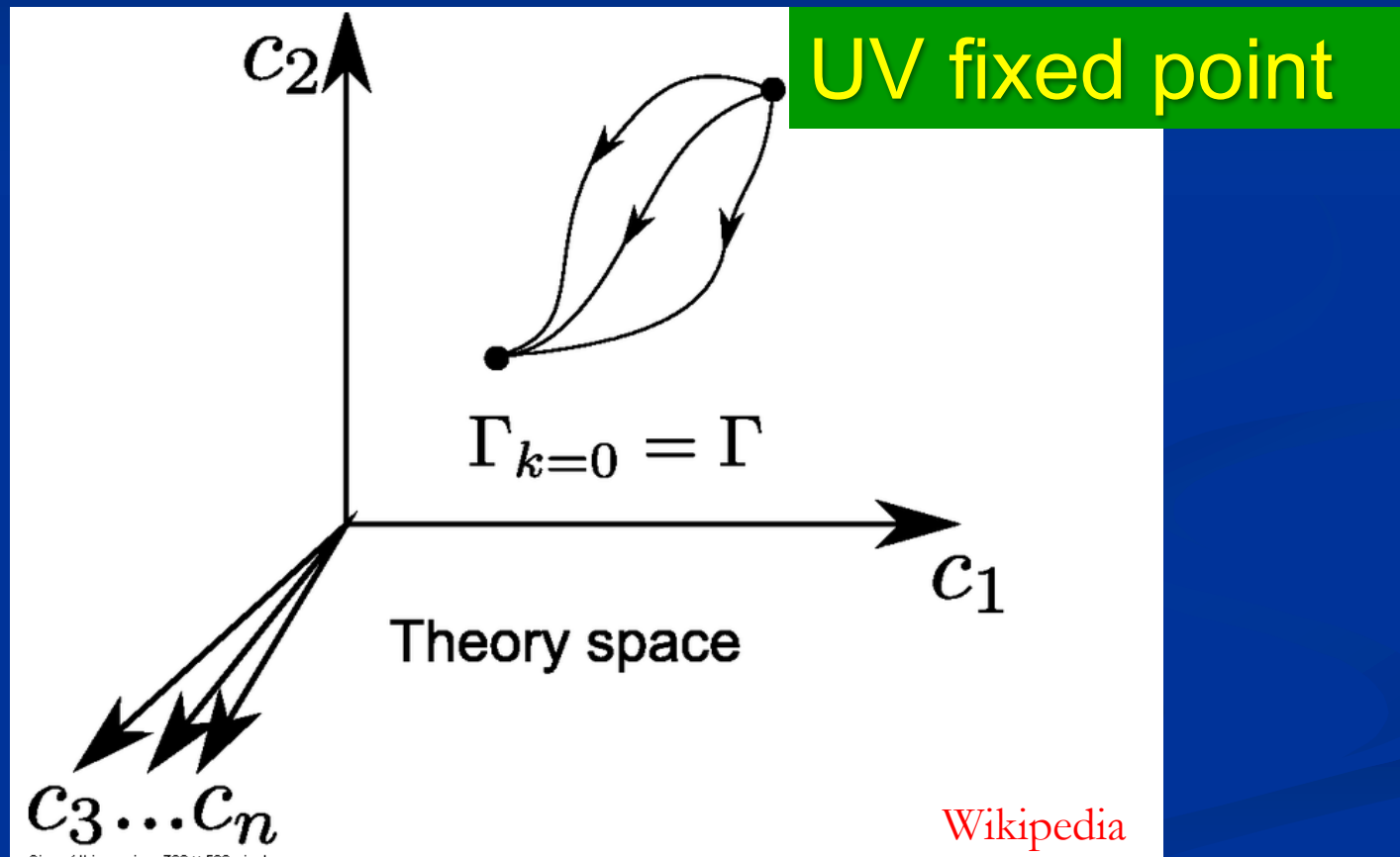
# Quantum scale symmetry

- quantum fluctuations violate scale symmetry
- running dimensionless couplings
- at fixed points , scale symmetry is exact !
- quantum fluctuations can generate scale symmetry !

# Functional renormalization : flowing action



# Ultraviolet fixed point



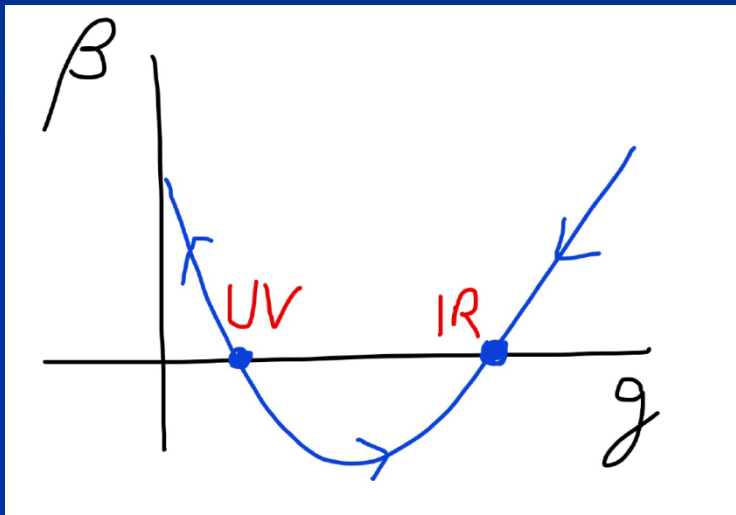
# Asymptotic safety of quantum gravity

if UV fixed point exists :

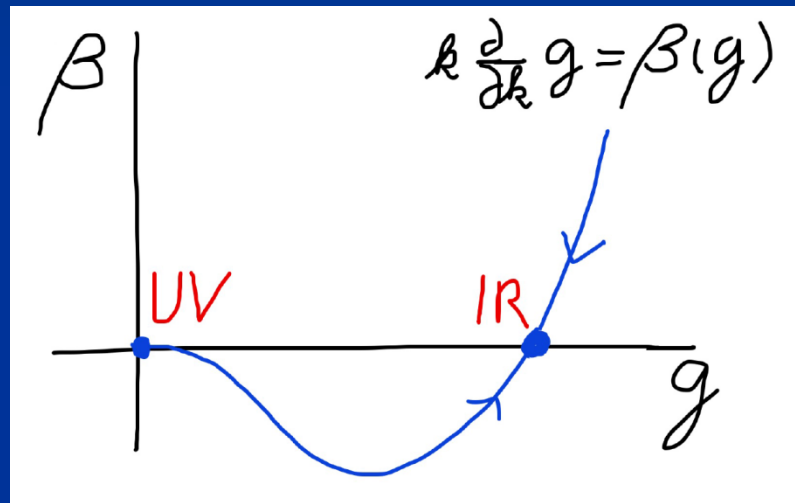
*quantum gravity is  
non-perturbatively renormalizable !*

S. Weinberg , M. Reuter

## Asymptotic safety



## Asymptotic freedom



Relevant parameters yield undetermined couplings.  
Quartic scalar coupling is not relevant and can  
therefore be predicted.

# a prediction...

## Asymptotic safety of gravity and the Higgs boson mass

Mikhail Shaposhnikov

*Institut de Théorie des Phénomènes Physiques, École Polytechnique Fédérale de Lausanne, CH-1015 Lausanne, Switzerland*

Christof Wetterich

*Institut für Theoretische Physik, Universität Heidelberg, Philosophenweg 16, D-69120 Heidelberg, Germany*

12 January 2010

### Abstract

There are indications that gravity is asymptotically safe. The Standard Model (SM) plus gravity could be valid up to arbitrarily high energies. Supposing that this is indeed the case and assuming that there are no intermediate energy scales between the Fermi and Planck scales we address the question of whether the mass of the Higgs boson  $m_H$  can be predicted. For a positive gravity induced anomalous dimension  $A_\lambda > 0$  the running of the quartic scalar self interaction  $\lambda$  at scales beyond the Planck mass is determined by a fixed point at zero. This results in  $m_H = m_{\min} = 126$  GeV, with only a few GeV uncertainty. This prediction is independent of the details of the short distance running and holds for a wide class of extensions of the SM as well.

s in  $m_H = m_{\min} = 126$  GeV, with o

quantum gravity with  
scalar field –  
the role of scale symmetry  
for cosmology

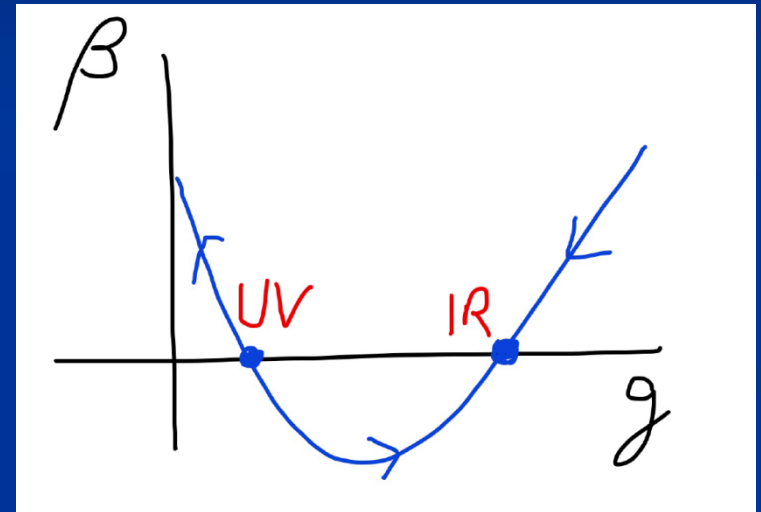
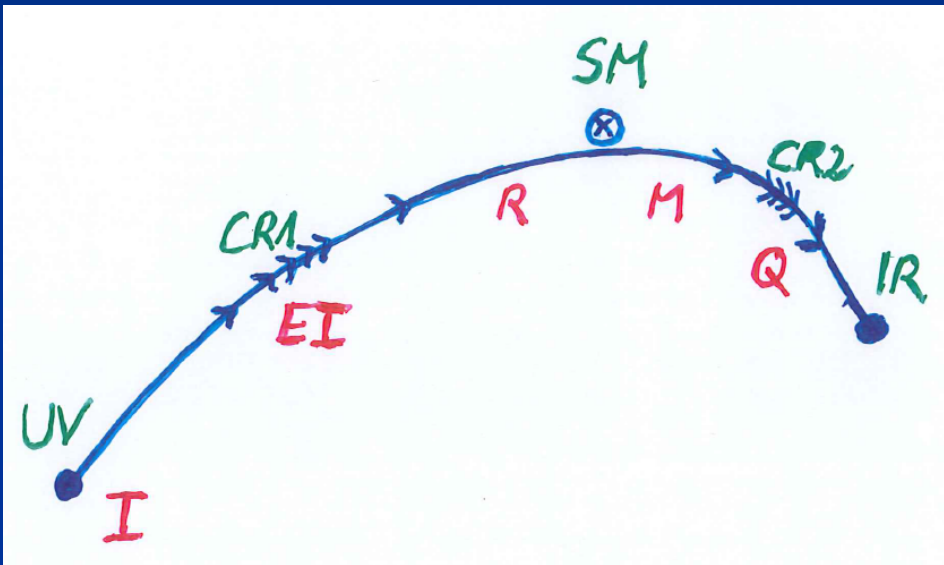
# Spontaneous breaking of scale symmetry

- expectation value of scalar field breaks scale symmetry spontaneously
- massive particles are compatible with scale symmetry
- in presence of massive particles : sign of exact scale symmetry is exactly **massless Goldstone boson** — the dilaton

# Approximate scale symmetry near fixed points

- UV : approximate scale invariance of primordial fluctuation spectrum from inflation
- IR : cosmon is pseudo Goldstone boson of spontaneously broken scale symmetry, tiny mass, responsible for dynamical Dark Energy

# Possible consequences of crossover in quantum gravity



Realistic model for inflation and dark energy  
with single scalar field

# variable gravity

*“Newton’s constant is not constant –  
and particle masses are not constant”*

# Variable Gravity

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

quantum effective action,  
variation yields field equations

Einstein gravity :  $\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} M^2 R \right\}$

# Scale symmetry in variable gravity ( IR – fixed point )

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \cancel{\mu^2 \chi^2} + \frac{1}{2} (\cancel{B(\chi/\mu)} - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

quantum effective action,  
variation yields field equations

Einstein gravity :  $\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} M^2 R \right\}$

# Variable Gravity

- Scalar field coupled to gravity
- Effective Planck mass depends on scalar field
- Simple quadratic scalar potential involves intrinsic mass  $\mu$
- Nucleon and electron mass proportional to dynamical Planck mass

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

# What is Dark Energy ?

Dark energy is energy density of scalar field  $\chi$

$$\rho = V + \text{kinetic term}$$

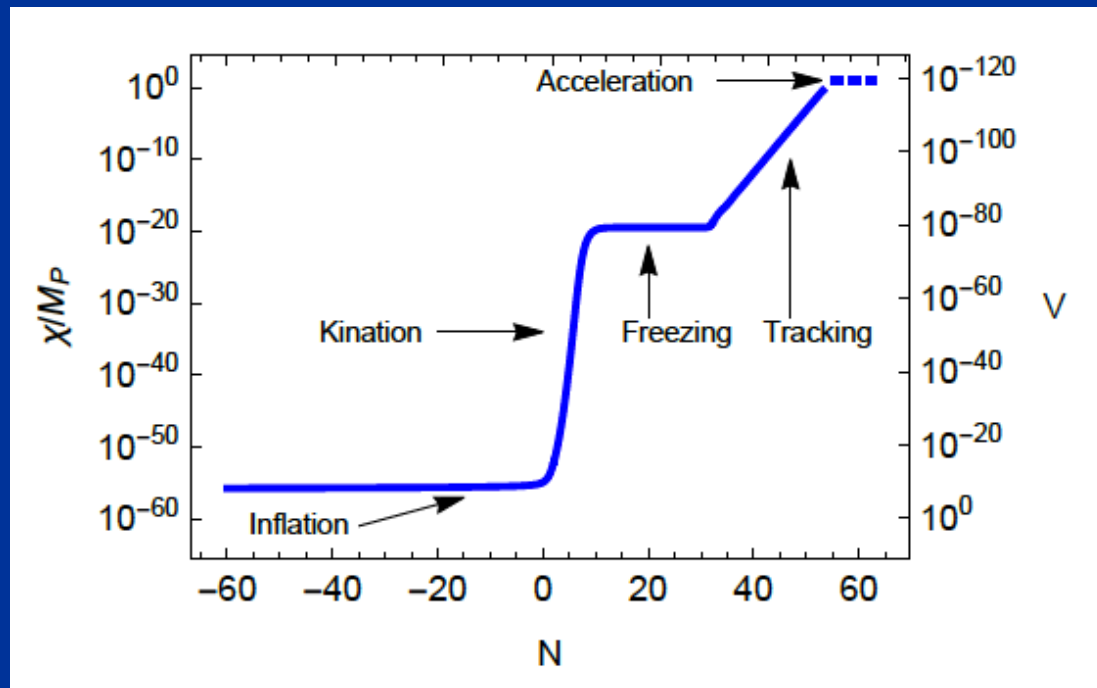
$$V = \mu^2 \chi^2$$

$$p = -V + \text{kinetic term}$$

Dark energy is dynamical if  $\chi$  changes with time

# Cosmological solution

- scalar field  $\chi$  vanishes in the infinite past
- scalar field  $\chi$  diverges in the infinite future



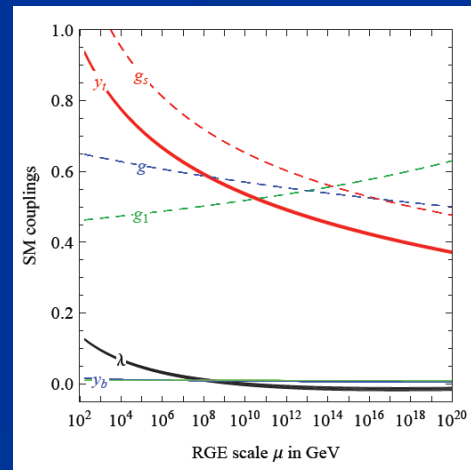
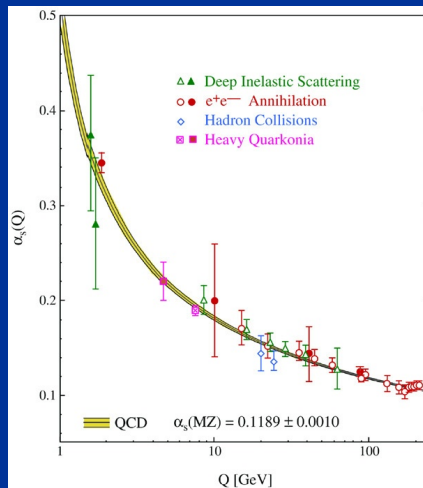
J.Rubio,...

# Kinetic B : running coupling

- B varies if intrinsic scale  $\mu$  changes

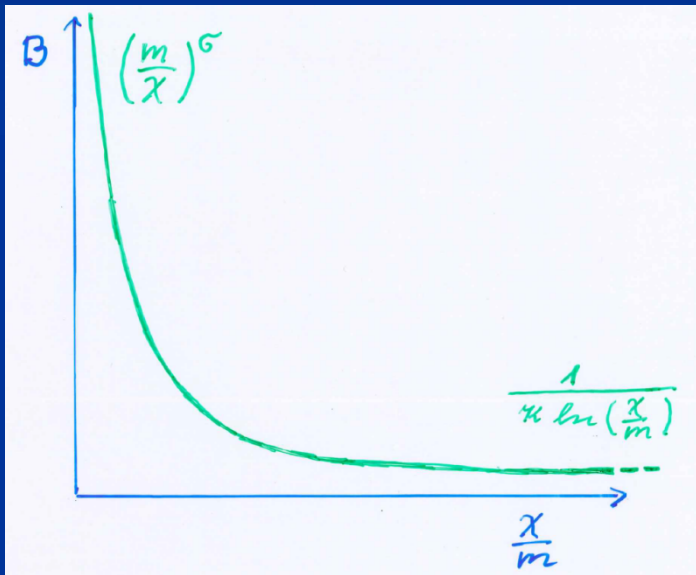
$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

- similar to QCD or standard model



# Kinetic B :

## Crossover between two fixed points



assumption:

running  
coupling obeys  
flow equation

$$\mu \frac{\partial B}{\partial \mu} = \frac{\kappa \sigma B^2}{\sigma + \kappa B}$$

$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[ \ln \left( \frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left( \frac{\chi}{m} \right)$$

$m$  : scale of crossover

can be exponentially larger than intrinsic scale  $\mu$

# Four-parameter model

- model has four dimensionless parameters
- three in kinetic :
  - $\sigma \sim 2.5$
  - $\kappa \sim 0.5$
  - $c_t \sim 14$  ( or  $m/\mu$  )
- one parameter for growth rate of neutrino mass over electron mass :  $\gamma \sim 8$
- + standard model particles and dark matter : sufficient for realistic cosmology from inflation to dark energy
- no more free parameters than  $\Lambda$ CDM

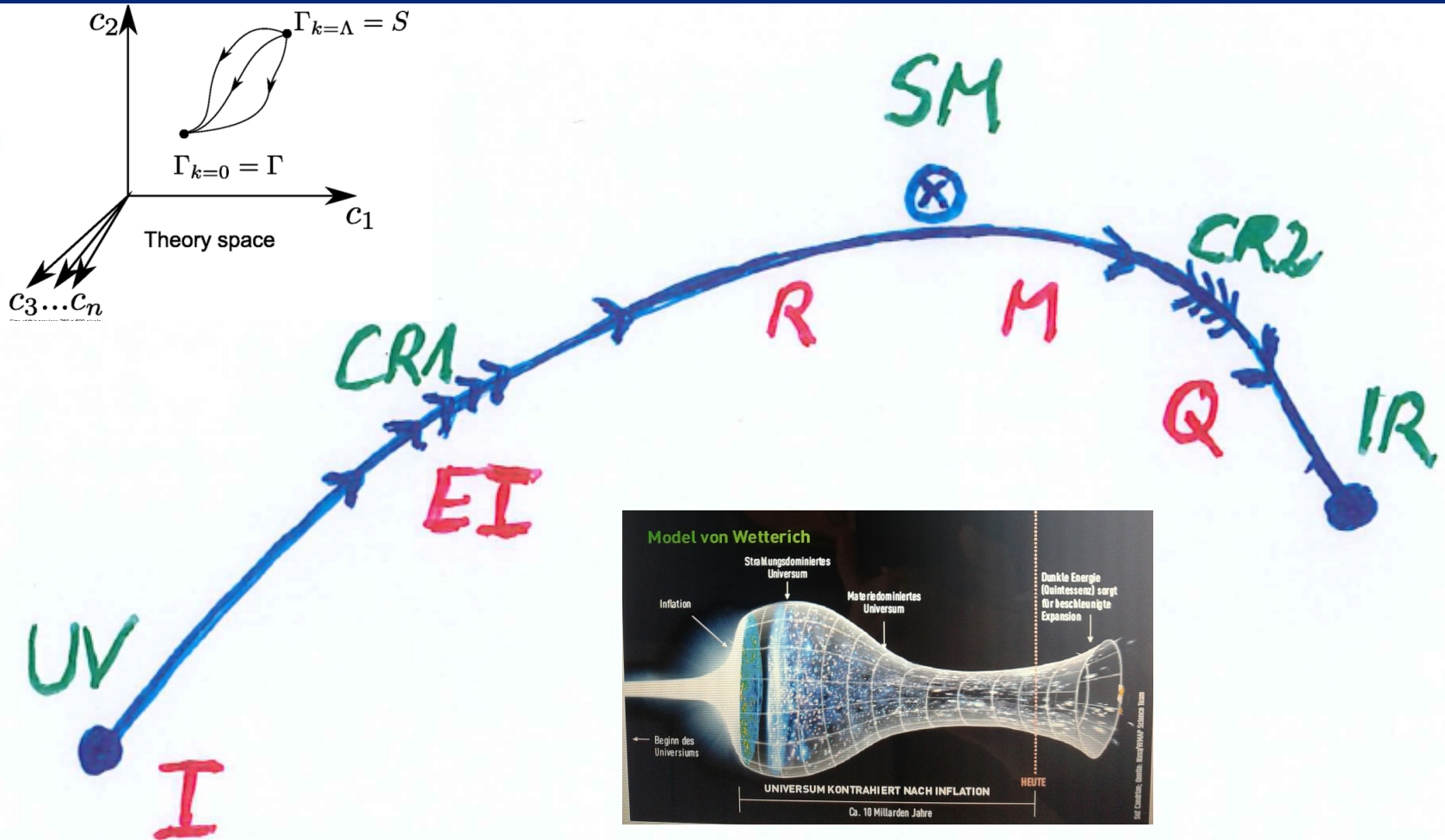
# Model is compatible with present observations

Together with variation of neutrino mass over  
electron mass in present cosmological epoch :  
model is compatible with all present  
observations, including inflation and dark energy

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[ \ln \left( \frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left( \frac{\chi}{m} \right)$$

# Crossover in quantum gravity and cosmology

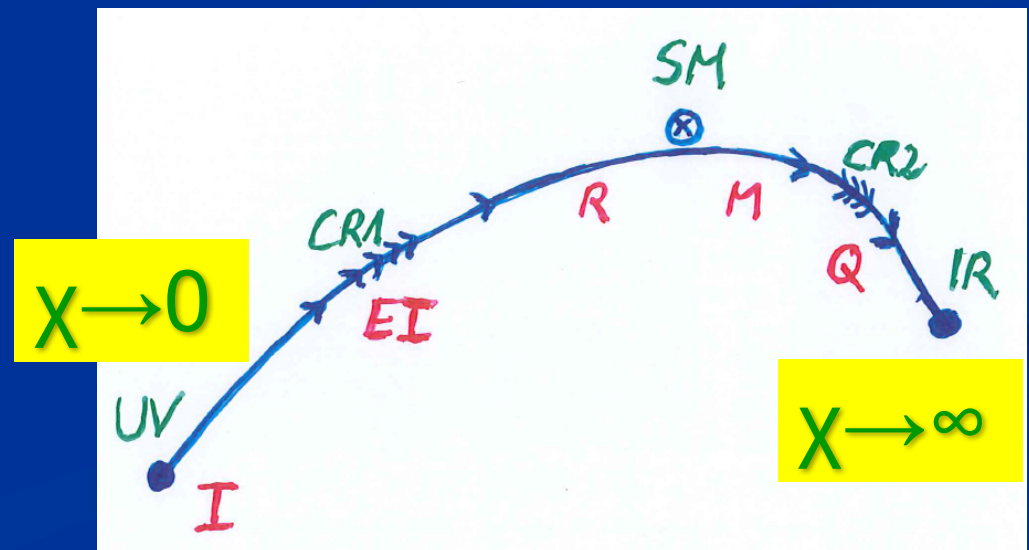


# Cosmological solution : crossover from UV to IR fixed point

- Dimensionless functions as  $B$  depend only on ratio  $\mu/\chi$ .
- IR:  $\mu \rightarrow 0$  ,  $\chi \rightarrow \infty$
- UV:  $\mu \rightarrow \infty$  ,  $\chi \rightarrow 0$

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

Cosmology makes  
crossover between  
fixed points by  
variation of  $\chi$ .



# Renormalization flow and cosmological evolution

- renormalization flow as function of  $\mu$

is mapped by dimensionless functions to

- field dependence of effective action on scalar field  $\chi$

translates by solution of field equation to

- dependence of cosmology on time  $t$  or  $\eta$

# No tiny dimensionless parameters ( except gauge hierarchy )

- one mass scale  $\mu = 2 \cdot 10^{-33} \text{ eV}$
- one time scale  $\mu^{-1} = 10^{10} \text{ yr}$
- Planck mass does not appear as parameter
- Planck mass grows large dynamically

# Slow Universe

Asymptotic solution in  
freeze frame :

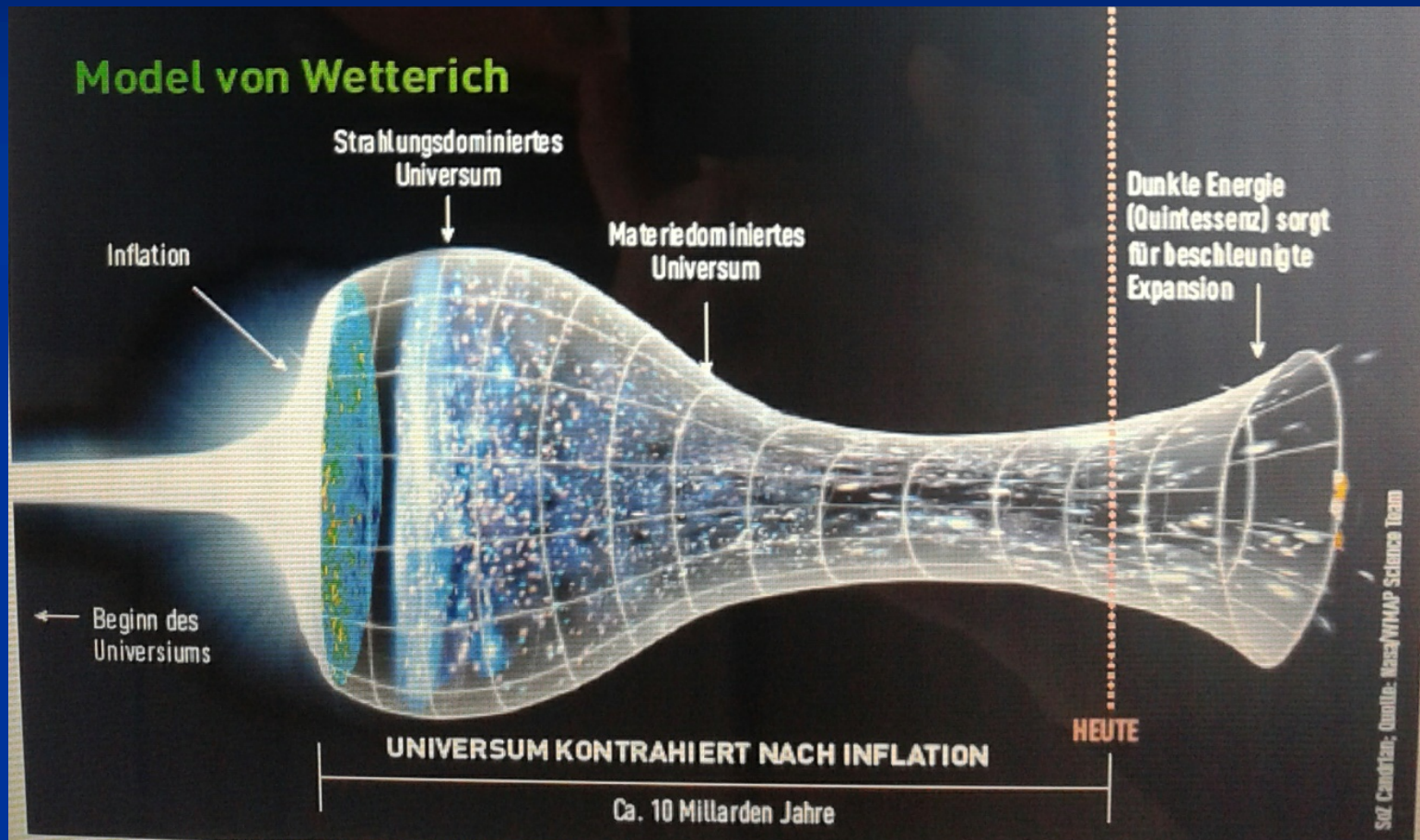
$$H = \frac{\mu}{\sqrt{3}} , \quad \chi = \frac{3^{\frac{1}{4}} m}{2\sqrt{\mu}} (t_c - t)^{-\frac{1}{2}}$$

$$\mu = 2 \cdot 10^{-33} \text{ eV}$$

Expansion or shrinking always slow ,  
characteristic time scale of the order of the age of the  
Universe :  $t_{\text{ch}} \sim \mu^{-1} \sim 10 \text{ billion years} !$

Hubble parameter of the order of **present** Hubble  
parameter for all times , including inflation and big bang !  
Slow increase of particle masses !

# Strange evolution of Universe



Sonntagszeitung Zürich , Laukenmann

# Einstein frame

- “Weyl scaling” maps variable gravity model to Universe with fixed masses and standard expansion history.
- Exact equivalence of different frames !  
“different pictures”
- Standard gravity coupled to scalar field.

# Einstein frame

Weyl scaling :

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu} , \quad \varphi = \frac{2M}{\alpha} \ln \left( \frac{\chi}{\mu} \right)$$

effective action in Einstein frame :

$$\Gamma = \int_x \sqrt{g'} \left\{ -\frac{1}{2} M^2 R' + V'(\varphi) + \frac{1}{2} k^2(\varphi) \partial^\mu \varphi \partial_\mu \varphi \right\}$$

$$V'(\varphi) = M^4 \exp \left( -\frac{\alpha \varphi}{M} \right)$$

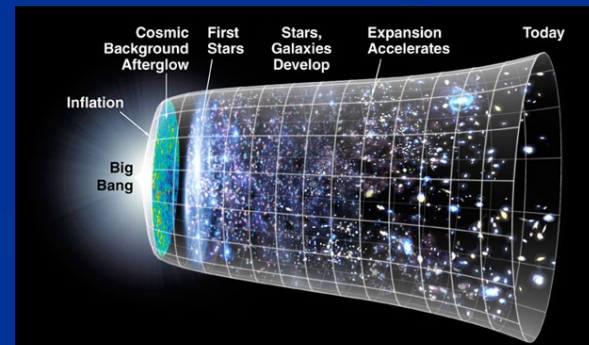
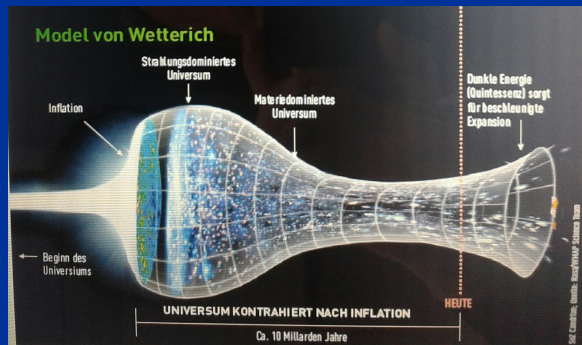
$$k^2 = \frac{\alpha^2 B}{4}$$

# Field relativity

Weyl scaling :

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu}$$

changes geometry,  
not a coordinate transformation



infinite past

# Infinite past : slow inflation

$\sigma = 2$  : field equations

$$\ddot{\chi} + \left( 3H + \frac{1}{2} \frac{\dot{\chi}}{\chi} \right) \dot{\chi} = \frac{2\mu^2 \chi^2}{m}$$

$$H = \sqrt{\frac{\mu^2}{3} + \frac{m\dot{\chi}^2}{6\chi^3}} - \frac{\dot{\chi}}{\chi}$$

approximative  
solution

$$H = \frac{\mu}{\sqrt{3}}, \quad \chi = \frac{3^{\frac{1}{4}} m}{2\sqrt{\mu}} (t_c - t)^{-\frac{1}{2}}$$

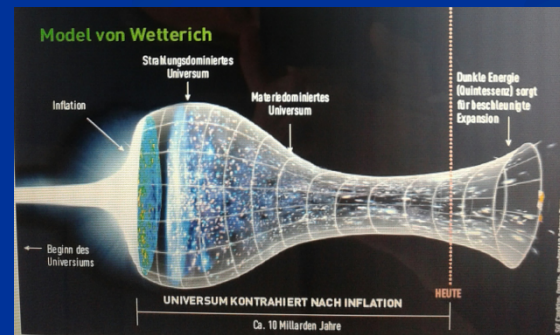
particles become massless in infinite past !

# Eternal Universe

Asymptotic solution in freeze frame :

$$H = \frac{\mu}{\sqrt{3}}, \quad \chi = \frac{3^{\frac{1}{4}} m}{2\sqrt{\mu}} (t_c - t)^{-\frac{1}{2}}$$

- solution valid back to the infinite past in physical time
- no singularity
- physical time to infinite past is infinite

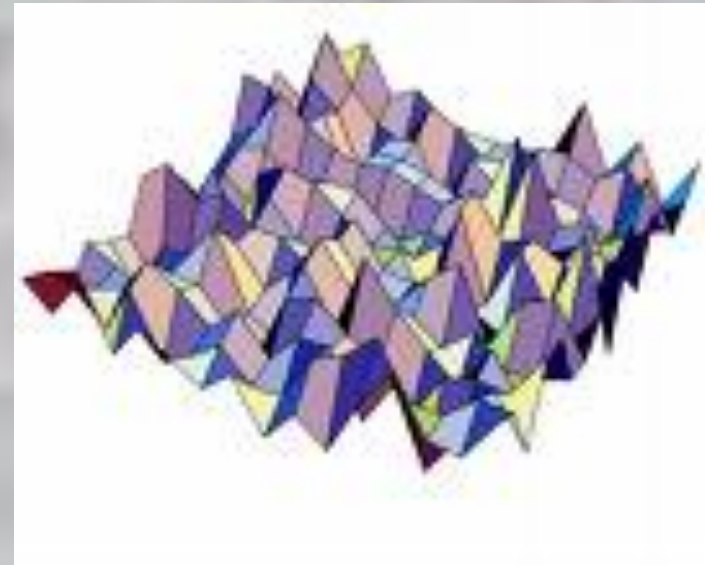


# Eternal light-vacuum

Everywhere almost nothing  
only fluctuations

All particles move  
with light velocity,  
similar to photons

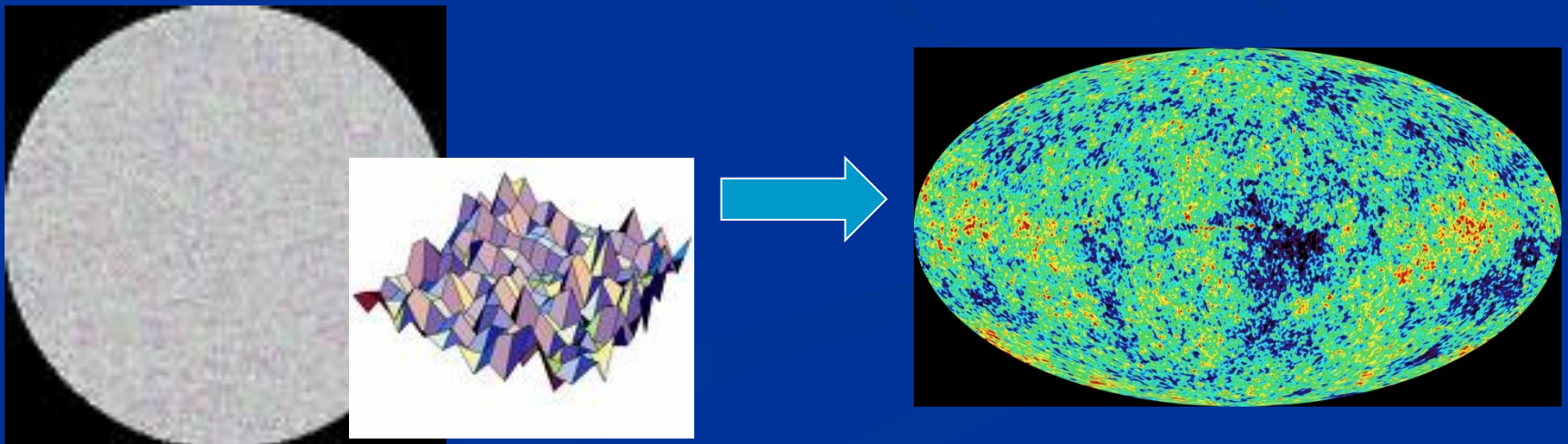
strength of gravity  
much stronger than today



*In the beginning was light-like emptiness.*

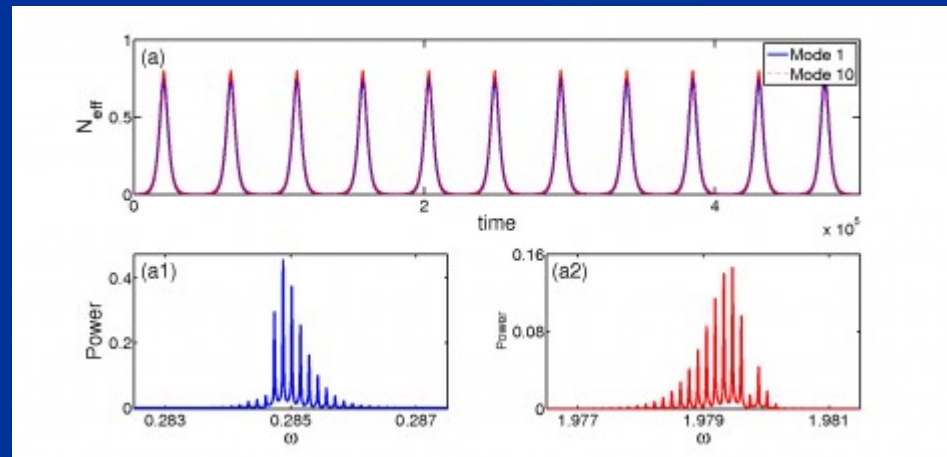
# Eternal light-vacuum is unstable

- Slow increase of particle masses and weakening of gravity
- Only slow change of space-time geometry
- Consequence for observation : primordial fluctuations become visible in cosmic background radiation
- We see fluctuations in a stage 5000 billion years ago.



# Physical time

count oscillations ....



# Physical time

field equation for scalar field mode

$$(\partial_\eta^2 + 2Ha\partial_\eta + k^2 + a^2m^2)\varphi_k = 0$$

$$\varphi_k = \frac{\tilde{\varphi}_k}{a} \quad \left\{ \partial_\eta^2 + k^2 + a^2 \left( m^2 - \frac{R}{6} \right) \right\} \tilde{\varphi}_k = 0$$

determine **physical time** by counting number of oscillations

$$\tilde{t}_p = n_k$$

$$n_k = \frac{k\eta}{\pi}$$

(  $m=0$  )

# Physical time

- counting : discrete
- invariant under field transformations
- same in all frames

*Big bang singularity  
in Einstein frame is  
field singularity !*

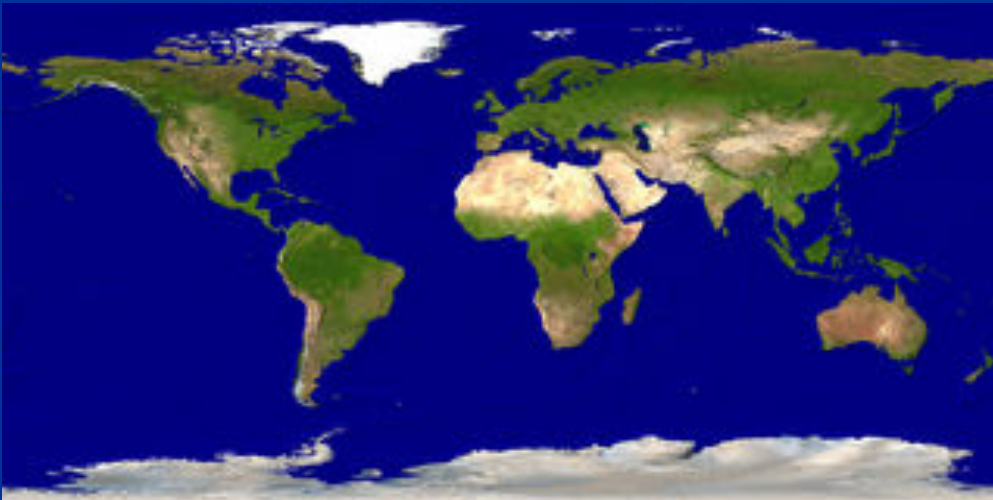
$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu} , \quad \varphi = \frac{2M}{\alpha} \ln \left( \frac{\chi}{\mu} \right)$$

choice of frame with constant particle masses is not well suited if physical masses go to zero !

# Field - singularity

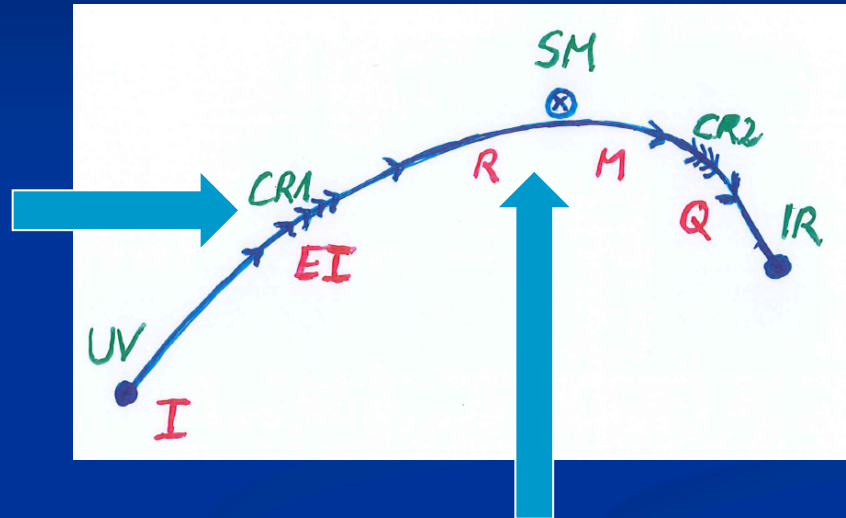
- Big Bang is field - singularity
- similar ( but not identical with )  
coordinate - singularity

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu}$$



# Scaling solution

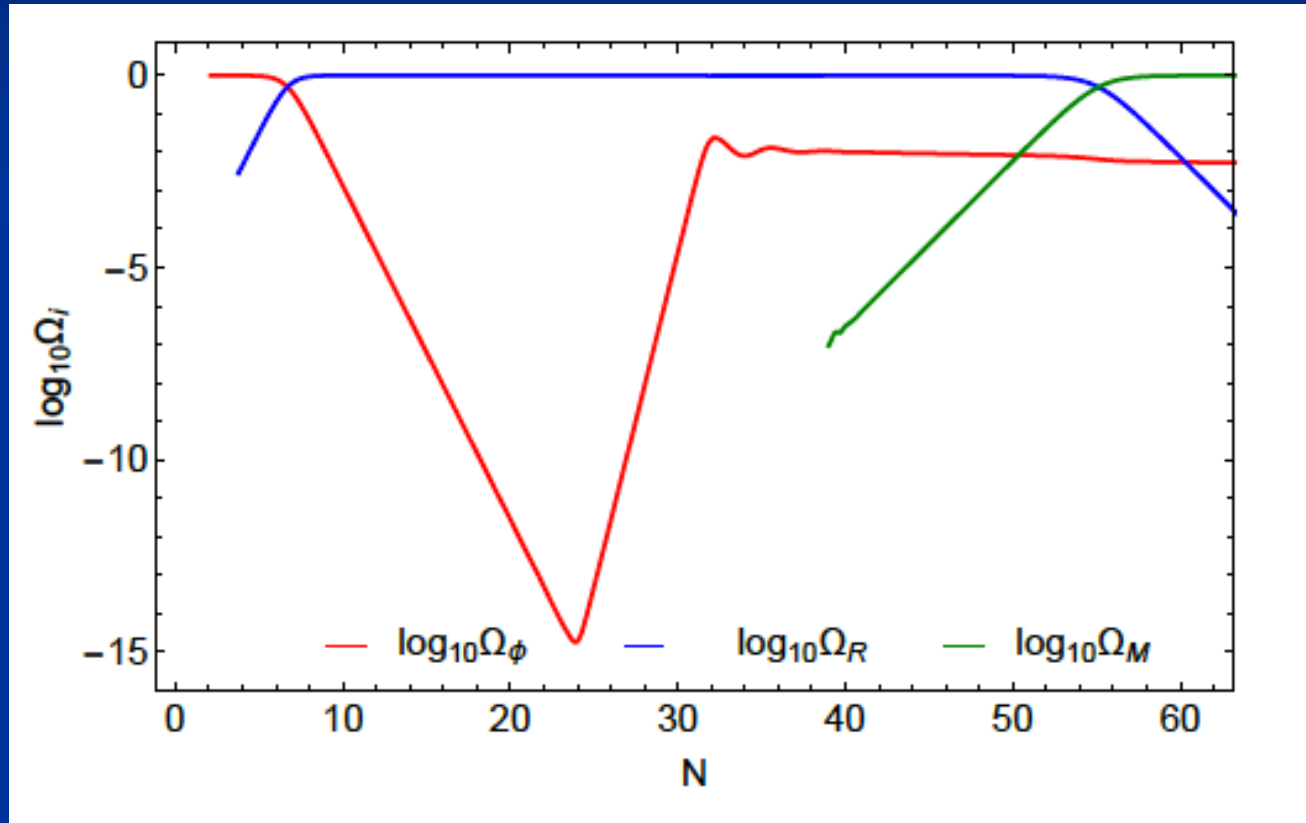
after end of inflation



Dark Energy decreases  
similar to radiation and  
matter

scaling solution with  
few percent  
of Early Dark Energy

# Evolution of dark energy fraction

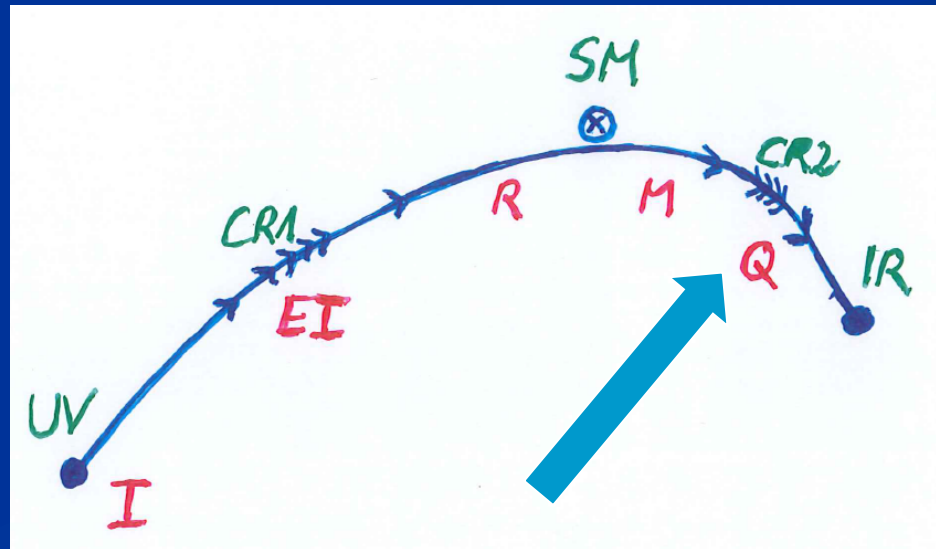


J. Rubio,...

# Growing neutrino masses and quintessence

# Second stage of crossover

- from SM to IR
- in sector Beyond Standard Model
- affects neutrino masses first ( seesaw or cascade mechanism )



# Varying particle masses at onset of second crossover

- **Except for neutrinos** all particle masses are proportional to  $\chi$ .
- Ratios of particle masses remain constant.
- Compatibility with observational bounds on time dependence of particle mass ratios.
- Neutrino masses show stronger increase with  $\chi$ , such that **ratio neutrino mass over electron mass grows**.

# Cosmic trigger

- Stop of evolution of scalar field when neutrinos become non-relativistic
- Transition from scaling solution to (almost) cosmological constant

# connection between dark energy and neutrino properties

$$[\rho_h(t_0)]^{\frac{1}{4}} = 1.27 \left( \frac{\gamma m_\nu(t_0)}{eV} \right)^{\frac{1}{4}} 10^{-3} eV$$

L.Amendola,  
M.Baldi, ...

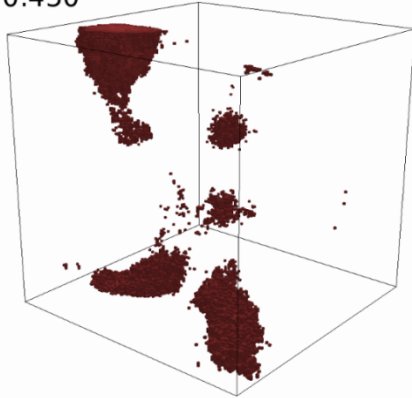
present dark energy density given by neutrino mass

present equation  
of state given by  
neutrino mass !

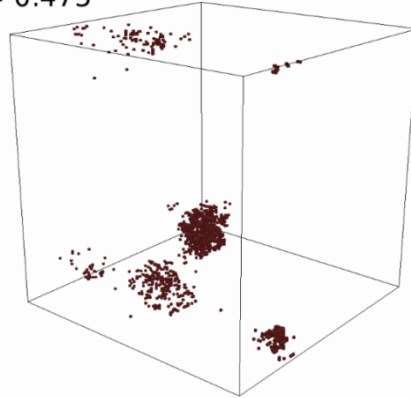
$$w_0 \approx -1 + \frac{m_\nu(t_0)}{12eV}$$

# Oscillating neutrino lumps

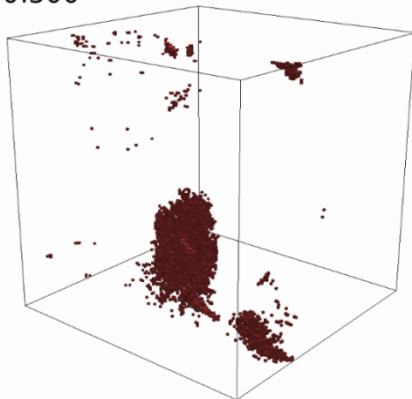
$a = 0.450$



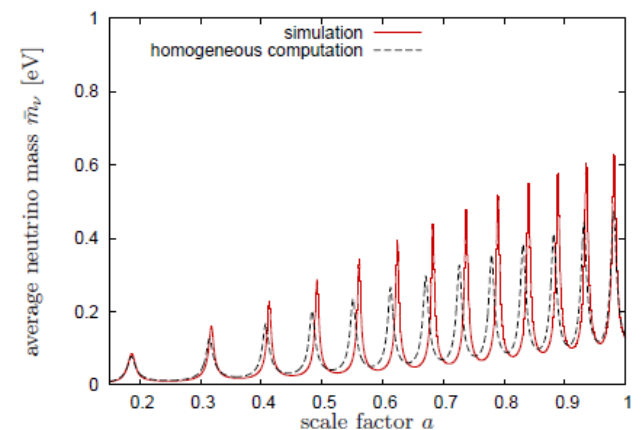
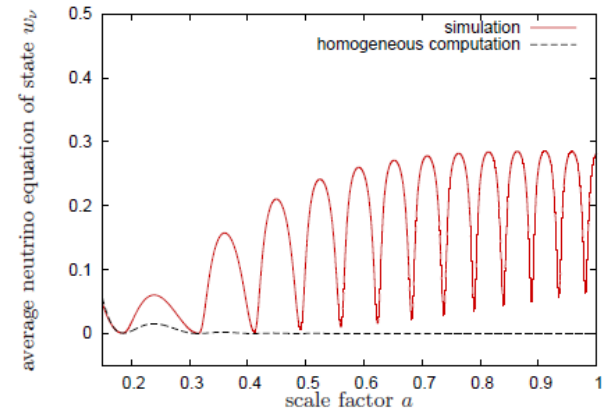
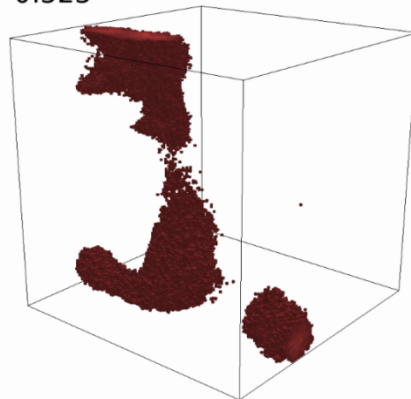
$a = 0.475$



$a = 0.500$



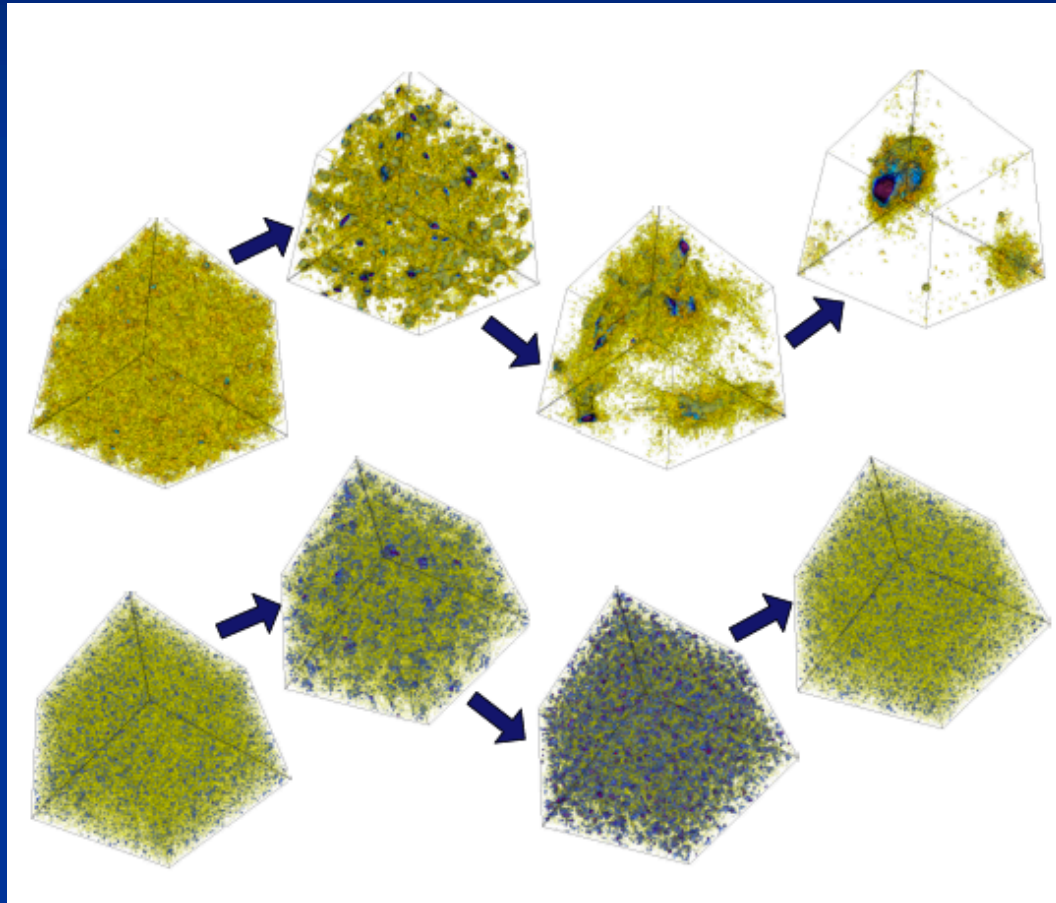
$a = 0.525$



Y.Ayaita, M.Weber,...

Ayaita, Baldi, Fuehrer,  
Puchwein,...

# Neutrino lumps

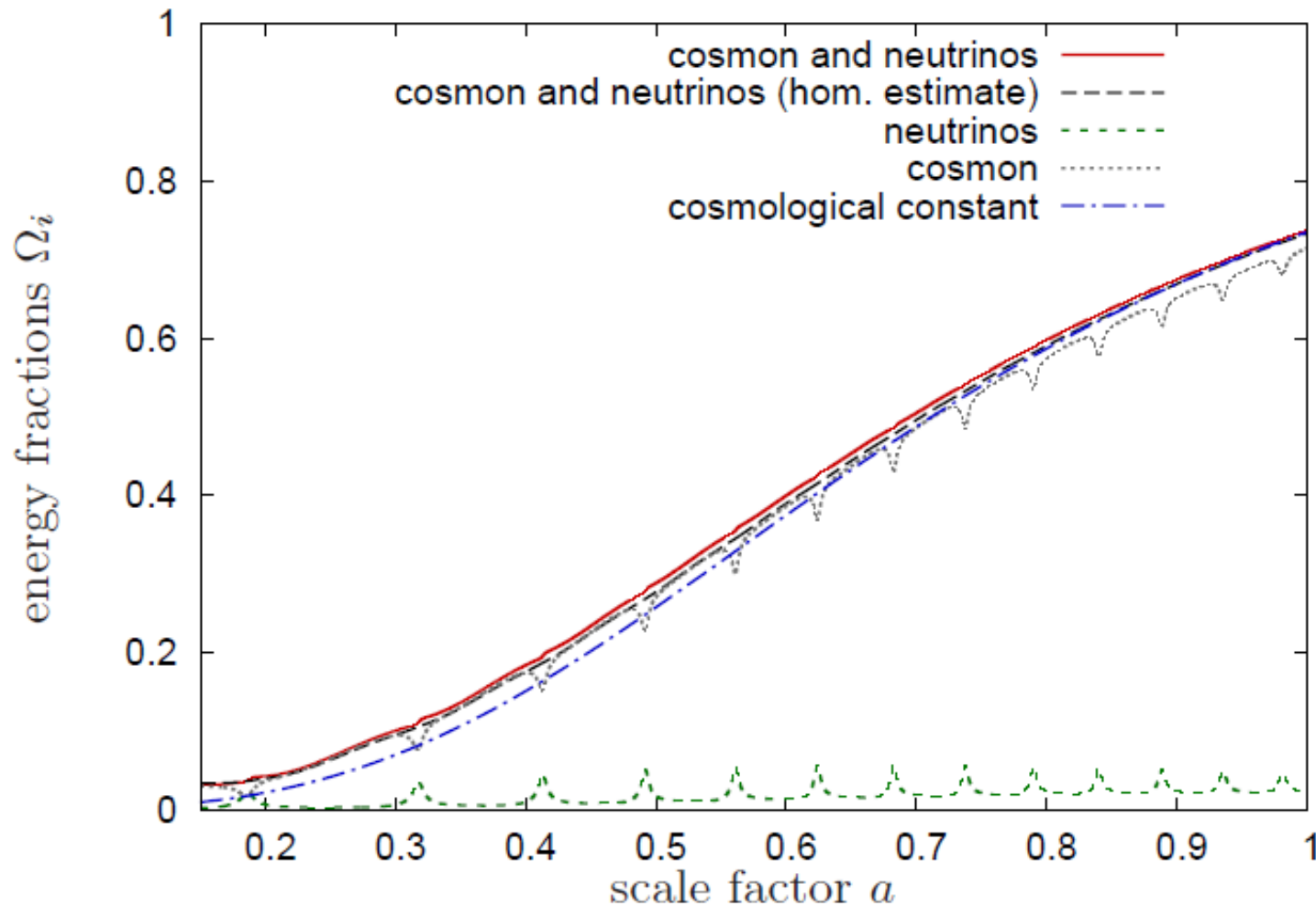


large  $m_\nu$

small  $m_\nu$

Casas, Pettorino,...

# Evolution of dark energy similar to $\Lambda$ CDM



# Conclusions

Quantum gravity may be observable in  
dynamics of present Universe

Fixed points and scale symmetry crucial

Big bang singularity is artefact  
of inappropriate choice of field variables –  
no physical singularity

# Compatibility with observations and possible tests

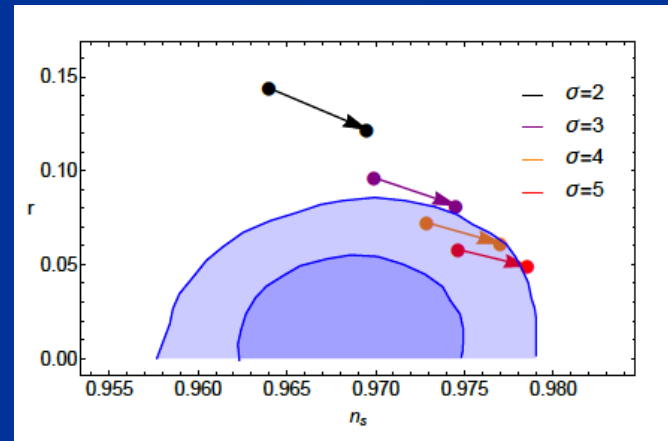
- Realistic inflation model
- Almost same prediction for radiation, matter, and Dark Energy domination as  $\Lambda$ CDM
- Presence of small fraction of Early Dark Energy
- Large neutrino lumps

# Simplicity

simple description of **all** cosmological epochs

natural incorporation of Dark Energy :

- inflation
- Early Dark Energy
- present Dark Energy dominated epoch



J.Rubio...

end

**No small parameter for  
dark energy**

# Four-parameter model

- model has four dimensionless parameters
- three in kinetic :
  - $\sigma \sim 2.5$
  - $\kappa \sim 0.5$
  - $c_t \sim 14$  ( or  $m/\mu$  )
- one parameter for growth rate of neutrino mass over electron mass :  $\gamma \sim 8$
- + standard model particles and dark matter : sufficient for realistic cosmology from inflation to dark energy
- no more free parameters than  $\Lambda$ CDM

# asymptotically vanishing cosmological „constant“

- What matters : Ratio of potential divided by fourth power of Planck mass

$$\frac{V}{\chi^4} = \frac{\mu^2 \chi^2}{\chi^4} = \frac{\mu^2}{\chi^2}$$

$$V = \mu^2 \chi^2$$

- vanishes for  $\chi \rightarrow \infty$  !

# small dimensionless number ?

- needs two intrinsic mass scales
- standard approach :  $V$  and  $M$  ( cosmological constant and Planck mass )
- variable gravity : Planck mass moving to infinity , with fixed  $V$  → ratio vanishes asymptotically !

# Einstein frame

Weyl scaling :

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu} , \quad \varphi = \frac{2M}{\alpha} \ln \left( \frac{\chi}{\mu} \right)$$

effective action in Einstein frame :

$$\Gamma = \int_x \sqrt{g'} \left\{ -\frac{1}{2} M^2 R' + V'(\varphi) + \frac{1}{2} k^2(\varphi) \partial^\mu \varphi \partial_\mu \varphi \right\}$$

$$V'(\varphi) = M^4 \exp \left( -\frac{\alpha \varphi}{M} \right)$$

$$k^2 = \frac{\alpha^2 B}{4}$$

# Quintessence

Dynamical dark energy ,  
generated by scalar field (cosmon )

C.Wetterich,Nucl.Phys.B302(1988)668, 24.9.87  
P.J.E.Peebles,B.Ratra,ApJ.Lett.325(1988)L17, 20.10.87

**Prediction :**

**homogeneous dark energy  
influences recent cosmology**

**- of same order as dark matter -**

Original models do not fit the present observations  
.... modifications  
( different growth of neutrino mass )

*In quantum gravity,  
the graviton fluctuations can  
play an important role on  
distances as large as the  
size of the Universe*

- for long range scalar fields and dynamical dark energy
- not for all quantities

# Instability of graviton propagator

effective action

$$\Gamma = \int_x \sqrt{g} \left( -\frac{M^2}{2} R + V \right)$$

flat space:

$$G^{-1} = \frac{M^2 q^2}{4} - \frac{V}{2}$$

Instability for  $V > 0$  : "tachyonic mass term"

$$-\frac{2V}{M^2}$$

curved space:

$$G^{-1} = \sqrt{g} \left\{ \frac{M^2}{4} \left( -D^2 + \frac{2R}{3} \right) - \frac{V}{2} \right\}$$

# Graviton barrier

Quantum gravity computation :

For  $\chi \rightarrow \infty$

$V$  cannot increase stronger than  $M^2$  !

Instability of graviton propagator is avoided

# Graviton barrier and solution of the cosmological constant problem

$V$  cannot increase stronger than  $M^2$  !

If  $M$  increases with  $\chi$ , and for cosmological solutions where  $\chi$  asymptotically diverges for time going to infinity:

Effective cosmological constant vanishes in infinite future

$$M = \chi \quad : \quad V = \mu^2 \chi^2$$

end

# Amplitude of density fluctuations

small because of logarithmic running  
near UV fixed point !

$$\mathcal{A} = \frac{(N+3)^3}{4} e^{-2c_t}$$

$$c_t = \ln \left( \frac{m}{\mu} \right) = 14.1. \quad \sigma=1$$

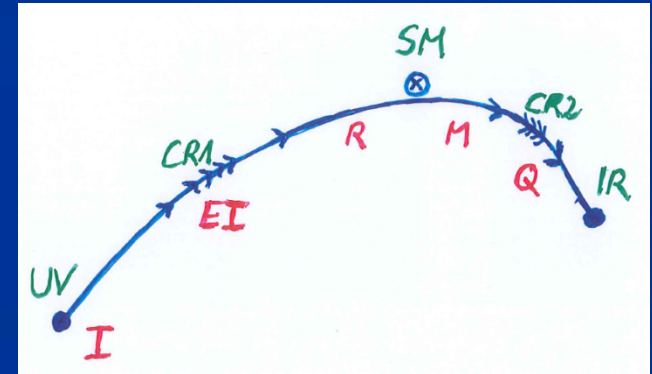
$$\frac{m}{\mu} = \frac{(N+3)^{\frac{3}{2}}}{2\sqrt{\mathcal{A}}} = 1.32 \cdot 10^6 \left( \frac{N}{60} \right)^{\frac{3}{2}}$$

$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[ \ln \left( \frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left( \frac{\chi}{m} \right)$$

N : number of e – foldings at horizon crossing

# Origin of mass

- UV fixed point : scale symmetry unbroken  
all particles are massless
- IR fixed point :  
scale symmetry spontaneously broken,  
massive particles , massless dilaton
- crossover : explicit mass scale  $\mu$  important
- approximate SM fixed point : approximate scale symmetry  
spontaneously broken, massive particles , almost massless  
cosmon, tiny cosmon potential



# On shell graviton propagator

$$G^{-1} = \sqrt{g} \left\{ \frac{M^2}{4} \left( -D^2 + \frac{2R}{3} \right) - \frac{V}{2} \right\}$$

on shell :

( for solution of field equations )

$$R = \frac{4V}{M^2}$$

homogenous isotropic metric,  
conformal time

$$g_{\mu\nu} = a^2(\eta) \delta_{\mu\nu} \quad \mathcal{H} = \frac{\partial \ln a}{\partial \eta}$$

inverse graviton  
propagator in  
de Sitter space

$$a^{-2} \left( -D^2 + \frac{R}{6} \right) a^2 = \frac{1}{a^2} (\partial_\eta^2 + 2\mathcal{H}\partial_\eta + \vec{q}^2)$$

milder instability, not tachyonic, absent for  
cosmologies close to de Sitter space

# IR – instability for graviton fluctuations

problem solved ?

- yes for primordial cosmic fluctuations ( on shell )
- no for quantum gravity ( off shell )
- Computation of effective action is an off-shell problem.
- example : one needs the effective potential for the Higgs field in the vicinity of its minimum ( off shell ), not only at the minimum ( on shell )

# Quantum gravity with scalar field

$M^2$  and  $V$  depend on scalar field  $\chi$

$$M^2 = c_1 + c_2 \chi^2$$

$$V = d_1 + d_2 \chi^2 + d_3 \chi^4$$

question : behavior of  $V$  for  $\chi \rightarrow \infty$

- $d_3 \neq 0$  excluded!
- $d_3 < 0$  unstable potential
- $d_3 > 0$  instability of graviton propagator