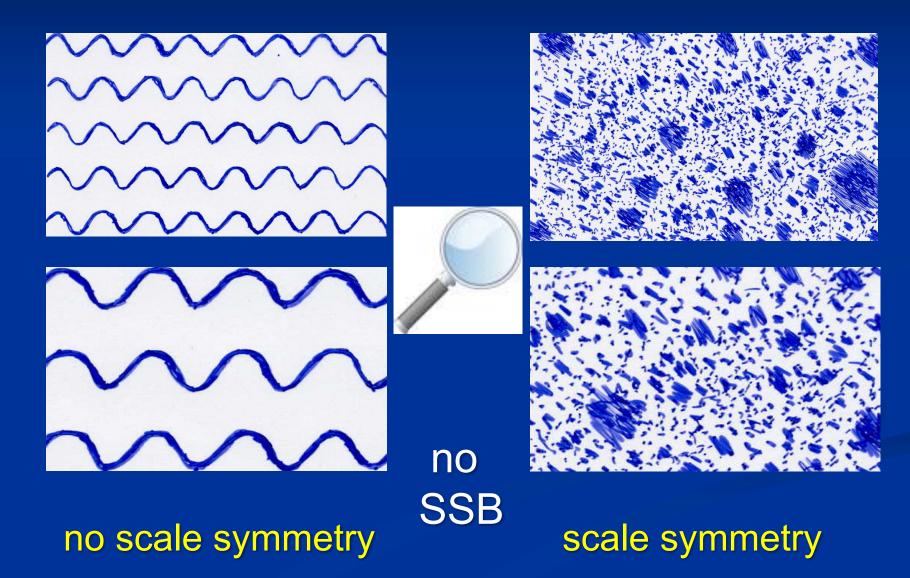
Scale symmetry

cosmology

11

Scale symmetry



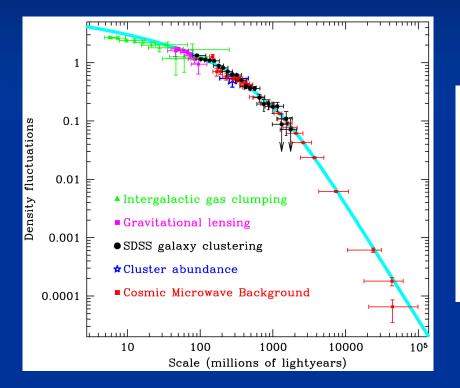
Scale symmetry

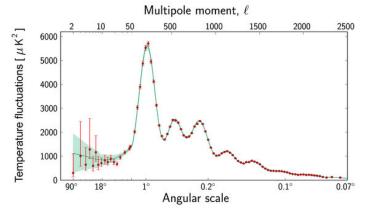
No parameter with dimension of length or mass is present in effective action.

Then invariance under dilatations or global scale transformations is realized.

Continuous global symmetry

Scale symmetry in cosmology ?





scales are present in cosmology

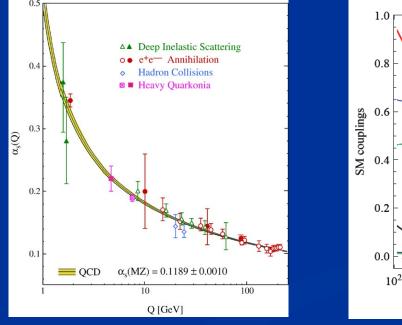
Scale symmetry in elementary particle physics ?

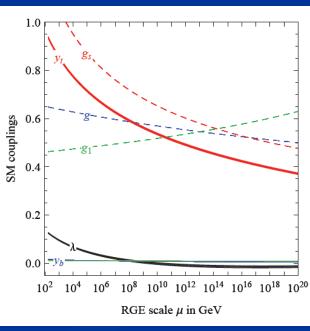
proton mass, electron mass

scales are present in particle physics

Quantum fluctuations induce running couplings

violation of scale symmetrywell known in QCD or standard model

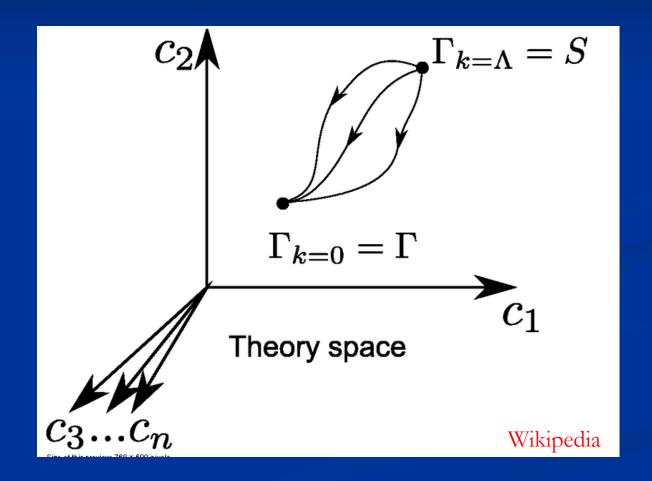




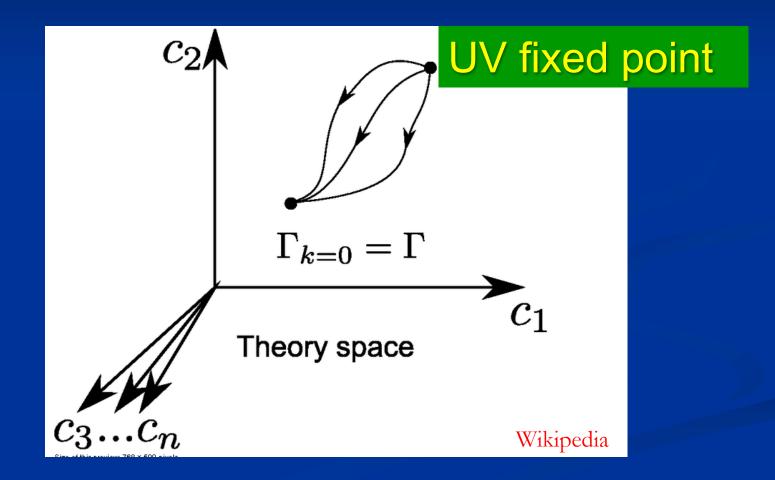
Quantum scale symmetry

quantum fluctuations violate scale symmetry
running dimensionless couplings
at fixed points , scale symmetry is exact !
quantum fluctuations can generate scale symmetry !

Functional renormalization : flowing action



Ultraviolet fixed point



Asymptotic safety of quantum gravity

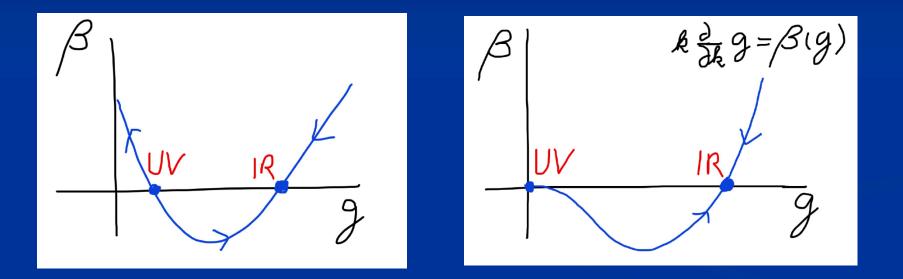
if UV fixed point exists :

quantum gravity is

non-perturbatively renormalizable !

S. Weinberg, M. Reuter

Asymptotic safety Asymptotic freedom



Relevant parameters yield undetermined couplings. Quartic scalar coupling is not relevant and can therefore be predicted.

a prediction...

Asymptotic safety of gravity and the Higgs boson mass

Mikhail Shaposhnikov

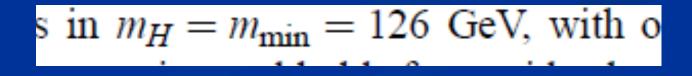
Institut de Théorie des Phénomènes Physiques, École Polytechnique Fédérale de Lausanne, CH-1015 Lausanne, Switzerland

Christof Wetterich

Institut für Theoretische Physik, Universität Heidelberg, Philosophenweg 16, D-69120 Heidelberg, Germany 12 January 2010

Abstract

There are indications that gravity is asymptotically safe. The Standard Model (SM) plus gravity could be valid up to arbitrarily high energies. Supposing that this is indeed the case and assuming that there are no intermediate energy scales between the Fermi and Planck scales we address the question of whether the mass of the Higgs boson m_H can be predicted. For a positive gravity induced anomalous dimension $A_{\lambda} > 0$ the running of the quartic scalar self interaction λ at scales beyond the Planck mass is determined by a fixed point at zero. This results in $m_H = m_{\min} = 126$ GeV, with only a few GeV uncertainty. This prediction is independent of the details of the short distance running and holds for a wide class of extensions of the SM as well.



quantum gravity with scalar field – the role of scale symmetry for cosmology Spontaneous breaking of scale symmetry

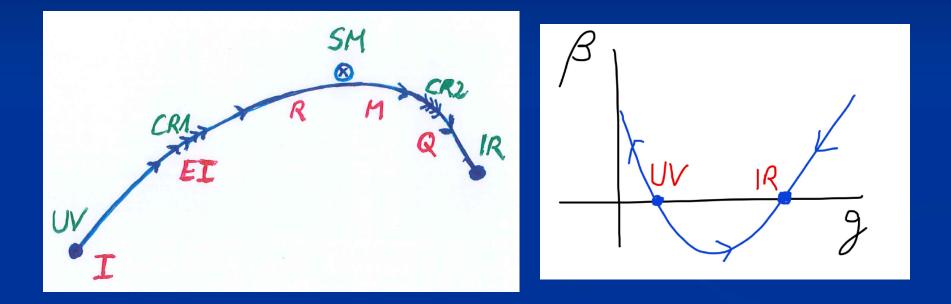
- expectation value of scalar field breaks scale symmetry spontaneously
- massive particles are compatible with scale symmetry
- in presence of massive particles : sign of exact scale symmetry is exactly massless Goldstone boson – the dilaton

Approximate scale symmetry near fixed points

UV : approximate scale invariance of primordial fluctuation spectrum from inflation

 IR : cosmon is pseudo Goldstone boson of spontaneously broken scale symmetry, tiny mass,
 responsible for dynamical Dark Energy

Possible consequences of crossover in quantum gravity



Realistic model for inflation and dark energy with single scalar field

variable gravity

"Newton's constant is not constant – and particle masses are not constant"

Variable Gravity

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2}\chi^2 R + \mu^2 \chi^2 + \frac{1}{2} \left(B(\chi/\mu) - 6 \right) \partial^\mu \chi \partial_\mu \chi \right\}$$

quantum effective action, variation yields field equations

Einstein gravity : $\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} M^2 R \right\}$

Scale symmetry in variable gravity (IR – fixed point)

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2}\chi^2 R + \mu^2 \chi^2 + \frac{1}{2} \left(B(\chi/\mu) - 6 \right) \partial^\mu \chi \partial_\mu \chi \right\}$$

quantum effective action, variation yields field equations

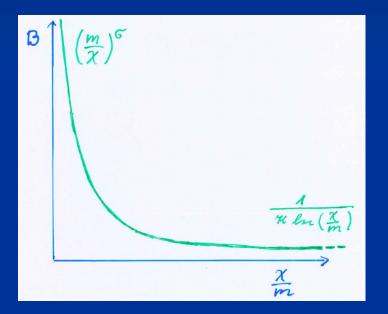
Einstein gravity : $\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} M^2 R \right\}$

Variable Gravity

- Scalar field coupled to gravity
- Effective Planck mass depends on scalar field
- Simple quadratic scalar potential involves intrinsic mass μ
- Nucleon and electron mass proportional to dynamical Planck mass

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} \left(B(\chi/\mu) - 6 \right) \partial^\mu \chi \partial_\mu \chi \right\}$$

Kinetial B : Crossover between two fixed points



assumption: running coupling obeys flow equation

$$\mu \frac{\partial B}{\partial \mu} = \frac{\kappa \sigma B^2}{\sigma + \kappa B}$$

$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[\ln \left(\frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left(\frac{\chi}{m} \right)$$

m : scale of crossover can be exponentially larger than intrinsic scale μ

Four-parameter model

- model has four dimensionless parametersthree in kinetial :
 - $\sigma \sim 2.5$
 - $\varkappa \sim 0.5$
 - $\mathbf{c}_{\mathrm{t}} \sim 14 \quad (\text{ or } m/\mu)$
- one parameter for growth rate of neutrino mass over electron mass : $\gamma \sim 8$
- + standard model particles and dark matter : sufficient for realistic cosmology from inflation to dark energy
- no more free parameters than ΛCDM

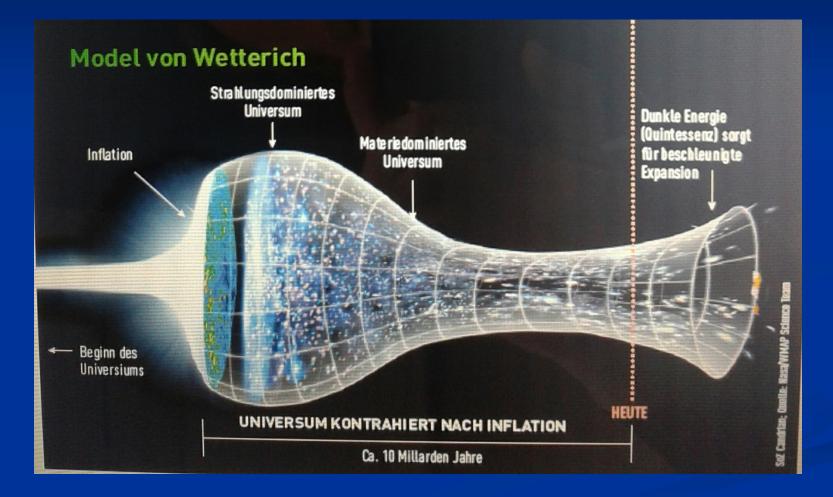
Model is compatible with present observations

Together with variation of neutrino mass over electron mass in present cosmological epoch : model is compatible with all present observations, including inflation and dark energy

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2}\chi^2 R + \mu^2 \chi^2 + \frac{1}{2} \left(B(\chi/\mu) - 6 \right) \partial^\mu \chi \partial_\mu \chi \right\}$$

$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[\ln \left(\frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left(\frac{\chi}{m} \right)$$

Strange evolution of Universe



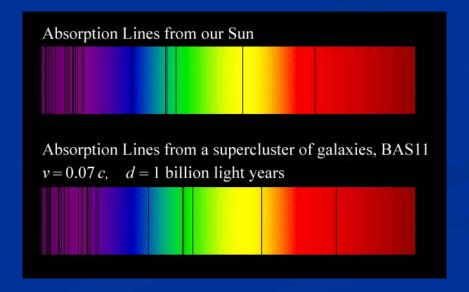
Sonntagszeitung Zürich, Laukenmann

Expanding Universe or shrinking atoms?

Hot big bang or freeze ?

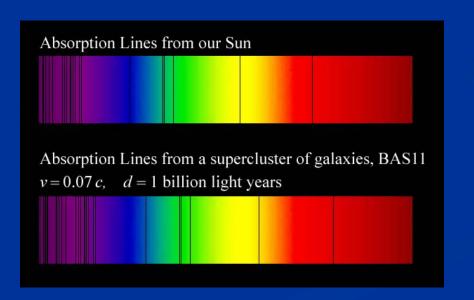
Do we know that the Universe expands ?

instead of redshift due to expansion : smaller frequencies have been emitted in the past, because electron mass was smaller !



Why do we see redshift of photons emitted in the distant past ?

photons are more red because they have been emitted with longer wavelength



frequency ~ mass

wavelength ~ atomsize

What is increasing ?

Ratio of distance between galaxies over size of atoms !

atom size constant : expanding geometry

alternative : shrinking size of atoms

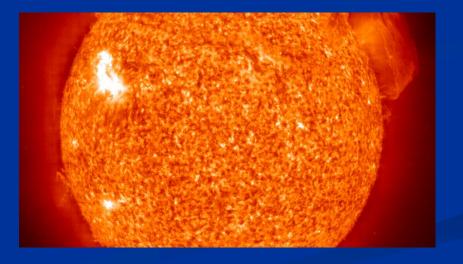
How can particle masses change with time ?

- Particle masses are proportional to scalar field χ.
 Similar to Higgs field.
- Scalar field varies with time.
- Ratios of particle masses are independent of χ and therefore remain constant.
- Compatibility with observational bounds on time dependence of particle mass ratios.
- \blacksquare Dimensionless couplings are independent of χ .

Do we know that the temperature was higher in the early Universe than now ?

Cosmic microwave radiation, nucleosynthesis

instead of higher temperature : smaller particle masses



Hot plasma?

Temperature in radiation dominated Universe : T ~ χ^{1/2} smaller than today
Ratio temperature / particle mass : T /m_p ~ χ^{-1/2} larger than today
T/m_p counts ! This ratio decreases with time.

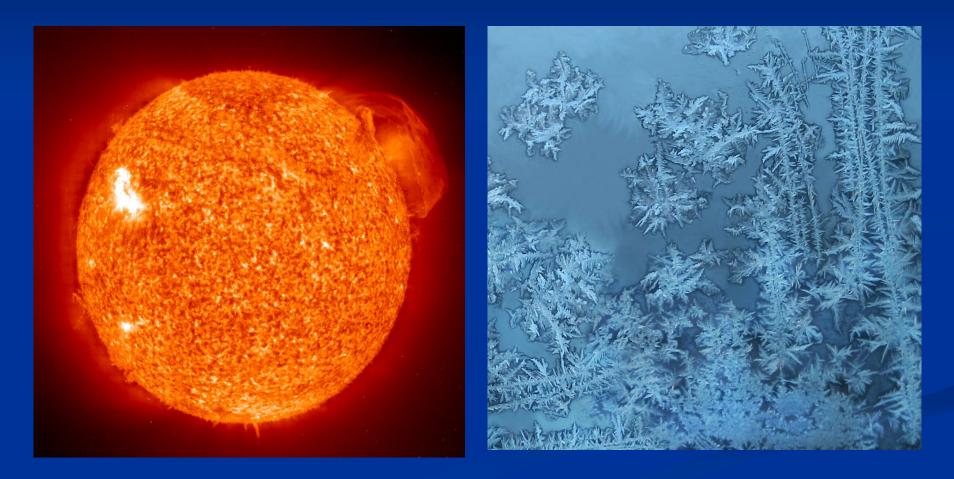
Nucleosynthesis, CMB emission as in standard cosmology !

Freeze Universe

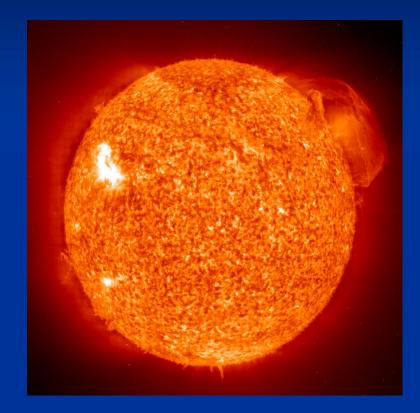
The Universe may have started very cold, and only later heat up.

Freeze picture of the Universe

Big bang or freeze ?



Big bang or freeze ?





freeze picture : only rods for measurements (masses) are different !

Big bang is not wrong,

but alternative pictures exist !

Einstein frame

"Weyl scaling" maps variable gravity model to Universe with fixed masses and standard expansion history.

Exact equivalence of different frames !
 " different pictures"

Standard gravity coupled to scalar field.

Einstein frame

Weyl scaling :

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu} , \ \varphi = \frac{2M}{\alpha} \ln\left(\frac{\chi}{\mu}\right)$$

effective action in Einstein frame :

$$\Gamma = \int_{x} \sqrt{g'} \left\{ -\frac{1}{2} M^2 R' + V'(\varphi) + \frac{1}{2} k^2(\varphi) \partial^{\mu} \varphi \partial_{\mu} \varphi \right\}$$

$$V'(\varphi) = M^4 \exp\left(-\frac{\alpha\varphi}{M}\right)$$

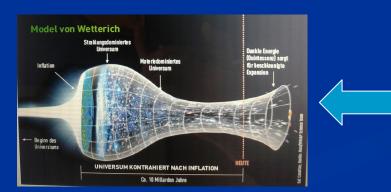
$$k^2 = \frac{\alpha^2 B}{4}$$

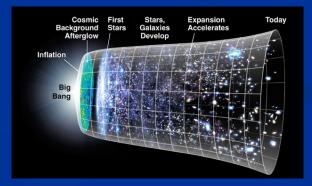
Field relativity

Weyl scaling :

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu}$$

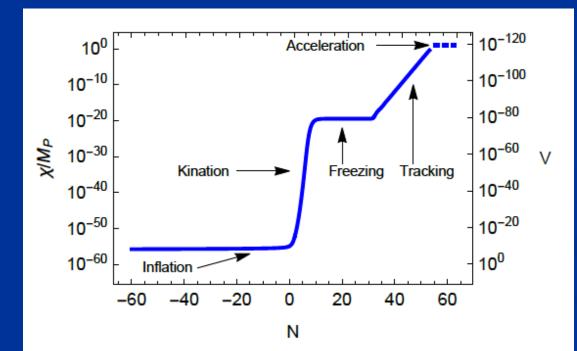
changes geometry, not a coordinate transformation





Cosmological solution

scalar field χ vanishes in the infinite past
 scalar field χ diverges in the infinite future



J.Rubio,...

Field relativity : different pictures of cosmology

- same physical content can be described by different pictures
- related by field redefinitions , e.g. Weyl scaling , conformal scaling of metric
 observables cannot depend on choice of fields
 metric is one of the fields
 which picture is usefull ?

Relativity of geometry

Euclid ... Newton : space and time are absolute



 Special relativity : space and time depend on observer
 General relativity : space-time is influenced by matter (including radiation) geometry is independent of coordinates geometry is observable
 Field relativity : geometry is relative Space-time is a description of correlations between "matter".

Observables cannot depend on choice of fields used to describe them.

Different pictures for geometry exist.

Why should you care about the freeze picture of the Universe ?

Some aspects are understood easier :

Natural tiny present dark energy
Beginning of Universe
Role of scale symmetry
Range of impact of quantum gravity

What is Dark Energy ?

Dark energy is energy density of scalar field χ

 $\rho = V + kinetic term$

 $V = \mu^2 \chi^2$

p = -V + kinetic term

Dark energy is dynamical if χ changes with time

No small parameter for dark energy

Four-parameter model

- model has four dimensionless parametersthree in kinetial :
 - $\sigma \sim 2.5$
 - $\varkappa \sim 0.5$
 - $\mathbf{c}_{\mathrm{t}} \sim 14 \quad (\text{ or } m/\mu)$
- one parameter for growth rate of neutrino mass over electron mass : $\gamma \sim 8$
- + standard model particles and dark matter : sufficient for realistic cosmology from inflation to dark energy
- no more free parameters than ΛCDM

asymptotically vanishing cosmological "constant"

What matters : Ratio of potential divided by fourth power of Planck mass

$$\frac{V}{\chi^4} = \frac{\mu^2 \chi^2}{\chi^4} = \frac{\mu^2}{\chi^2}$$

 $V = \mu^2 \chi^2$

 \square vanishes for $\chi \rightarrow \infty$!

small dimensionless number?

needs two intrinsic mass scales
 standard approach :V and M (cosmological constant and Planck mass)
 variable gravity : Planck mass moving to infinity , with fixed or moderately increasing V
 ratio vanishes asymptotically !

Quintessence

Dynamical dark energy, generated by scalar field (cosmon)

C.Wetterich,Nucl.Phys.B302(1988)668, 24.9.87 P.J.E.Peebles,B.Ratra,ApJ.Lett.325(1988)L17, 20.10.87



homogeneous dark energy influences recent cosmology

- of same order as dark matter -

Original models do not fit the present observations modifications (different growth of neutrino mass) No tiny dimensionless parameters (except gauge hierarchy)

• one mass scale $\mu = 2 \cdot 10^{-33} \text{ eV}$

• one time scale $\mu^{-1} = 10^{10} \text{ yr}$

Planck mass does not appear as parameter
Planck mass grows large dynamically
Dark energy is tiny because Universe is old

Slow Universe

Asymptotic solution in freeze frame :

$$H = \frac{\mu}{\sqrt{3}} , \ \chi = \frac{3^{\frac{1}{4}}m}{2\sqrt{\mu}} (t_c - t)^{-\frac{1}{2}}$$

 $\mu = 2 \cdot 10^{-33} \, \text{eV}$

Expansion or shrinking always slow , characteristic time scale of the order of the age of the Universe : t_{ch} ~ µ⁻¹ ~ 10 billion years !
Hubble parameter of the order of present Hubble parameter for all times , including inflation and big bang !
Slow increase of particle masses !

infinite past

Infinite past : slow inflation

$\sigma = 2$: field equations

$$\ddot{\chi} + \left(3H + \frac{1}{2}\frac{\dot{\chi}}{\chi}\right)\dot{\chi} = \frac{2\mu^2\chi^2}{m} \qquad H = \sqrt{\frac{\mu^2}{3} + \frac{m\dot{\chi}^2}{6\chi^3}} - \frac{\dot{\chi}}{\chi}$$

approximative solution

$$H = \frac{\mu}{\sqrt{3}} , \ \chi = \frac{3^{\frac{1}{4}}m}{2\sqrt{\mu}} (t_c - t)^{-\frac{1}{2}}$$

1

particles become massless in infinite past !

Eternal Universe

Asymptotic solution in freeze frame :

$$H = \frac{\mu}{\sqrt{3}} , \ \chi = \frac{3^{\frac{1}{4}}m}{2\sqrt{\mu}} (t_c - t)^{-\frac{1}{2}}$$

solution valid back to the infinite past in physical time
 no singularity

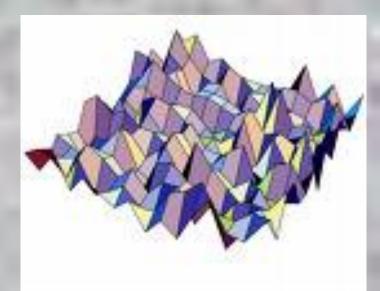
physical time to infinite past is infinite

Eternal light-vacuum

Everywhere almost nothing only fluctuations

All particles move with light velocity, similar to photons

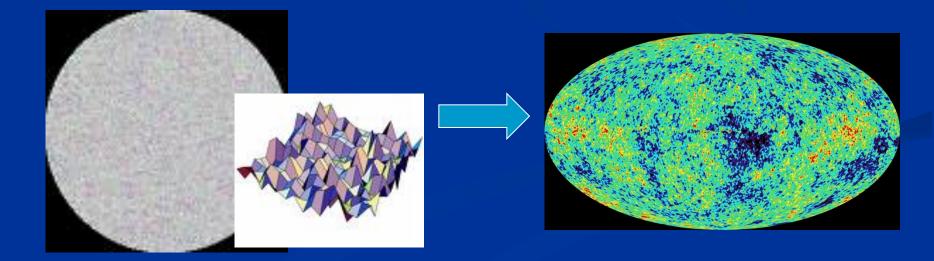
strength of gravity much stronger than today



In the beginning was light-like emptiness.

Eternal light-vacuum is unstable

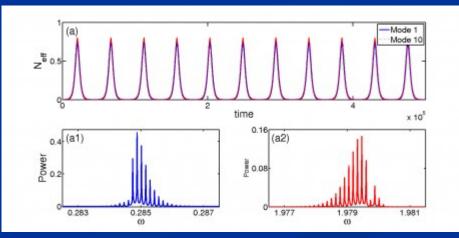
- Slow increase of particle masses and weakening of gravity
- Only slow change of space-time geometry
- Consequence for observation : primordial fluctuations become visible in cosmic background radiation
- We see fluctuations in a stage 5000 billion years ago.



Physical time

count oscillations





Physical time

field equation for scalar field mode

$$(\partial_{\eta}^2 + 2Ha\partial_{\eta} + k^2 + a^2m^2)\varphi_k = 0$$

$$\varphi_k = \frac{\tilde{\varphi}_k}{a} \left\{ \partial_\eta^2 + k^2 + a^2 \left(m^2 - \frac{R}{6} \right) \right\} \tilde{\varphi}_k = 0$$

determine physical time by counting number of oscillations

$$\tilde{t}_p = n_k$$

$$n_k = \frac{k\eta}{\pi}$$

(m=0)

Physical time

counting : discrete
invariant under field transformations
same in all frames

Big bang singularity in Einstein frame is field singularity !

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu} , \ \varphi = \frac{2M}{\alpha} \ln\left(\frac{\chi}{\mu}\right)$$

choice of frame with constant particle masses is not well suited if physical masses go to zero !

Field - singularity

 Big Bang is field - singularity
 similar (but not identical with) coordinate - singularity

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu}$$





Conclusions

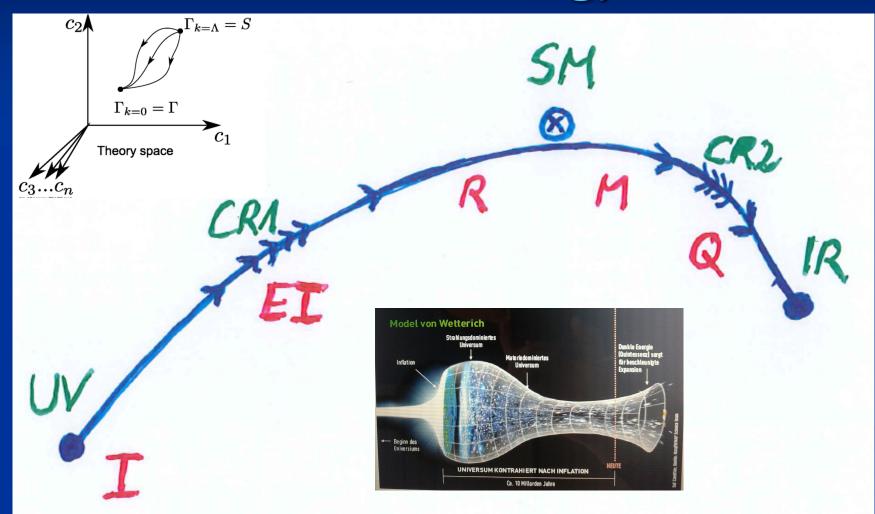
Quantum gravity may be observable in dynamics of present Universe

Fixed points and scale symmetry crucial

Big bang singularity is artefact of inappropriate choice of field variables – no physical singularity

end

Crossover in quantum gravity and cosmology



Cosmological solution : crossover from UV to IR fixed point

Dimensionless functions as B depend only on ratio μ/χ.
IR: μ→0 , χ→∞
UV: μ→∞ , χ→0

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2}\chi^2 R + \mu^2 \chi^2 + \frac{1}{2} \left(B(\chi/\mu) - 6 \right) \partial^\mu \chi \partial_\mu \chi \right\}$$

Cosmology makes crossover between fixed points by variation of χ.

$$X \rightarrow 0$$

$$I$$

$$SM$$

$$SM$$

$$R$$

$$M$$

$$SM$$

$$Q$$

$$R$$

$$R$$

$$M$$

$$Q$$

$$R$$

$$Q$$

$$X$$

$$M$$

$$Q$$

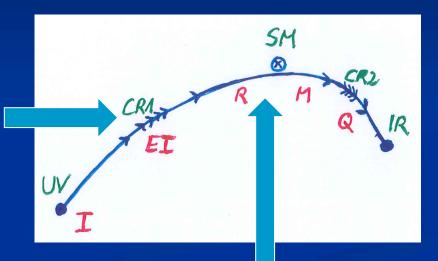
$$X$$

Renormalization flow and cosmological evolution

renormalization flow as function of μ
is mapped by dimensionless functions to
 field dependence of effective action on scalar
field χ
translates by solution of field equation to
 dependence of cosmology an time t or η

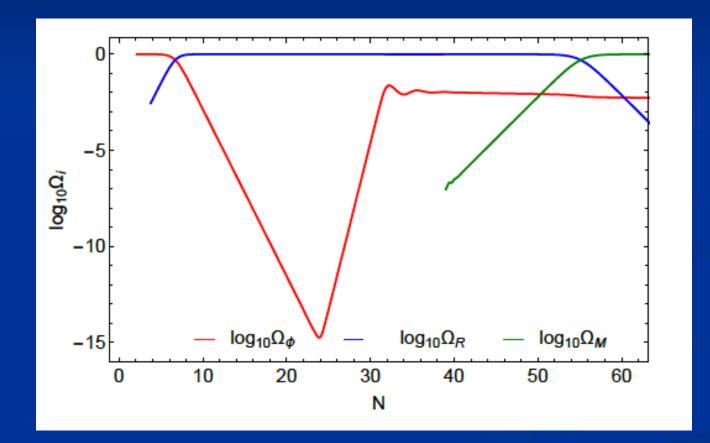
Scaling solution

after end of inflation



Dark Energy decreases similar to radiation and matter scaling solution with few percent of Early Dark Energy

Evolution of dark energy fraction



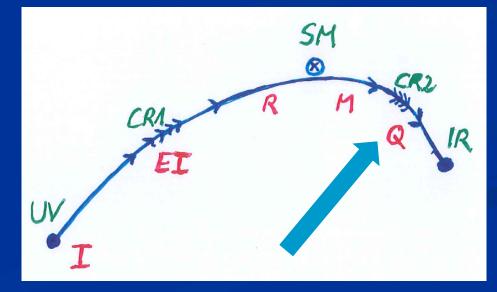
J. Rubio,...

Growing neutrino masses and quintessence

Second stage of crossover

■ from SM to IR

in sector Beyond Standard Model
 affects neutrino masses first (seesaw or cascade mechanism)



Varying particle masses at onset of second crossover

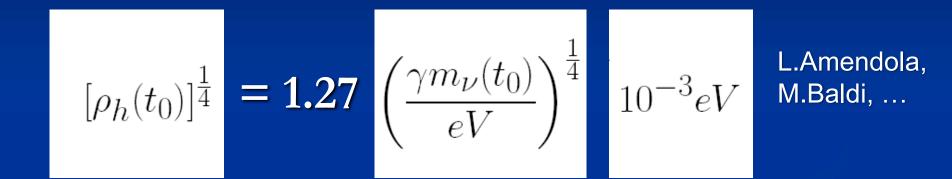
- Except for neutrinos all particle masses are proportional to χ.
- Ratios of particle masses remain constant.
- Compatibility with observational bounds on time dependence of particle mass ratios.
- Neutrino masses show stronger increase with χ, such that ratio neutrino mass over electron mass grows.

Cosmic trigger

Stop of evolution of scalar field when neutrinos become non-relativistic

 Transition from scaling solution to (almost) cosmological constant

connection between dark energy and neutrino properties

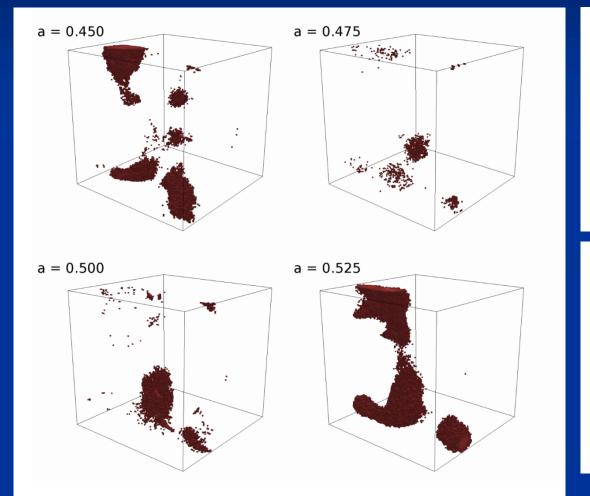


present dark energy density given by neutrino mass

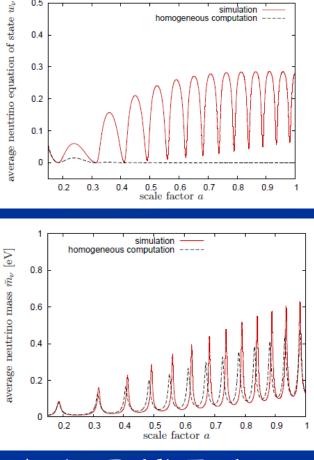
present equation of state given by neutrino mass !

$$w_0 \approx -1 + \frac{m_\nu(t_0)}{12 \text{eV}}$$

Oscillating neutrino lumps



Y.Ayaita, M.Weber,...



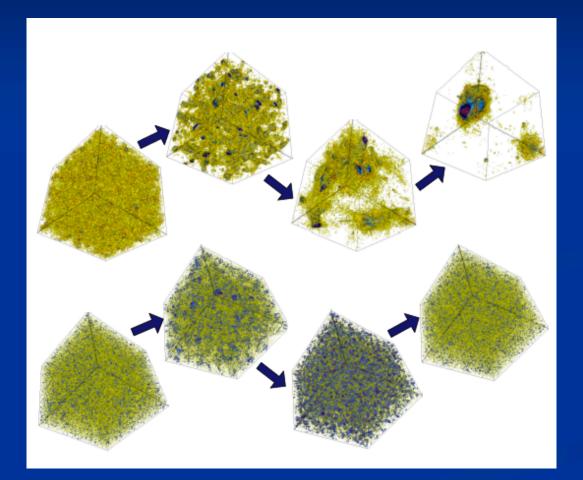
simulation

homogeneous computation

0.5

Ayaita, Baldi, Fuehrer, Puchwein,...

Neutrino lumps

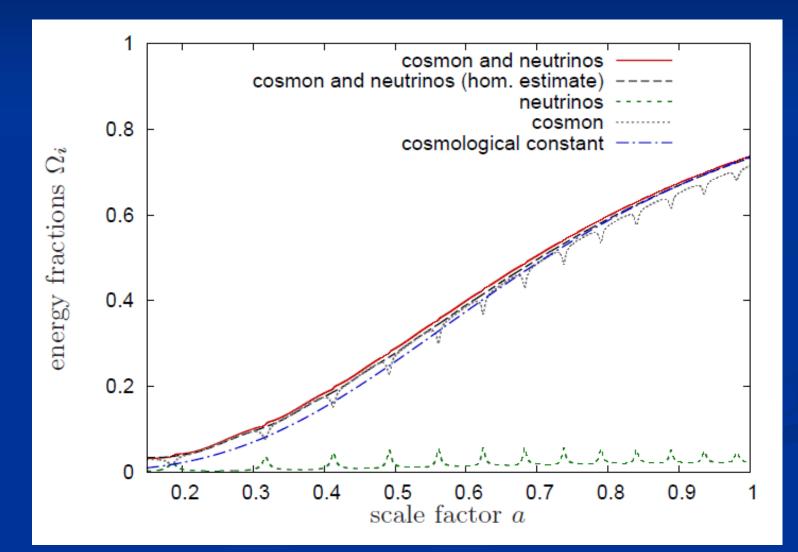


large m_{v}

small m_{ν}

Casas, Pettorino,...

Evolution of dark energy similar to ΛCDM



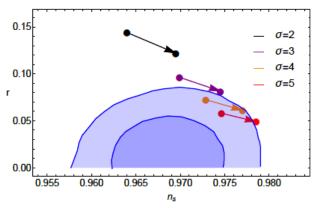
Compatibility with observations and possible tests

- Realistic inflation model
- Almost same prediction for radiation, matter, and Dark Energy domination as ACDM
- Presence of small fraction of Early Dark Energy
- Large neutrino lumps



simple description of all cosmological epochs

natural incorporation of Dark Energy: ■ inflation 0.15 Early Dark Energy 0 10 0.05 present Dark Energy 0.00 0.955 0.960 dominated epoch



J.Rubio...

In quantum gravity, the graviton fluctuations can play an important role on distances as large as the size of the Universe

for long range scalar fields and dynamical dark energy
not for all quantities

Instability of graviton propagator

effective action
$$\Gamma = \int_x \sqrt{g} \left(-\frac{M^2}{2} R + V \right)$$

flat space:
$$G^{-1} = \frac{M^2 q^2}{4} - \frac{V}{2}$$

Instability for V>0 : "tachyonic mass term"



curved space:

$$G^{-1} = \sqrt{g} \left\{ \frac{M^2}{4} \left(-D^2 + \frac{2R}{3} \right) - \frac{V}{2} \right\}$$

Graviton barrier

Quantum gravity computation :

For $\chi \to \infty$

V cannot increase stronger than M²!

Instability of graviton propagator is avoided

Graviton barrier and solution of the cosmological constant problem

V cannot increase stronger than M² !

If M increases with χ , and for cosmological solutions where χ asymptotically diverges for time going to infinity: Effective cosmological constant vanishes in infinite future

$$\mathbf{M} = \boldsymbol{\chi} : \mathbf{V} = \boldsymbol{\mu}^2 \, \boldsymbol{\chi}^2$$

Amplitude of density fluctuations

small because of logarithmic running near UV fixed point !

$$\mathcal{A} = \frac{(N+3)^3}{4} e^{-2c_t}$$

$$c_t = \ln\left(\frac{m}{\mu}\right) = 14.1.$$

<u>σ=1</u>

$$\frac{m}{\mu} = \frac{(N+3)^{\frac{3}{2}}}{2\sqrt{\mathcal{A}}} = 1.32 \cdot 10^6 \left(\frac{N}{60}\right)^{\frac{3}{2}}$$

$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[\ln \left(\frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left(\frac{\chi}{m} \right)$$

N : number of e – foldings at horizon crossing