

STRANGENESS NEUTRALITY AND THE QCD PHASE STRUCTURE

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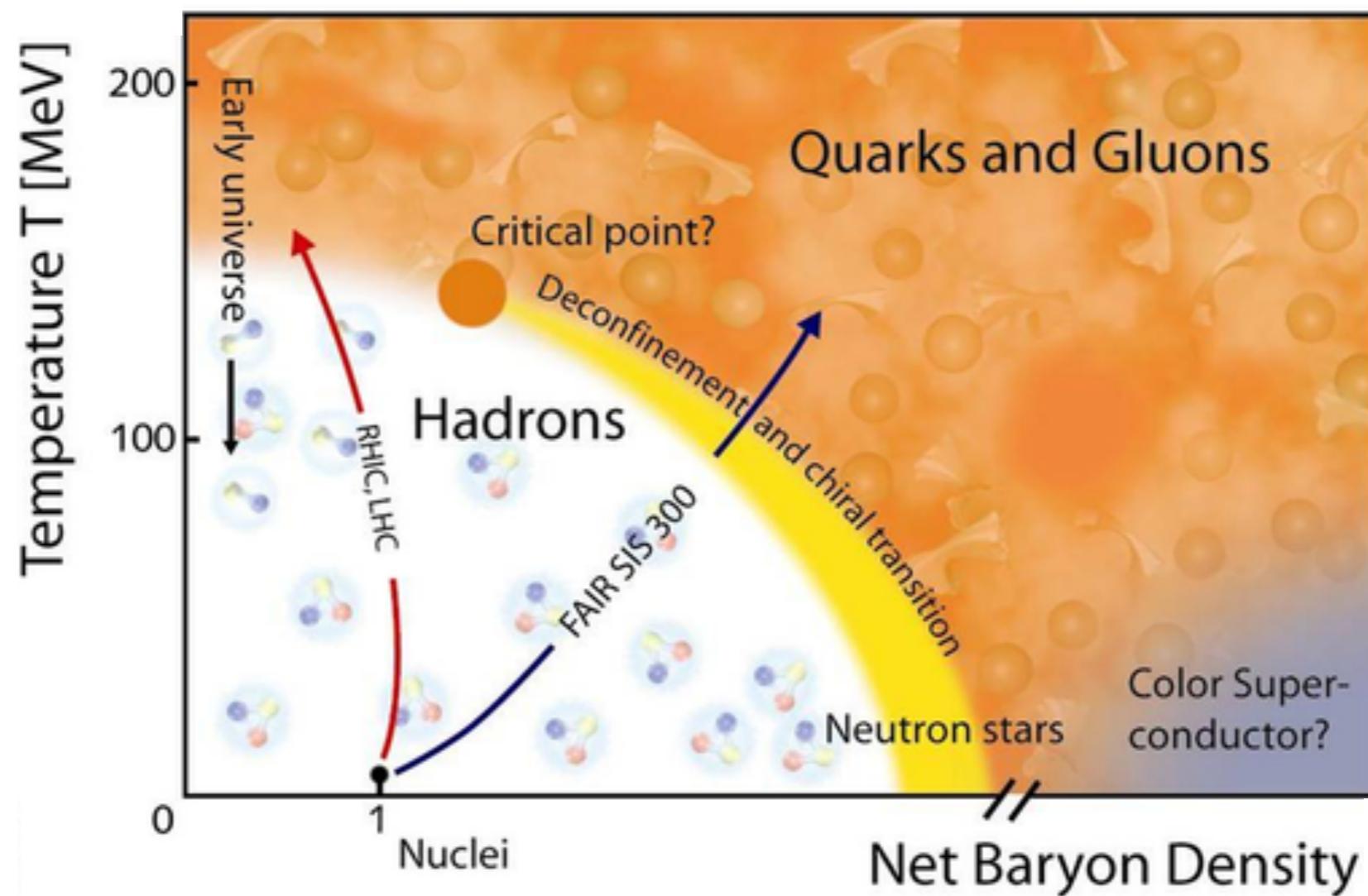
[FR, Fu, Pawłowski, work in progress]



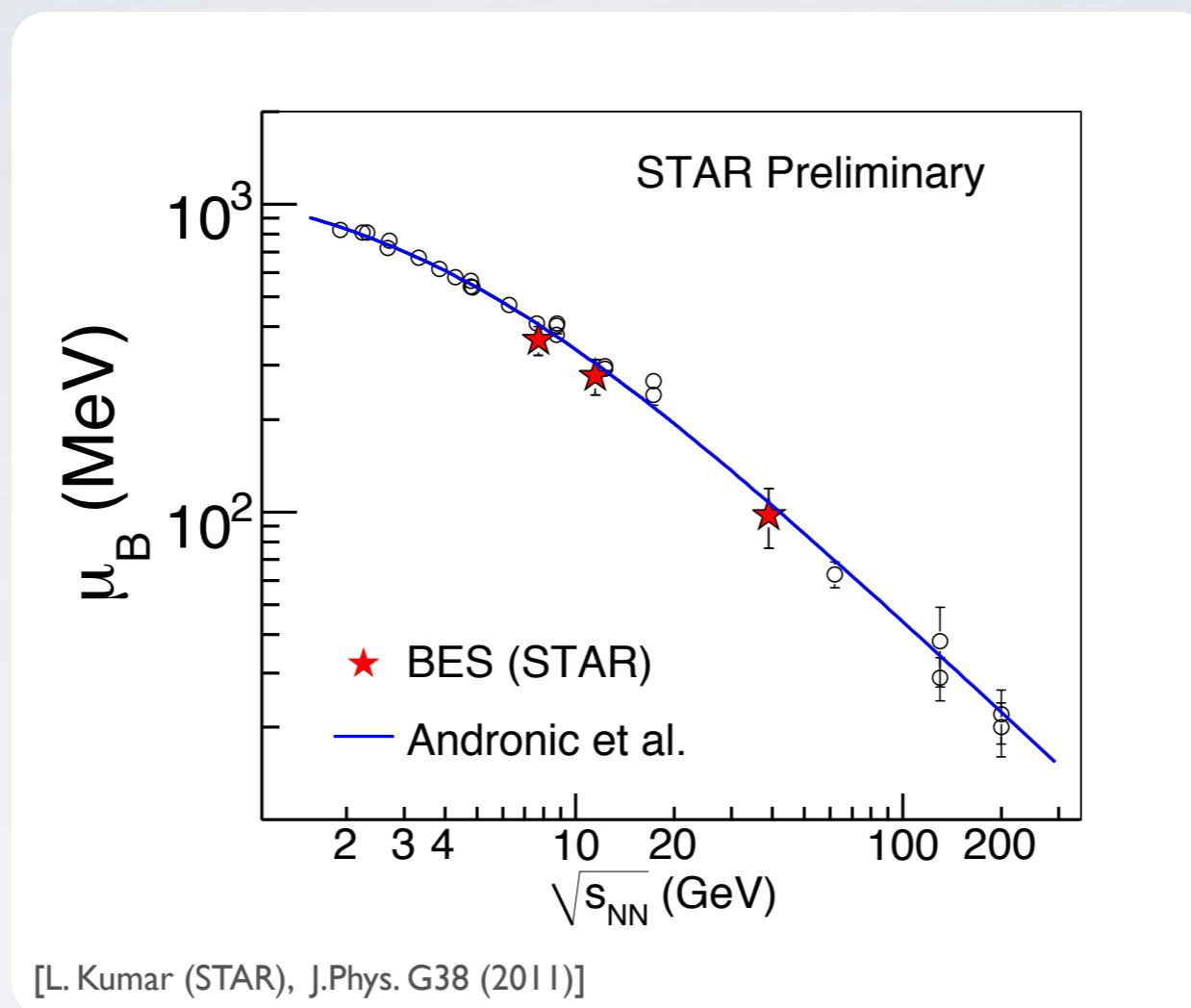
— FROM CORRELATION FUNCTIONS TO QCD PHENOMENOLOGY —

BAD HONNEF, 03/04/2018

QCD PHASE DIAGRAM



PROBING THE PHASE DIAGRAM IN HICS



- increasing baryon chemical potential with decreasing beam energy
- net baryon content determined by incident nuclei
(quark numbers are conserved under strong interactions)
- net strangeness has to be zero \longrightarrow **strangeness neutrality**

NOMENCLATURE

- chemical potentials:

$$q = \begin{pmatrix} u \\ d \\ s \end{pmatrix} \rightarrow \mu = \begin{pmatrix} \mu_u \\ \mu_d \\ \mu_s \end{pmatrix} = \begin{pmatrix} \frac{1}{3}\mu_B + \frac{1}{2}\mu_I \\ \frac{1}{3}\mu_B - \frac{1}{2}\mu_I \\ \frac{1}{3}\mu_B - \mu_S \end{pmatrix}$$

↑
baryon ↑ strangeness
 ↑
 isospin

- here: $\mu_I = 0$

- cumulants of conserved charges

$$\chi_{ij}^{BS} = T^{i+j-4} \frac{\partial^{i+j} p(T, \mu_B, \mu_S)}{\partial \mu_B^i \partial \mu_S^j}$$

↑
pressure

net baryon number: $B = \langle N_B - N_{\bar{B}} \rangle = \chi_{10}^{BS} V T^3$

net strangeness: $S = \langle N_S - N_{\bar{S}} \rangle = \chi_{01}^{BS} V T^3$

BARYON-STRANGENESS CORRELATION

- B-S correlations:

[Koch, Majumder, Randrup, nucl-th/0505052]

$$C_{BS} \equiv -3 \frac{\chi_{11}^{BS}}{\chi_{02}^{BS}} = -3 \frac{\langle BS \rangle - \langle B \rangle \langle S \rangle}{\langle S^2 \rangle - \langle S \rangle^2} = -3 \frac{\langle BS \rangle}{\langle S^2 \rangle}$$

strangeness neutrality

- diagnostic tool for deconfinement:

QGP

- all strangeness is carried by s, \bar{s}
- strict relation between B and S: $B_s = -S_s/3$
- if all flavors are independent: $\chi_{11}^{BS} = -\chi_{02}^{BS}/3$

$$\longrightarrow C_{BS} = 1$$

hadronic phase

- mesons can carry only strangeness, baryons both
- χ_{11}^{BS} : only strange baryons
 χ_{02}^{BS} : strange baryons & mesons

$$\longrightarrow C_{BS} \neq 1$$

STRANGENESS NEUTRALITY

- HIC: colliding nuclei have zero strangeness $\rightarrow S = 0 \ \forall T, \mu_B$
- strangeness neutrality implicitly defines $\mu_S(\mu_B)$

$$\chi_{01}^{BS}(\mu_B, \mu_S(\mu_B)) = 0 \Rightarrow \frac{d\chi_{01}^{BS}}{d\mu_B} = 0 \Leftrightarrow \frac{\partial \mu_S}{\partial \mu_B} = \frac{1}{3} C_{BS}$$

- access B-S correlation through strangeness neutrality
- effect of strangeness neutrality on thermodynamics / phase structure?

LOW-ENERGY MODELING OF QCD

PQM MODEL

- Polyakov-loop enhanced Quark-Meson model (in the local potential approximation LPA):

$$\Gamma_k = \int_x \left\{ \bar{q} (\gamma_\nu D_\nu + \gamma_\nu C_\nu) q + \bar{q} h \cdot \Sigma_5 q + \text{tr}(\bar{D}_\nu \Sigma \cdot \bar{D}_\nu \Sigma^\dagger) + \tilde{U}_k(\Sigma) + U_{\text{glue}}(\langle L \rangle, \langle \bar{L} \rangle) \right\}$$

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- scalar and pseudoscalar meson nonets:

$$\Sigma = T^a (\sigma^a + i\pi^a) \ni \begin{cases} \{\sigma, f_0, a_0^0, a_0^+, a_0^-, \boxed{\kappa^0, \bar{\kappa}^0, \kappa^+, \kappa^-}\} \\ \{\eta, \eta', \pi^0, \pi^+, \pi^-, \boxed{K^0, \bar{K}^0, K^+, K^-}\} \end{cases} \quad \text{open strange mesons: } l\bar{s}, s\bar{l}$$

$$\Sigma_5 = T_a (\sigma_a + i\gamma_5 \pi_a)$$

- quarks (assume light isospin symmetry):

$$q = \begin{pmatrix} l \\ l \\ s \end{pmatrix} \quad \mu = \begin{pmatrix} \frac{1}{3}\mu_B \\ \frac{1}{3}\mu_B \\ \frac{1}{3}\mu_B - \mu_S \end{pmatrix}$$

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cov. derivative with A_0 background

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quarks and mesons:

$$q = \begin{pmatrix} l \\ l \\ s \end{pmatrix} \quad \begin{aligned} \Sigma &= T^a(\sigma^a + i\pi^a) \\ \Sigma_5 &= T_a(\sigma_a + i\gamma_5\pi_a) \end{aligned}$$

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vector source / cov. derivative for the chemical potential

$$C_\nu = \delta_{\nu 0} \mu$$

$$\bar{D}_\nu \Sigma = \partial_\nu \Sigma + [C_\nu, \Sigma]$$

couples μ s to mesons!

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effective meson potential:

$$\tilde{U}_k = U_k(\rho_1, \tilde{\rho}_2) - j_l \sigma_l - j_s \sigma_s - c_k \xi$$

$U(3) \times U(3)$ symmetric potential (as a function of two chiral invariants)

$$\rho_i = \text{tr}(\Sigma \cdot \Sigma^\dagger)^i$$

explicit chiral symmetry breaking: finite light & strange current quark masses

anomalous $U(1)_A$ breaking via 't Hooft determinant

$$\xi = \det(\Sigma + \Sigma^\dagger)$$

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Polyakov loop potential: [Lo et. al., hep-lat/1307.5958]

$$L = \frac{1}{N_c} \left\langle \text{Tr}_f \mathcal{P} e^{ig \int_0^\beta d\tau A_0(\tau)} \right\rangle$$

$$\frac{U_{\text{glue}}(L, \bar{L})}{T^4} = -\frac{1}{2}a(T)\bar{L}L + b(T) \ln [M_H(L, \bar{L})] + \frac{1}{2}c(T)(L^3 + \bar{L}^3) + d(T)(\bar{L}L)^2$$

$$M_H(L, \bar{L}) = 1 - 6\bar{L}L + 4(L^3 + \bar{L}^3) - 3(\bar{L}L)^2$$

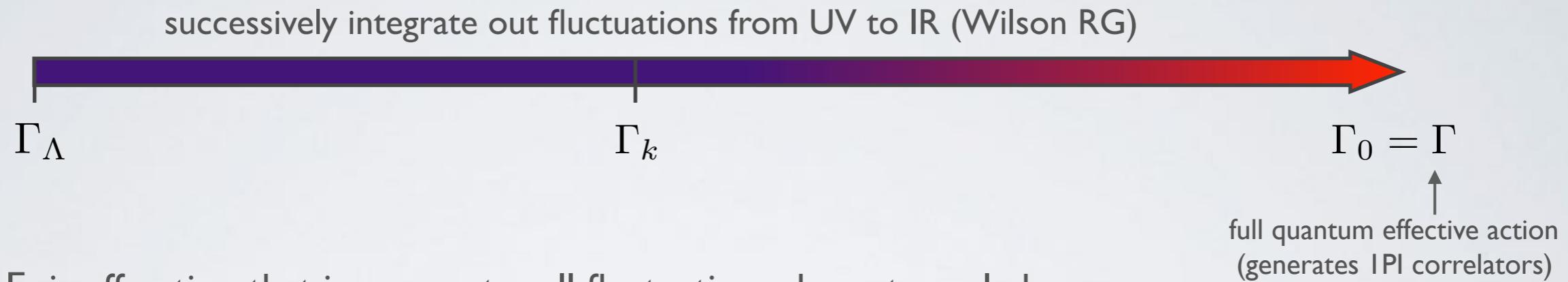
- parameters fitted to reproduce lattice pressure and Polyakov loop susceptibilities
- approximate N_f and μ dependence from QCD and HTL/HDL arguments

[Herbst et. al., hep-ph/1008.0081, 1302.1426]
[Haas et. al., hep-ph/1302.1993]

FUNCTIONAL RG

non-perturbative quantum fluctuations via FRG

- relevant object: **scale dependent effective action Γ_k**



- Γ_k is eff. action that incorporates all fluctuations down to scale k
- lowering k : **zooming out / coarse graining**

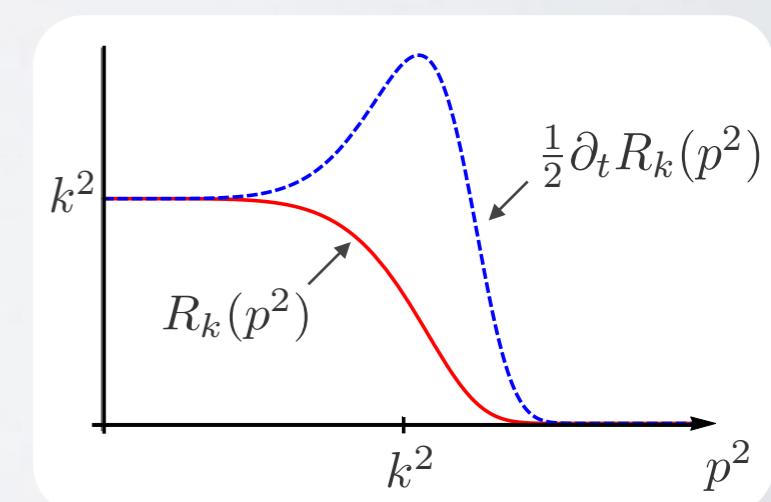
- evolution equation for Γ_k :

$$\partial_t \Gamma_k = \frac{1}{2} S \text{Tr} \left[\left(\Gamma_k^{(2)} + R_k \right)^{-1} \partial_t R_k \right]$$

mass-like IR regulator

[Wetterich 1993]

$$\partial_t = k \frac{d}{dk}$$



PQM + FUNCTIONAL RG

- dynamical chiral symmetry breaking through U_k
- ‘statistical’ confinement through A_0 background (U_{glue})
- thermal quark distributions modified through feedback from A_0

$$n_F(E) = \frac{1}{e^{(E-\mu)/T} + 1} \xrightarrow{A_0 \neq 0} N_F(E; L, \bar{L}) = \frac{1 + 2\bar{L}e^{(E-\mu)/T} + Le^{2(E-\mu)/T}}{1 + 3\bar{L}e^{(E-\mu)/T} + 3Le^{2(E-\mu)/T} + e^{3(E-\mu)/T}}$$

$$\rightarrow \begin{cases} \frac{1}{e^{3(E-\mu)/T} + 1}, & L \rightarrow 0 \text{ (confinement)} \\ \frac{1}{e^{(E-\mu)/T} + 1}, & L \rightarrow 1 \text{ (deconfinement)} \end{cases}$$

→ ‘interpolation’ between baryon and quark d.o.f.

[Fukushima, hep-ph/0808.3382]
[Fu & Pawłowski, hep-ph/1508.06504]

→ correct ‘ N_c - scaling’ of particle number fluctuations

[Ejiri et al., hep-ph/0509051]
[Skokov et al., hep-ph/1004.2665]

- thermodynamics from Euclidean (off-shell) formulation

→ simple hierarchy of relevant fluctuations: the lighter the particle, the more relevant it is

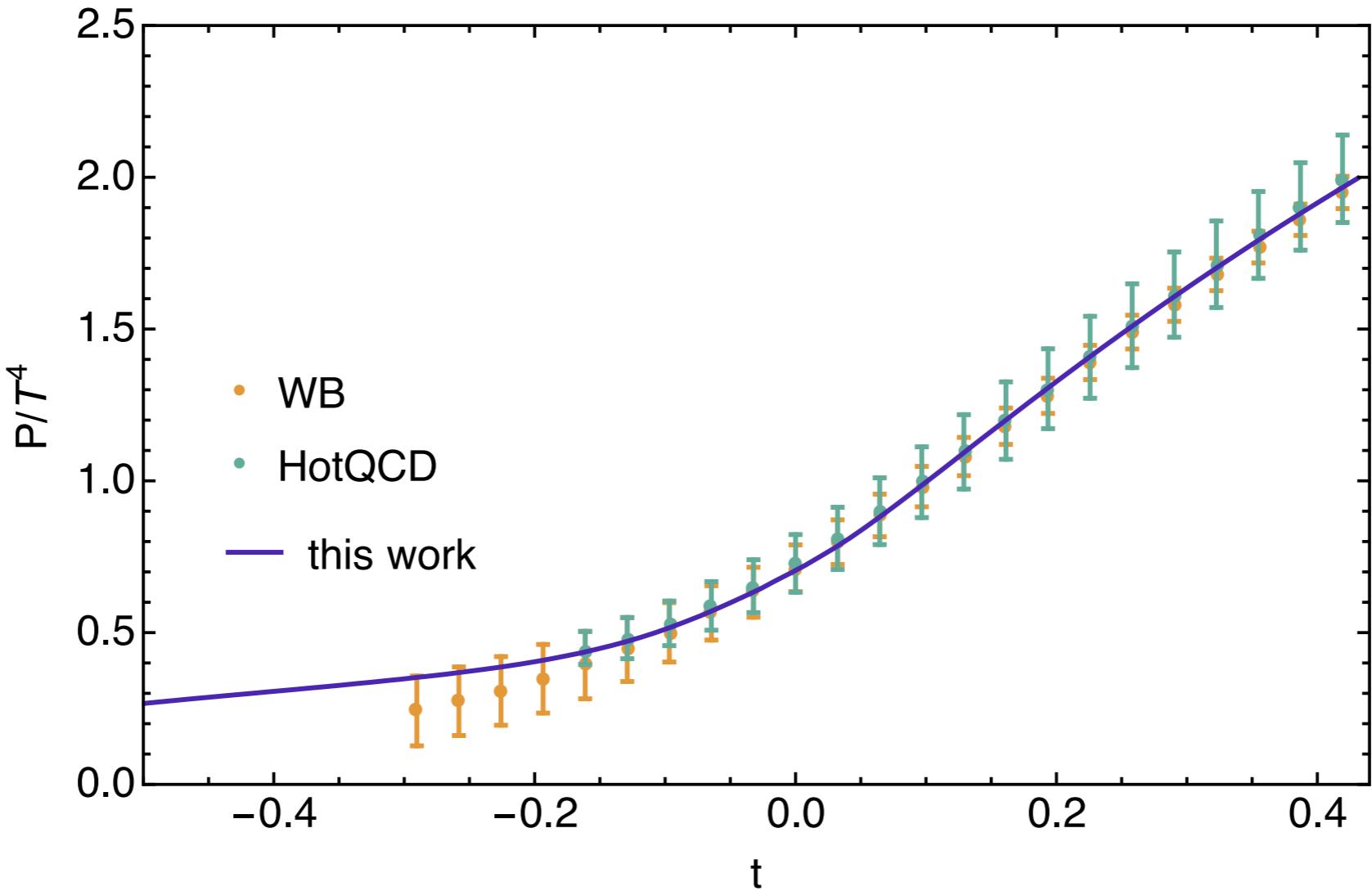
→ fluctuations of kaons and s-quarks (coupled to A_0) already sufficient for qualitative description of the relevant strangeness effects (for moderate μ)

preliminary

RESULTS

MODEL VS LATTICE EOS

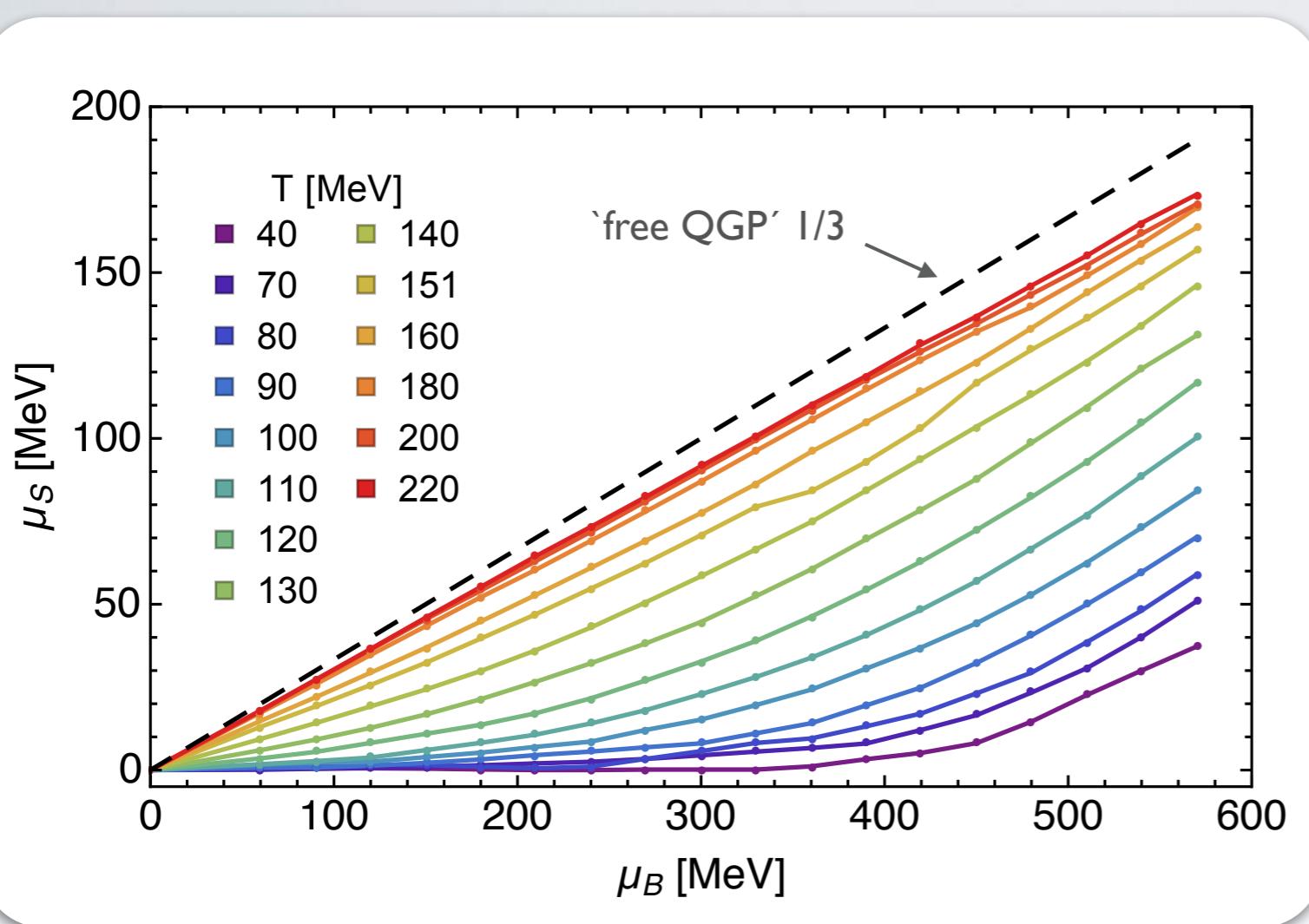
cf. [Herbst et al., hep-ph/1308.3621]



$$t = \frac{T - T_c}{T_c}$$

STRANGENESS NEUTRALITY

$\mu_s(\mu_B)$ at strangeness neutrality



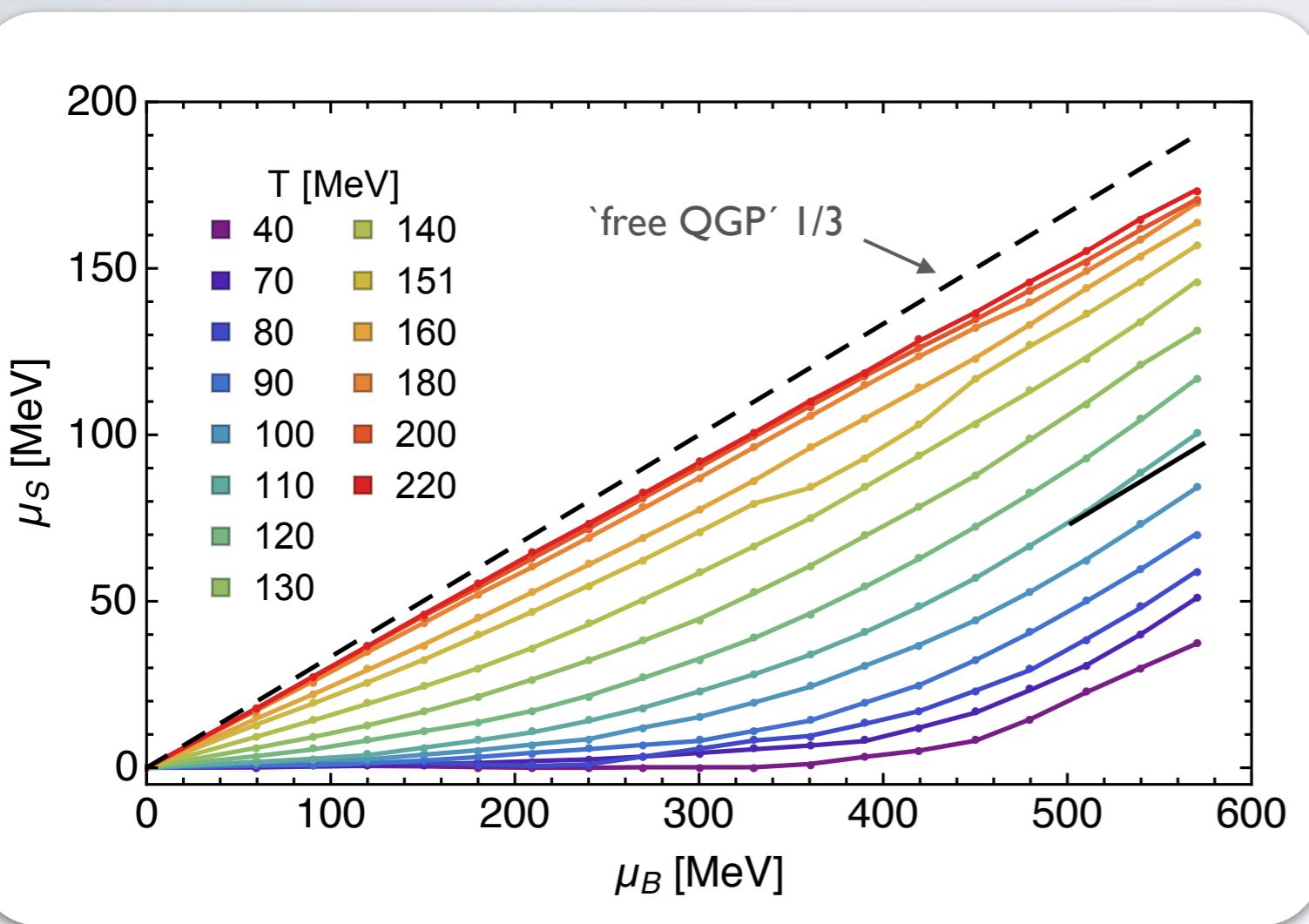
- slope directly related to baryon-strangeness correlations:

$$\frac{\partial \mu_S}{\partial \mu_B} = \frac{1}{3} C_{BS}$$

- C_{BS} for any T and μ
- competition between baryonic and mesonic sources of strangeness!

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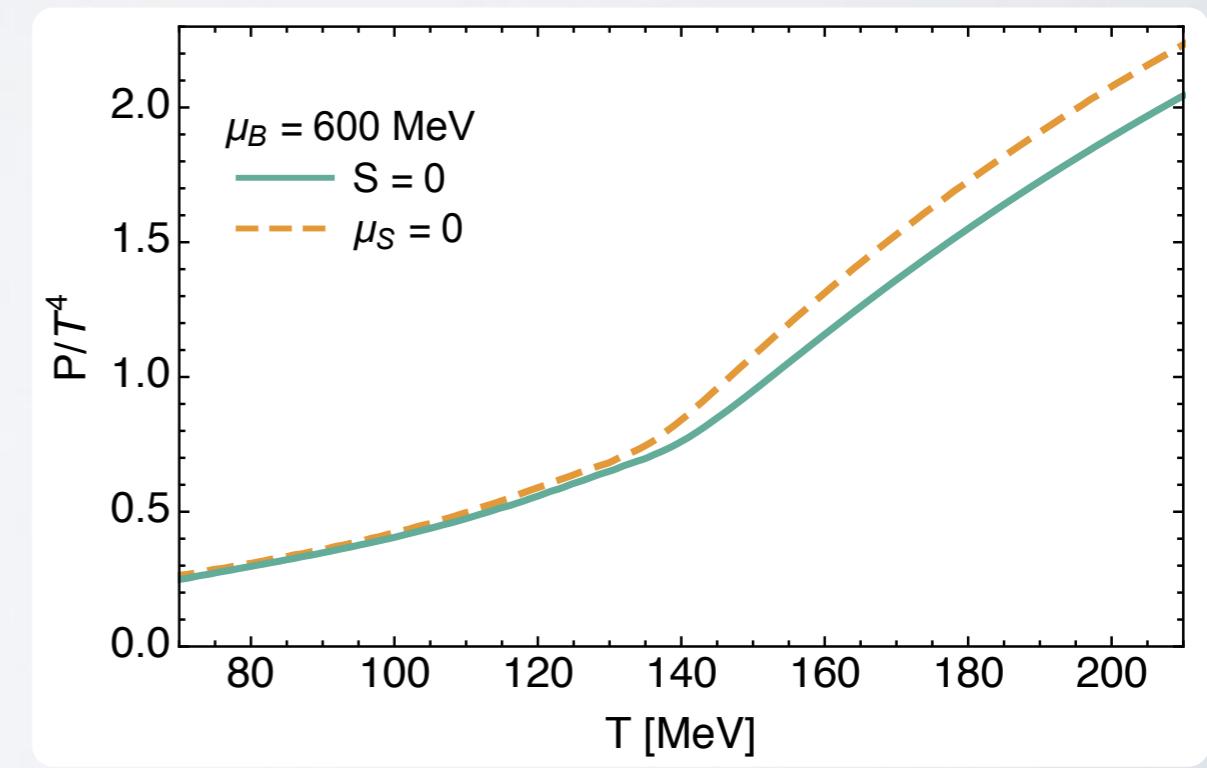
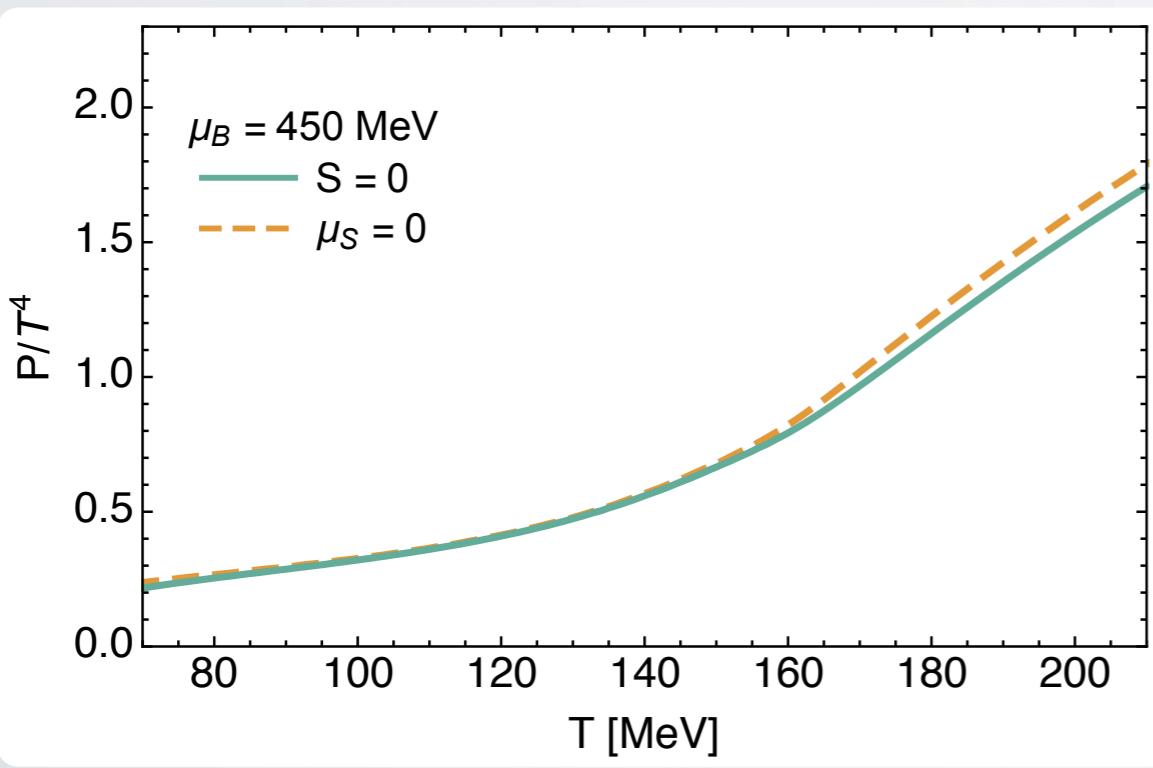
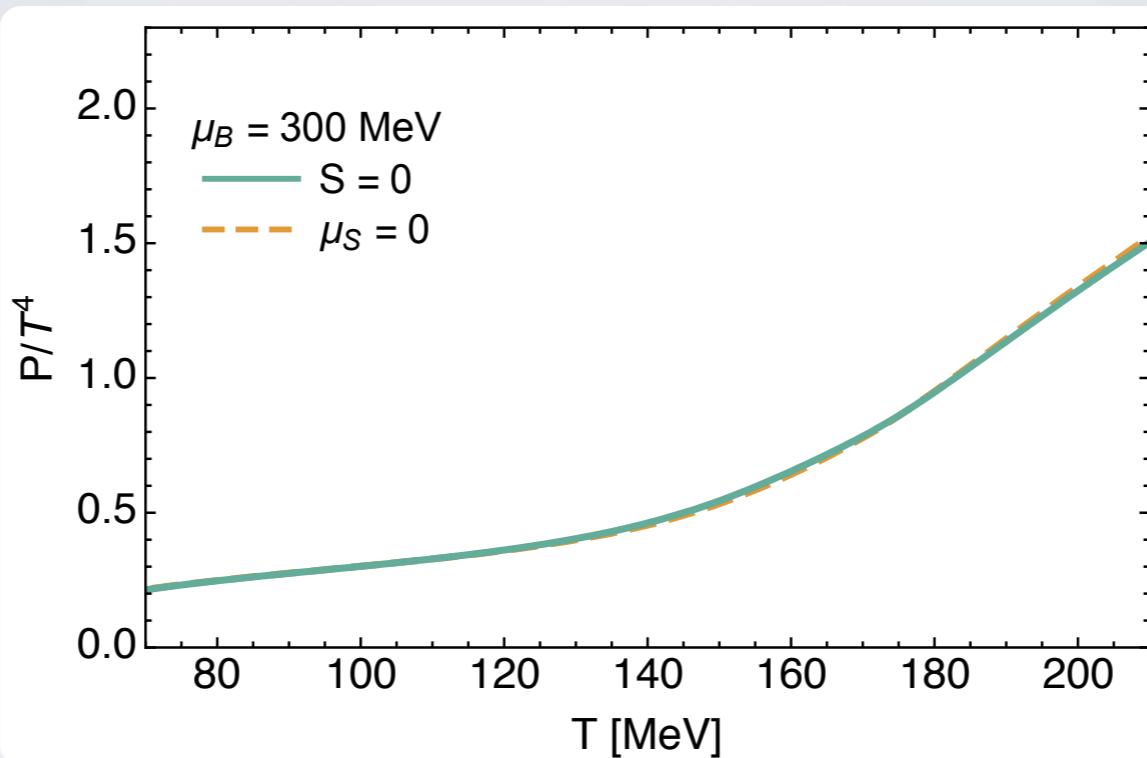
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- C_{BS} for any T and μ
- competition between baryonic and mesonic sources of strangeness!

$$3 \frac{\partial \mu_S}{\partial \mu_B} = C_{BS} \sim \frac{\langle \text{strange baryons} \rangle}{\langle (\text{strange baryons} \& \text{mesons})^2 \rangle} \left\{ \begin{array}{ll} < 1 & \text{mesons dominate} \\ = 1 & \text{mesons \& baryons (or free flavors)} \\ > 1 & \text{baryons dominate} \end{array} \right.$$

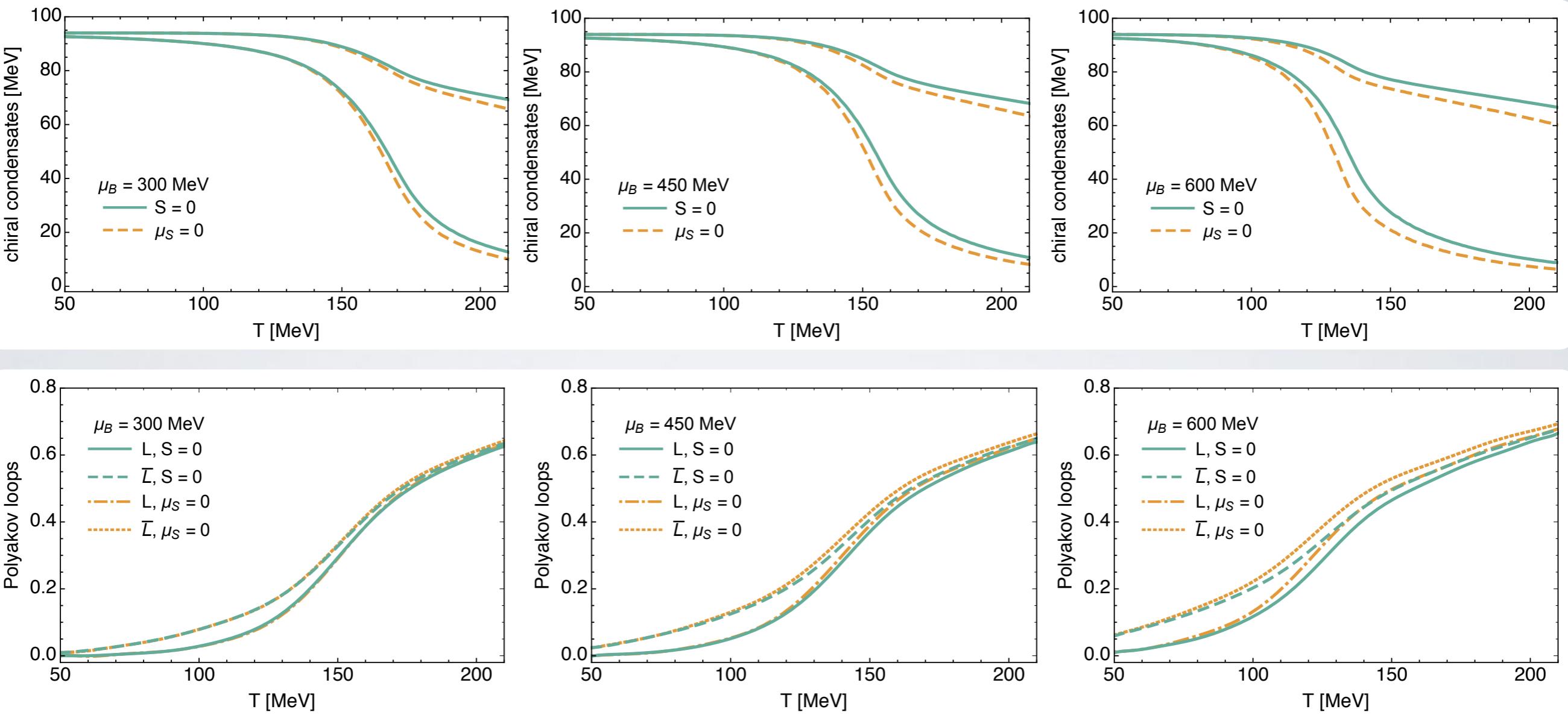
STRANGENESS NEUTRALITY

EoS at strangeness neutrality



STRANGENESS NEUTRALITY

phase structure at strangeness neutrality



- critical temperature starts increasing at moderate μ_B due to strangeness neutrality
- smaller curvature of the phase boundary
- CEP at larger T (?)

SUMMARY & OUTLOOK

- **strangeness neutrality in heavy ion collisions**
 - intimate relation to baryon strangeness correlations
 - sensitive to QCD phase transition
- **relevant for phase structure and thermodynamics at finite μ_B**
 - phase transition at larger T for moderate μ_B
 - likely to affect position of the CEP

In progress:

- study larger μ and the CEP
- eigenvalue potential vs loop potential: minimum vs saddle point
- going beyond LPA
- including gluon fluctuations: dynamical hadronization
- self-consistent computation of the A_0 potential

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