

Dalitz-Plot Analyses

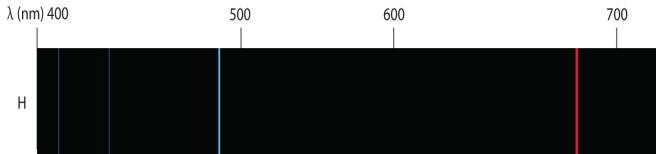
RTG Lecture 1: Decay rates and phase-space

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27.06.2018

Spectroscopy

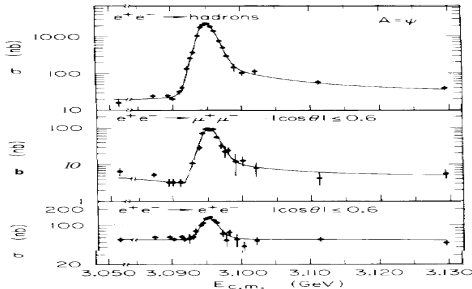
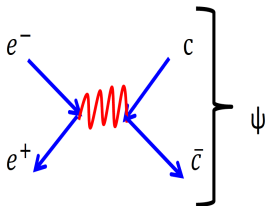


- **Atomic spectroscopy:**

Spectral lines were observed before their origin was understood
 $\Rightarrow$ Key role in development of Quantum Mechanics (QM)

- **Hadron spectroscopy** $\Rightarrow$ Understanding of strong interaction
(Reminder: Hadron = Bound state of quarks: $(q\bar{q})$, (qqq) , ...)

November Revolution 1974

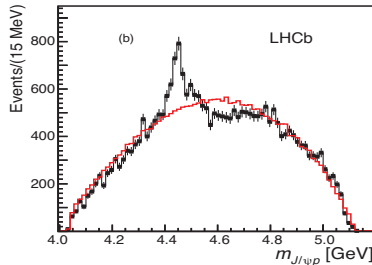
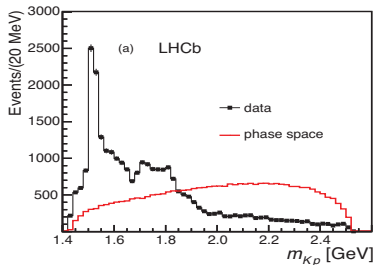


- Quark Model at that time: several hundred hadronic states explained as bound states of 3 different quarks: u, d, s
- SLAC-Mark-I experiment found new long-lived particle: $J/\psi = |c\bar{c}\rangle$ (Simultaneously confirmed by independent group: BNL)
- Soon followed by excited states: $\psi(2S), \psi(3770), \dots$

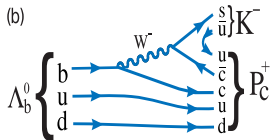
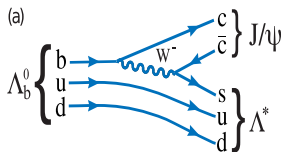
⇒ Key role in development of SM

See Dominiks lecture for details

Pentaquark in $\Lambda_b \rightarrow J/\psi K p$ decays ?



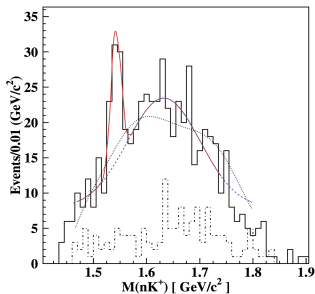
[Phys. Rev. Lett. 115, 072001]



See Marians lecture for details

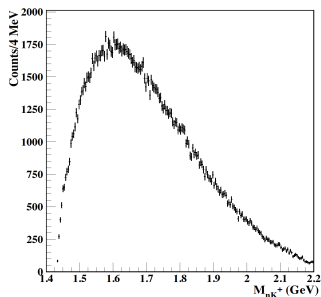
Lesson from the past:

Reaction: $\gamma d \rightarrow pK^-(K^+n)$



[PRL 91 252001]

$\Rightarrow$
30 · stat.

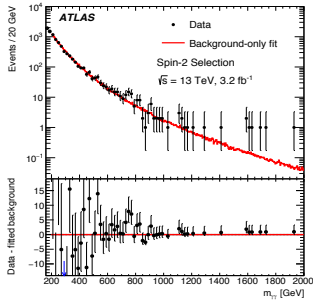


[PRL 96 212001]

Peaks can come and go ...

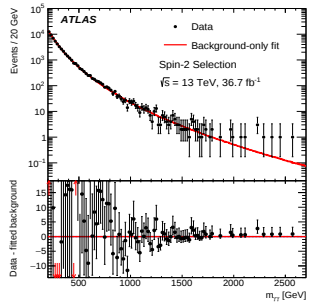
See Marians lecture for details

Lesson from the past:



[JHEP 09 (2016) 001]

⇒
12 · stat.



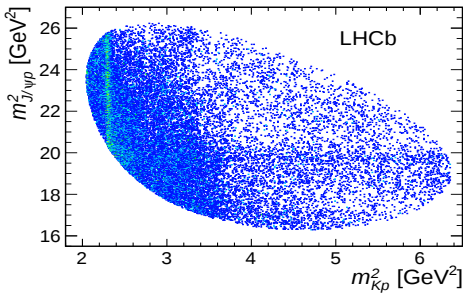
[Phys. Lett. B 775 (2017) 105-125]

Peaks can come and go ...

See physics teams presentation for details

Dalitz Plots

$$\Lambda_b \rightarrow J/\psi K p$$



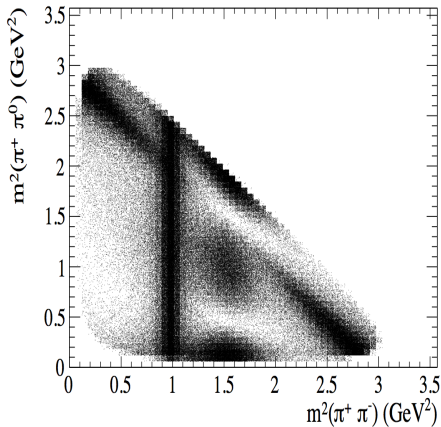
[Phys. Rev. Lett. 115, 072001]

Make use of full decay information:

- Angular distributions $\Rightarrow$ Spin-Parity
- Interference patterns provide sensitivity to phases
($\Rightarrow$ Also interesting for CPV studies)

Lecture 1+2:

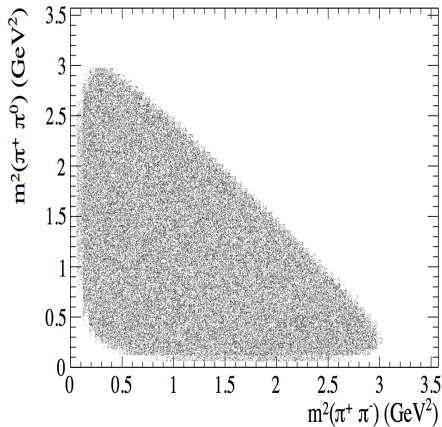
Dalitz Plot Technique



$(D^0 \rightarrow \pi^+ \pi^- \pi^0 \text{ Toy Simulation})$

Lecture 1:

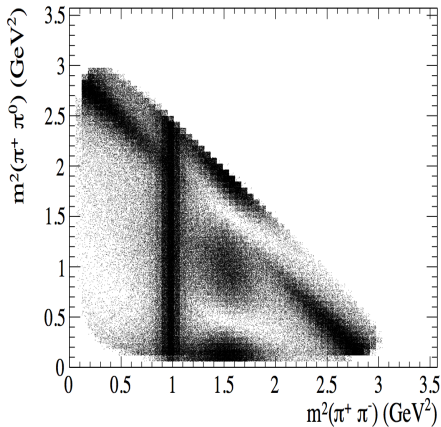
Decay rates and Phasespace



($D^0 \rightarrow \pi^+ \pi^- \pi^0$ Toy Simulation)

Lecture 2:

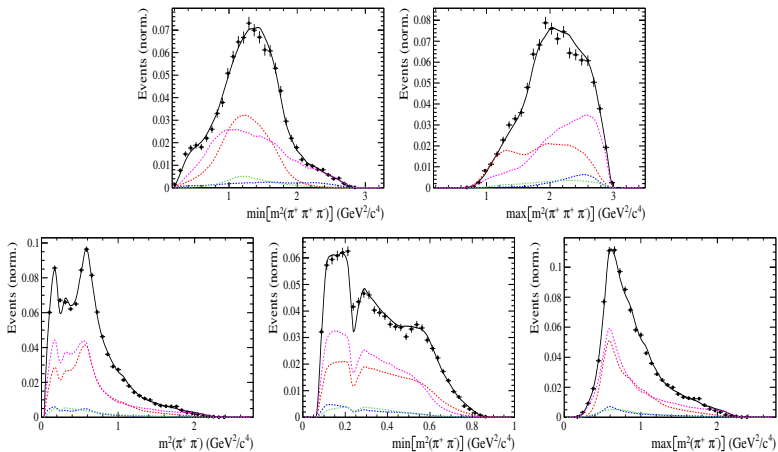
Resonances and angular distributions



($D^0 \rightarrow \pi^+ \pi^- \pi^0$ Toy Simulation)

Lecture 3:

Amplitude analysis of $D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$



[JHEP 05 (2017) 143]

Two-body Decays: Examples

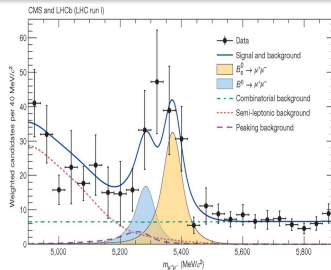
$$\Gamma(M \rightarrow 12) \propto \frac{[(M^2 - (m_1 + m_2)^2)(M^2 - (m_1 - m_2)^2)]^{1/2}}{M^3}$$

$$\frac{\Gamma(D \rightarrow K^+ K^-) \Gamma(D \rightarrow \pi^+ \pi^-)}{\Gamma(D \rightarrow K^+ \pi^-) \Gamma(D \rightarrow K^- \pi^+)}$$

- Naive expectation (Phasespace): 0.98
- Experiment: 1.04 ± 0.06

$$\frac{\Gamma(B_0 \rightarrow \mu\mu)}{\Gamma(B_s \rightarrow \mu\mu)}$$

- Phasespace: $104\% \cdot \frac{|V_{td}|^2}{|V_{ts}|^2} = 5\%$
- Experiment: $14 \pm 8\%$
 $\Rightarrow$ CKM hierarchy

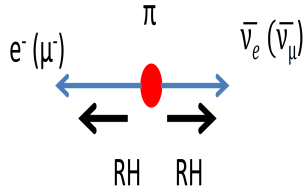
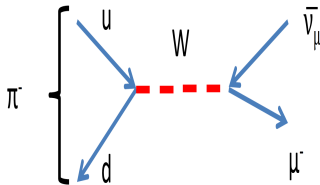


[Nature 522, 68-72]

Two-body Decays: Historic puzzles

Pion decay

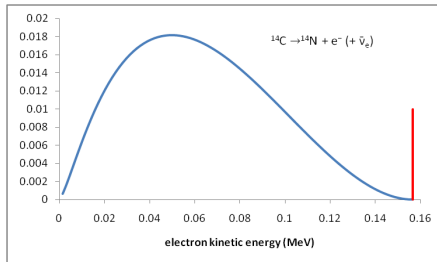
- Naive expectation (Phasespace): $\frac{\Gamma(\pi \rightarrow e \nu)}{\Gamma(\pi \rightarrow \mu \nu)} = \frac{m_\pi^2 - m_e^2}{m_\pi^2 - m_\mu^2} = 3.3$
- Experiment: $\frac{\Gamma(\pi \rightarrow e \nu)}{\Gamma(\pi \rightarrow \mu \nu)} = (1.230 \pm 0.004) \cdot 10^{-4}$
- Weak interaction violates parity: $A \propto q_\mu (\bar{u}_e \gamma^\mu \frac{1}{2}(1 - \gamma^5) u_\nu)$
 $\Rightarrow \frac{\Gamma(\pi \rightarrow e \nu)}{\Gamma(\pi \rightarrow \mu \nu)} = \left(\frac{m_e^2}{m_\mu^2} \right) \cdot \frac{m_\pi^2 - m_e^2}{m_\pi^2 - m_\mu^2} = 1.275 \cdot 10^{-4}$



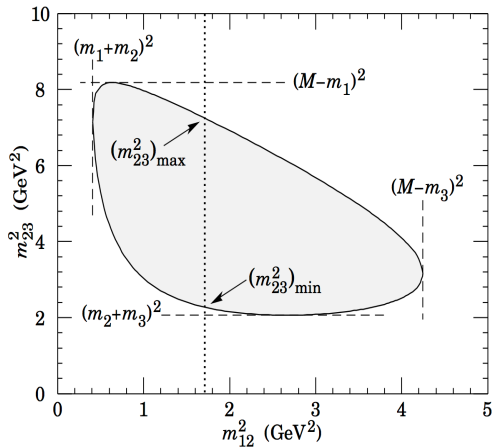
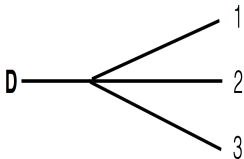
Two-body Decays: Historic puzzles

$$\beta\text{-Decay: } n \rightarrow pe^-(\nu)$$

- Expect discrete energy in 2-body decay
- Observe continuous energy spectrum of emitted e^-
 $\Rightarrow$ Prediction of neutrino



Dalitz Plots



$$(m_i^2 + m_j)^2 \leq m_{ij}^2 \leq (M - m_k)^2$$

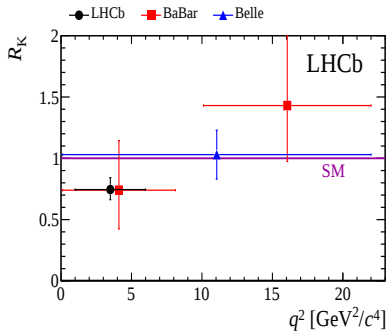
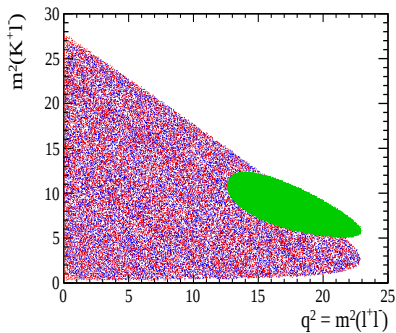
Three-body Decays: Example

$$\Gamma(M \rightarrow 123) \approx \frac{1}{M} \int dm_{12}^2 dm_{23}^2 \propto V_{phsp}$$

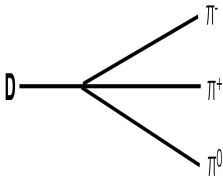
Search for lepton flavor violation

$$\frac{\Gamma(B^+ \rightarrow K^+ \mu \mu)}{\Gamma(B^+ \rightarrow K^+ e e)} \approx 0.99$$

$$\frac{\Gamma(B^+ \rightarrow K^+ \mu \mu)}{\Gamma(B^+ \rightarrow K^+ \tau \tau)} \approx 9$$



[Phys. Rev. Lett. 113, 151601]



$$A_{D \rightarrow 3\pi} = \text{const.}$$

