Towards a Swampland Global Symmetry Conjecture

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based work with T. Daus / J. March-Russell / S. Leonhardt (for wormhole part see also review with T. Mikhail / P. Soler)

<u>Outline</u>

- Introduction / Motivation
- Different types of approximate global symmetries
- Constraining the gauge-derived case
- Relation to euclidean wormhole arguments and general wormhole issues

- Are there low-energy phenomena relevant to QG?
- One approach: Swampland Program (Search for necessary features of consistent low-energy EFTs).
- One example: No Global Symmetries see e.g. Banks/Dixon '88, Kamionkowksi/March-Russell, Holman et al. '92, Kallosh/Linde²/Susskind '95, Banks/Seiberg '10
- But is this really a 'Swampland Conjecture'?
 - Consider an EFT with a global symmetry.
 - Standard BH evaporation physics will induce the expected violation.

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- the EFT is not constrained by this!

Introduction/Motivation (continued)

• Clearly, 'standard' BH evaporation physics is an overstatement. In, fact, at least in AdS (and with some assumptions), an independent argument for

No (exact) global symmetries

can be given.

Harlow/Ooguri '18



- However, our interest will be approximate global symmetries.
- Those are not forbidden and it is crucial to constrain their quality. In a sense, the low-energy effective field theorist has no other way to approach the issue.

Introduction/Motivation (continued)

- Again: Our interest is in quantitative conjectures against approximate global symmetries.
- One such approach is, of course, the Weak Gravity Conjecture:

 $g \rightarrow 0$ (Ideal) claim of WGC: $g \gtrsim m/M_P$, where *m* is the mass of the lightest charged particle.

Gauge symmetry \rightarrow global symmetry

- Such a strong statement has not yet been proven.
- Rigorous progress has only been made in the context of the BH mass spectrum (i.e. masses of highly charged particles)

Cheung/Remmen Hamada/Noumi/Shiu '16..'20

Introduction/Motivation (continued)

We want to consider a second route for approaching exact global symmetries:

 $\begin{array}{rcl} \mbox{gauge symm.} & \rightarrow & \mbox{global symm.} & \leftarrow & \mbox{approx. global symm.} \\ g & \rightarrow & 0 & & 0 & \leftarrow & c \mbox{ (operator coeffs.)} \end{array}$

- This second way of approaching a global symmetry is fundamentally different: no light vector is part of the EFT.
- Arguably, it is in fact the practically most useful way to think about a global symmetry

(B-L, flavor symmetries, DM stability, flat axion potentials, ...)

What is the definition of an approximate global symmetry?

- Consider EFT with some (global) group action.
- Approximate Symmetry: All non-singlet operators are either irrelevant or have small coefficients (c ≪ 1).
- Our goal: Quantify the smallness.

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see also Coleman/Lee, Rey \sim'90 .... Alonso/Urbano '17 AH/Mikhail/Soler '18 ..... Alvey/Escudero '20 (relies on wormholes – more details later...)
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see also Fichet/Saraswat '19
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(New conjecture inspired by BH evaporation:

In a thermal plasma, the BH-induced violation effect should not exceed the effect of symmetry-violating local operators. $\)$

• We want a derivation instead of a new conjecture (at least for a subclass of global symmetries).

Types of approximate global symmetries

• (1) Gauge derived

Start with gauged U(1); 'Higgs' it using an axion

- \Rightarrow vector and axion become heavy
- ⇒ any light charged particle now sees an approximate global symmetry.
- (2) Accidental

Spacetime and gauge symmetries forbid all relevant and marginal non-singlet operators.

• (3) Fine-tuned

Coefficients of relevant and marginal non-singlet operators are small by landscape-type tuning.

Our focus will be on the gauge-derived case.

Minimal setting / basic idea

$$\mathcal{L} \supset \frac{1}{g^2} F_{\mu\nu}^2 + |D\Phi|^2 + m^2 |\Phi|^2 + f^2 |\partial_\mu \varphi + A_\mu|^2$$

- If $m \ll gf$, the light field Φ sees a surviving global U(1).
- φ started out as an axion, i.e. a scalar with gauged discrete shift symmetry $(\varphi \rightarrow \varphi + 2\pi n)$.
- Instanton (wormhole?) effects break the associated continuous shift symmetry very weakly (non-perturbatively).
- <u>Natural question</u>: Can this be used to apply the Weak Gravity/Swampland logic to quantitatively constrain global symmetry violation? (of our lin.-realized global U(1))

For this purpose, recall the

Generalized Weak Gravity Conjecture:

• Consider a *p*-form gauge theory $(p \neq 1)$: $S \sim \int (F_{p+1})^2 + T \int_{p-dim.} dV + g \int_{p-dim.} A_p$. It is claimed that $T/M_P \leq g$.

• In particular, the axionic (p = 0) case reads:

$$S ~\sim~ \int (darphi)^2 ~+~ S_{inst.} ~+~ g ~arphi(x_{inst.}) \,.$$

or, for gauge instantons,

cf.
$$S \sim \int (d\varphi)^2 + \int \operatorname{tr}(F^2) + \int \frac{1}{f} \varphi \operatorname{tr}(F\tilde{F}).$$

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Generalization to axions / instantons

• Thus, with the substitutions $g \rightarrow 1/f$ and $T \rightarrow S_{inst.}$, the WGC now says:

$$T/M_P < g \Rightarrow S_{inst.} < M_P/f$$
.

• This implies a lower bound on the strength of instanton effects: $\exp(-S_{inst.}) > \exp(-M_P/f)$.



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- We want to gauge the axion by a U(1).
- Recall more generally how a *p*-form is gauged by a (p+1)-form:

$$\frac{1}{g_{\rho}^{2}}|dA_{\rho}|^{2} + \frac{1}{g_{\rho+1}^{2}}|dA_{\rho+1}|^{2} \quad \rightarrow \quad \frac{1}{g_{\rho}^{2}}|dA_{\rho} + A_{\rho+1}|^{2} + \frac{1}{g_{\rho+1}^{2}}|dA_{\rho+1}|^{2}$$

 Crucially, in the gauged/Higgsed version, the charged (p-1)-branes of the p-form theory cease to exist as independent objects:

They would break the gauge invariance

 $\delta A_{p+1} = d\chi_p$, $\delta A_p = -\chi_p$

 Instead, those brains can appear only as boundaries of the *p*-branes B_p charged under A_{p+1}:

$$S \supset \int_{B_p} A_{p+1} + \int_{\partial B_p} A_p \, .$$

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- In our case of Gauge-derived global symmetries, we gauge an axion (0-form) with a U(1) vector (1-form).
- Thus, instantons become boundaries of worldlines.
- In other words: Instantons automatically destroy globally-charged particles

(cf. many stringy examples: Ibanez/Marchesano/Rabadan '01 Antoniadis/Kiritsis/Rizos Uranga ... Blumenhagen/Cvetic/Kachru/Weigand Martucci '15)



By the WGC for axions, this particlenumber violation is suppressed by $\exp(-S_{inst.}) \sim \exp(-M_P/f)$

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• Moreover, according to the magnetic WGC for axions (for the dual B_2 -theory with strings) the string tension is bounded by $T \lesssim M_P f$.

AH/Soler '17

• This implies a UV-cutoff for the EFT:

 $\Lambda \sim \sqrt{M_P f}$

Hence, in total, the global-symmetry violation is bounded below by $(-C_{--})$

 $\exp(-S_{inst.}) \sim \exp(-M_P^2/\Lambda^2)$

• Very intriguingly, this is the same as the plasma-motivated bound of Fichet/Saraswat and as the bound expected from wormholes:

$$S_{WH} ~\sim~ M_P^2 \int {\cal R} ~\sim~ M_P^2/\Lambda^2$$

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An example with 'UV-complete' instantons:

$$\mathcal{L}_1 = -rac{1}{e^2}F^2 + \overline{\psi}ioldsymbol{D}\psi \quad, \qquad \mathcal{L}_2 = -f^2(\partial arphi)^2 - rac{1}{g^2}\mathrm{tr}G^2 + rac{arphi\,\mathrm{tr}G\,\hat{G}}{8\pi^2}$$

- Gauge: $\partial \varphi_{\mu} \rightarrow \partial_{\mu} \varphi + A_{\mu}$ and take ψ in the N of SU(N).
- Now standard SU(N) instantons induce a 't Hooft vertex

$$\mathcal{O} = e^{-S_I} \,\overline{\psi}_L \psi_R \, e^{i\varphi} + \text{h.c.}$$

 After gauge-fixing to φ = 0, as appropriate in the IR, this is precisely the effect we claimed on general grounds.

For more general situations and stringy origins of such models see e.g. Anastasopoulos/Bianchi/Dudas/Kiritsis '06

A simple 5d example on S^1/\mathbb{Z}_2 :

--- particle worldline



- The 5d U(1) is Higgsed on brane 2.
- The field ψ on brane 1 becomes globally charged.
- This global U(1) is broken exponentially weakly (by the massive charged 5d particle Φ, required by the WGC)
- The resulting toy-model 'exotic instanton' has an action consistent with our general result.

A potential loophole

 If the light charged particle has U(1)-charge n ≫ 1, the low-energy observers may be mislead:

They see an *n*-instanton effect $(-\exp(-n M_P^2/\Lambda^2))$ and take it for a single-instanton effect $(-\exp(-M_P^2/\Lambda^2))$.

So they expect a cutoff $\tilde{\Lambda} = \Lambda/\sqrt{n}$ that is too low and suspect a violation of our bound.

 In examples we studied, light high charges can only be constructed at the price of lowering the EFT-cutoff.
 ⇒ probably no loophole (but more work needed).

• We already mentioned the parametrically similar wormhole-based arguments against global symmetries – let us develop this line of thought

16/27

Euclidean wormholes / gravitational instantons

• In Euclidean Einstein gravity, supplemented with an axionic scalar φ , instantonic solutions exist:

Giddings/Strominger '88



- The 'throat' is supported by the kinetic energy of $\varphi = \varphi(r)$, with r the radial coordinate of the throat/instanton.
- A wormhole-end looks like an instanton to the low-energy observer

(recently revived in the Swampland/WGC context by

Montero/Uranga/Valenzuela, Heidenreich/Reece/Rudelius '15 AH/Mangat/Theisen/Witkowski '17,)

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Euclidean wormholes (continued)

• The underlying lagrangian is simply

 $\mathcal{L} \sim M_P^2 \, \mathcal{R} + f^2 |d\varphi|^2 \,, \quad ext{now with} \quad \varphi \equiv \varphi + 2\pi \,.$

• This can be dualized $(dB_2 \equiv f^2 * d\varphi)$ to give

$$\mathcal{L} \sim M_P^2 \, \mathcal{R} + rac{1}{f^2} |dB_2|^2 \, .$$

• The 'throat' exists due the compensation of these two terms: Placing one unit of flux (of $H_3 = dB_2$) on the transverse S^3 of radius R, we have

$$M_P^2 R^{-2} \sim \frac{1}{f^2} R^{-6} \Rightarrow M_P R^2 \sim \frac{1}{f}.$$

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- Thus, the instanton action is $S \sim M_P/f$
- This coincides parametrically with the lowest-action instanton of the WGC.
- The maximal WH-curvature scale is $\sqrt{f M_P}$, which should not exceed the UV cutoff:

 $f M_P < \Lambda^2 \quad \Rightarrow \quad S \sim M_P^2 / \Lambda^2$

- This agrees with our WGC-bound on global-symm.-violation
- Also technically (cf. our Appendix), one finds a new class of wormholes carrying our gauge-derived global charge:

19/27

Euclidean wormholes - conceptual issues

• However, euclidean wormholes come at the price of deep conceptual issues.

Hawking '78..'88, Coleman '88, Preskill '89 Giddings/Strominger/Lee/Klebanov/Susskind/Rubakov/Kaplunovsky/.. Fischler/Susskind/...

Recent review: AH, P. Soler, T. Mikhail '18

• First, with wormholes come baby universes:



Second, with baby universes comes a 'baby universe state'

 (α vacuum) encoding information on top of our 4d geometry.

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- In our concrete (single-axion) case, an α parameter now governs the naively calculable e^{-S_l} -effects.
- Most naively, 4d measurements collapse α parameters to random constants.
- However, one should really include the full quantum dynamics of α parameters ...

• In 1+1 dimensions this corresponds to the target-space-dynamics of string theory.



Polchinski, Banks/Lykken/O'Loughlin, Cooper/Susskind/Thorlacius, Strominger '89...'92

- What is the analogue in 3+1 dimensions?
- Another key problem is a possible clash with locality on the CFT-side of AdS/CFT (factorization problem)

Maldacena/Maoz '04, Arkani-Hamed/Orgera/Polchinski '07,, 'SYK'

- With all these problems in mind, maybe one should dismiss wormholes altogether?
- One option is to forbid topology change, but certainly (?) not in *d* = 2.
- Is there a reason to forbid topology change just in d > 2?
- A different argument is that these wormhole solutions have negative modes and should hence be dismissed.

Rubakov/Shvedov '96, Maldacena/Maoz '04, see however Alonso/Urbano '17, ...

In particular: Van Riet et al. '04 ... '17/'18 (and talk)

• But, while this is even technically still an open issue, it does not appear to be a strong enough objection

Indeed, once a non-zero amplitude

universe \rightarrow universe + baby-universe is accepted, the reverse process is hard to forbid.

- As a result, one gets all the wormhole effects.
- The negative mode issue may be saying: 'Giddings-Strominger' does not approximate the amplitude well.



• ...hard to see how it would dispose of the problem altogether...

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Recent developments related to Wormholes

• Recently, a concrete proposal for calculating the entropy of an evaporating BH has emerged (method of 'Islands')

Penington, Almheiri/Engelhardt/Marolf/Maxfield, Almheiri/Mahajan/Maldacena/Zhao, '19/20

- The concrete mechanism by which entropy leaves the BH in this approach is related to euclidean WHs
- Motivated by this, a new 2d toy model developing Coleman's baby universe calculation has been suggested



Marolf/Maxfield '20

25/27

(For a different model see Ambjorn/Sato/Watabiki '21)

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Recent developments related to wormholes (continued)

- In particular, Marolf/Maxfield proposed to mod out the naive BU Hilbert space by a certain equivalence (related to 1 BU → 2 BU transitions, etc.)
- It has then been proposed that, in d ≥ 4, this equivalence should be so strong that the BU Hilbert space is 1-dimensional McNamara/Vafa '20
- This would not remove the effect of BUs completely, but it would get rid of the arbitrariness of α parameters
- But can we do a proper calculation in d ≥ 4 ?

Summary/Conclusions

- The WGC for axions demands certain minimal-action instantons.
- This leads to a universal bound on the quality of gauge-derived global symmetries: ≥ exp(-M²_P/Λ²).
 (In agreement with other effects, such as wormholes.)
- But the latter come at the price of α vacua (and other disasters).
- Keep struggling with these fundamental unresolved issues!

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