

# Nonperturbative $\beta$ function and effective radiative corrections

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*2nd Winter Workshop on Non-Perturbative Quantum Field Theory*

*5-7 October 2011*

*Sophia-Antipolis (France)*

7 October 2011



# Table of Contents I

## Trace anomaly for $\theta_{\mu\nu}$ and nonperturbative $\beta$ function

- Historical remarks and objective

- Trace anomaly, effectively

- Running coupling: temperature vs. resolution

- Evaluation of gluon condensate

- Nonperturbative gauge-coupling evolution

## Effective radiative correction

- Pressure: 2-loops and 3-loops

- Polarization tensor of massless mode

  - Transverse dispersion relation

  - Black-body spectrum

  - Longitudinal dispersion relation

- Monopole properties from a 2-loop correction to pressure

Trace anomaly for  $\theta_{\mu\nu} \equiv 2 \operatorname{tr} \left( -F_{\mu\lambda} F_{\nu}^{\lambda} + \frac{1}{4} g_{\mu\nu} F^{\kappa\lambda} F_{\kappa\lambda} \right)$

- ▶ to any loop order in PT, trace anomaly:

$$\theta_{\mu\mu} = \frac{\beta(g)}{2g} F_{\mu\nu}^a F_{\mu\nu}^a \quad (*)$$

[Collins, A. Duncan, and Joglekar 1977; Fujikawa 1980]

- ▶ to any loop order in PT and nonperturbatively (path integral), chiral anomaly:

$$\partial_{\mu} j_{\mu}^5 = \frac{1}{32\pi^2} F_{\mu\nu}^a \tilde{F}_{\mu\nu}^a .$$

[Adler, Adler and Bardeen 1969; Bell and Jackiw 1969; Fujikawa 1979,1980]

- ▶ in contrast to trace anomaly **chiral anomaly not renormalized** and topologically saturated

## Trace anomaly, effectively

- ▶ **idea:** use operator identity (\*) to extract  $\beta(g)$  and thus  $g(T)$  from (effective) knowledge of  $\langle \theta_{\mu\mu} \rangle_T$  and  $\langle F_{\mu\nu}^a F_{\mu\nu}^a \rangle_T$  in deconfining SU(2) and SU(3) Yang-Mills thermodynamics [Giacosa and RH 2008]
- ▶ on one-loop level, one has in effective theory:

$$\begin{aligned}\langle \theta_{\mu\mu} \rangle_T &= \rho - 3p \\ &= T^4 \left( 2\frac{\pi^2}{30} + \frac{3}{\pi^2} \int_0^\infty dx \frac{x^2 \sqrt{x^2 + a^2}}{e^{\sqrt{x^2 + a^2}} - 1} + \frac{2(2\pi)^4}{\lambda^3} \right. \\ &\quad \left. - 6\frac{\pi^2}{90} + \frac{3}{\pi^2} \int_0^\infty x^2 dx \ln \left( 1 - e^{-\sqrt{x^2 + a^2}} \right) + 6\frac{(2\pi)^4}{\lambda^3} \right),\end{aligned}$$

where  $a \equiv \frac{2e|\phi|}{T}$ ,  $|\phi| = \sqrt{\frac{\Lambda^3}{2\pi T}}$ ,  $\lambda \equiv \frac{2\pi T}{\Lambda}$ , and  $e \equiv \sqrt{8\pi}$  **almost everywhere** in deconfining phase.

## Trace anomaly, effectively

- ▶ use of one-loop approximation justified by **hierarchically suppressed, effective radiative corrections** (later)
- ▶ going from **fundamental** to **effective** fields  $\Rightarrow$  fundamental field strength  $F_{\mu\nu}$  suffers wave-function renormalization (**fundamental** radiative corrections); thus

$$\langle \mathcal{L}_{\text{YM}} \rangle_T = \frac{1}{4} \langle F_{\mu\nu}^a F^{a,\mu\nu} \rangle_T = f^2(g) \langle \mathcal{L}_{\text{dec-eff}} \rangle_T = f^2(g) \rho_{gs}$$

where  $\rho_{gs} = 4\pi\Lambda^3 T$ , and real function  $f(g)$  to be determined later.

(effective excitations do not contribute to average over action density!)

## Running coupling: temperature vs. resolution

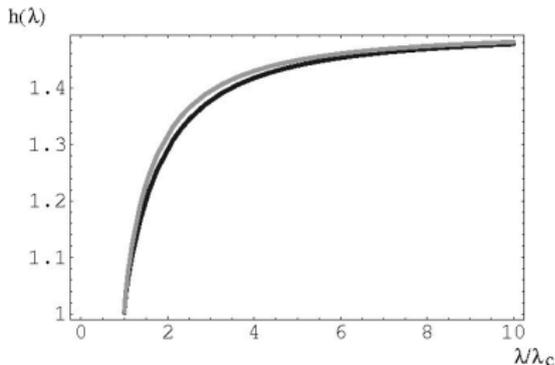
- ▶ in general:  $\beta(g) \equiv \mu \partial_\mu g$ .
- ▶ since (derivation of effective theory) a *natural* value for  $\mu$  is

$$\mu = |\phi| = \sqrt{\frac{\Lambda^3}{2\pi T}} \Rightarrow$$

$$\beta(g) \equiv |\phi| \partial_{|\phi|} g = -2T \partial_T g \equiv -2\beta_T(g)$$

- ▶ **moreover:** (\*) recast as  $h(\lambda) \equiv \frac{\rho-3\rho}{4\rho_{gs}} = -\frac{\beta_T(g)}{g} f^2(g)$ ,  
where perturbatively  $\beta_T(g) = -bg^3$  ( $b = \frac{11N}{48\pi^2}$ ,  $N = 2, 3$ ) at one loop

But:



Function  $h(\lambda)$  for SU(2) (gray) and SU(3) (black).

## Running coupling: temperature vs. resolution

⇒

$\beta$  function for running of  $g$  in dependence of  $T$   
**negative.**

⇒

$\beta$  function for running of  $g$  in dependence of  
resolution ( $\mu = |\phi|$ ) **positive.**

# Evaluation of gluon condensate

- ▶ **assumption:** in

$$h(\lambda) \equiv \frac{\rho - 3p}{4\rho_{gs}} = -\frac{\beta_T(g)}{g} f^2(g)$$

all nonperturbative and higher-loop effects contributing to  $h$  reside in  $\beta_T(g)$

$\Rightarrow f^2(g)$  can be determined from high- $T$  asymptotics  
(one-loop expression for  $\beta_T(g)$  and  $h_\infty = \frac{3}{2}$ )

$$\Rightarrow f(g) = \sqrt{\frac{3}{2b}} \frac{1}{g}.$$

- ▶ **gluon condensate:**  $\frac{1}{4} \langle F_{\mu\nu}^a F^{a,\mu\nu} \rangle_T = 4\pi\Lambda^3 T \frac{3}{2b} \frac{1}{g^2}$ ,  
where  $g$  is solution to

$$\beta_T(g) = -\frac{2}{3} b h(\lambda) g^3 \Leftrightarrow \partial_\lambda g = -\frac{2}{3} b \frac{h(\lambda)}{\lambda} g^3.$$

# Nonperturbative gauge-coupling evolution

- ▶ **without calculation:** evolution equation

$$\beta_T(g) = -\frac{2}{3} b h(\lambda) g^3 \Leftrightarrow \partial_\lambda g = -\frac{2}{3} b \frac{h(\lambda)}{\lambda} g^3.$$

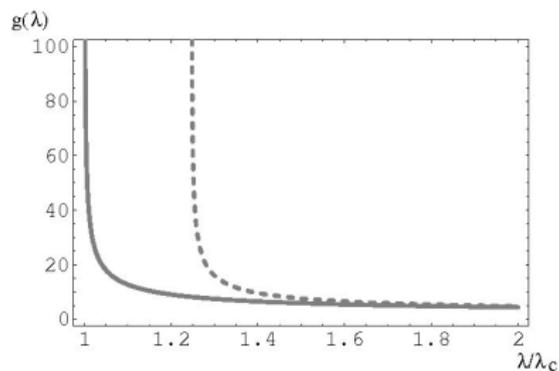
$\Rightarrow$  since  $h(\lambda) \leq \frac{3}{2}$  negative slope nonperturbatively screened

$\Rightarrow$  nonpert. Landau pole at lower  $T$  than pert. one

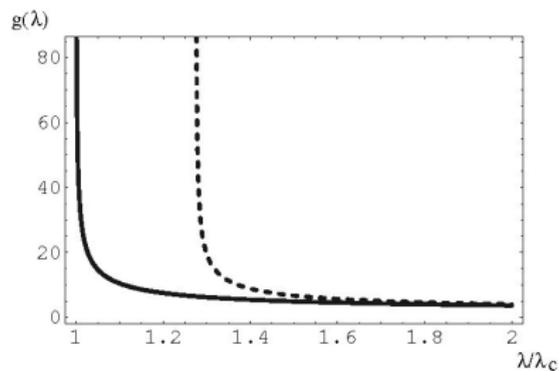
(Recall:  $T_L = T_0 \exp\left(-\frac{1}{2bg_0^2}\right)$  .)

- ▶ boundary conditions to evolution of  $g$ :
  - $e(\lambda)$  logarithmic pole at  $\lambda_c = 13.87$
  - $g(\lambda)$  nonperturbative Landau pole at  $\lambda_c = 13.87$
  - $g_P(\lambda)$  matches  $g(\lambda)$  at high  $\lambda$ , say, at  $\lambda = 10 \lambda_c$

# Nonperturbative gauge-coupling evolution:

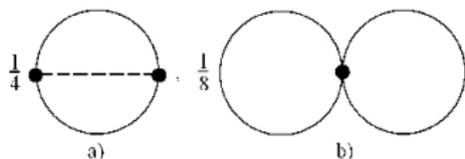


$g(\lambda)$  and  $g_P(\lambda)$  for SU(2).



$g(\lambda)$  and  $g_P(\lambda)$  for SU(3).

## Effective radiative corrections: 2-loop diagrams



solid (dashed) lines  $\leftrightarrow$  massive (massless) modes

$$\Delta P_a = \frac{1}{8i} \int \frac{d^4 p d^4 k}{(2\pi)^8} \Gamma_{[3]abc}^{\lambda\mu\nu}(p, k, -p, -k) \Gamma_{[3]rst}^{\rho\delta\tau}(-p, -k, p+k) \\ \times D_{\lambda\rho, ar}(p) D_{\mu\rho, bs}(k) D_{\nu\tau, ct}(-p, -k),$$

$$\Delta P_b = \frac{1}{8i} \int \frac{d^4 p d^4 k}{(2\pi)^8} \Gamma_{[4]abcd}^{\mu\nu\rho\delta} D_{\mu\nu, ab}(p) D_{\rho\delta, cd}(k)$$

plus constraints: on-shellness of massive modes,  $|(p+k)^2| \leq |\phi|^2$   
in diagram (b)

## 2-loop diagrams, constraints

- ▶ Potentially noncompact independent loop variables for 2-loop diag are  $(p_0, |\mathbf{p}|)$  and  $(k_0, |\mathbf{k}|)$ .  
Number of potentially noncompact independent loop variables  $\tilde{K} = 4$
- ▶ The constraints for 2-loop diagrams are
  - on-shellness:  $p^2 = k^2 = 4e^2|\phi|^2$
  - compositeness constraints:

$$\left| 4e^2 \pm \sqrt{x_1^2 + 4e^2} \sqrt{x_2^2 + 4e^2} - x_1 x_2 z_{12} \right| \leq \frac{1}{2},$$

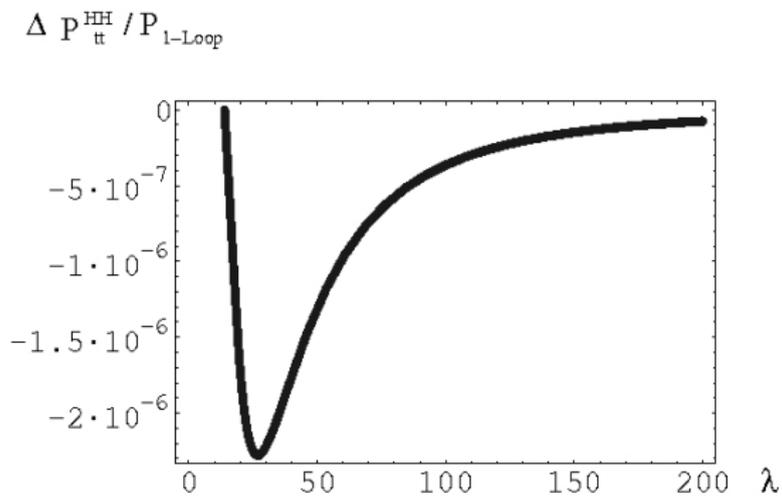
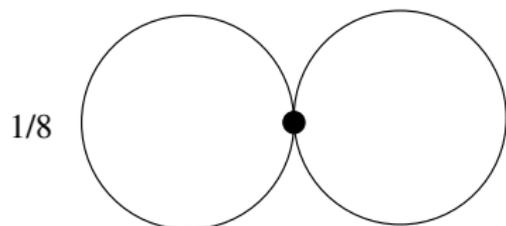
where  $x_1 \equiv \frac{|\mathbf{p}|}{|\phi|}$  and  $x_2 \equiv \frac{|\mathbf{k}|}{|\phi|}$

- ▶ For 2-loop, we have a total number of constraints

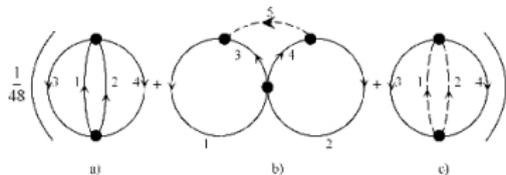
$$K = 1 + 2 = 3$$

- ▶ Thus for the 2-loop case: more noncompact loop variables than constraints:  $\tilde{K} > K$
- ▶  $\Rightarrow$  noncompact integration region

selected 2-loop diag. (b)



# Effective radiative corrections: 3-loop diagrams



Ir. 3-loop diagrams: Solid (dashed) lines are associated with the propagators of massive (massless) modes

$$\Delta P_a = \frac{1}{48} \int \frac{d^4 p_1 d^4 p_2 d^4 p_3}{(2\pi)^4 (2\pi)^4 (2\pi)^4} \Gamma_{[4]abcd}^{\mu\nu\rho\sigma} \Gamma_{[4]\bar{a}\bar{b}\bar{c}\bar{d}}^{\bar{\mu}\bar{\nu}\bar{\rho}\bar{\sigma}} \times D_{\rho\bar{\rho},c\bar{c}}(p_1) D_{\sigma\bar{\sigma},d\bar{d}}(p_2) D_{\mu\bar{\mu},a\bar{a}}(p_3) D_{\nu\bar{\nu},b\bar{b}}(p_4),$$

$$\Delta P_b = \frac{1}{48} \int \frac{d^4 p_1 d^4 p_2 d^4 p_3}{(2\pi)^4 (2\pi)^4 (2\pi)^4} \Gamma_{[4]hijk}^{\alpha\beta\gamma\lambda} \Gamma_{[3]abc}^{\mu\nu\rho} \Gamma_{[3]\bar{a}\bar{b}\bar{c}}^{\bar{\mu}\bar{\nu}\bar{\rho}} D_{\mu\alpha,ah}(p_1) \times D_{\bar{\mu}\bar{\beta},\bar{a}\bar{i}}(p_2) D_{\gamma\rho,jc}(p_3) D_{\lambda\bar{\rho},k\bar{c}}(p_4) D_{\mu\bar{\nu},b\bar{b}}(p_5)$$

$$\Delta P_c = \frac{1}{48} \int \frac{d^4 p_1 d^4 p_2 d^4 p_3}{(2\pi)^4 (2\pi)^4 (2\pi)^4} \Gamma_{[4]abcd}^{\mu\nu\rho\sigma} \Gamma_{[4]\bar{a}\bar{b}\bar{c}\bar{d}}^{\bar{\mu}\bar{\nu}\bar{\rho}\bar{\sigma}} D_{\rho\bar{\rho},c\bar{c}}(p_1) \times D_{\sigma\bar{\sigma},d\bar{d}}(p_2) D_{\mu\bar{\mu},a\bar{a}}(p_3) D_{\nu\bar{\nu},b\bar{b}}(p_4)$$

## 3-loop diagrams, general constraints

- ▶ Potentially noncompact independent loop variables for ir. 3-loop diags are  $(p_0, |\mathbf{p}|)_i$  for  $i = 1, 2, 3$ .  
Number of potentially noncompact independent loop variables

$$\tilde{K} = 6$$

- ▶ The compositeness constrains for ir. 3-loop diags. are

$$|(p_1 + p_2)^2| \leq |\phi|^2 \quad (s \text{ channel})$$

$$|(p_3 - p_1)^2| \leq |\phi|^2 \quad (t \text{ channel})$$

$$|(p_2 - p_3)^2| \leq |\phi|^2 \quad (u \text{ channel})$$

- ▶ Additional constraints depend on the number of massless and massive propagators in each individual ir. 3-loop diag.

## Constraints and compactness: ir. 3-loop diag. (a) and (b)

- ▶ We have 3 compositeness constraints due to the s-, t-, u-channels
- ▶ In addition to the compositeness constraints, we have the on-shellness conditions:

$$p_1^2 = m^2, \quad p_2^2 = m^2, \quad p_3^2 = m^2, \quad p_4^2 = (p_1 + p_2 - p_3)^2 = m^2$$

- ▶ The max. off-shellness of the massless mode in diag. (b) is automatically satisfied by the t-channel due to momentum conservation,  $p_5 = p_1 - p_3$
- ▶ The total number of constraints for diag. (a) and (b) is

$$K = 3 + 4 = 7$$

- ▶ Thus for ir. 3-loop diag. (a) and (b) we have

$$\tilde{K} = 6 < 7 = K$$

⇒ Compact integration region

## Constraints and compactness: ir. 3-loop diag. (c)

- ▶ As before, we have 3 compositeness constraints over the s-, t-, u-channels
- ▶ In addition to the compositeness constraints, the on-shellness relations for the massive modes in diag. (c)

$$p_3^2 = m^2, \quad p_4^2 = (p_1 + p_2 - p_3)^2 = m^2$$

- ▶ For diag. (c), we also have the following constraints due to the max. off-shellness

$$|p_1^2| \leq |\phi|^2, \quad |p_2^2| \leq |\phi|^2$$

- ▶ The above constraints yield for diag. (c)

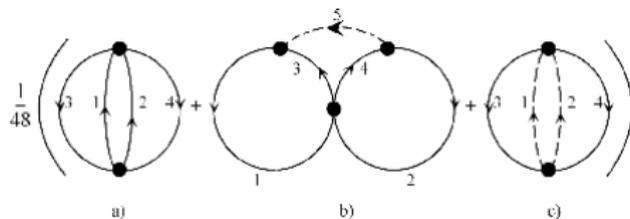
$$K = 3 + 4 = 7$$

- ▶ Thus for all ir. 3-loop diag.  $K = 3 + 4 = 7$  and

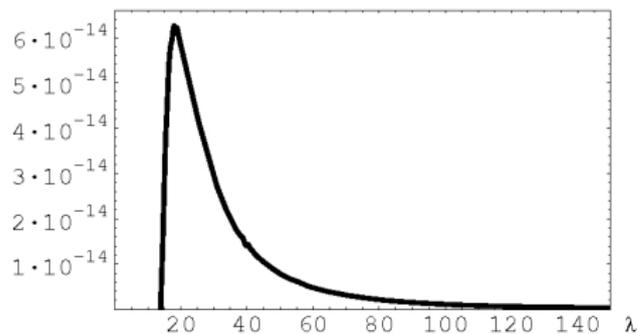
$$\tilde{K} < K$$

⇒ Compact or empty integration region

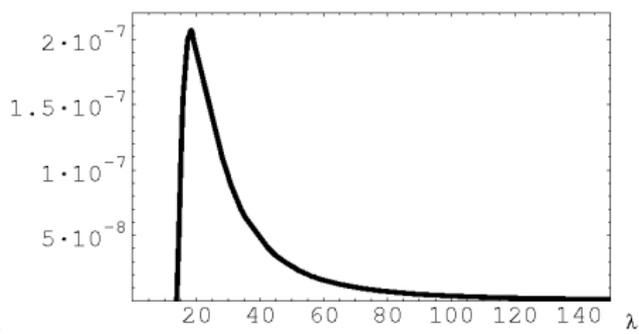
results: ir. 3-loop diag. (a) and (b)



$>|\Delta P_A|/P_{1\text{-loop}}$



$>|\Delta P_B|/P_{1\text{-loop}}$



## Hierarchy between 2-loop and 3-loop corrections

- ▶ Ir. 3-loop integrations generate **hierarchically suppressed contributions** to the pressure over the 2-loop contributions:

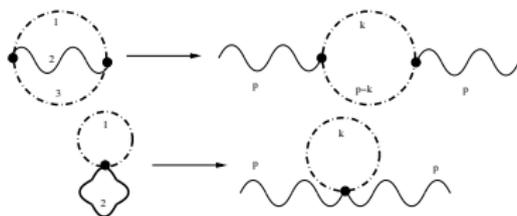
$$\frac{P_{2\text{-loop}}}{P_{1\text{-loop}}} \leq 10^{-2}$$

$$\frac{P_{3\text{-loop}}}{P_{1\text{-loop}}} \leq 10^{-5} \frac{P_{2\text{-loop}}}{P_{1\text{-loop}}} = 10^{-7}$$

- ▶ Ir. 3-loop integrations are **either compact** (ir. diags. (a)-(b)) **or empty** (ir. diag. (c)) whereas 2-loop integrations are noncompact
- ▶ The most striking difference between 2-loop and 3-loop corrections: the contribution from the ir. 3-loop diag. (c) is vanishing; no 2-loop diagram has this property

## Relation between pressure and polarization tensor

The polarization tensor is a sum over connected bubble diags. with one internal line of momentum  $p$  cut, such that the diag. remains connected, and the two so-obtained external lines amputated



Consequences:

- ▶ The hierarchical suppression of 3-loop compared to 2-loop justifies the **calculation of the polarization tensor on 1-loop level**.
- ▶ The vanishing of a connected bubble diag. due to a zero-measure support for its loop-momenta integrations implies that the associated contribution to a polarization tensor is also nil.

## Effective radiative corrections: Pol. tensor massless mode

**modified dispersion laws:** transverse and longitudinal parts (real time)

$$D_{\mu\nu,ab}^{TLM}(p_t) = -\delta_{a3}\delta_{b3}P_{\mu\nu}^T \left[ \frac{i}{p_t^2 - G} + 2\pi\delta(p_t^2 - G) n_B(|p_{0,t}|/T) \right]$$
$$D_{\mu\nu,ab}^{TLM}(p_l) = \delta_{a3}\delta_{b3}u_\mu u_\nu \left[ \frac{p_l^2}{\mathbf{p}_l^2} \frac{i}{p_l^2 - F} - 2\pi\delta(p_l^2 - F) n_B(|p_{0,l}|/T) \right]$$

Poles yield dispersion relations ( $p_0 = \omega + i\gamma$ , assume  $\gamma \ll \omega$ ):

$$\omega_t^2(\mathbf{p}_t) = \mathbf{p}_t^2 + \text{Re}G(\omega(\mathbf{p}_t), \mathbf{p}_t) \qquad \omega_l^2(\mathbf{p}_l) = \mathbf{p}_l^2 + \text{Re}F(\omega_L(\mathbf{p}_l), \mathbf{p}_l)$$
$$\gamma(\mathbf{p}_t) = -\text{Im}G(\omega(\mathbf{p}_t), \mathbf{p}_t)/2\omega \qquad \gamma_l(\mathbf{p}_l) = -\text{Im}F(\omega_l(\mathbf{p}_l), \mathbf{p}_l)/2\omega_l$$

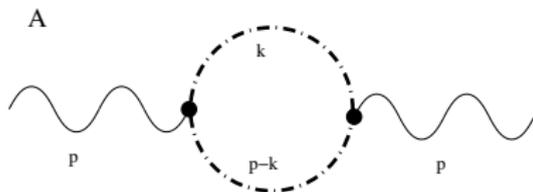
## Pol. tensor massless mode cntd.

Choosing  $\mathbf{p} \parallel \mathbf{e}_3$ :

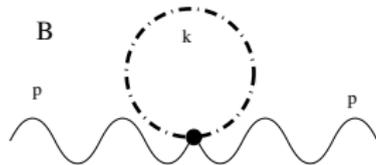
$$G(p_0, \mathbf{p}) = \Sigma^{11} = \Sigma^{22}$$

$$F(p_0, \mathbf{p}) = \left(1 - \frac{p_0^2}{p^2}\right)^{-1} \Sigma^{00}$$

$\Sigma^{\mu\nu}$  sum of two diagrams:



Purely imaginary:  $\Rightarrow$  yields  $\gamma$   
One-loop level sufficient!



Purely real:  $\Rightarrow$  yields dispersion  
relation

## Full calculation of $G$

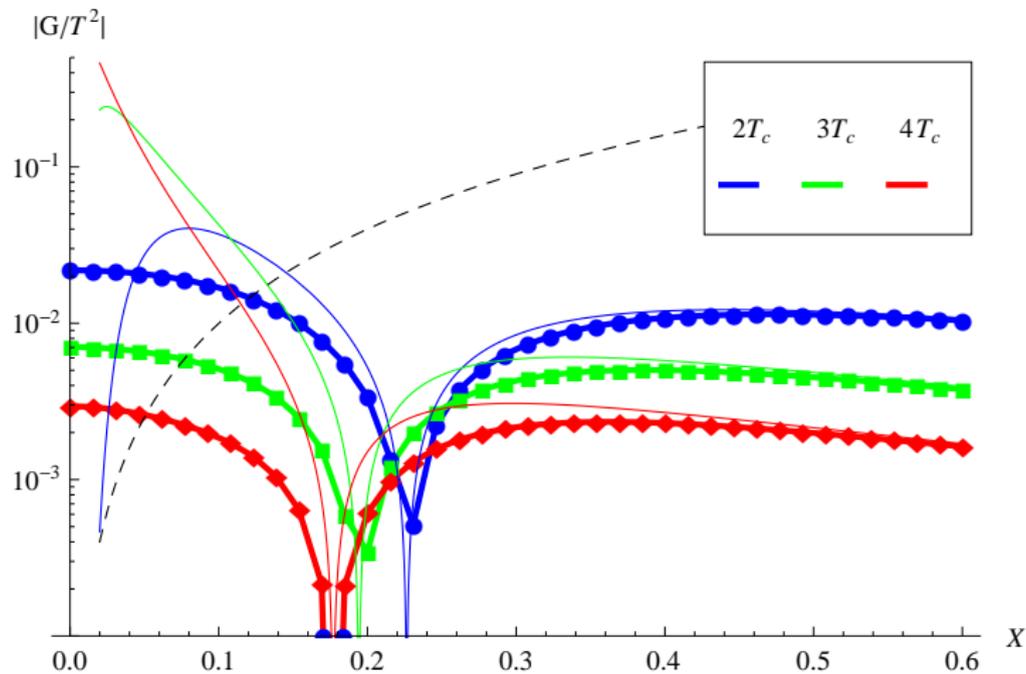
Gap equation:

$$\begin{aligned}\operatorname{Re}G(p_0, \mathbf{p}) &= 8\pi e^2 \int_{|(p+k)^2| \leq |\phi|^2} \left[ - \left( 3 - \frac{k^2}{m^2} \right) + \frac{k^1 k^1}{m^2} \right] \\ &\quad \times n_B(|k_0|/T) \delta(k^2 - m^2) \frac{d^4 k}{(2\pi)^4} \Big|_{p^2=G} \\ &\equiv H(T, \mathbf{p}, G)\end{aligned}$$

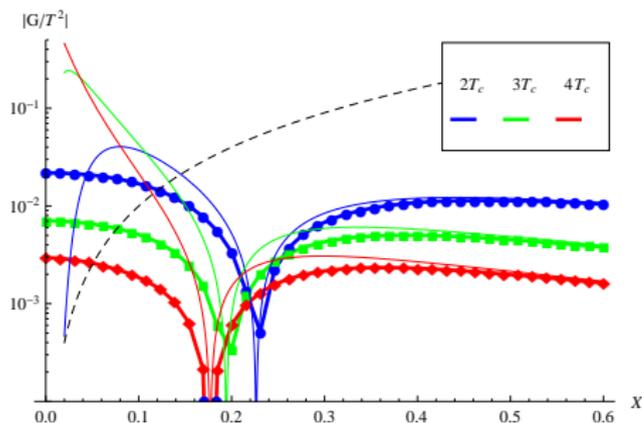
Via  $\delta$ -function, integration over  $k_0$  yields  $k_0 \rightarrow \pm\sqrt{\mathbf{k}^2 + m^2}$ .  
With  $p_0 = \pm\sqrt{\mathbf{p}^2 + G(p_0, \mathbf{p})}$  and  $\mathbf{p} \parallel \mathbf{e}_3$  constraint reads

$$\left| G + 2 \left( \pm\sqrt{\mathbf{p}^2 + G} \sqrt{\mathbf{k}^2 + m^2} - pk_3 \right) + m^2 \right| \leq |\phi|^2$$

# Selfconsistent result for $G$ , real part



## Selfconsistent result for $G$ , real part



- ▶  $X \gtrsim 0.2$ :  $G < 0$   
(anti-screening)
- ▶ Dip:  $G = 0$
- ▶  $X \lesssim 0.2$ :  $G > 0$   
(screening)

Comparison with approximate result:

- ▶ Zeros of  $G$  agree (must be)
- ▶ For  $X \gtrsim 0.2$ , approximate agrees with selfconsistent result (expected)
- ▶ Results different when  $G \gtrsim X^2$  (not surprising)

## Selfconsistent result for $G$ , imaginary part

Imaginary part:  $\text{Im}G \propto$  

At left vertex: particle with mass  $\sqrt{G}$  decaying into two on-shell particles with mass  $m$  only possible if

$$\frac{G}{T^2} \geq 4 \frac{m^2}{T^2} = 64\pi^2 \frac{e^2}{\lambda^3} \quad (1)$$

- ▶  $G \leq 0$ : condition (1) never satisfied
- ▶  $G > 0$ :

$$\frac{G(X=0, T)}{T^2} \propto \frac{1}{\lambda^3} \ll 64\pi^2 \frac{e^2}{\lambda^3} \sim 5 \times 10^4 / \lambda^3$$

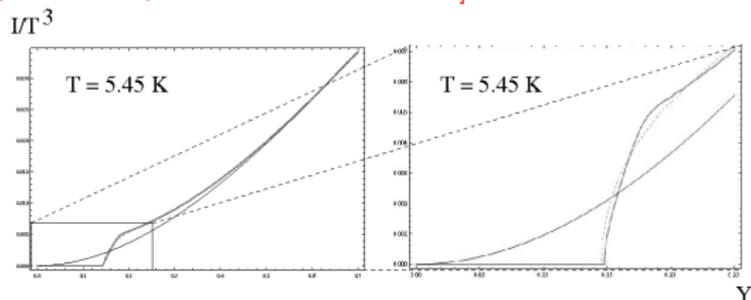
condition (1) never satisfied

Diagram  $A = 0$ , hence no imaginary part of  $G$ , hence  $\gamma = 0$  and assumption  $\gamma \ll \omega$  satisfied trivially.

# Black-body spectra for $T \sim T_c$

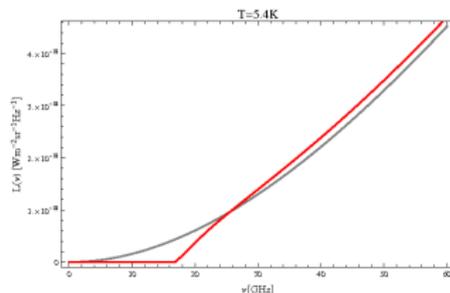
## modification of U(1) by screening function $G$ :

[Schwarz, Hofmann, Giacosa 2006; Ludescher and Hofmann 2008]



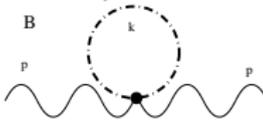
## postulating SU(2) as theory for photon propagation:

- ▶  $T_c = 2.725$  K, UEGE confirmed by Arcade2 [Hofmann 2009]
- ▶ measurable gap in spectral radiance [Falquez, Hofmann, Baumbach 2010]



## Full calculation of $F$

Assume  $F \in \mathbb{R}$  (turns out to be selfconsistent)

Apply Feynman rules to  $\mathbf{p}^2 = \text{Re}\Sigma^{00} =$    
yields gap equation:

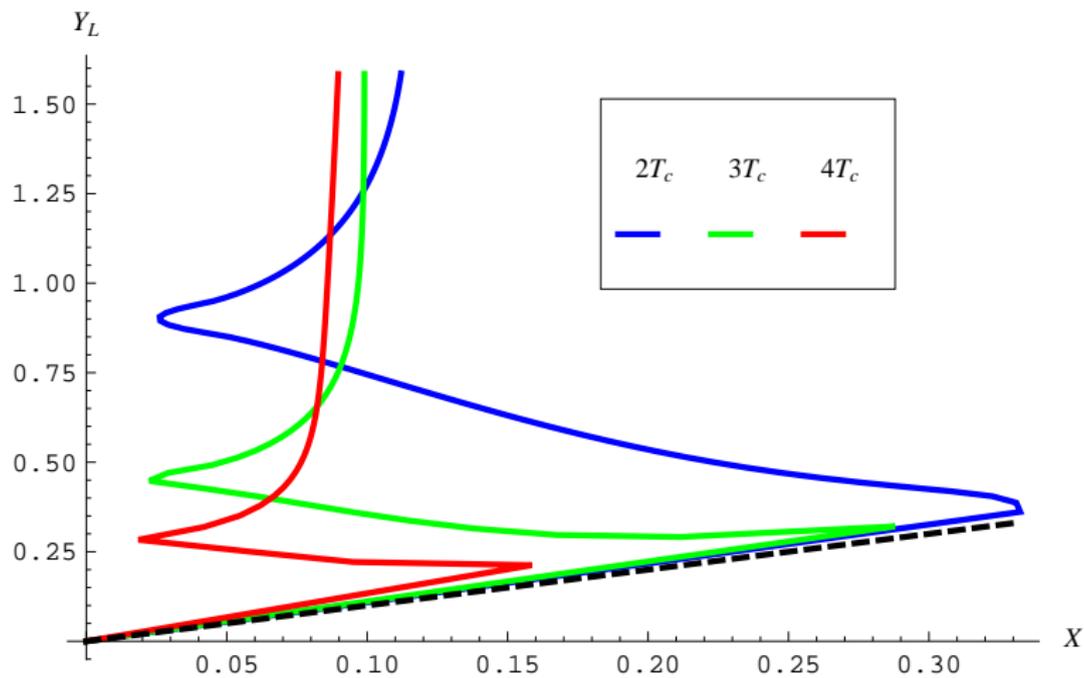
$$\mathbf{p}^2 = \Sigma_{\text{B}}^{00}(p) = 8\pi e^2 \int_{|(p+k)^2| \leq |\phi|^2} \left[ \left( 3 - \frac{k^2}{m^2} \right) + \frac{k^0 k^0}{m^2} \right] \times n_{\text{B}}(|k_0|/T) \delta(k^2 - m^2) \frac{d^4 k}{(2\pi)^4} \Big|_{p^2=F} \quad (2)$$

Strategy to find  $F$  similar to that of finding  $G$

[Falquez, Hofmann, Baumbach 2010].

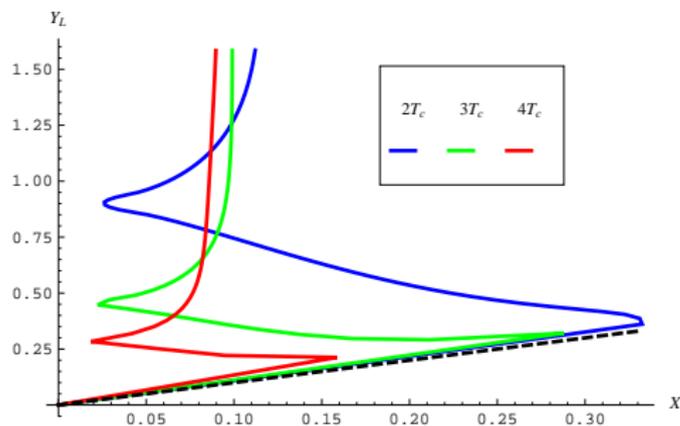
## Selfconsistent result for $F$

$$Y_l \equiv \frac{\omega_l(\mathbf{p}_l, T)}{T} = \sqrt{\frac{F(p_l^2, T)}{T^2} + \frac{\mathbf{p}_l^2}{T^2}}, \quad X \equiv |\mathbf{p}_l|/T$$



## Selfconsistent result for $F$

$$Y_l \equiv \frac{\omega_l(\mathbf{p}_l, T)}{T} = \sqrt{\frac{F(p_l^2, T)}{T^2} + \frac{\mathbf{p}_l^2}{T^2}}, \quad X \equiv |\mathbf{p}_l|/T$$



- ▶ 3 branches
- ▶  $Y_L$  defined only for  $X \lesssim 0.34$
- ▶ superluminal group velocity

# Selfconsistent result for $F$ , interpretation

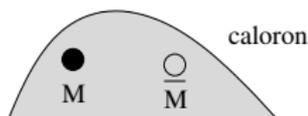
charge-density waves  $\leftrightarrow$  interpretation in terms of magnetic monopoles

[Falquez, Hofmann, Baumbach 2011]

- ▶ longitudinal modes due to charge density waves
- ▶ light like propagation:
  - ▶ stable (yet unresolved) monopoles released by large holonomy caloron dissociation [Diakonov et al. 2004]
  - ▶ density disturbance can only be propagated by radiation field, which propagates at the speed of light



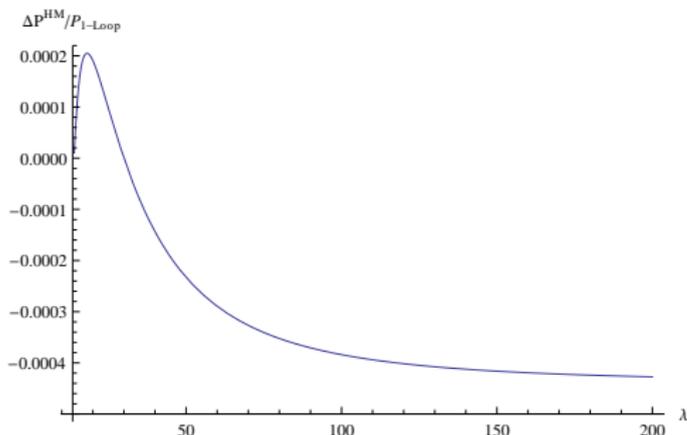
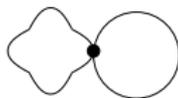
- ▶ superluminal propagation:
  - ▶ unstable monopoles contained in small holonomy caloron
  - ▶ extended calorons provide instantaneous correlation between monopoles, leading to superluminal propagation



## A particular 2-loop correction to pressure

▶ “Bubble diagrams” yield pressure

▶ For  $T \gg T_c$  only relevant diagram:



▶  $\Delta P \propto -4 \times 10^{-4} T^4$

▶ Temperature of TLM gas reduced!

# Monopole properties

## Explanation

Energy used to break up calorons, creating monopole anti-monopole pairs

[Schwarz et al. 2006; Ludescher et al. 2008]

Detailed analysis shows [Ludescher et al. 2008]:

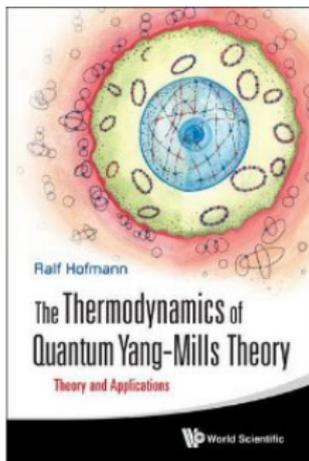
- ▶ average monopole-antimonopole distance  $\bar{d} < |\phi|^{-1}$   
⇒ monopoles unresolved in effective theory
- ▶ screening length  $l_s$  due to small-holonomy calorons:  $l_s = 3.3\bar{d}$   
⇒ magnetic flux of monopole and antimonopole cancel (no area law for spatial Wilson loop)

# Summary

## Summary:

- ▶ computation of nonperturbative running of **fundamental** coupling  $g$ :  
definition via trace anomaly,  $\beta$  function **positive** w.r.t. running **resolution**,  $\beta$  function **negative** w.r.t. running **temperature**, mild screening of Landau pole
- ▶ radiative corrections: pressure at 2-loops and 3-loops; large hierarchy
- ▶ radiative corrections: polarization tensor of massless mode
- ▶ radiative corrections: black-body anomaly
- ▶ radiative corrections: monopole-antimonopole density, mean distance, screening length

To appear early November 2011.



Contains **applications** of  $SU(2)_{\text{CMB}}$   
( $\Lambda \sim 10^{-4}$  eV) to:

- ▶ black-body anomaly
- ▶ contradiction to SM Higgs sector derived from primordial He abundance bounds on freezeout temperature for nucleosynthesis in case  $SU(2)_{\text{CMB}}$  confirmed
- ▶ **U**nexplained **E**xtra**G**alactic **E**mission
- ▶ primordial, magnetic seed fields
- ▶ stability of cold, dilute H1 clouds in Milky Way

**Thank you.**