

# **SUSY parameter determination with SFITTER**

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## Introduction

SFITTER is designed to be a tool to determine SUSY parameters from experimental measurements

Started in the GDR and as a project in Les Houches 2003

Languages used: C and Fortran

Different approaches used:

- analytical calculations (J.-L. Kneur et al., J. Kalinowski et al.)
- calculating model sets and interpolating (G. Polesello)

Difficulties:

- many parameters, e.g. MSSM
  - not so good for a GRID (CPU-time), slightly better for fit
- starting point dependence of fit
  - fit by starting values could be confined to a “wrong” region or biased to the “right region”, GRID is less biased

SFITTER uses both approaches and allows to combine them

Complete use:

1. GRID (subset of parameters with subset of measurements) others fixed
2. GRID parameters fixed and non-GRID parameters fit
3. fit of all parameters

Caveat: for the GRID separable subset of parameters and measurements, e.g. in the MSSM neutralino and chargino masses for  $M_1, M_2, \mu, \tan\beta$

## SFITTER

Backbone of SFITTER are

- SUSPECT (Jean-Loic, Abdelhak, Gilbert) for the mass calculations
- MSMLib (Gerardo Ganis) for branching ratios and  $e^+e^-$  cross sections
- Prospino (Michael Spira, T.P. et al) NLO for pp cross sections
- MINUIT

Long term: be able to use different calculations/tools such a PYTHIA, SoftSUSY, etc

In practice

driven by sfit\_params.in

```
// Select model : MSUGRA GMSB AMSB pMSSM pMSSM-HighScale
MODEL = MSUGRA
// pre-fit/SCAN
GRID = 0
//Parameters for MSUGRA - Only sign of MU matters
M0 = 500. [G/M] STEP=20. LOW=0. HIGH=1000. GRID=10
M1/2 = 500. [G/M] STEP=50. LOW=0. HIGH=1000. GRID=10
TANB = 50. [G/M] STEP=20. LOW=0. HIGH=100. GRID=10
A0 = 0. [G/M] STEP=200. LOW=-1000. HIGH=1000. GRID=20
SGNMU = 1. [-/-] STEP=0 LOW=1. HIGH=1.
```

and sfit\_data.in

```
// Automatically set data error to 0.5%
DATA_ERR = 0.005
// Automatically smear data measurements with a gaussian
RANDOMIZE = 0
// Higgs masses
m_h = 111.6 +/- 11.16 [-/M]
// neutralino masses
m_chi+_1 = 182.3 +/- 18.23 [G/M]
m_chi0_1 = 97.03 +/- 97.03 [G/M]
// Correlations
//CORR(m_chi+_1,m_chi+_2) = 0.03
```

## Data Sets SPS1a by G. Blair, G. Polesello et al.

Scope of the analysis:

central value of all masses of SPS1a MSUGRA by SUSPECT

theoretical errors zero

no correlations between measurements

Particle	mass	DATA Set LHC	DATA Set LC	DATA Set LHCLC
h	111.6	0.1	0.05	0.05
A	399.1		1.5	1.5
H	399.6		1.5	1.5
H+	407.1		1.5	1.5
$\chi_1$	97.03	4.8	0.05	0.05
$\chi_2$	182.9	4.7	1.2	0.08
$\chi_4$	370.3	5.1		2.3
$\chi_1^\pm$	182.3		0.55	0.55
$\chi_2^\pm$	370.6		3.0	3.0
$\tilde{g}$	615.7	8.0		6.4
$\tilde{t}_1$	411.8		2.0	2.0
$\tilde{b}_1$	520.8	7.5		5.7
$\tilde{b}_2$	550.4	7.9		6.2
$\tilde{c}_1$	551.0	23.6		23.6
$\tilde{c}_2$	570.8	17.4		9.8
$\tilde{u}_1$	551.0	23.6		23.6
$\tilde{u}_2$	570.8	17.4		9.8
$\tilde{s}_1$	549.9	23.6		23.6
$\tilde{s}_2$	576.4	17.4		9.8
$\tilde{d}_1$	549.9	23.6		23.6
$\tilde{d}_2$	576.4	17.4		9.8
$\tilde{\tau}_1$	135.5	8.6	0.3	0.3
$\tilde{\tau}_2$	207.9		1.1	1.1
$\tilde{\mu}_1$	144.9	4.8	0.2	0.2
$\tilde{\mu}_2$	204.2	5.0	0.5	0.5
$\tilde{e}_1$	144.9	4.8	0.05	0.05
$\tilde{e}_2$	204.2	5.0	0.2	0.2
$\tilde{\nu}_e$	188.2		0.7	0.7

LC strong on Higgs and Sleptons plus stop

LHC strong on gluinos and squarks

Giacomo et al: use of LC  $\chi_1$  mass in LHC analyses improves

## MSUGRA in SPS1a

all parameters correlated in MSUGRA

→ fit from an unbiased starting point (GRID would be full set of parameters)

Parameter	SPS1a	Starting point
$m_0$	100	500
$m_{1/2}$	250	500
$\tan \beta$	10	50
$A_0$	-100	0
$\mu$	+	+

Results:

Parameter	LHC	$\Delta$ LHC	LC	$\Delta$ LC	LHCLC	$\Delta$ LHCLC
M0	100.08	4.1	100.03	0.08	100.04	0.08
M1/2	249.95	1.8	250.02	0.13	250.01	0.10
$\tan \beta$	9.87	1.0	9.98	0.15	9.98	0.14
A0	-99.00	30.8	-98.24	4.56	-98.21	4.23
$\chi^2/\text{dof}$	0.00291/16		0.68719/12		0.71148/24	

- central values ok → good chi2 for all fits
- LC is more precise by at least a factor 10 on all parameters
- the errors for LHCLC are improved slightly over LC alone
- the errors for LHCLC are improved significantly over LHC

Correlation Matrix for the LHC measurement

	M0	M1/2	$\tan \beta$	A0
M0	1.00000	-0.40043	-0.02132	-0.14219
M1/2	-0.40043	1.00000	0.16614	0.43014
$\tan \beta$	-0.02132	0.16614	1.00000	0.88300
A0	-0.14219	0.43014	0.88300	1.00000

To be added: correlations in measurements

LC: error on  $m_h$  10 times worse  $A_0$  and  $\tan \beta$  wrong with bad  $\chi^2$

## MSSM

- using all sparticle and Higgs masses with 0.5% precision on all masses
- GRID in  $\mu$ ,  $\tan \beta$ ,  $M_1$ ,  $M_2$  (GRID 100GeV, 10, 100GeV, 100GeV)
- GRID for chargino and neutralino masses
- other starting points: “SOLUTION”  
 → unbiased in first approx only for  $\mu$ ,  $\tan \beta$ ,  $M_1$ ,  $M_2$
- SUSPECT M(MSUGRA→MSSM)!=M(MSSM)  $\sim 1\%$   
 → datasets MSUGRA  $\neq$  MSSM  
 → new version from Jean-Loic expected soon

	AfterGrid	AfterFit	SPS1a		AfterGrid	AfterFit	SPS1a
$\tan \beta$	100	$10.02 \pm 3.4$	10	$M_{\tilde{u}_R}$	532.1	$532.1 \pm 2.8$	532.1
$M_1$	100	$102.2 \pm 0.74$	102.2	$M_{\tilde{d}_R}$	529.3	$529.3 \pm 2.8$	529.3
$M_2$	200	$191.79 \pm 1.9$	191.8	$M_{\tilde{c}_R}$	532.1	$532.1 \pm 2.8$	532.1
$M_3$	589.4	$589.4 \pm 7.0$	589.4	$M_{\tilde{s}_R}$	529.3	$529.3 \pm 2.8$	529.3
$\mu$	300	$344.3 \pm 1.3$	344.3	$M_{\tilde{t}_R}$	420.2	$420.08 \pm 13.3$	420.2
$m_A$	399.35	$399.1 \pm 1.2$	399.1	$M_{\tilde{b}_R}$	525.6	$525.5 \pm 10.1$	525.6
$M_{\tilde{e}_R}$	138.2	$138.2 \pm 0.76$	138.2	$M_{\tilde{q}1_L}$	553.7	$553.7 \pm 2.1$	553.7
$M_{\tilde{\mu}_R}$	138.2	$138.2 \pm 0.76$	138.2	$M_{\tilde{q}2_L}$	553.7	$553.7 \pm 2.1$	553.7
$M_{\tilde{\tau}_R}$	135.5	$135.48 \pm 2.3$	135.5	$M_{\tilde{q}3_L}$	501.3	$501.42 \pm 10.$	501.3
$M_{\tilde{e}_L}$	198.7	$198.7 \pm 0.68$	198.7	$A_{\tilde{\tau}}$	-253.5	$-244.7 \pm 1428$	-253.5
$M_{\tilde{\mu}_L}$	198.7	$198.7 \pm 0.68$	198.7	$A_{\tilde{t}}$	-504.9	$-504.62 \pm 27.$	-504.9
$M_{\tilde{\tau}_L}$	197.8	$197.81 \pm 0.92$	197.8	$A_{\tilde{b}}$	-797.99	$-825.2 \pm 2494$	-799.4

- GRID: ok for  $\mu$ ,  $M_1$ ,  $M_2$ , not ok for  $\tan \beta$  (secondary minimum)  
 → but Higgs masses undefined in this point (info needs to be added)
- Fit after Grid converging correctly in spite of  $\tan \beta$  problem
- precision of 0.5% is insufficient for  $A_{\tilde{\tau}}$  and  $A_{\tilde{b}}$

- Datasets LC, LHC with all starting points: “SOLUTION” and FIT only
  - Dataset LHCLC with all starting points: “SOLUTION”
- except GRID  $\mu$ ,  $M_1$ ,  $M_2$ ,  $\tan \beta$  with chargino and neutralino masses

Parameter	LHC	LC	LHCLC	SPS1a
$\tan \beta$	$10.23 \pm 4.3$	$10.26 \pm 1.6$	$10.16 \pm 1.4$	10
$M_1$	$102.45 \pm 5.1$	$102.32 \pm 0.3$	$102.17 \pm 0.2$	102.2
$M_2$	$191.8 \pm 6.0$	$192.52 \pm 1.2$	$191.71 \pm 0.8$	191.8
$M_3$	$578.68 \pm 15.$	<b>FIXED 500</b>	$589.51 \pm 15.$	589.4
$M_{\tilde{\tau}_L}$	<b>FIXED 500</b>	$197.68 \pm 3.3$	$198.62 \pm 2.9$	197.8
$M_{\tilde{\tau}_R}$	$129.03 \pm 9.0$	$135.66 \pm 4.4$	$134.28 \pm 4.0$	135.5
$M_{\tilde{\mu}_L}$	$198.7 \pm 5.1$	$198.7 \pm 0.5$	$198.7 \pm 0.5$	198.7
$M_{\tilde{\mu}_R}$	$138.2 \pm 5.0$	$138.2 \pm 0.2$	$138.2 \pm 0.2$	138.2
$M_{\tilde{e}_L}$	$198.7 \pm 5.1$	$198.7 \pm 0.2$	$198.7 \pm 0.2$	198.7
$M_{\tilde{e}_R}$	$138.2 \pm 5.0$	$138.2 \pm 0.06$	$138.2 \pm 0.06$	138.2
$M_{\tilde{q}_3 L}$	$498.1 \pm 108$	$497.6 \pm 51.$	$499.97 \pm 32.$	501.3
$M_{\tilde{t}_R}$	<b>FIXED 500</b>	$420 \pm 24.$	$420.25 \pm 15.$	420.2
$M_{\tilde{b}_R}$	$522.38 \pm 112$	<b>FIXED 500</b>	$526.93 \pm 32.$	525.6
$M_{\tilde{q}_2 L}$	$550.73 \pm 13.$	<b>FIXED 500</b>	$553.74 \pm 7.0$	553.7
$M_{\tilde{c}_R}$	$529.02 \pm 24.$	<b>FIXED 500</b>	$532.14 \pm 24.$	532.1
$M_{\tilde{s}_R}$	$526.21 \pm 24.$	<b>FIXED 500</b>	$529.34 \pm 24.$	529.3
$M_{\tilde{q}_1 L}$	$550.73 \pm 13.$	<b>FIXED 500</b>	$553.74 \pm 7.1$	553.7
$M_{\tilde{u}_R}$	$529.02 \pm 24.$	<b>FIXED 500</b>	$532.14 \pm 24.$	532.1
$M_{\tilde{d}_R}$	$526.2 \pm 24.$	<b>FIXED 500</b>	$529.34 \pm 24.$	529.3
$A_{\tilde{\tau}}$	<b>FIXED 0</b>	$-202.7 \pm 1007$	$118.32 \pm 1100$	-253.5
$A_{\tilde{t}}$	$-507.7 \pm 54.$	$-501.95 \pm 15.$	$-503.11 \pm 13.$	-504.9
$A_{\tilde{b}}$	$-741.55 \pm 35228$	<b>FIXED 0</b>	$-250.7 \pm 13513$	-799.4
$m_A$	<b>FIXED 500</b>	$399.1 \pm 0.9$	$399.1 \pm 0.9$	399.1
$\mu$	$345.21 \pm 6.4$	$344.34 \pm 3.5$	$344.36 \pm 2.1$	344.3
$\chi^2/\text{dof}$	0 / 0	0.00097 / 1	0.00058 / 4	

- the MSSM results show better the complementarity of LHC and LC than MSUGRA
  - use of cross sections and branching ratios should improve  $A_\tau$ ,  $A_b$
  - LC and LHC with GRID as LHCLC converge on a secondary minimum with a GOOD  $\chi^2$
- compatibility of secondary minimum to be investigated, GRID size etc

## Conclusions and Perspectives

### SFITTER

- GRID and FIT of MSUGRA and MSSM
- uses masses from SUSPECT
- uses  $e^+e^-$  cross sections and branching ratios from MSMlib
- uses pp cross sections Prospino
- MSUGRA in SPS1a
  - LHC, LC and LHCLC datasets converge correctly
  - LC may be sensitive to error on Higgs mass
  - improvement of LHC by adding LC seen in parameter errors
  - improvement of LC by LHC not obvious....
- MSSM in SPS1a
  - GRID use for subset of parameters and measurements with good convergence
  - system underdetermined for LC and LHC, but ok for LHCLC
  - $A_\tau$  and  $A_b$  undetermined
  - many parameters show the superiority LHCLC with respect to LHC and LC alone

Future:

- unbias MSSM-SPS1a further
- use correlations in measurements
- check dependence of the result on the fixed parameters
- implement edge measurements
- new version of SUSPECT expected soon
- AMB, GMSB implemented and to be debugged