

MEASURING THE MSSM LAGRANGEAN

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- Supersymmetry at the LHC
- Higher order cross sections: Prospino2
- SUSY plus jets: SmadGraph
- Parameter extraction: Sfitter

TeV SCALE SUPERSYMMETRY

Bright side

- ★ 3 running gauge couplings meet — GUT gauge group
- ★ 2 Higgs doublets — radiative symmetry breaking
- ★ R parity — stable proton yields dark matter
- ★ local supersymmetry – including gravity?
- ★ **rich LHC phenomenology** — no nasty surprises

Dark side

- ★ unknown SUSY breaking
 - masses, scalar couplings, phases...
 - e.g. hierarchical spectrum? [Split SUSY]
 - ★ flavor physics and SUSY breaking
 - CKM and lepton flavor?
 - ★ 2 Higgs doublet model
 - μ parameter and SUSY breaking?
- ⇒ **as many as exclusive analyses as possible**

		spin	d.o.f.	
quark	q_L, q_R	1/2	1+1	6 flavors
→ squark	\tilde{q}_L, \tilde{q}_R	0	1+1	
gluon	G, μ	1	n-2	Majorana
→ gluino	\tilde{g}	1/2	2	
gauge bosons	γ, Z	1	2+3	Majorana
Higgs bosons	h^0, H^0, A^0	0	3	
→ neutralinos	$\tilde{\chi}_i^0$	1/2	4 · 2	
gauge bosons	W^\pm	1	2 · 3	Dirac
Higgs bosons	H^\pm	0	2	
→ charginos	$\tilde{\chi}_i^\pm$	1/2	2 · 4	

SUSY LES HOUCHES ACCORD

Problem: Supersymmetric parameter conventions

- comparison of specialized codes [remember: e.g. Comphep–Pythia–Isajet]
- ⇒ fix SUSY conventions once for all
 - soft breaking parameters [e.g. $\pm A_t$]
 - scale dependence of couplings, masses [e.g. $m(q = \text{TeV}, \nu, m_t)$?]
 - definitions of mass matrixes, mixing angles [e.g. $\tilde{t}_{L,R}$ up or down?]

SUSY Les Houches Accord [P. Skands et al.]

- spectrum generators: SoftSusy, SPheno, FeynHiggs,...
- multi-purpose Monte Carlos: Pythia, Herwig, Sherpa
- matrix element generators: Whizard, SmadGraph
- NLO cross sections: Prospino2
- NLO decay rates: Sdecay
- SUSY parameter extraction: Fittino, Sfitter
- dark matter: Micromegas
- ⇒ **fixed parameter convention and read-write format**

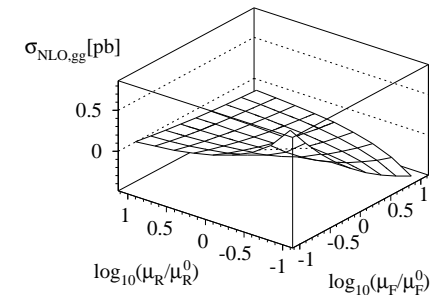
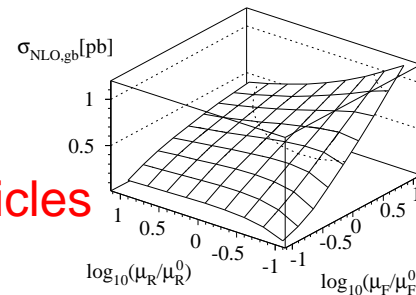
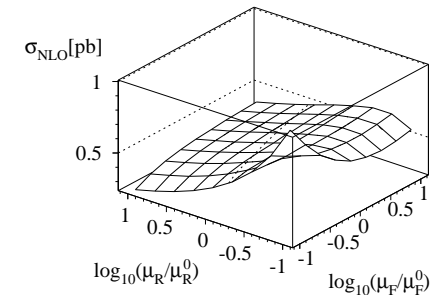
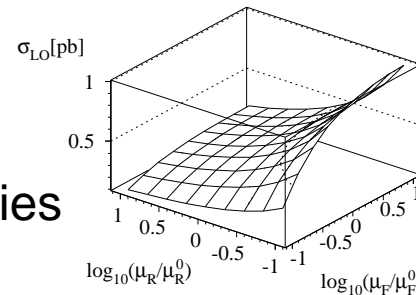
SUSY SIGNALS AT LHC: 1

Supersymmetry at the LHC

- (1) **possible discovery** — signals for new physics, exclusion of parameter space
 - (2) **measurements** — masses, cross sections, decays
 - (3) **parameter studies** — MSSM Lagrangean, SUSY breaking
- ⇒ at least 10% precision to be matched at LHC (theorist's nightmare)

Hadron collider observables with errors

- renormalization scale from $\alpha_s, y_{b,t}$
 - factorization scale from parton densities
 - perturbative series $N_c \alpha_s / \pi \sim 10\%$
 - finite terms
- [LO-NLO-NNLO: Drell-Yan, Higgs]
- ⇒ **NLO errors: 15...40 % for SUSY particles**



SUSY SIGNALS AT LHC: 2

Prospino2: NLO cross sections for Tevatron and LHC

- all two-particle SUSY production channels included
- download from Prospino2 page: <http://pheno.physics.wisc.edu/~plehn>
- extended version beyond Prospino2: $pp \rightarrow SS^*, tH^- \dots$

[thanks to: W. Beenakker, R.Höpker, M. Krämer, M. Spira, P. Zerwas]

SUSY signals included

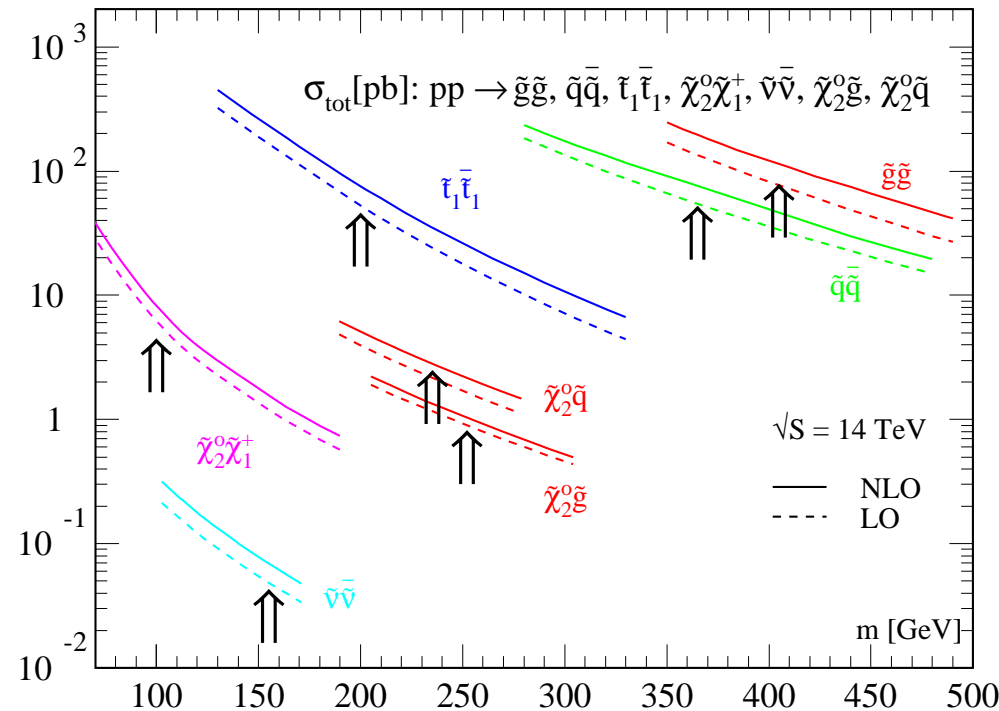
- jets and E_T : $pp \rightarrow \tilde{q}\tilde{q}^*, \tilde{g}\tilde{g}, \tilde{q}\tilde{g}$
- bottoms and E_T : $pp \rightarrow \tilde{b}_1\tilde{b}_1^*$
- like sign dileptons: $pp \rightarrow \tilde{g}\tilde{g}$

$[\tilde{g} \rightarrow \tilde{u}\tilde{u} \rightarrow \tilde{\chi}_1^+ d\bar{u} \text{ or c.c.}]$

- tri-leptons: $pp \rightarrow \tilde{\chi}_2^0\tilde{\chi}_1^-$

$[\tilde{\chi}_2^0 \rightarrow \tilde{\ell}\bar{\ell} \rightarrow \tilde{\chi}_1^0\ell\bar{\ell}; \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0\ell\bar{\nu}]$

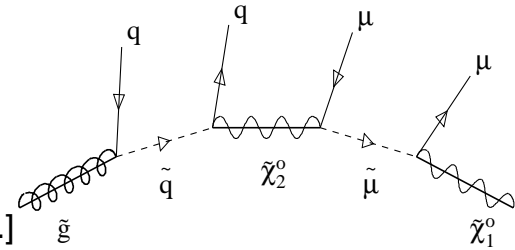
- funny tops: $pp \rightarrow \tilde{t}_1\tilde{t}_1^*$



SUSY MEASUREMENTS AT LHC: 1

SUSY spectra from cascade decays

- decay $\tilde{g} \rightarrow \tilde{q}\bar{q} \rightarrow \tilde{\chi}_2^0 q\bar{q} \rightarrow \mu^+ \mu^- q\bar{q} \tilde{\chi}_1^0$ [hopefully not via Z]
- cross sections some 100 pb [more than 3×10^5 events]
- thresholds & edges in spectra [Hinchliffe, Paige...;Allanach, Parker,...]
critical: enough thresholds and edges available?



$$\text{classical } m_{\ell\ell}^2 < (m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\ell}}^2)(m_{\tilde{\ell}}^2 - m_{\tilde{\chi}_1^0}^2)/m_{\tilde{\ell}}^2$$

⇒ detector resolution, calibration, systematic errors?

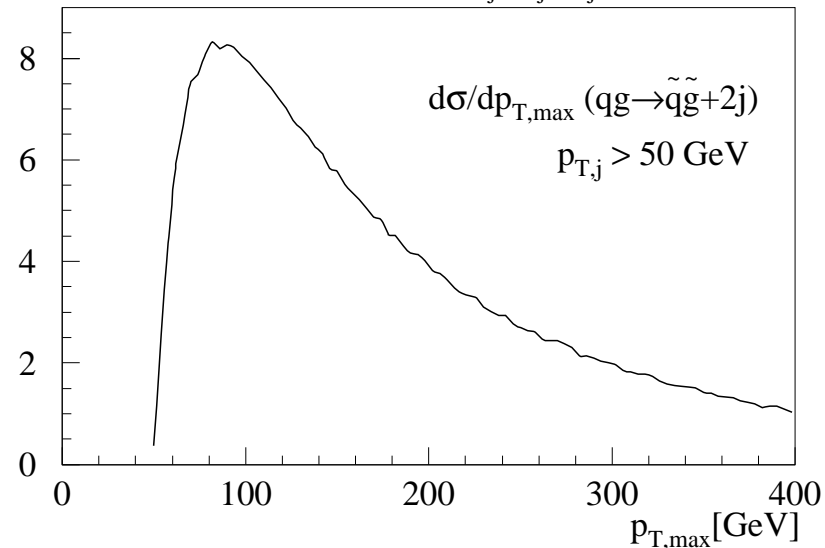
Problem in decay studies

- typical cuts: $p_{T,j} > 150, 100, 50, 50$ GeV
- (a) cuts on $p_{T,j}$ hierarchy?
- (b) combinatorics through jet radiation?

⇒ matrix elements for SUSY + hard jets

⇒ **Smadgraph** [Hagiwara, Kanzaki, TP, Rainwater, Stelzer]

total rates $\sigma_{0j}:\sigma_{1j}:\sigma_{2j} = 1 : 0.7 : 0.4$



SUSY MEASUREMENTS AT LHC: 2

Theorist's point of view

- measured masses, cross sections, decays secondary
- parameters in SUSY Lagrangean from measurements
- ⇒ SUSY breaking parameters at TeV (or higher) scale

Warmup exercise: SUGRA top–down fit

- fit including all errors

[Allanach et al; Jack & Jones]

abs. errors	SPS1a	Δ at LHC		Δ at LC		Δ at LHC+LC	
		stat	stat+theo	stat	stat+theo	stat	stat+theo
m_0	100	4.0	4.7	0.09	0.6	0.08	0.6
$m_{1/2}$	250	1.8	2.6	0.13	0.6	0.11	0.5
$\tan\beta$	10	1.3	3.5	0.14	0.3	0.14	0.4
A_0	-100	31.8	32.4	4.43	8.5	4.23	12.6

- spectrum from Suspect [Djouadi, Kneur]
- fit Suspect and Softsusy [Allanach]

LHC	Suspect	Δ	Softsusy	Δ
m_0	100.00	4.7	97.9	4.6
$m_{1/2}$	250.00	2.7	252.5	2.9
$\tan\beta$	10.00	3.5	11.6	3.6
A_0	-99.96	32.4	14.7	58.9

LHC+LC				
m_0	100.0	0.59	98.4	0.7
$m_{1/2}$	249.99	0.49	254.3	0.8
$\tan\beta$	9.99	0.44	7.3	0.3
A_0	-100.1	12.6	902.0	18

- ⇒ **best way to estimate theory errors?**

SUSY MEASUREMENTS AT LHC: 3

SUSY parameters from observables

- parameters: weak-scale MSSM Lagrangean
- measurements: masses [Suspect, Softsusy, FeynHiggs...]
 branching fractions [MSMlib, Sdecay]
 cross sections [Prospino, MSMlib],...
- errors: general correlation, statistics & systematics & theory
- problem in grid: huge phase space, local minimum?
 problem in fit: domain walls, starting values, global minimum?

SFitter [Lafaye, TP, D. Zerwas, also Fittino]

- (1) grid for closed subset
- (2) fit of remaining parameters
- (3) complete fit

⇒ **LHC+LC without assumptions**

	LHC	LC	LHC+LC	SPS1a
$\tan\beta$	10.22 ± 9.1	10.26 ± 0.3	10.06 ± 0.2	10
M_1	102.45 ± 5.3	102.32 ± 0.1	102.23 ± 0.1	102.2
M_3	578.67 ± 15	fi x 500	588.05 ± 11	589.4
$M_{\tilde{\tau}_L}$	fi x 500	197.68 ± 1.2	199.25 ± 1.1	197.8
$M_{\tilde{\tau}_R}$	129.03 ± 6.9	135.66 ± 0.3	133.35 ± 0.6	135.5
$M_{\tilde{\mu}_L}$	198.7 ± 5.1	198.7 ± 0.5	198.7 ± 0.5	198.7
$M_{\tilde{q}_{3L}}$	498.3 ± 110	497.6 ± 4.4	521.9 ± 39	501.3
$M_{\tilde{t}_R}$	fi x 500	420 ± 2.1	411.73 ± 12	420.2
$M_{\tilde{b}_R}$	522.26 ± 113	fi x 500	504.35 ± 61	525.6
A_τ	fi x 0	-202.4 ± 89.5	352.1 ± 171	-253.5
A_t	-507.8 ± 91	-501.95 ± 2.7	-505.24 ± 3.3	-504.9
A_b	-784.7 ± 35603	fi x 0	-977 ± 12467	-799.4

Theory tools for supersymmetry at LHC

- spectrum generators → LHC cross sections all available with SLHA
- major progress on errors for SUSY at LHC
- many tools in testing phase or beyond, for example...

Prospino2 — NLO cross sections at Tevatron/LHC

SmadGraph — MSSM matrix elements

Sfitter — MSSM parameter extraction