

# New Methods for New Physics

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CERN, 11/2006

# Outline

TeV-scale supersymmetry

Supersymmetric signatures at LHC

New physics mass measurements

New physics spin measurements

Supersymmetric parameter studies

Under construction

# TeV-scale supersymmetry: 1

## Starting from data...

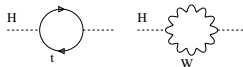
- ...which seem to indicate a light Higgs
- problem of light Higgs: mass driven to cutoff of effective Standard Model:  

$$\delta m_H^2 \propto g^2 (2m_W^2 + m_Z^2 + m_H^2 - 4m_t^2) \Lambda^2$$
- ⇒ easy solution: counter term to cancel loops ⇒ **artificial, unmotivated, ugly**
- ⇒ or new physics at TeV scale: **supersymmetry**  
 extra dimensions  
 little Higgs (pseudo-Goldstone Higgs)  
 Higgsless, composite Higgs, TopColor,  
 YourFavoriteNewPhysics...
- ⇒ typically cancellation by new particles or discussing away high scale
- ⇒ beautiful concepts and symmetries
- ⇒ problematic to realize at TeV scale [data seriously in the way]

## Idea of supersymmetry:

cancellation of divergences through statistics factor (-1)

[ SM fermions to scalar; SM gauge bosons to fermions; SM scalars to fermions]



## TeV-scale supersymmetry: 2

### SUSY breaking: (yet) unobserved partners heavy

- mechanism for SUSY masses unknown [soft SUSY breaking mediated somehow?]
  - link to flavor physics and baryogenesis/leptogenesis unknown
  - link to dark matter promising [Ellis, Falk, Olive,...]
  - maximally blind mediation: mSUGRA/cMSSM [not a LHC paradigm!]  
 scalars:  $m_0$ , fermions:  $m_{1/2}$ , tri-scalar term:  $A_0$   
 plus  $\text{sign}(\mu)$  and  $\tan\beta$  in Higgs sector [Higgs masses free: NUHM]
  - alternatives: gauge, anomaly, gaugino mediation ... ?
- ⇒ **measure spectrum at LHC instead**

### LHC phenomenology: MSSM

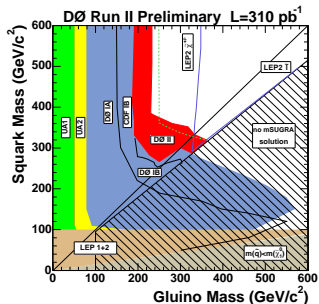
- conjugate Higgs field not allowed  
 → give mass to  $t$  and  $b$ ?  
 → two Higgs doublets
  - SUSY Higgs alone interesting
- ⇒ would be another talk...
- ⇒ **SUSY partners at LHC**

		spin	d.o.f.	
fermion	$f_L, f_R$	1/2	1+1	
→ sfermion	$\tilde{f}_L, \tilde{f}_R$	0	1+1	
gluon	$G_\mu$	1	n-2	
→ gluino	$\tilde{g}$	1/2	2	Majorana
gauge bosons	$\gamma, Z$	1	2+3	
Higgs bosons	$H^0, H^\pm, A^0$	0	3	
→ neutralinos	$\tilde{\chi}_i^0$	1/2	4 · 2	Majorana
gauge bosons	$W^\pm$	1	2 · 3	
Higgs bosons	$H^\pm$	0	2	
→ charginos	$\tilde{\chi}_i^\pm$	1/2	2 · 4	Dirac
graviton	$G$	2	2	
→ gravitino	$\tilde{G}$	3/2	2	tough

# Supersymmetry at LHC: 1

## Inclusive: squarks and gluinos at Tevatron

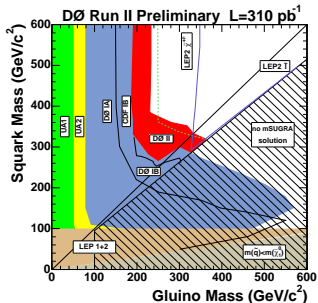
- squarks, gluinos strongly interacting  
 $p\bar{p} \rightarrow \tilde{q}\tilde{q}^*, \tilde{q}\tilde{g}, \tilde{g}\tilde{g}$  [best if  $m(\tilde{q}) \sim m(\tilde{g})$ ]
  - cross sections large at hadron colliders
  - decays to jets and LSP  
 $\tilde{g} \rightarrow \tilde{q}\bar{q}, \tilde{q}_L \rightarrow q\tilde{\chi}_2^0, \tilde{q}_R \rightarrow q\tilde{\chi}_1^0$   
[additional jets and leptons possible]
  - gaugino mass unification assumed for details
- ⇒ experienced in inclusive jets plus LSP



# Supersymmetry at LHC: 1

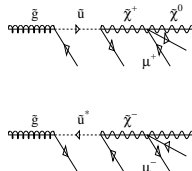
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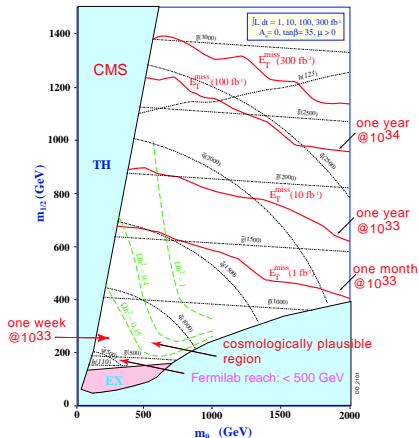
## When will I believe we see SUSY-QCD?

- gluinos Majorana fermions
  - jet in gluino decay  $q$  or  $\bar{q}$
  - final-state leptons with both charges
- ⇒ like-sign dileptons from  $\tilde{g}\tilde{g}$  [Barger,...; Barnett,...; Baer,...]



## New physics at the LHC

- (1) possible discovery — signals for new physics, exclusion of parameter space
- (2) measurements
- (3) parameter studies



# Supersymmetry at LHC: 2

## New physics at the LHC

- (1) **possible discovery** — signals for new physics, exclusion of parameter space
  - (2) **measurements** — masses, cross sections, decays
  - (3) **parameter studies** — MSSM Lagrangean, SUSY breaking
- ⇒ approach independent of new physics model

## Some SUSY signals [NLO: Prospino2]

– jets and  $\cancel{E}_T$ :  $pp \rightarrow \tilde{q}\tilde{q}^*, \tilde{g}\tilde{g}, \tilde{q}\tilde{g}$

– funny tops:  $pp \rightarrow \tilde{t}_1\tilde{t}_1^*$

– like-sign dileptons:  $pp \rightarrow \tilde{g}\tilde{g}$

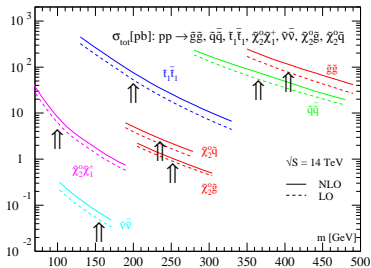
$[\tilde{g} \rightarrow \bar{u}u \rightarrow \tilde{\chi}_1^+ d\bar{u} \text{ or } \tilde{g} \rightarrow \bar{u}^*u \rightarrow \tilde{\chi}_1^- \bar{d}u]$

– tri-leptons:  $pp \rightarrow \tilde{\chi}_2^0\tilde{\chi}_1^-$

$[\tilde{\chi}_2^0 \rightarrow \bar{\ell}\ell \rightarrow \tilde{\chi}_1^0\ell\bar{\ell}; \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0\ell\bar{\nu}]$

⇒ inclusive: similar to Tevatron

⇒ **exclusive: enough events for studies at LHC**





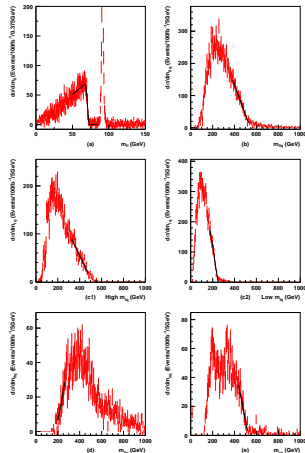
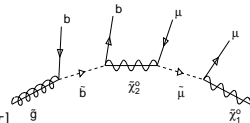
# New physics mass measurements: 1

## Spectra from cascade decays

- decay  $\tilde{g} \rightarrow \tilde{b}\tilde{b} \rightarrow \tilde{\chi}_2^0 b\tilde{b} \rightarrow \mu^+ \mu^- b\tilde{b}\tilde{\chi}_1^0$  [better not via Z or to  $\tau$ ]
- cross sections some 100 pb [more than  $3 \times 10^7$  events]
- thresholds & edges [  $m_{\tilde{\ell}\ell}^2 < (m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\ell}}^2)(m_{\tilde{\ell}}^2 - m_{\tilde{\chi}_1^0}^2)/m_{\tilde{\ell}}^2$  ]
- detector resolution, calibration, systematic errors, shape analysis, cross sections as input?

⇒ spectrum information from decay kinematics

[Hinchliffe,...;Allanach,...; not only SUSY: Reece & Meade]





# New physics mass measurements: 2

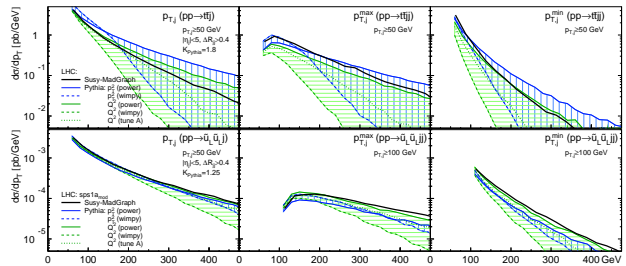
## SUSY plus jets: complex final states [Smadgraph: Cho, Hagiwara, Kanzaki, TP, Rainwater, Stelzer]

- Majoranas and fermion number violation in tools like Madgraph
- complete set of Feynman rules [400+ processes compared: Madgraph - Whizard - Sherpa]
- available in Madevent [Alwall, Maltoni, Louvain group]

## Squarks and gluinos always with many jets [TP, Rainwater, Skands]

- cascade studies sensitive to jet simulation?
  - matrix element  $\tilde{g}\tilde{g}+2j$  and  $\tilde{u}_L\tilde{g}+2j$  [ $p_{T,j} > 100$  GeV]
  - Pythia shower tuned at Tevatron
- ⇒ **QCD no killer for decay analyses** [the heavier the better]

$\sigma$ [pb]	$t\bar{t}_{600}$	$\tilde{g}\tilde{g}$	$\tilde{u}_L\tilde{g}$
$\sigma_{0j}$	1.30	4.83	5.65
$\sigma_{1j}$	0.73	2.89	2.74
$\sigma_{2j}$	0.26	1.09	0.85



# New physics mass measurements: 2

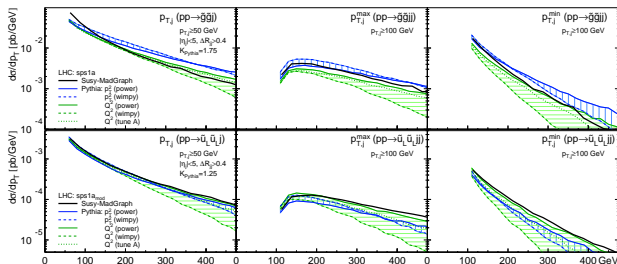
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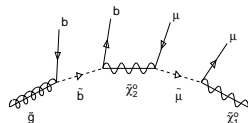




## New physics spin measurements: 2

### Back to my SUSY-QCD

- given like-sign dileptons, gluino Majorana fermion?
- always like-sign dileptons from bosonic gluon
- ⇒ show gluino fermionic
- ⇒ compare with usual straw man [UED-Madgraph: Alves]



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## Gluino-bottom cascade [Alves, Eboli, TP]

- decay chain like for gluino mass
- compare with first KK  $g$ ,  $q$ ,  $Z$ , and  $\ell$

(1) replace initial-state asymmetry by  $b$  vs.  $\bar{b}$

- asymmetry to write down:

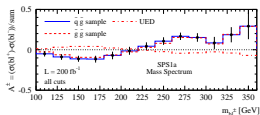
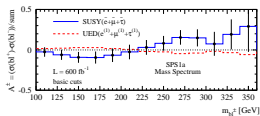
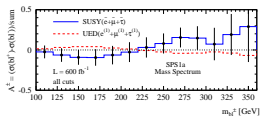
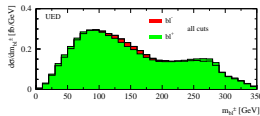
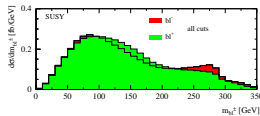
$$\mathcal{A} = [\sigma(bl^+) - \sigma(bl^-)] / [\sigma(bl^+) + \sigma(bl^-)]$$

[still visible after cuts and smearing]

- independent on production channels

(2) purely hadronic  $m_{bb}$  [sensitive to gluino boost]

⇒ masses and spins accessible at LHC



## Theory output from LHC: SUSY parameters

- parameters: weak-scale Lagrangean [Sfitter: Lafaye, TP, Rauch, Zerwas; Fittino; Arkani-Hamed,...]
- measurements: masses or edges  
branching fractions  
cross sections
- errors: general correlation, statistics & systematics & theory
- problem in grid: huge phase space, local minimum?  
problem in fit: domain walls, starting values, global minimum?

## First go at problem

- ask a friend how SUSY is broken  $\Rightarrow$  mSUGRA/cMSSM
  - fit  $m_0, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
  - no problem, include indirect constraints [Ellis, Heinemeyer, Olive, Weiglein,...]
- $\Rightarrow$  probability map today [Allanach, Lester, Weber]
- $\Rightarrow$  best fit from LHC/ILC measurements

	SPS1a	$\Delta$ LHC masses	$\Delta$ LHC edges	$\Delta$ ILC	$\Delta$ LHC+ILC
$m_0$	100	3.9	1.2	0.09	0.08
$m_{1/2}$	250	1.7	1.0	0.13	0.11
$\tan\beta$	10	1.1	0.9	0.12	0.12
$A_0$	-100	33	20	4.8	4.3



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## MSSM instead of mSUGRA/cMSSM [TP, Lafaye, Zerwas]

- (1) grid for closed subset
  - (2) fit of other parameters
  - (3) complete fit
  - LHC+ILC perfect [Weiglein etal]
- ⇒ too few measurements?  
secondary minima? ...

	LHC	ILC	LHC+ILC	SPS1a
$\tan\beta$	$10.22\pm 9.1$	$10.26\pm 0.3$	$10.06\pm 0.2$	10
$M_1$	$102.45\pm 5.3$	$102.32\pm 0.1$	$102.23\pm 0.1$	102.2
$M_2$	$578.67\pm 15$	fix 500	$588.05\pm 11$	589.4
$M_{\tilde{\tau}_L}$	fix 500	$197.68\pm 1.2$	$199.25\pm 1.1$	197.8
$M_{\tilde{\tau}_R}$	$129.03\pm 6.9$	$135.66\pm 0.3$	$133.35\pm 0.6$	135.5
$M_{\tilde{\mu}_L}$	$198.7\pm 5.1$	$198.7\pm 0.5$	$198.7\pm 0.5$	198.7
$M_{\tilde{g}_L}$	$498.3\pm 110$	$497.6\pm 4.4$	$521.9\pm 39$	501.3
$M_{\tilde{t}_R}$	fix 500	$420\pm 2.1$	$411.73\pm 12$	420.2
$M_{\tilde{b}_R}$	$522.26\pm 113$	fix 500	$504.35\pm 61$	525.6
$A_\tau$	fix 0	$-202.4\pm 89.5$	$352.1\pm 171$	-253.5
$A_t$	$-507.8\pm 91$	$-501.95\pm 2.7$	$-505.24\pm 3.3$	-504.9
$A_b$	$-784.7\pm 35603$	fix 0	$-977\pm 12467$	-799.4

## Supersymmetric parameters: 2

### Bayes' theorem and new physics [Ben's talk]

- Pythia/Herwig/Sherpa: data given the model:  $p(d|m)$
  - theorist's prejudice: model  $p(m)$
  - new model extraction:  $p(m|d) = p(d|m) p(m)/p(d)$   $[p(d)$  through normalization]
- ⇒ given measurements: (1) compute probability map  $p(m|d)$  of parameter space  
(2) rank local minima

### Weighted Markov chains [scanning algorithm for many dimensions: Rauch & TP]

- classical: produce representative set of spin states  
compute average energy based on this reduced sample
- ⇒ map (chain) based on probability of a state  
expensive energy function on sample
- BSM physics: produce map  $p(m|d)$  of parameter points  
evaluate same probability from (binned) density [Allanach, Lester; Baltz, Gondolo]
- ⇒ phase-space MC approach: weighted chain [two bins with  $p \approx 1 : 10$  with 2 or 11 points]
- already for mSUGRA/cMSSM: MC resolution not sufficient
- ⇒ use additional probability maximization to rank maxima

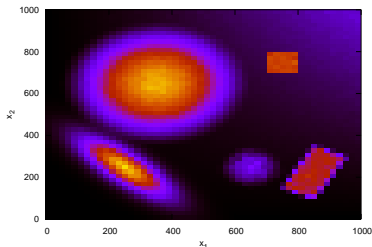
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### Toy model [Rauch & TP]

- test function  $V(\vec{x})$  in 5 dimensions [general high-dimensional extraction tool]
- Sfi tter output #1: probability map
- Sfi tter output #2: list of local maxima



$V=74.929$  @ (655.00,253.72,347.83,348.57,349.59)

$V=59.972$  @ (850.04,224.99,650.00,649.99,654.56)

$V=58.219$  @ (849.97,225.01,587.08,650.01,650.02)

$V=25.110$  @ (750.00,749.99,450.00,450.01,450.01)

$V=16.042$  @ (245.45,253.44,552.51,542.58,544.75)

$V=12.116$  @ (350.70,650.40,650.36,650.40,650.38)

...

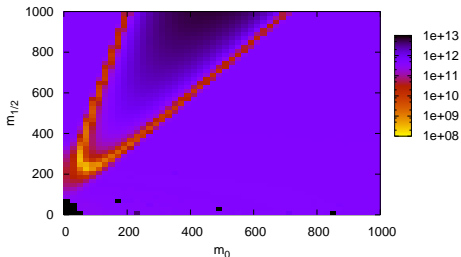
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## mSUGRA/cMSSM with LHC measurements

- SPS1a kinematic edges and free  $m_t$
- as of yesterday: Sfi tter probability map [Lafaye, TP, Rauch, Zerwas]



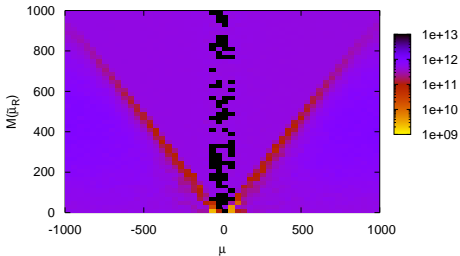
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## MSSM with LHC measurements

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# Under construction: 1

## Problems in the spin/mass extraction

- strong correlations between masses from edges
  - strong correlations between  $m_{xyz}$  in cascades
  - split of mass and spin extraction artificial
  - model-independent spin analysis unlikely
- ⇒ Proper hypothesis treatment

## Statistics: Neyman–Pearson lemma

- assume correct hypothesis  $m_1$ : SUSY cascade  
assume wrong hypothesis  $m_2$ : UED cascade
  - likelihood ratio  $p(d|m_1)/p(d|m_2)$  most powerful estimator  
[lowest probability to mistake right for fluctuation of wrong (type-II error)]
  - probability of event  $p(d|m) \sim |\mathcal{M}|^2$
  - combined likelihood ratios of events → PS integral over likelihood ratio
- ⇒ Compute maximum statistical significance

## 'Matrix element method' [CDF, D0; McElrath]

- compute likelihood of top events estimating  $|\mathcal{M}|^2$
- maximize probability  $p(d|SM, m_t)$  as function of  $m_t$ ...

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## Under construction: 2

Search for WBF  $H \rightarrow \mu\mu$  [Cranmer & TP]

- assume correct hypothesis  $m_{s+b}$ : Higgs signal  
assume wrong hypothesis  $m_b$ : SM background
  - likelihood ratio  $p(d|m_{s+b})/p(d|m_b)$  most powerful estimator
  - probability of event  $p(d|m) \sim |\mathcal{M}|^2$
  - combined likelihood ratios of events  $\rightarrow$  PS integral over likelihood ratio
- $\Rightarrow$  **Compute maximum statistical significance**

## Maximum significance for LHC signals

- example: combined  $n$ -event Poisson statistics  $[p(n|s+b) = e^{-(s+b)} (s+b)^n / n!]$

$$q = \log \frac{p(n|s+b)}{p(n|b)} = -s + n \log \left( 1 + \frac{s}{b} \right) \rightarrow - \sum_j s_j + \sum_j n_j \log \left( 1 + \frac{s_j}{b_j} \right)$$

- phase space integration of  $s, b \rightarrow p(s, b) \sim |\mathcal{M}_{s,b}|^2$  [LEP-Higgs inspired]

$$q(\vec{r}) = -\sigma_s \mathcal{L} + \log \left( 1 + \frac{|\mathcal{M}_s(\vec{r})|^2}{|\mathcal{M}_b(\vec{r})|^2} \right)$$

- probability distribution function via Fourier transform:  $\rho_{s,b}(q)$
- $\rightarrow$  compute  $CL_b(q) = \int_q^\infty dq' \rho_b(q')$  [ $5\sigma$  is  $CL_b = 2.85 \cdot 10^{-7}$ ]



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## Semi-realistic results

- irreducible & unsmeared [full parameter space 1:1]

$$\sigma_{tot} = \int dPS M_{PS} d\sigma_{PS} = \int d\vec{r} M(\vec{r}) d\sigma(\vec{r})$$

- smearing  $\Delta m_{\mu\mu}^{width} \ll \Delta m_{\mu\mu}^{meas}$  [unobserved dimensions]

$$\sigma_{tot} = \int d\vec{r}_{\perp} dr_m^* \int_{-\infty}^{\infty} dr_m M(\vec{r}) d\sigma(\vec{r}) W(r_m, r_m^*)$$

- acceptance cuts to reduce phase space... [bad measurements]
- $\Rightarrow$  WBF  $H \rightarrow \mu\mu$ :  $3.5\sigma$  in  $300 \text{ fb}^{-1}$

- $\Rightarrow$  Tool works, new physics one obvious application

# New physics at the LHC

## A lot has been done

- higher-order calculations
- improved background estimates
- web-based signal event generators
- mass and spin measurements
- parameter extraction/probability maps
- ....

## A lot is still left to do

- more higher-order calculations
  - better background estimates
  - QCD effects on new physics measurements
  - combination of many measurements
  - scanning of high-dimensional parameter spaces
  - ....
- ⇒ Exciting times require serious work

**New Methods  
for New Physics**

**Tilman Plehn**

Supersymmetry

LHC Signals

Masses

Spins

Parameters

**Some ideas**