

New Methods for New Physics

Tilman Plehn

MPI für Physik & University of Edinburgh

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Outline

Supersymmetry

LHC Signals

Masses

Spins

Parameters

Some ideas

TeV-scale supersymmetry

Supersymmetric signatures at LHC

New physics mass measurements

New physics spin measurements

Supersymmetric parameter studies

Under construction

TeV-scale supersymmetry: 1

Starting from data...

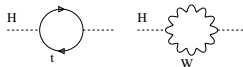
- ...which seem to indicate a light Higgs
- problem of light Higgs: mass driven to cutoff of effective Standard Model:

$$\delta m_H^2 \propto g^2 (2m_W^2 + m_Z^2 + m_H^2 - 4m_t^2) \Lambda^2$$
- ⇒ easy solution: counter term to cancel loops ⇒ **artificial, unmotivated, ugly**
- ⇒ or new physics at TeV scale:
 - supersymmetry
 - extra dimensions
 - little Higgs (pseudo-Goldstone Higgs)
 - Higgsless, composite Higgs, TopColor,
 - YourFavoriteNewPhysics...
- ⇒ typically cancellation by new particles or discussing away high scale
- ⇒ beautiful concepts and symmetries
- ⇒ problematic to realize at TeV scale [data seriously in the way]

Idea of supersymmetry:

cancellation of divergences through statistics factor (-1)

[SM fermions to scalar; SM gauge bosons to fermions; SM scalars to fermions]



TeV-scale supersymmetry: 2

SUSY breaking: (yet) unobserved partners heavy

- mechanism for SUSY masses unknown [soft SUSY breaking mediated somehow?]
 - link to flavor physics and baryogenesis/leptogenesis unknown
 - link to dark matter promising [Falk,...]
 - maximally blind mediation: mSUGRA/cMSSM [not a LHC paradigm!]
 scalars: m_0 , fermions: $m_{1/2}$, tri-scalar term: A_0
 plus $\text{sign}(\mu)$ and $\tan\beta$ in Higgs sector [Higgs masses free: NUHM]
 - alternatives: gauge, anomaly, gaugino mediation ... ?
- ⇒ **measure spectrum at LHC instead**

LHC phenomenology: MSSM

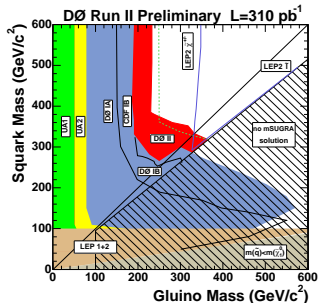
- conjugate Higgs field not allowed
 → give mass to t and b ?
 → two Higgs doublets
 - SUSY Higgs alone interesting
- ⇒ would be another talk...
- ⇒ **SUSY partners at LHC**

		spin	d.o.f.	
fermion	f_L, f_R	1/2	1+1	
→ sfermion	\tilde{f}_L, \tilde{f}_R	0	1+1	
gluon	G_μ	1	n-2	
→ gluino	\tilde{g}	1/2	2	Majorana
gauge bosons	γ, Z	1	2+3	
Higgs bosons	H^0, H^\pm, A^0	0	3	
→ neutralinos	$\tilde{\chi}_j^0$	1/2	4 · 2	Majorana
gauge bosons	W^\pm	1	2 · 3	
Higgs bosons	H^\pm	0	2	
→ charginos	$\tilde{\chi}_j^\pm$	1/2	2 · 4	Dirac
graviton	G	2	2	
→ gravitino	\tilde{G}	3/2	2	tough

Supersymmetry at LHC: 1

Inclusive: squarks and gluinos at Tevatron

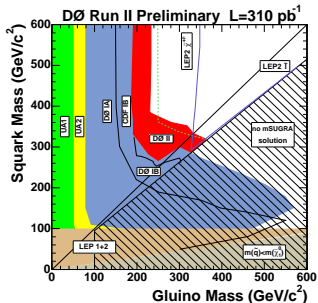
- squarks, gluinos strongly interacting
 $p\bar{p} \rightarrow \tilde{q}\tilde{q}^*, \tilde{q}\tilde{g}, \tilde{g}\tilde{g}$ [best if $m(\tilde{q}) \sim m(\tilde{g})$]
 - cross sections large at hadron colliders
 - decays to jets and LSP
 $\tilde{g} \rightarrow \tilde{q}\bar{q}, \tilde{q}_L \rightarrow q\tilde{\chi}_2^0, \tilde{q}_R \rightarrow q\tilde{\chi}_1^0$
[additional jets and leptons possible]
 - gaugino mass unification assumed for details
- ⇒ experienced in inclusive jets plus LSP



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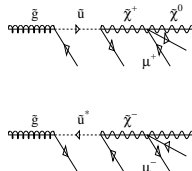
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When will I believe we see SUSY-QCD?

- gluinos Majorana fermions
 - jet in gluino decay q or \bar{q}
 - final-state leptons with both charges
- ⇒ like-sign dileptons from $\tilde{g}\tilde{g}$ [Barger,...; Barnett,...; Baer,...]



Supersymmetry at LHC: 2

New physics at the LHC

- (1) **possible discovery** — signals for new physics, exclusion of parameter space
 - (2) **measurements** — masses, cross sections, decays
 - (3) **parameter studies** — MSSM Lagrangean, SUSY breaking
- ⇒ approach independent of new physics model

Some SUSY signals [NLO: Prospino2]

– jets and \cancel{E}_T : $pp \rightarrow \tilde{q}\tilde{q}^*, \tilde{g}\tilde{g}, \tilde{q}\tilde{g}$

– funny tops: $pp \rightarrow \tilde{t}_1\tilde{t}_1^*$

– like-sign dileptons: $pp \rightarrow \tilde{g}\tilde{g}$

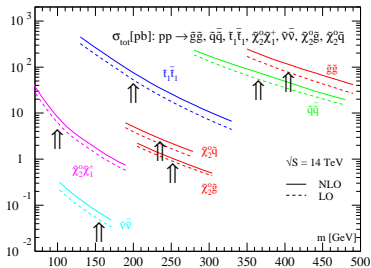
$[\tilde{g} \rightarrow \bar{u}u \rightarrow \tilde{\chi}_1^+ d\bar{u} \text{ or } \tilde{g} \rightarrow \bar{u}^*u \rightarrow \tilde{\chi}_1^- \bar{d}u]$

– tri-leptons: $pp \rightarrow \tilde{\chi}_2^0\tilde{\chi}_1^-$

$[\tilde{\chi}_2^0 \rightarrow \bar{\ell}\ell \rightarrow \tilde{\chi}_1^0\ell\bar{\ell}; \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0\ell\bar{\nu}]$

⇒ inclusive: similar to Tevatron

⇒ **exclusive: enough events for studies at LHC**



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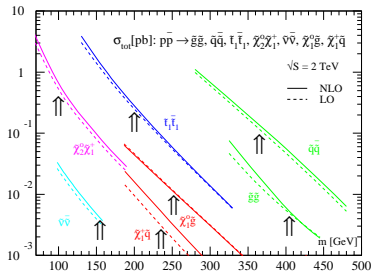
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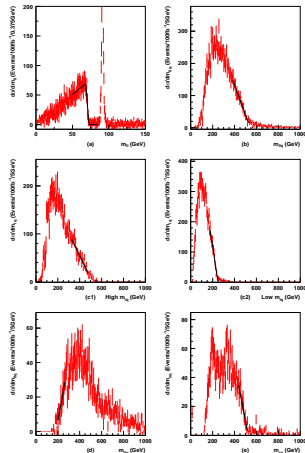
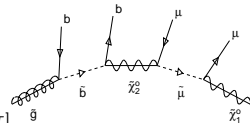
New physics mass measurements: 1

Spectra from cascade decays

- decay $\tilde{g} \rightarrow \tilde{b}\tilde{b} \rightarrow \tilde{\chi}_2^0 b\tilde{b} \rightarrow \mu^+ \mu^- b\tilde{b}\tilde{\chi}_1^0$ [better not via Z or to τ]
- cross sections some 100 pb [more than 3×10^7 events]
- thresholds & edges [$m_{\tilde{\ell}\ell}^2 < (m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\ell}}^2)(m_{\tilde{\ell}}^2 - m_{\tilde{\chi}_1^0}^2)/m_{\tilde{\ell}}^2$]
- detector resolution, calibration, systematic errors, shape analysis, cross sections as input?

⇒ spectrum information from decay kinematics

[Hinchliffe,...;Allanach,...; not only SUSY: Reece & Meade]



New physics mass measurements: 2

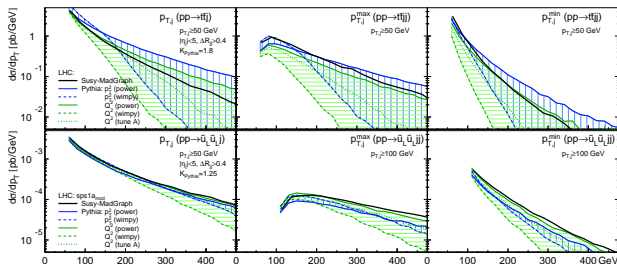
SUSY plus jets: complex final states [Smadgraph: Cho, Hagiwara, Kanzaki, TP, Rainwater, Stelzer]

- Majoranas and fermion number violation in Madgraph
- set of Feynman rules [400+ processes: Madgraph - Whizard (Reuter) - Sherpa (Schumann)]
- available in Madevent [Alwall, Maltoni, Louvain group]

Squarks and gluinos always with many jets [TP, Rainwater, Skands]

- cascade studies sensitive to jet simulation?
 - matrix element $\tilde{g}\tilde{g}+2j$ and $\tilde{u}_L\tilde{g}+2j$ [$p_{T,j} > 100$ GeV]
 - Pythia shower tuned at Tevatron
- ⇒ **QCD no killer for decay analyses** [the heavier the better]

σ [pb]	$t\bar{t}_{600}$	$\tilde{g}\tilde{g}$	$\tilde{u}_L\tilde{g}$
σ_{0j}	1.30	4.83	5.65
σ_{1j}	0.73	2.89	2.74
σ_{2j}	0.26	1.09	0.85



New physics mass measurements: 2

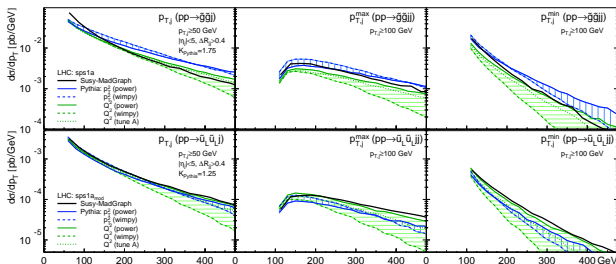
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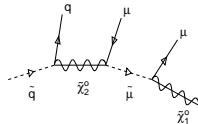


New physics spin measurements: 1

All new physics is hypothesis testing

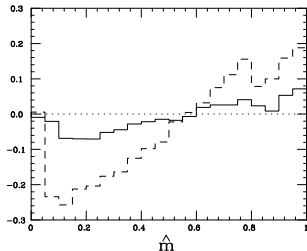
- assume squark cascade observed
- ⇒ strongly interacting scalar?
- ⇒ straw-man model where squark is a fermion: universal extra dimensions

[Appelquist, Cheng, Dobrescu; Cheng, Matchev, Schmaltz; spectra degenerate —ignore; cross section larger —ignore]



Squark–slepton cascade [Smillie, Webber, Athanasiou, Lester]

- decay chain $\tilde{\chi}_2^0 \rightarrow l\tilde{l}^* \rightarrow l\tilde{l}\tilde{\chi}_1^0$
- trick 1: compare with KK q, Z, l, γ
- trick 2: mass variables, ‘normalized angles’
⇒ $\hat{m} = m_{je}/m_{je}^{\max}$ most promising [Barr]
- typically largest $pp \rightarrow \tilde{q}\tilde{q}^*$
- trick 3: production asymmetry $\tilde{q} : \tilde{q}^* \sim 2 : 1$
⇒ $\mathcal{A} = [\sigma(j\ell^+) - \sigma(j\ell^-)]/[\sigma(j\ell^+) + \sigma(j\ell^-)]$



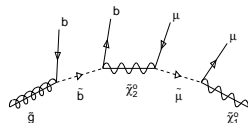
Masses or spin or both? [Arkani-Hamed,...]

- masses from kinematic endpoints [use $m_{ej}, m_{\ell\ell}, m_{j\ell\ell}\dots$]
- spins from distributions between endpoints [endpoints identical in SUSY and UED]

New physics spin measurements: 2

Back to my SUSY-QCD

- given like-sign dileptons, gluino Majorana fermion?
- always like-sign dileptons from bosonic gluon
- ⇒ show gluino fermionic
- ⇒ compare with usual straw man [UED-Madgraph: Alves]



New physics spin measurements: 2

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Gluino-bottom cascade [Alves, Eboli, TP]

- decay chain like for gluino mass
- compare with first KK g , q , Z , and ℓ

(1) replace initial-state asymmetry by b vs. \bar{b}

- asymmetry to write down:

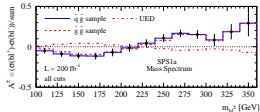
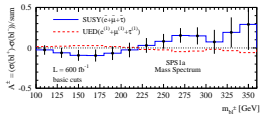
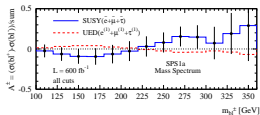
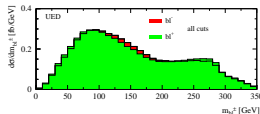
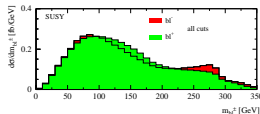
$$\mathcal{A} = [\sigma(bl^+) - \sigma(bl^-)] / [\sigma(bl^+) + \sigma(bl^-)]$$

[still visible after cuts and smearing]

- independent on production channels

(2) purely hadronic m_{bb} [sensitive to gluino boost]

⇒ masses and spins accessible at LHC



Theory output from LHC: SUSY parameters

- parameters: weak-scale Lagrangean [Sfitter: Lafaye, TP, Rauch, Zerwas; Fittino; Arkani-Hamed,...]
- measurements: masses or edges
branching fractions
cross sections
- errors: general correlation, statistics & systematics & theory
- problem in grid: huge phase space, local minimum?
problem in fit: domain walls, global minimum?

MSSM instead of mSUGRA/cMSSM [TP, Lafaye, Zerwas]

- (1) grid for closed subset
 - (2) fit of other parameters
 - (3) complete fit
 - LHC+ILC perfect [Weiglein etal]
- ⇒ too few measurements?
secondary minima? ...

	LHC	ILC	LHC+ILC	SPS1a
$\tan\beta$	10.22 ± 9.1	10.26 ± 0.3	10.06 ± 0.2	10
M_1	102.45 ± 5.3	102.32 ± 0.1	102.23 ± 0.1	102.2
M_2	578.67 ± 15	fix 500	588.05 ± 11	589.4
$M_{\tilde{T}L}$	fix 500	197.68 ± 1.2	199.25 ± 1.1	197.8
$M_{\tilde{T}R}$	129.03 ± 6.9	135.66 ± 0.3	133.35 ± 0.6	135.5
$M_{\tilde{b}L}$	198.7 ± 5.1	198.7 ± 0.5	198.7 ± 0.5	198.7
$M_{\tilde{g}L}$	498.3 ± 110	497.6 ± 4.4	521.9 ± 39	501.3
$M_{\tilde{t}R}$	fix 500	420 ± 2.1	411.73 ± 12	420.2
$M_{\tilde{b}R}$	522.26 ± 113	fix 500	504.35 ± 61	525.6
A_τ	fix 0	-202.4 ± 89.5	352.1 ± 171	-253.5
A_t	-507.8 ± 91	-501.95 ± 2.7	-505.24 ± 3.3	-504.9
A_b	-784.7 ± 35603	fix 0	-977 ± 12467	-799.4

Supersymmetric parameters: 2

Bayes' theorem and new physics [Allanach, Roszkowski]

- Pythia/Herwig/Sherpa: data given the model: $p(d|m)$
 - theorist's prejudice: model $p(m)$
 - new model extraction: $p(m|d) = p(d|m) p(m)/p(d)$ [$p(d)$ through normalization]
- ⇒ given measurements: (1) compute probability map $p(m|d)$ of parameter space
(2) rank local minima

Weighted Markov chains [scanning algorithm for many dimensions: Rauch & TP]

- classical: produce representative set of spin states
compute average energy based on this reduced sample
- ⇒ map (chain) based on probability of a state
expensive energy function on sample
- BSM physics: produce map $p(m|d)$ of parameter points
evaluate same probability from (binned) density [Allanach,...; Baltz,...; Roszkowski,...]
- ⇒ phase-space MC approach: weighted chain [two bins with $p \approx 10$ with 2 or 11 points]
- already for mSUGRA/cMSSM: MC resolution not sufficient
- ⇒ use additional probability maximization to rank maxima

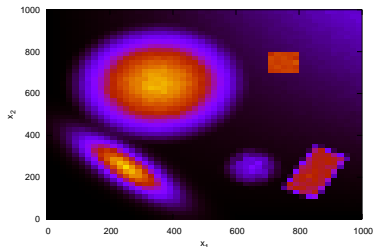
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Toy model [Rauch & TP]

- test function $V(\vec{x})$ in 5 dimensions [general high-dimensional extraction tool]
- Sfi tter output #1: probability map
- Sfi tter output #2: list of local maxima



$V=74.929$ @(655.00,253.72,347.83,348.57,349.59)

$V=59.972$ @(850.04,224.99,650.00,649.99,654.56)

$V=58.219$ @(849.97,225.01,587.08,650.01,650.02)

$V=25.110$ @(750.00,749.99,450.00,450.01,450.01)

$V=16.042$ @(245.45,253.44,552.51,542.58,544.75)

$V=12.116$ @(350.70,650.40,650.36,650.40,650.38)

...

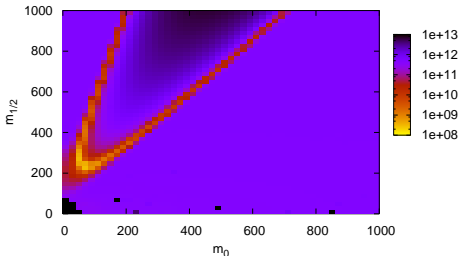
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mSUGRA/cMSSM with LHC measurements

- SPS1a kinematic edges and free m_t
- as of yesterday: Sfi tter probability map [Lafaye, TP, Rauch, Zerwas]



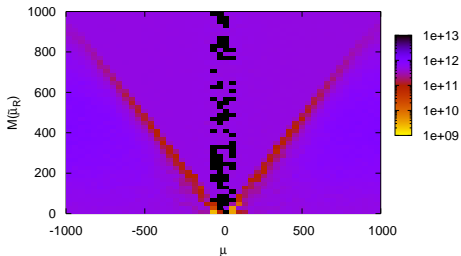
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MSSM with LHC measurements

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Under construction: 1

Problems in the spin/mass extraction

- strong correlations between masses from edges
 - strong correlations between m_{xyz} in cascades
 - split of mass and spin extraction artificial
 - model-independent spin analysis unlikely
- ⇒ Proper hypothesis treatment

Statistics: Neyman–Pearson lemma

- assume correct hypothesis m_1 : SUSY cascade
assume wrong hypothesis m_2 : UED cascade
 - likelihood ratio $p(d|m_1)/p(d|m_2)$ most powerful estimator
[lowest probability to mistake right for fluctuation of wrong (type-II error)]
 - probability of event $p(d|m) \sim |\mathcal{M}|^2$
 - combined likelihood ratios of events → PS integral over likelihood ratio
- ⇒ Compute maximum statistical significance

'Matrix element method' [CDF, D0; McElrath]

- compute likelihood of top events estimating $|\mathcal{M}|^2$
- maximize probability $p(d|SM, m_t)$ as function of m_t ...

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Under construction: 2

Search for WBF $H \rightarrow \mu\mu$ [Cranmer & TP]

- assume correct hypothesis m_{s+b} : Higgs signal
assume wrong hypothesis m_b : SM background
 - likelihood ratio $p(d|m_{s+b})/p(d|m_b)$ most powerful estimator
 - probability of event $p(d|m) \sim |\mathcal{M}|^2$
 - combined likelihood ratios of events \rightarrow PS integral over likelihood ratio
- \Rightarrow Compute maximum statistical significance

Maximum significance for LHC signals

- example: combined n -event Poisson statistics $[p(n|s+b) = e^{-(s+b)} (s+b)^n / n!]$

$$q = \log \frac{p(n|s+b)}{p(n|b)} = -s + n \log \left(1 + \frac{s}{b} \right) \rightarrow - \sum_j s_j + \sum_j n_j \log \left(1 + \frac{s_j}{b_j} \right)$$

- phase space integration of $s, b \rightarrow p(s, b) \sim |\mathcal{M}_{s,b}|^2$ [LEP-Higgs inspired]

$$q(\vec{r}) = -\sigma_s \mathcal{L} + \log \left(1 + \frac{|\mathcal{M}_s(\vec{r})|^2}{|\mathcal{M}_b(\vec{r})|^2} \right)$$

- probability distribution function via Fourier transform: $\rho_{s,b}(q)$
- \rightarrow compute $CL_b(q) = \int_q^\infty dq' \rho_b(q')$ [5σ is $CL_b = 2.85 \cdot 10^{-7}$]

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 - probability of event $p(d|m) \sim |\mathcal{M}|^2$
 - combined likelihood ratios of events \rightarrow PS integral over likelihood ratio
- \Rightarrow **Compute maximum statistical significance**

Semi-realistic results

- irreducible & unsmeared [full parameter space 1:1]

$$\sigma_{tot} = \int dPS M_{PS} d\sigma_{PS} = \int d\vec{r} M(\vec{r}) d\sigma(\vec{r})$$

- smearing $\Delta m_{\mu\mu}^{width} \ll \Delta m_{\mu\mu}^{meas}$ [unobserved dimensions]

$$\sigma_{tot} = \int d\vec{r}_{\perp} dr_m^* \int_{-\infty}^{\infty} dr_m M(\vec{r}) d\sigma(\vec{r}) W(r_m, r_m^*)$$

- acceptance cuts to reduce phase space... [bad measurements]
- \Rightarrow WBF $H \rightarrow \mu\mu$: 3.5σ in 300 fb^{-1}

- \Rightarrow **Tool works, new physics one obvious application** [Whizard: Cranmer, TP, Reuter]

New physics at the LHC

A lot has been done

- higher-order calculations
- improved background estimates
- web-based signal event generators
- mass and spin measurements
- parameter extraction/probability maps
-

A lot is still left to do

- more higher-order calculations
 - better background estimates
 - QCD effects on new physics measurements
 - scanning of high-dimensional parameter spaces
 - automatized statistics tools for phenomenologists
 -
- ⇒ Exciting times require serious work

**New Methods
for New Physics**

Tilman Plehn

Supersymmetry

LHC Signals

Masses

Spins

Parameters

Some ideas