

CHARGED HIGGS AND QCD

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- QCD issue — bottom partons
- associated production with top
- associated production with W
- pair production

CHARGED HIGGS PRODUCTION

Why look for a charged Higgs?

- single Higgs multiplet (plus conjugate) only minimal solution
- neutral scalars mixing with Higgs not unique [e.g. radion–Higgs mixing]
- charged Higgs couplings sign of doublet/triplet and flavor structure [Spannofski]

Production processes, mostly known to NLO–QCD [sorry, only few NLO citations]

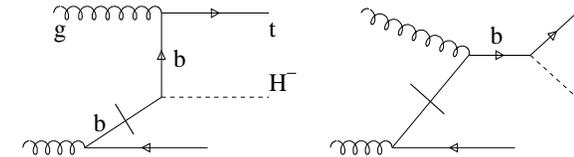
- associated with top: $gg \rightarrow \bar{b}tH^-$ [Zhu; TP; Berger, Han, Jiang, TP; Alwall & Rathsmann, Peng et al;...]
 - associated with W: $gg \rightarrow b\bar{b}W^+H^-$ [Hollik & Zhu; Barrientos Bendezu & Kniehl;...]
 - pair production: $gg \rightarrow b\bar{b}H^+H^-, q\bar{q} \rightarrow H^+H^-$ [Sheng et al; Alves & TP;...]
 - leading order loop: $gg \rightarrow H^+H^-$ [Willenbrock; Krause, TP, Spira, Zerwas; Brein & Hollik;...]
 - leading order loop: $gg \rightarrow W^+H^-$ [Barrientos Bendezu & Kniehl; Brein, Hollik, Kanemura;...]
- ⇒ (1) bottom Yukawa coupling $\sigma \sim y_b^2 \tan^2 \beta + \dots$ [SUSY, see Jaime Guasch and Oliver Brein]
⇒ (2) gluon splitting into bottom partons [purely QCD in 2HDM]

Decay processes

- bottom Yukawa definition and higher orders [too many QCD loop papers to list here]
- ⇒ Hdecay with everything you need [thanks, Michael SI]

COLLINEAR GLUON SPLITTING

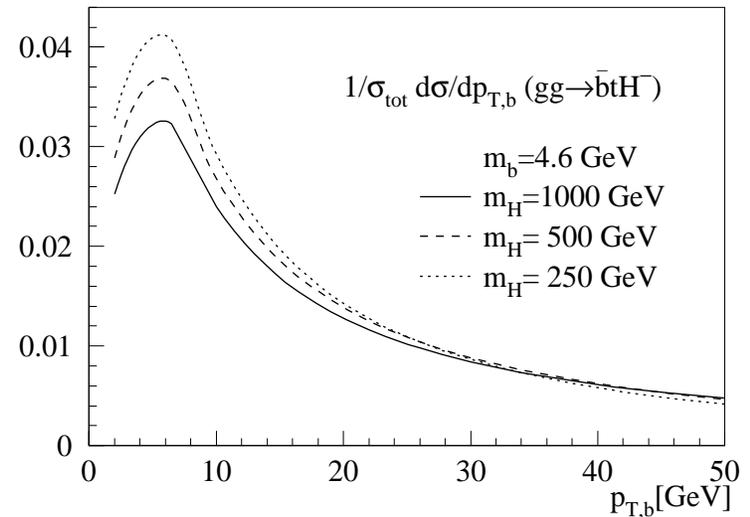
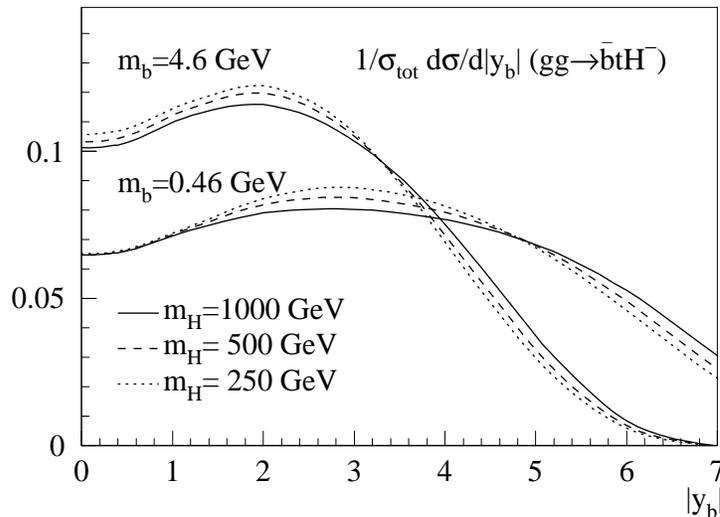
Problem with gluon splitting [one final-state bottom: $gg \rightarrow \bar{b}tH^-$]



- e.g. MadEvent output: forward jets, $p_{T,b}$ peaked at m_b
- bottom-inclusive cross section for $gg \rightarrow \bar{b}tH^-$?
- QCD: collinear bottom from gluon splitting, IR-regularized by m_b
- asymptotic behavior $d\sigma/dp_{T,b} \propto p_{T,b}/m_b^2$

\Rightarrow inclusive total rate $\sigma \propto \log p_{T,b}^{\max}/p_{T,b}^{\min} \sim \log p_{T,b}^{\max}/m_b$

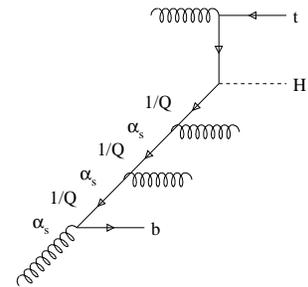
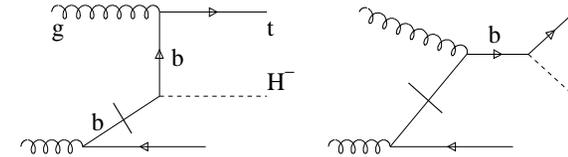
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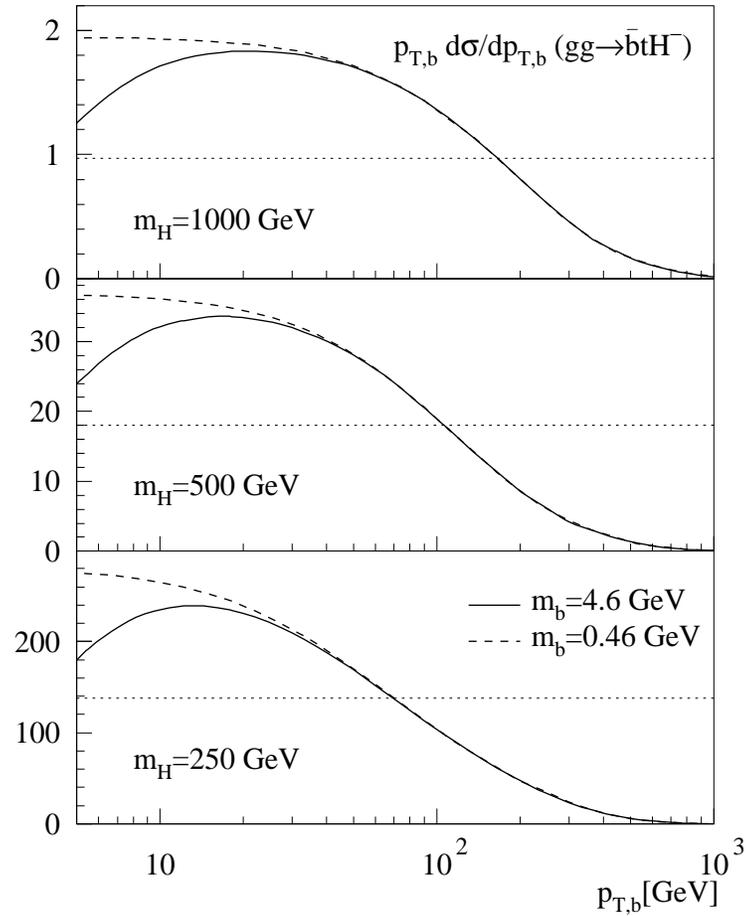


Bottom partons [Aivazis, Collins, Olness, Tung, Willenbrock]

- collinear description of gluon splitting valid below $p_{T,b}^{\max}$ [Johan Alwall's talk]
 - resummation defines bottom parton density [e.g. $bg \rightarrow tH^-$]
 - $\mu_{F,b}$ 'transverse momentum size' of inclusive bottom parton [$\mu_{F,b} \equiv p_{T,b}^{\max}$ perturbative!]
 - usually matrix elements in limit $m_b \rightarrow 0$
- \rightarrow (1) check bottom-inclusive total rate
 (2) check bottom-inclusive distributions

COMPUTING BOTTOM PARTONS

Before tests: understand $p_{T,b}$ and $\mu_{F,b}$



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- QCD factorization: start with virtuality Q for $gg \rightarrow \bar{b}X_M$
- Russian style approximation: [$\mathcal{L} = \mathcal{L}_0/x^2$, etc; Boos & TP]

$$\sigma = \frac{2\sigma_0\mathcal{L}_0}{16\pi} \int_0^{S-M^2} \frac{dQ_b}{Q_b} F(Q_b)$$

- $F(Q_b)$ correction to asymptotic behavior $d\sigma/dQ_b \sim 1/Q_b$
- $\Rightarrow Q_b^{\max} \sim M/2$ at turning point of $F(\log Q)$ [usually only $Q_b^{\max} \propto M$, see also Alwall & Rathsmann]
- $\Rightarrow Q_b \rightarrow p_{T,b}$ point by point: $\mu_{F,b} \equiv p_{T,b}^{\max} \sim Q_b^{\max}/2 \sim M/4$ [same as numerical results]

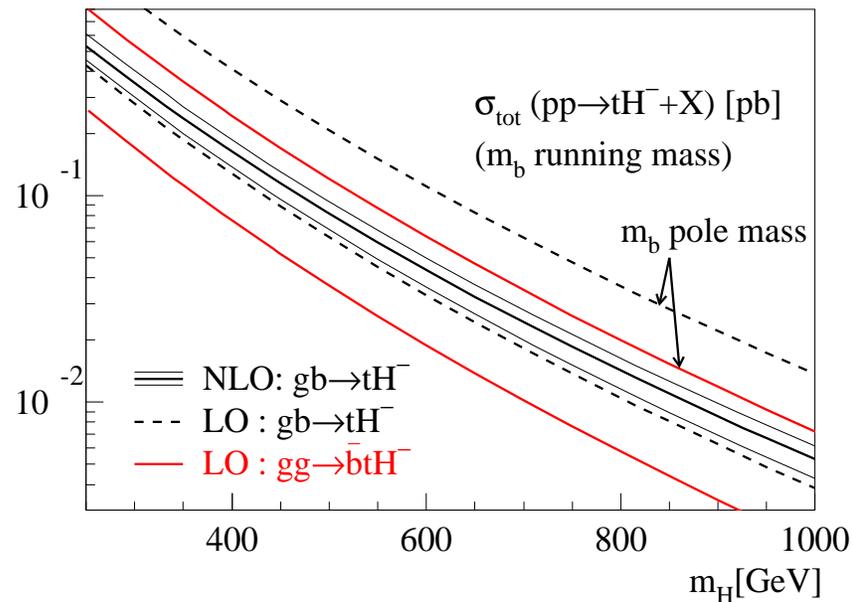
Bottom partons in perturbative QCD

- ‘large’ logs at maximum $\log p_{T,b}/m_b < \log M/(5m_b)$ [also: Maltoni & Willenbrock]
 - inclusive $gg \rightarrow \bar{b}X_M$ factorization scale $\mu_{F,b} \sim M/5$
 - confirmed by NNLO calculations for $b\bar{b} \rightarrow h$ [Harlander & Kilgore]
 - not valid for (quark-induced) single top production
- \Rightarrow **cross section with bottom partons understood**

TOP-HIGGS TOTAL CROSS SECTION AT NLO

Bread-and-butter NLO corrections to $bg \rightarrow tH^-$

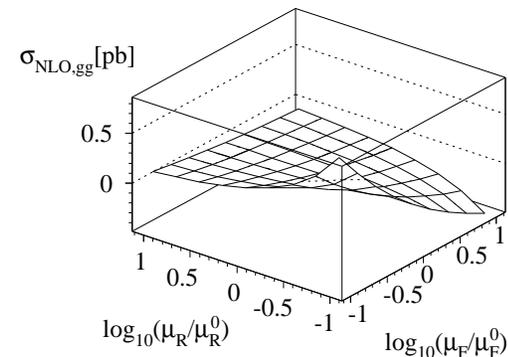
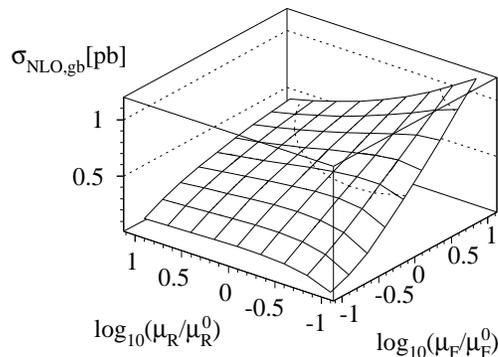
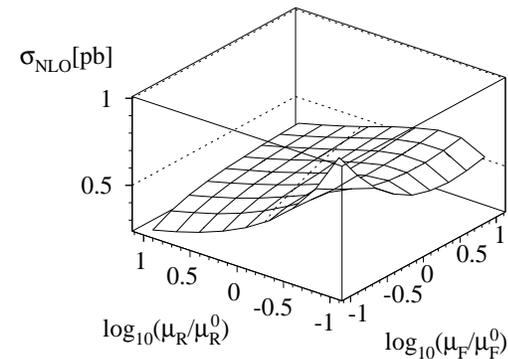
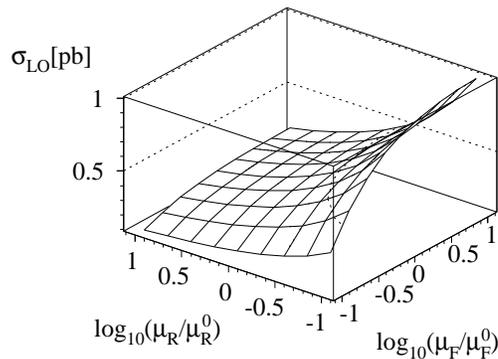
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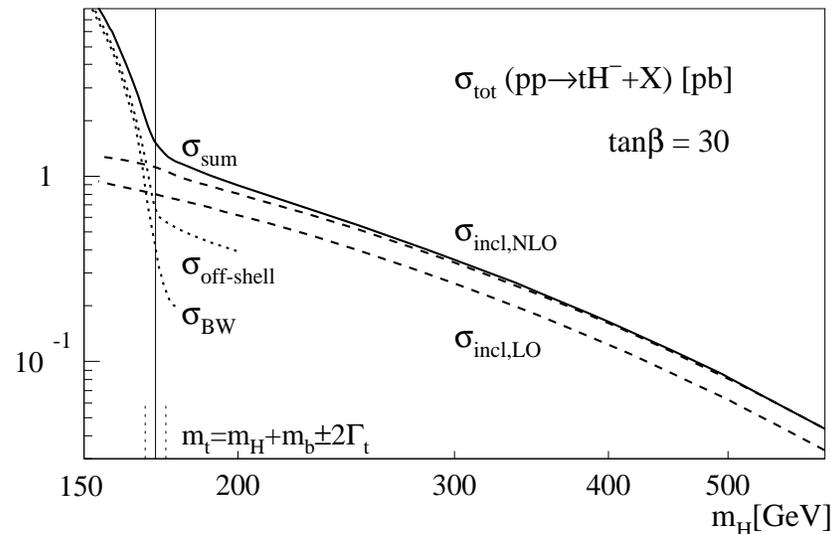
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- exclusive $gg \rightarrow \bar{b}tH^-$ part of NLO $bg \rightarrow tH^-$
 \Rightarrow problems with bottom partons butcher NLO perturbative expansion
- double counting of $pp \rightarrow t\bar{t}^* \rightarrow t(\bar{b}H^-)$
 \Rightarrow subtract on-shell $t\bar{t}$ from $bg \rightarrow tH^-$ at NLO [Berger, Han, Jiang, TP]
 \Rightarrow simply add samples with NLO normalization



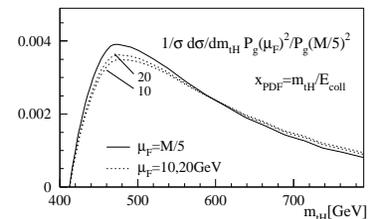
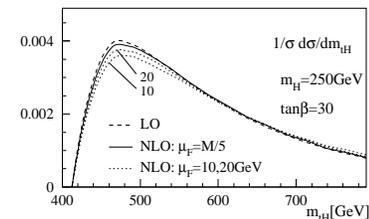
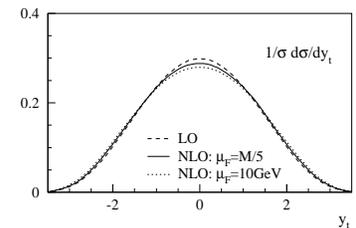
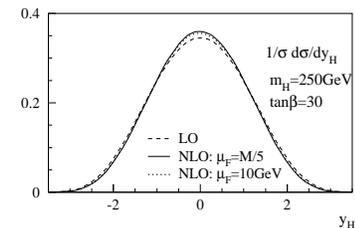
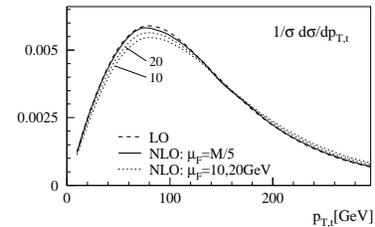
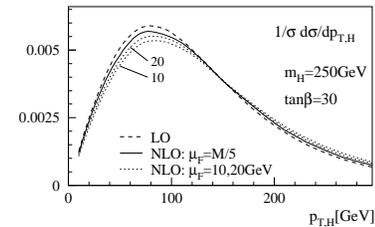
TOP-HIGGS DISTRIBUTIONS AT NLO

As far I know only checked in $bg \rightarrow tH^-$ [Berger, Han, Jiang, TP]

- bottom parton description appropriate for total rate [review on $b\bar{b} \rightarrow h$: Dawson, ...]
- Higgs and top distributions?

Approximation $p_{z,b} \gg p_{T,b} \rightarrow 0$

- compare $gb \rightarrow tH^-$ and $gg \rightarrow \bar{b}tH^-$ [as part of NLO]
 - switch on/off bottom partons via $\mu_F \rightarrow m_b$
- \Rightarrow slightly harder distributions
[gluon PDF, not bottom partons]



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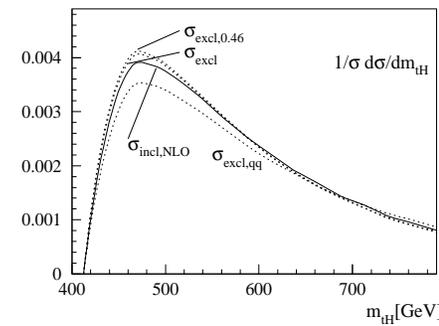
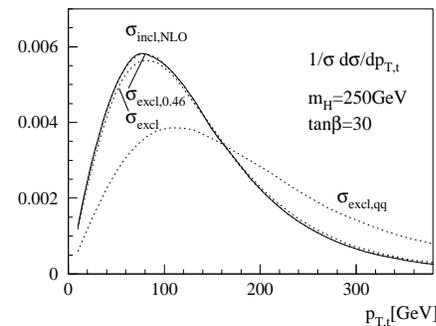
Approximation $m_b \rightarrow 0$

- bottom mass dependence of $pp \rightarrow \bar{b}tH^-$
- collinear log subtraction instead of dimensional regularization

[Krämer, Olness, Soper]

- perfect agreement

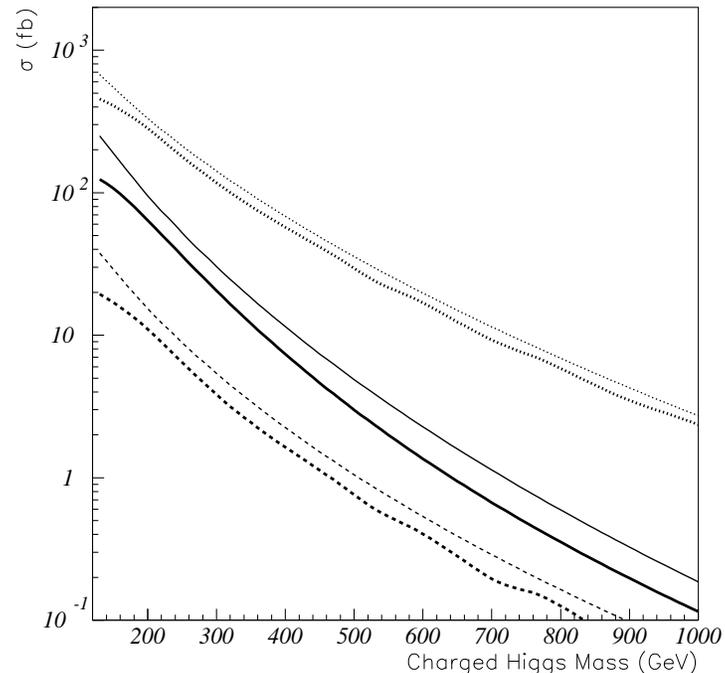
\Rightarrow **bottom parton picture established**



W-HIGGS CROSS SECTION AT NLO

Similarly for $gg \rightarrow b\bar{b}W^+H^-$ [Hollik & Zhu]

- competing with loop-induced $gg \rightarrow W^+H^-$ [see Oliver's talk]
 - two bottom partons $b\bar{b} \rightarrow W^+H^-$ [each proportional to $\log \mu_{F,b}/m_H$]
 - same scale argument applicable because of initial-state gluons
 - NLO computed before bottom parton issues were resolved
- ⇒ **too large $\mu_{F,b}$ compensated by NLO corrections: $K < 1$**
[There is no really 'correct scale' in QCD, but there are wrong, perturbative unstable ones...]



HIGGS-PAIR CROSS SECTIONS AT NLO

Charged Higgs pairs [Alves & TP]

- bottom fusion $b\bar{b} \rightarrow H^+ H^-$

$\tan^4 \beta$ beta enhancement of rate

QCD as $bg \rightarrow tH^-$ and $b\bar{b} \rightarrow H^+ H^-$

NLO corrections small and positive for appropriate $\mu_{F,b}$

- Drell–Yan process $q\bar{q} \rightarrow H^+ H^-$

valence quarks for heavy masses

no $\tan \beta$ enhancement

(N)NLO corrections just like Drell–Yan [Anastasiou, Melnikov, Petriello; Kilgore]

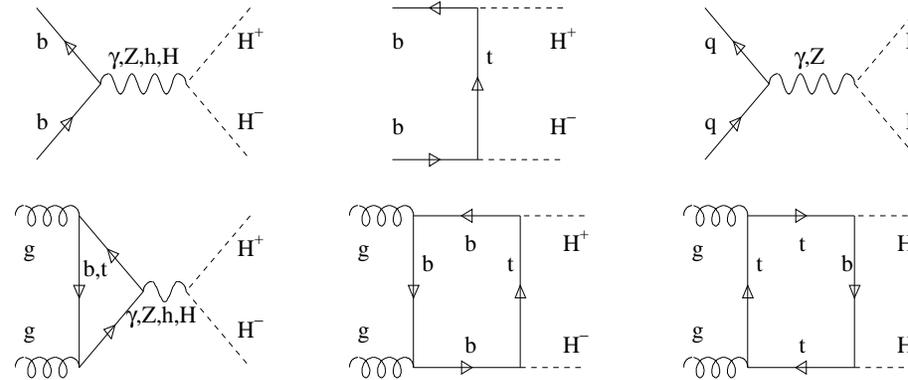
- loop–induced gluon fusion

$\tan^4 \beta$ beta enhancement of box

no effective higher–dimensional coupling for Madevent

loop sensitive to particle content of model [SUSY talks by Jaume and Oliver]

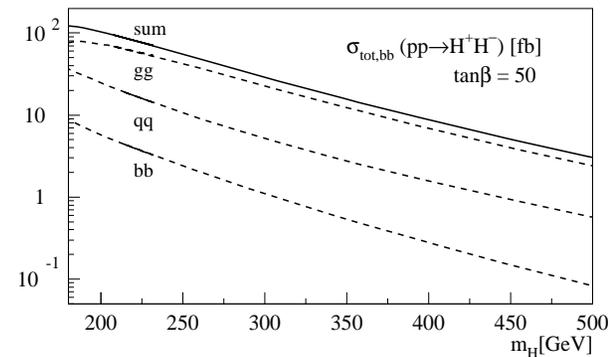
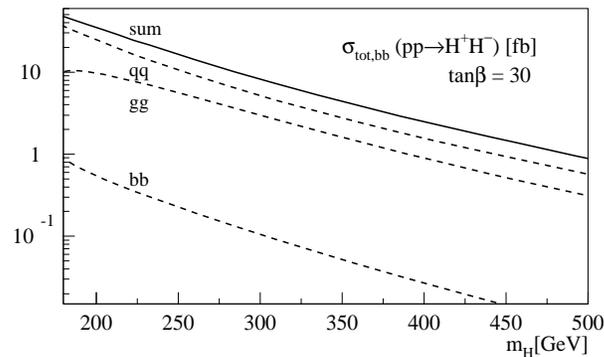
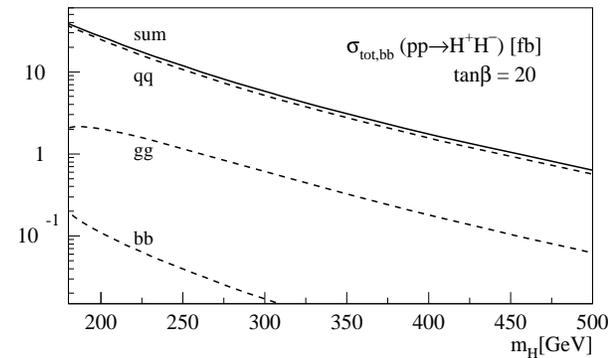
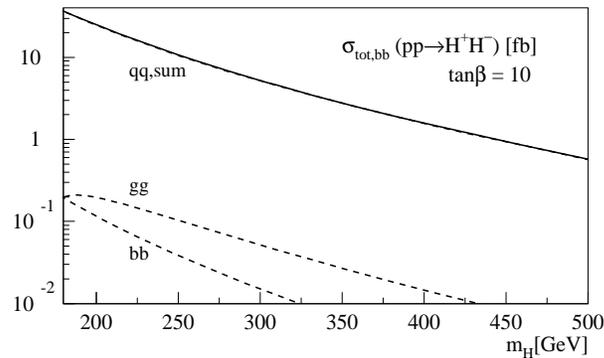
NLO (probably) similar to neutral pairs [Dawson, Dittmaier, Spira]



HIGGS-PAIR CROSS SECTIONS AT NLO

Total cross sections [Alves, TP]

- bottom factorization scale argument as before [It's QCD, stupid!]
 - bottom approximations quantitatively tested [m_b and $p_{T,b}$ approximations fine]
 - reliable cross section values to compare [NLO to loop process hard without effective coupling]
- ⇒ race between loop amplitude and Drell–Yan [$b\bar{b}$ process killed]



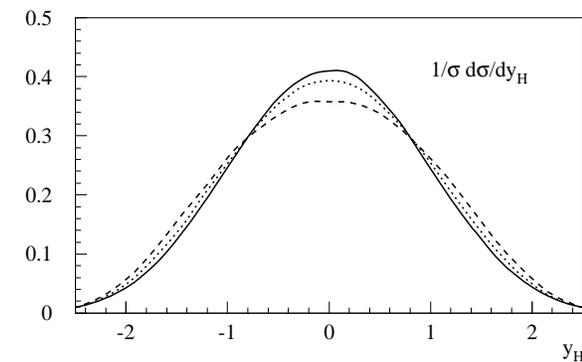
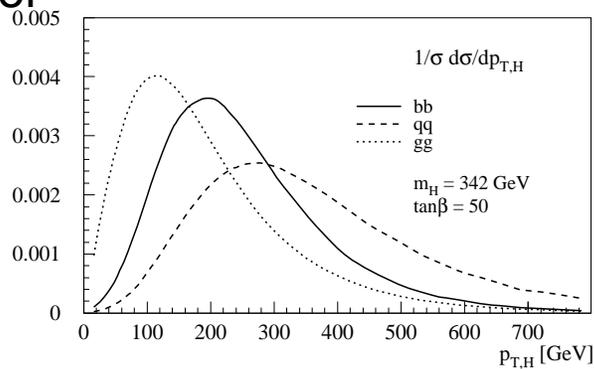
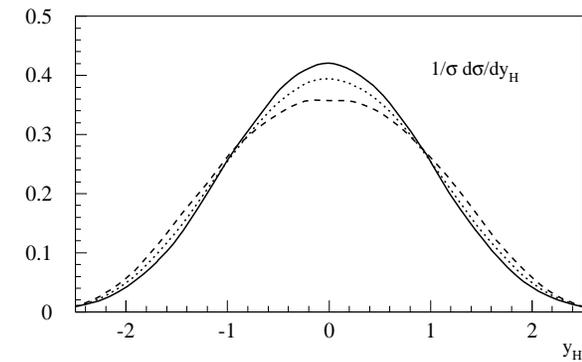
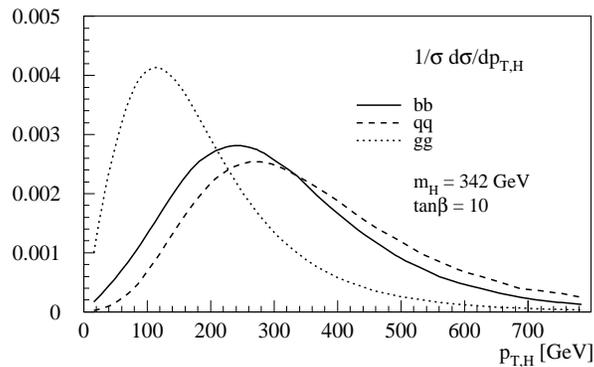
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Distributions

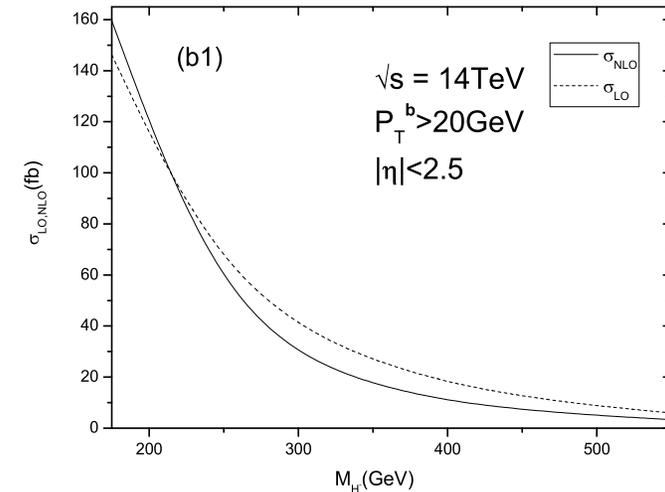
- gg process soft
- $b\bar{b}$ harder
- Drell–Yan process hard
- ⇒ add samples at given order



WHAT ELSE

Further reading and checking

- threshold resummation at NNNLO
possible rate enhancement of $\sim 15\%$ [Kidonakis]
- NLO corrections to exclusive $gg \rightarrow \bar{b}tH^-$ [Peng et al]



Outlook

- charged Higgs physics exciting from QCD and SUSY point of view
 - many channels computed, what else do you need us to think about?
- \Rightarrow **Let's go and find that thing!**