

# Phenomenology: QCD

Tilman Plehn

University of Edinburgh

Graduiertenkolleg Freiburg, 11/2007

# Outline

Hadron Colliders — Stars on the Physics Sky

QCD for New Physics Searchers

Collinear jets

QCD scales

Important Standard–Model Processes

Jet Radiation

# Organization

Collider basics

QCD basics

Collinear jets

QCD scales

Some processes

Jet radiation

## 5 1/2 hours on LHC phenomenology

- collider basics
- scales in QCD
- hard vs collinear jets
- merging jet descriptions
- why new physics?
- why supersymmetry?
- searches for new physics
- new-physics properties
- new-physics parameters
- why extra dimensions?

## One way of teaching phenomenology

- let's try to get to current topics
- past colliders are physics history and PDG entries
- we'll all spend 10+ years in the shadow of LHC
- you ask — I'll try to answer
- ....

# Signals for new particles

## Real-particle production [gluon, top quark]

- produce searched-for particle
  - observe decay [before hadronization]
  - reconstruct decay products [(transverse) mass peak with side bins]
- ⇒ measure mass, spin, branching ratios beyond Standard Model
- ⇒ highest-energy colliders

## Virtual-particle effects [gauge bosons $W, Z, b \rightarrow s\gamma$ ]

- produce and measure something else (like  $W, Z$ )
  - compare to Standard-Model predictions
- ⇒ find deviations from Standard-Model relations
- ⇒ highest-precision colliders

## Rare effect or rare decays [ $B$ physics, EDMs, LHC signatures?]

- produce something else (like  $B_S, \dots$ )
  - find effect forbidden in Standard Model
- ⇒ observe effect beyond Standard Model
- ⇒ best-chosen experiment

## Collider basics

## Collider basics

## QCD basics

## Collinear jets

## QCD scales

## Some processes

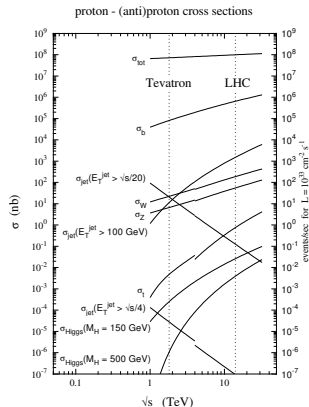
## Jet radiation

## Most powerful colliders: hadron colliders

- inside 27 km LEP tunnel [used to be  $e^+e^-$  with 200 GeV, now  $pp$  with 14 TeV]
- proton–proton collisions [Tevatron: proton–antiproton at 2 TeV]
- hadronic c.m. energy divided into partons [first approximation  $p = (uud)$ ]
- luminosity:  $N = \sigma \mathcal{L}$  with  $\mathcal{L} \propto f n_1 n_2 / a$  [measured in  $\text{cm}^{-2} \text{s}^{-1} = 10^{-39} \text{fb}^{-1} \text{s}^{-1}$ ]

## Everything you always wanted to know...

- signal: everything new, exciting and rare  
background: yesterday's signal
- Standard Model: theory of background  
QCD: evil background theory trying to kill us
- $N_{\text{events}} = \sigma \cdot \mathcal{L} \cdot \epsilon$
- trigger: no leptons/photons — not on tape
- jet: everything except for leptons/photons  
crucial: what is inside a jet [q, g, b,  $\tau$  tagged?]
- **discovery**  $N_S / \sqrt{N_B} > 5$



# Collider basics

## Collider basics

## QCD basics

## Collinear jets

## QCD scales

## Some processes

## Jet radiation

## Computing what goes on at hadron colliders

- incoming protons resolved at TeV-scale energy
- to first approximation described by valence quarks ( $uud$ )

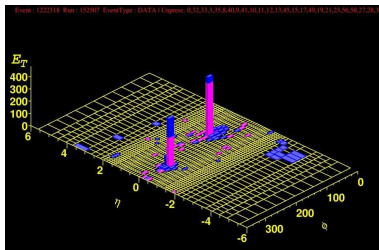
$$\sigma_{AB} = \sum_{a,b} \int_0^1 dx_a dx_b f_{a/A}(x_a) f_{b/B}(x_b) \hat{\sigma}_{ab}$$

- (1) parton density  $f_{a/A}(x_a)$ :  
probability to find parton  $a$  of momentum fraction  $x_a$  in proton  $A$   
kinematics of partons collinear with proton
  - parton densities measured in many experiments [mostly HERA]
- (2) partonic cross section  $\hat{\sigma}_{ab}$ :  
just like  $e^+ e^-$ , but with incoming quarks and gluons ['hard process']  
defined perturbatively counting interaction vertices
  - partonic cross section calculated (numerically) for any imaginable final state

## Collider basics

## Kinematics at a hadron collider

- incoming momenta in lab frame:  $p_{a,b} = x_{a,b} (E_{A,B}, 0, 0, p_{A,B})$  [partons massless]
- center-of-mass frame moving in  $z$  direction
- cylindrical coordinates  $d^3\vec{p} = p_T d\phi dp_T dp_z$  [transverse momentum  $p_T = \sqrt{p_x^2 + p_y^2}$ ]
- (1) usual event sample:  $\phi$  symmetry
- (2) transverse momentum and mass:  $E_T = \sqrt{p_T^2 + m^2}$
- (3) rapidity
 
$$y = \frac{1}{2} \log \frac{E + p_z}{E - p_z} \quad y_{\text{boosted}} = y + y_{z\text{-shift}} \quad |y_{\text{observed}}| \lesssim 5$$
- lego plot ( $p_T, y, \phi$ ) or ( $E_T, \eta, \phi$ ) [ $\eta = \log \cot \theta/2$ ]
- distance between two tracks  $\Delta R = \sqrt{(\Delta y)^2 + (\Delta\phi)^2}$



## Collider basics

## Collider basics

## QCD basics

## Collinear jets

## QCD scales

## Some processes

## Jet radiation

## Kinematics at a hadron collider

– incoming momenta in lab frame:  $p_{a,b} = x_{a,b} (E_{A,B}, 0, 0, p_{A,B})$  [partons massless]

– center-of-mass frame moving in  $z$  direction

– cylindrical coordinates  $d^3\vec{p} = p_T d\phi dp_T dp_z$  [transverse momentum  $p_T = \sqrt{p_x^2 + p_y^2}$ ]

– (1) usual event sample:  $\phi$  symmetry

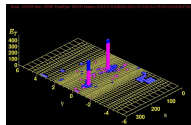
(2) transverse momentum and mass:  $E_T = \sqrt{p_T^2 + m^2}$

(3) rapidity

$$y = \frac{1}{2} \log \frac{E + p_z}{E - p_z} \quad y_{\text{boosted}} = y + y_{z\text{-shift}} \quad |y_{\text{observed}}| \lesssim 5$$

– lego plot  $(p_T, y, \phi)$  or  $(E_T, \eta, \phi)$  [ $\eta = \log \cot \theta/2$ ]

– distance between two tracks  $\Delta R = \sqrt{(\Delta y)^2 + (\Delta\phi)^2}$



## Useful observables

– invariant mass  $(p_{\ell,1} + p_{\ell,2})^2 = m_{\ell\ell}^2 \sim m_Z^2$

– transverse mass [massless invisible neutrino]

$$\begin{aligned} m_{e\nu}^2 &= (E_e + E_\nu)^2 - (\vec{p}_{T,e} + \vec{p}_{T,\nu})^2 - (\vec{p}_{z,e} + \vec{p}_{z,\nu})^2 \\ &> (E_{T,e} + E_{T,\nu})^2 - (\vec{p}_{T,e} + \vec{p}_{T,\nu})^2 \\ &= (E_{T,e} + |\vec{p}_{T,\nu}|)^2 - (\vec{p}_{T,e} + \vec{p}_{T,\nu})^2 = m_{T,e\nu}^2 \end{aligned}$$



## Collider basics

## Collider basics

## QCD basics

## Collinear jets

## QCD scales

## Some processes

## Jet radiation

## Trigger

- flood of data from each bunch crossing not manageable [event rate 1 GHz with 1 MB]
  - use some prejudice to write ‘interesting’ events on tape [realistic 100 Hz]
  - **LHC is not built to test QCD!** [interesting events  $1/10^6$ ]
  - soft jets, multiple interactions,... into trash
  - leptons, photons, hard jets, missing momentum,... of high priority
- open problems: invisible Higgs decays, stable particles, super-fast top jets,...
- ⇒ trigger menue  $T(t, k, \$)$  [a function of time, knowledge and money]

Level-1 trigger menue from Atlas [down to  $10^5$  Hz, always outdated]

Objects	Atlas	
	$ \eta ^{\max}$	$p_T^{\min}$ (GeV)
$\mu$ inclusive	2.4	6 (20)
$e$ /photon inclusive	2.5	17 (26)
two $e$ 's or two photons	2.5	12 (15)
1-jet inclusive	3.2	180 (290)
3 jets	3.2	75 (130)
4 jets	3.2	55 (90)
$\tau$ /hadrons	2.5	43 (65)
$\cancel{p}_T$	4.9	100
jets + $\cancel{p}_T$	3.2, 4.9	50,50 (100,100)

## QCD basics

Simple hadron collider process:  $pp \rightarrow Z(+\text{jets})$ 

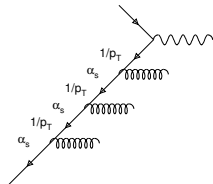
- Drell–Yan process: single gauge boson production [could be  $W, Z$  with  $Z \rightarrow \ell\ell$ ]
- **what is the final state in hadronic  $\sigma_{AB}$ ?**
- more specific: what about additional jets  $\sigma(pp \rightarrow Z + \text{jets})$ ?
- to get an idea: compute  $q\bar{q} \rightarrow Z$  and  $q\bar{q} \rightarrow Zg$
- phase space integration over gluon IR divergent: soft —  $E_g \rightarrow 0$   
collinear —  $\theta_{gX} \rightarrow 0$

## Similarly for initial–state radiation

- gluon off incoming quark with  $p_{Tj}$  [soft and collinear, needs virtual–gluon diagrams]
  - same for incoming gluon splitting into quarks with  $p_{Tj}$  [ $qg \rightarrow Zq$  only collinear]
- $\Rightarrow$  partonic cross section  $\hat{\sigma}_{Z+\text{jet}}$  IR divergent

$$\frac{d\sigma_{Zg}}{dp_{Tj}} \propto \frac{\alpha_s p_{Tj}}{p_{Tj}^2 + m_j^2} = \frac{\alpha_s}{p_{Tj}}$$

$$\Rightarrow \sigma_{Zg} \propto \alpha_s \log \frac{p_{Tj}^{\max}}{p_{Tj}^{\min}}$$



## QCD basics

Collider basics

QCD basics

Collinear jets

QCD scales

Some processes

Jet radiation

Simple hadron collider process:  $pp \rightarrow Z(+\text{jets})$ 

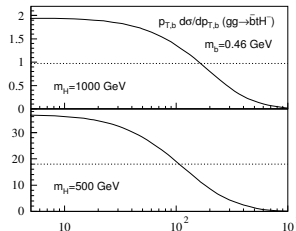
- Drell–Yan process: single gauge boson production [could be  $W, Z$  with  $Z \rightarrow \ell\ell$ ]
- **what is the final state in hadronic  $\sigma_{AB}$ ?**
- more specific: what about additional jets  $\sigma(pp \rightarrow Z + \text{jets})$ ?
- to get an idea: compute  $q\bar{q} \rightarrow Z$  and  $q\bar{q} \rightarrow Zg$
- phase space integration over gluon IR divergent: soft —  $E_g \rightarrow 0$   
collinear —  $\theta_{gX} \rightarrow 0$

## Similarly for initial–state radiation

- gluon off incoming quark with  $p_{Tj}$  [soft and collinear, needs virtual–gluon diagrams]
  - same for incoming gluon splitting into quarks with  $p_{Tj}$  [ $qg \rightarrow Zq$  only collinear]
- $\Rightarrow$  partonic cross section  $\hat{\sigma}_{Z+\text{jet}}$  IR divergent

$$\frac{d\sigma_{Zg}}{dp_{Tj}} \propto \frac{\alpha_s p_{Tj}}{p_{Tj}^2 + m_j^2} = \frac{\alpha_s}{p_{Tj}}$$

$$\Rightarrow \sigma_{Zg} \propto \alpha_s \log \frac{p_{Tj}^{\max}}{p_{Tj}^{\min}}$$



## QCD basics

Collider basics

QCD basics

Collinear jets

QCD scales

Some processes

Jet radiation

## Divergences, regularization and renormalization scale

- remember  $q\bar{q} \rightarrow b\bar{b}$  via  $s$ -channel gluon to NLO
- including chain of (reducible) gluon self energies
- regularize gluon self-energy bubbles  $[n = 4 - 2\epsilon < 4]$

$$\int \frac{d^4 k}{(2\pi)^4} \rightarrow r_\epsilon(\mu_R) \int \frac{d^{4-2\epsilon} k}{(2\pi)^{4-2\epsilon}} \sim \mu_R^{2\epsilon} \int \frac{d^{4-2\epsilon} k}{(2\pi)^{4-2\epsilon}}$$

rewrite  $\mu_R^\epsilon = \exp(\log \mu_R^\epsilon) = \exp(\epsilon \log \mu_R) = 1 + \epsilon \log \mu_R + \dots$

- naked divergent gluon self energy

$$\frac{\Sigma^{\mu\nu}(p^2)}{p^2} = \frac{\alpha_s}{4\pi} \frac{r_\epsilon(\mu_R)}{\epsilon} \left( \frac{4T_R N_F}{3} - \frac{5C_A}{3} \right) \left( -g^{\mu\nu} + \frac{p^\mu p^\nu}{p^2} \right)$$

- add chains of one, two, three,.... one-loop bubbles [will show in detail later]  
call the resulting scale-dependent coupling  $\alpha_s(p^2)$  [ $\overline{\text{MS}}$  scheme]

$$\frac{1}{\alpha_s(p^2)} = \frac{1}{\alpha_s(\mu_R^2)} + \frac{1}{4\pi} \left( \frac{11C_A}{3} - \frac{4T_R N_F}{3} \right) \log \frac{p^2}{\mu_R^2}$$

$$\Leftrightarrow \frac{\partial \alpha_s(\mu^2)}{\partial \log \mu^2} = -\frac{\alpha_s^2}{4\pi} \left( \frac{11C_A}{3} - \frac{4T_R N_F}{3} \right) + \dots$$

$\Rightarrow$  renormalization group sums chains of divergent diagrams

## Collinear jets

Collider basics

QCD basics

Collinear jets

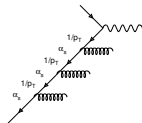
QCD scales

Some processes

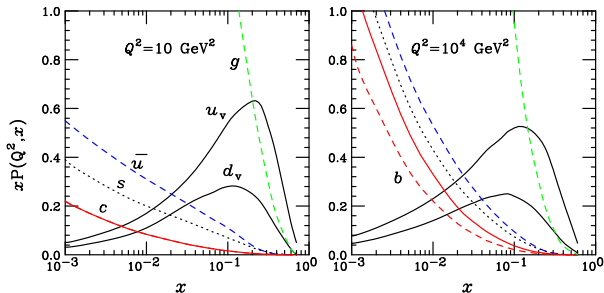
Jet radiation

## Initial-state gluon radiation

- back to multiple gluon radiation off incoming quark
  - each splitting  $\alpha_s \log p_{Tj}^{\max} / p_{Tj}^{\min}$  [also possible as  $1/\epsilon$ ]
  - IR-divergent in collinear limit
  - geometric series just like multiple gluon self energies [IR problem instead of UV problem]
- ⇒ sum diagrams and absorb in running of parton density [DGLAP]



$$\frac{df_{a/A}(x, \mu_F)}{d \log \mu_F^2} = \sum_B \int_x^1 \frac{dz}{z} P_{a \leftarrow b} \left( \frac{x}{z}, \alpha_s \right) f_{b/A}(z, \mu_F)$$



## Collinear jets

Collider basics

QCD basics

Collinear jets

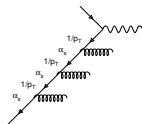
QCD scales

Some processes

Jet radiation

## Initial-state gluon radiation

- back to multiple gluon radiation off incoming quark
  - each splitting  $\alpha_s \log p_{Tj}^{\max} / p_{Tj}^{\min}$  [also possible as  $1/\epsilon$ ]
  - IR-divergent in collinear limit
  - geometric series just like multiple gluon self energies [IR problem instead of UV problem]
- ⇒ sum diagrams and absorb in running of parton density [DGLAP]



$$\frac{df_{a/A}(x, \mu_F)}{d \log \mu_F^2} = \sum_B \int_x^1 \frac{dz}{z} P_{a \leftarrow b} \left( \frac{x}{z}, \alpha_s \right) f_{b/A}(z, \mu_F)$$

- with universal collinear splitting kernels [means factorization]

$$P_{q \leftarrow q}(x) = C_F \frac{1+x^2}{1-x}$$

$$P_{q \leftarrow g}(x) = T_R (x^2 + (1-x)^2)$$

$$P_{g \leftarrow q}(x) = C_F \frac{1+(1-x)^2}{x}$$

$$P_{g \leftarrow g}(x) = C_A \left( \frac{x}{1-x} + \frac{1-x}{x} + x(1-x) \right)$$

- jet radiation absorbed into collinear pdf [jet distributions for  $p_{Tj} < \mu_F$  from parton shower]
  - divergence  $p_{Tj}^{\min} \rightarrow 0$  removed,  $p_{Tj}^{\max} \equiv \mu_F$  artificial parameter [smart choice?]
- ⇒ jet radiation below factorization scale ( $p_{Tj} < \mu_F$ ) included in pdf

## QCD scales

Collider basics

QCD basics

Collinear jets

QCD scales

Some processes

Jet radiation

## Scales in QCD processes

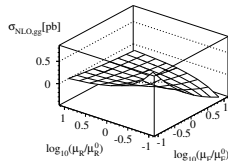
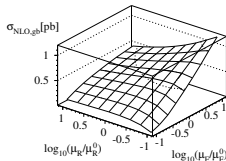
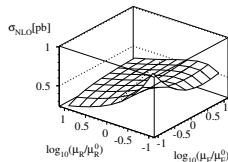
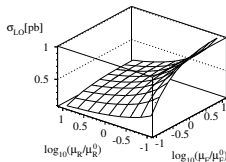
gluon propagator in $s$ channel	initial–state jet radiation
UV divergence $1/(n - 4)$ absorbed into counter term (renormalization) universality: renormalizability	IR divergence $\log p_T^{\min}$ absorbed into parton densities (mass factorization) universality: factorization
running coupling $\alpha_s(\mu_R)$ renormalization scale $\mu_R$ evolution by beta function of $\alpha_s$ 'physics choice' $\mu_R \sim p_{T,j}$	running parton density $f_{a/A}(x, \mu_F)$ factorization scale $\mu_F$ evolution by DGLAP equation 'physics choice' $\mu_F \sim p_{T,j}^{\max}$
all scales artificial parameters not unique for multi–scale problems scale dependence vanishing including all orders	

## QCD scales

## Error estimates in QCD

- QCD at colliders always perturbative in  $\alpha_S$  [plus possibly logs]
  - let's hope, large logarithms identified and summed
  - all observables function of scales  $O = O(\mu_F, \mu_R)$
- ⇒ scales artifact of perturbation theory, so vanish at all orders
- ⇒ **scale dependence (only?) measure of theoretical uncertainty**

Example:  $pp \rightarrow tH^-$





# QCD scales

## Error estimates in QCD

- QCD at colliders always perturbative in  $\alpha_S$  [plus possibly logs]
  - let's hope, large logarithms identified and summed
  - all observables function of scales  $O = O(\mu_F, \mu_R)$
- ⇒ scales artifact of perturbation theory, so vanish at all orders
- ⇒ **scale dependence (only?) measure of theoretical uncertainty**

## Caveats

- total cross section with jets  $\sigma(\mu_F, \mu_R)$ 
    - (1) asymptotic freedom:  $\sigma(\mu_R \rightarrow 0) = \infty$  and  $\sigma(\mu_R \rightarrow \infty) = 0$
    - (2)  $p_T$  size of proton:  $\sigma(\mu_F \rightarrow 0) = 0$  and  $\sigma(\mu_F \rightarrow \infty) = \infty$
- ⇒ scale dependences can cancel [more on DY process later]
- there is no 'correct' scale, but there are idiotic scales [introducing large logs]

# QCD scales

## Error estimates in QCD

- QCD at colliders always perturbative in  $\alpha_S$  [plus possibly logs]
  - let's hope, large logarithms identified and summed
  - all observables function of scales  $O = O(\mu_F, \mu_R)$
- ⇒ scales artifact of perturbation theory, so vanish at all orders
- ⇒ **scale dependence (only?) measure of theoretical uncertainty**

## Physics of wrong scales

- $\mu_F$  defining  $p_T$ -size of parton, perturbative part  $f_{a/A} \propto \log \mu_F$
- large  $\mu_F$  means (too) many collinear jets included LO  
corrected by correct NLO jet radiation:  $K = \sigma_{\text{NLO}}/\sigma_{\text{LO}} \ll 1$   
small  $\mu_F$  means (too) few jets included in LO  
corrected by correct NLO jets:  $K \gg 1$
- $\mu_R$  defining scale in coupling constants or masses  $\propto \log \mu_1/\mu_2$
- $\alpha_S(\mu_R)$  leading higher-order contributions, but NLO with explicit argument  
 $\log Q/\mu_R$  explicitly contributing to  $K$
- known trick: mimic soft jet radiation using  $\alpha_S(p_{Tj})$

## Jets

Collider basics

QCD basics

Collinear jets

QCD scales

Some processes

Jet radiation

## Definition of jets

- jet-parton duality  $\Leftrightarrow$  partons in detector
- jet-rich environment at (hadron) colliders [mostly but not only soft or collinear]
- $\Rightarrow$  need jet algorithm to decide what comes from one parton
- stable w.r.t inclusion of soft or collinear jet [IR safe]
- crucial for  $m_{qq}$  searching for  $Z' \rightarrow q\bar{q}$ , etc
- even more crucial if likelihood  $|\mathcal{M}|^2$  of interest

Should be standard:  $k_T$  algorithm [experts: exclusive with  $R = 1$ ]

- define a distance jet-jet  $d_{kl}$  and jet-beam  $d_{kB}$   
only requirement:  $d_{kl} \sim k_{T,k}^2$  for  $\theta_{kl} \rightarrow 0$  [e.g.  $d_{kB} = E_k^2 \theta_k^2$ ]
- (0) define resolution  $d_{\text{cut}}$  [or number of jets]
- (1) find minimum  $d_{\text{min}} = \min_{kl}(d_{kl}, d_{kB})$ 
  - (2a) if  $d_{\text{min}} > d_{\text{cut}}$  all objects are jets
  - (2b) if  $d_{\text{min}} = d_{kl} < d_{\text{cut}}$  combine  $k$  and  $l$ , go to (1)
  - (2c) if  $d_{\text{min}} = d_{kB} < d_{\text{cut}}$  remove  $k$  from list, go to (1)
- $\Rightarrow d_{\text{cut}}$  separating hard from soft-collinear physics
- if pheno analysis requires jet algorithms, you'll likely get it wrong

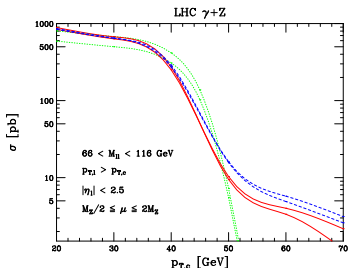
# Processes

## Example processes everyone will need

- total cross section (coupling) measurements need luminosity
- effectively: normalization to standard candle
- simple (leptonic) final state  
well-controlled QCD corrections  
high-precision Monte-Carlo [NNLO if possible]

⇒ Drell-Yan production  $pp \rightarrow \mu^+ \mu^-$

## Example: Drell-Yan at LO, NLO, NNLO [error from scales?]

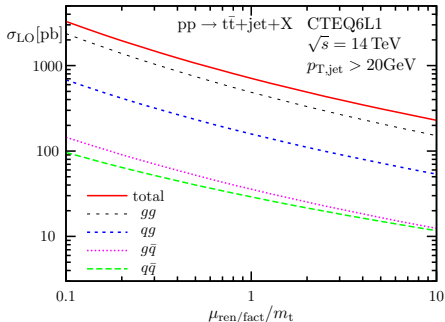


# Processes

## Example processes everyone will need

- new physics usually including bottom jets, lepton, missing momentum
- ⇒ **main background  $t\bar{t}$ +jets**
- background rate after cuts problematic [phase space fragmented]
- NLO corrections to  $pp \rightarrow t\bar{t}$  available in MC@NLO
- exclusive NLO corrections to  $pp \rightarrow t\bar{t}j$  almost done

## Example: $pp \rightarrow tj$ at LO



# Jet radiation

Collider basics

QCD basics

Collinear jets

QCD scales

Some processes

Jet radiation

## Hard jets [remember $Z + g$ example]

- strictly perturbative, no large logarithms
- described by matrix elements [finite at given order in  $\alpha_S$ , e.g.  $q\bar{q} \rightarrow Z + g + b + \bar{b} + g$ ]

## Soft and collinear jets [no technical details here]

- perturbation theory spoiled by collinear logarithm [fixed-order divergence]
  - total cross sections: defined only jet-inclusively [collinear jets always part of pdf]
  - collinear jet distributions by parton shower [SCET with improved theoretical description?]
- ⇒ **holy grail of QCD at colliders: combine the two**

## Sudakov factors

- Poisson statistics: event with expected  $p$  hits occurring  $n$  times

$$f(n; p) = \frac{p^n e^{-p}}{n!} \quad \text{no event: } f(0; p) = e^{-p}$$

- collinear gluon/photon radiation described by energy-dependent probability

$$dP(x) = \frac{\alpha_S}{2\pi} P(x) dx \quad f(0; x_{\min}, x_{\max}) = \exp\left(-\int_{x_{\min}}^{x_{\max}} dP(x)\right)$$

- ⇒ **Sudakov giving probability of no radiation/splitting**

## Jet radiation: MC@NLO

## MC@NLO approach

- one hard jet correctly described by exclusive NLO corrections
- soft and collinear jet radiation for all jets from parton shower

## Bryan Webber's toy model

- observable for photon radiated with energy  $0 < x < 1$

$$\langle O \rangle = \mu_F^{2\epsilon} \int_0^1 dx \frac{O(x)}{x^{2\epsilon}} \left[ \left. \frac{d\sigma}{dx} \right|_B + \left. \frac{d\sigma}{dx} \right|_V + \left. \frac{d\sigma}{dx} \right|_R \right]$$

with Born, virtual, real contributions  $[\lim_x R(x) = B, a: \text{coupling}]$

$$\left. \frac{d\sigma}{dx} \right|_B = B \delta(x) \quad \left. \frac{d\sigma}{dx} \right|_V = a \left( \frac{B}{2\epsilon} + V \right) \delta(x) \quad \left. \frac{d\sigma}{dx} \right|_R = a \frac{R(x)}{x}$$

- usual subtraction to cancel IR divergence in photon emission

$$\begin{aligned} \langle O \rangle_R &= a B O(0) \int_0^1 dx \frac{1}{x^{1+2\epsilon}} + a \int_0^1 dx \frac{R(x)O(x) - BO(0)}{x^{1+2\epsilon}} \\ &= -a \frac{BO(0)}{2\epsilon} + a \int_0^1 dx \frac{R(x)O(x) - BO(0)}{x} \end{aligned}$$

# Jet radiation: MC@NLO

## MC@NLO approach

- one hard jet correctly described by exclusive NLO corrections
- soft and collinear jet radiation for all jets from parton shower

## Bryan Webber's toy model

- finite NLO Monte-Carlo

$$\langle O \rangle = B O(0) + a V O(0) + a \int_0^1 dx \frac{R(x) O(x) - B O(0)}{x}$$

- generating functional with additional photon–emission probability  
 $d\sigma/dx|_{PS} = B aQ(x)/x$

$$\begin{aligned} & \int_0^1 dx \left[ F \left( B + aV - \frac{aB}{x} \right) + F \frac{aR(x)}{x} \right] \\ \rightarrow & \int_0^1 dx \left[ F \left( B + aV - \frac{aB}{x} + \frac{aBQ(x)}{x} \right) + F a \frac{R(x) - BQ(x)}{x} \right] \end{aligned}$$

- now: two subtraction terms, new one not at  $x = 0$  [harder in practice!]
- ⇒ **MC@NLO subtraction scheme with proper non-collinear subtraction term**



# Jet radiation: MC@NLO

## MC@NLO approach

- one hard jet correctly described by exclusive NLO corrections
- soft and collinear jet radiation for all jets from parton shower

## Comments

- + first hard jet correct
- + normalization correct strictly to NLO
- + available from Herwig authors
- additional jets only via parton shower
- subtraction terms not easy or universal
- possible negative weights [why a problem?]

## Jet radiation: CKKW

## CKKW approach

- combine leading-order  $X + j, X + jj, X + jjj, X + jjjj$  matrix elements
- avoid double counting between hard matrix elements
- avoid double counting with parton shower for collinear radiation

## Combining jet-inclusive matrix elements

- for example 2-jet and 3-jet final state  $g \rightarrow q\bar{q}(g)$
- complete splitting probabilities in terms of virtuality

$$\Gamma_q(Q_{\text{out}}, Q_{\text{in}}) \equiv \Gamma_{q \leftarrow q}(Q_{\text{out}}, Q_{\text{in}}) = \frac{2C_F}{\pi} \frac{\alpha_s(Q_{\text{out}})}{Q_{\text{out}}} \left( \log \frac{Q_{\text{in}}}{Q_{\text{out}}} - \frac{3}{4} \right)$$

$$\Gamma_g(Q_{\text{out}}, Q_{\text{in}}) \equiv \Gamma_{g \leftarrow q}(Q_{\text{out}}, Q_{\text{in}}) = \frac{2C_A}{\pi} \frac{\alpha_s(Q_{\text{out}})}{Q_{\text{out}}} \left( \log \frac{Q_{\text{in}}}{Q_{\text{out}}} - \frac{11}{12} \right)$$

$$\Delta_{q,g}(Q_{\text{out}}, Q_{\text{in}}) = \exp \left[ - \int_{Q_{\text{out}}}^{Q_{\text{in}}} dq \Gamma_{q,g}(Q_{\text{out}}, Q_{\text{in}}) \right]$$

- 2 jets only:  $[\Delta_q(Q_1, Q_2)]^2$  [gluon splitting at  $Q_2$ ; parton shower below  $Q_1$ ]
- 3 jets only:  $\Gamma_q(Q_2, Q_q) [\Delta_q(Q_1, Q_2)]^2 \Delta_g(Q_1, Q_g)$  [gluon/quark after splitting:  $Q_{g,q}$ ]
- 4 jets only....

⇒ additional Sudakov factors with simple algebra

## Jet radiation: CKKW

## CKKW approach

- combine leading-order  $X + j, X + jj, X + jjj, X + jjjj$  matrix elements
- avoid double counting between hard matrix elements
- avoid double counting with parton shower for collinear radiation

## Preparing event sample

- (1) compute hard  $n$ -jet samples and cross sections [set of momenta with resolution  $d_{\text{cut}}$ ]
- (2) choose jet multiplicity  $n$  according to

$$p_n = \frac{\sigma_n}{\sum_{k=0} \sigma_k} \quad \text{with} \quad \sigma_k = \sigma_k(d_{\text{cut}})$$

- (3) compute  $|\mathcal{M}|^2$  and virtualities at splitting points [ $k_T$  algorithm]
  - (4) apply Sudakov correction factors to weight, re-weight  $\alpha_s$   
MLM scheme: veto events instead of Sudakovs  
Madevent scheme: test splitting with matrix elements
  - (5) use parton shower for soft/collinear end [independent of matching point!]
  - (6) normalize total rate to highest known order
- ⇒ **CKKW: combine exclusive  $n$ -jet rates with parton shower**

# Jet radiation: CKKW

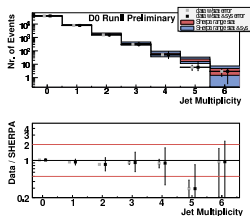
## CKKW approach

- combine leading-order  $X + j$ ,  $X + jj$ ,  $X + jjj$ ,  $X + jjjj$  matrix elements
- avoid double counting between hard matrix elements
- avoid double counting with parton shower for collinear radiation

## Comments

- + all additional jets correct
- + available from Sherpa, MadEvent, Alpgen authors
- normalization of different processes with leading-order error
- over-all normalization unknown

## Sherpa-CKKW and Tevatron data



# QCD Outlook

## LHC physicists need to know QCD [model builders too]

- not all collider events can be analysed: trigger
- perturbative QCD is not perfect, but the best we have
- some processes need to be known precisely: luminosity, backgrounds
- renormalization/factorization scales from higher orders
- collinear jets described by parton shower
- hard jets described by fixed-order matrix elements
- jets properly described: ME-PS matching

⇒ next: what LHC can do with that

## Apologies...

- ...to the people I did not cite, because it is a lecture
- ...to you for not explaining things like parton shower
- ...to those for whom I went to fast
- ...to those I bored to death

**Phenomenology:**  
QCD

**Tilman Plehn**

Collider basics

QCD basics

Collinear jets

QCD scales

Some processes

**Jet radiation**