

Jet Scaling

Tilman Plehn

Exclusive jets

Staircase

Jet veto

New physics

From Jet Scaling to Jet Vetos

Tilman Plehn

Heidelberg

Madgraph Meeting, Rome, 9/2011

Exclusive jet counting

Remember $qg \rightarrow qZ$ [intro: arXiv:0910.4182, Springer Lecture Notes]

- collinear divergence from $g \rightarrow q\bar{q}$ splitting

$$\int_{p_T^{\min}}^{p_T^{\max}} dp_T^2 \frac{C}{p_T^2} = 2 \int_{p_T^{\min}}^{p_T^{\max}} dp_T p_T \frac{C}{p_T^2} \simeq 2C \int_{p_T^{\min}}^{p_T^{\max}} dp_T \frac{1}{p_T} = 2C \log \frac{p_T^{\max}}{p_T^{\min}}$$

universal form following factorization

$$\sigma_{n+1} = \int \sigma_n \frac{dp_a^2}{p_a^2} dz \frac{\alpha_s}{2\pi} \hat{P}(z)$$

- but still divergent, fixed order prediction poorly defined
- **find object to 'renormalize'** [i.e. absorb universal divergence]

DGLAP equation and logarithms

- re-organize perturbation series [sum collinear logs]

$$\sigma_{n+1}(x, \mu) \sim \frac{1}{n!} \left(\frac{1}{2\pi b_0} \log \frac{\alpha_s(\mu_0^2)}{\alpha_s(\mu^2)} \right)^n \int_{x_0}^1 \frac{dx_n}{x_n} \hat{P} \left(\frac{x}{x_n} \right) \cdots \int_{x_0}^1 \frac{dx_1}{x_1} \hat{P} \left(\frac{x_2}{x_1} \right) \sigma_1(x_1, \mu_0)$$

- DGLAP equivalent to infrared RGE
- **collinear jets included, only jet-inclusive observables**

Successive radiation

Soft gluon radiation [Peskin & Schroeder]

- example: photons off hard electron
only abelian diagrams, successive radiation
- eikonal approximation

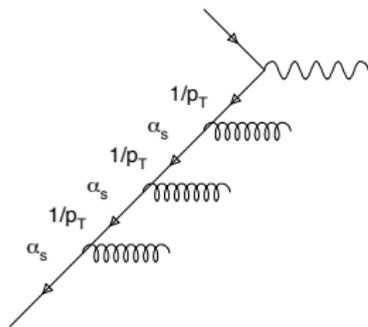
$$\mathcal{M}_{n+1} = g_s T^a \epsilon_{\mu}^*(k) \bar{u}(q) \frac{q^{\mu} + \mathcal{O}(k)}{(qk) + \mathcal{O}(k^2)} \mathcal{M}_n$$

- factorization of ‘hard process’ and soft radiation factors
- **Poisson distribution** [normalized pdf for n if n_0 expected]

$$f(n; n_0) = \frac{n_0^n e^{-n_0}}{n!} \iff \frac{f(n+1; n_0)}{f(n; n_0)} = \frac{n_0}{n+1}$$

Ingredients of Poisson distribution

- 1– radiation matrix element n_0^n :
abelian fine, non-abelian fine for leading log
 - 2– phase space factor $1/n!$:
only combinatorics effect, matrix element ordered
 - 3– normalization factor e^{-n_0} :
nothing to worry about...
- **anyone reminded of ISR parton shower?**



Staircase scaling: W +jets

From UA2 to ATLAS [Steve Ellis, Kleiss, Stirling]

Volume 154B, number 5,6

PHYSICS LETTERS

9 May 1985

W's, Z's AND JETS

S.D. ELLIS^{1,2}, R. KLEISS and W.J. STIRLING

CERN, CH 1211 Geneva 23, Switzerland

Received 24 January 1985

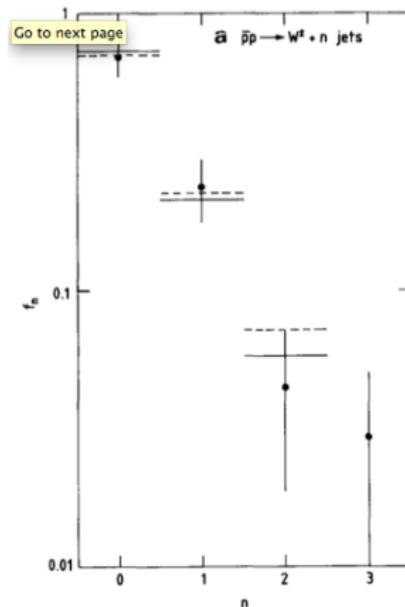
The process $p + \bar{p} \rightarrow W^\pm, Z^0$ plus 2 jets is discussed in the context of perturbative QCD. The magnitude of the expected rate for this process and the correlations anticipated between the jets are presented.

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From UA2 to ATLAS [Steve Ellis, Kleiss, Stirling]

- exclusive staircase scaling [Berends scaling???
- many equivalent descriptions

$$R_{(n+1)/n} = \frac{\sigma_{n+1}}{\sigma_n} = \text{const}$$



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- same for inclusive and exclusive rates

$$R_{(n+1)/n}^{\text{incl}} = \frac{\sum_{j=n+1}^{\infty} \sigma_j^{(\text{excl})}}{\sigma_n^{(\text{excl})} + \sum_{j=n+1}^{\infty} \sigma_j^{(\text{excl})}} = R_{(n+1)/n}^{\text{excl}}$$

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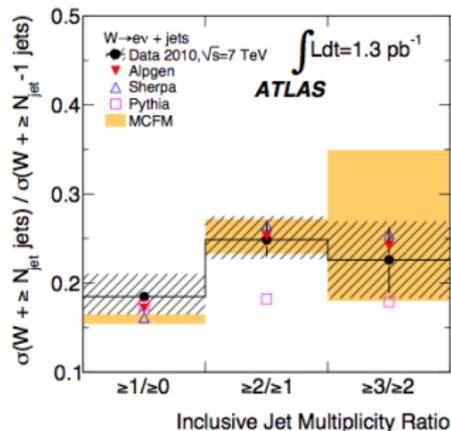
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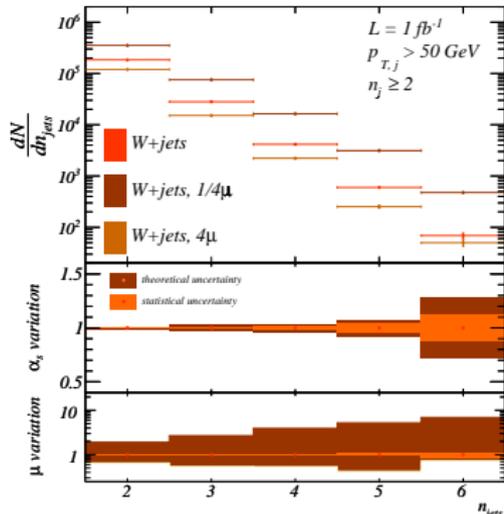
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Simulations with uncertainties [Englert, TP, Schichtel, Schu]

- appropriate tool: CKKW/MLM [Sherpa]
- phase space effects? \rightarrow moderate
- α_s uncertainties? \rightarrow small
- scale uncertainties? \rightarrow tuning parameter?
- **correctly described by ME-PS merging**



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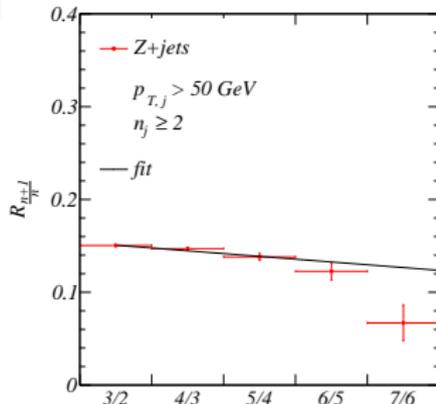
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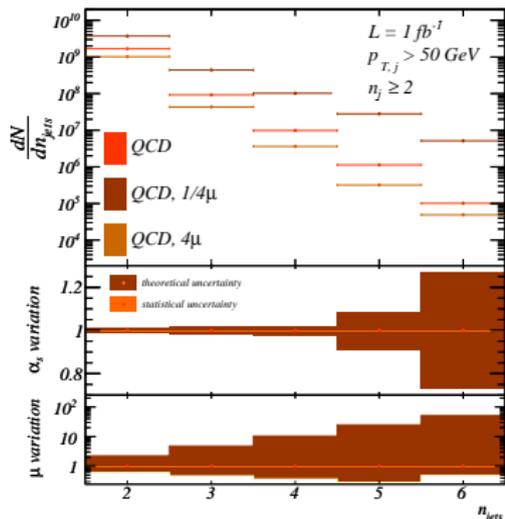
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Staircase scaling: QCD jets

Democratic cuts

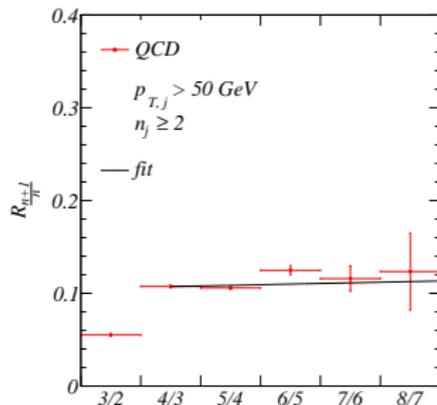
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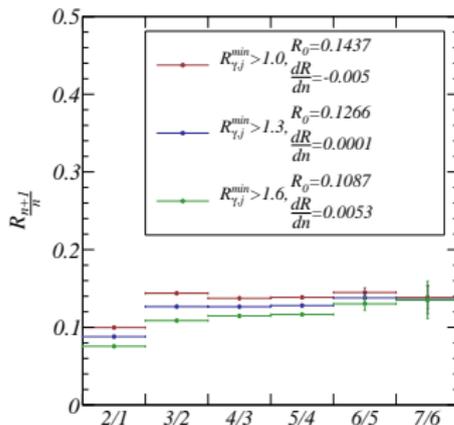
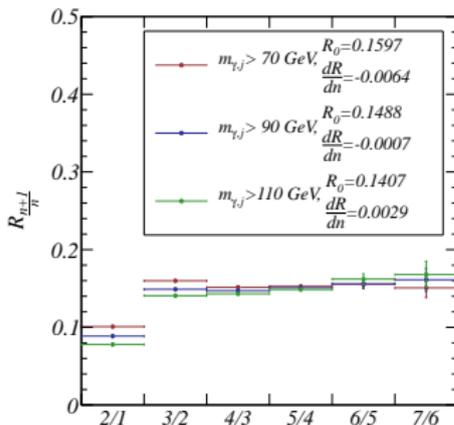
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Staircase scaling: Photon plus jets

Ensure scaling properties [Englert, TP, Schichtel, Schumann]

- naively, no scaling observed [CMS, private complaint]
- remove any logarithmic enhancement
high separation requirement [compare m and ΔR]
democratic γ and jet acceptance
- no phase space effects
- dominant diagram: FSR gluon splitting of single ISR jet



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- **best process to test scaling**

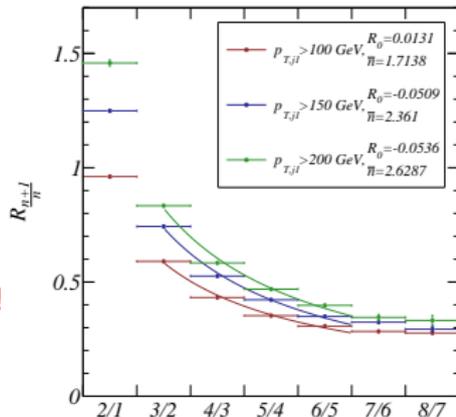
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What about Poisson scaling?

- generate a ‘hard process’
many options: $m, p_T, \Delta R, \dots$
- turns out $p_{T,j_1} > 100$ GeV works best
lower standard p_T enhances logarithm
- high- n tail always staircase
- dominant diagram: successive ordered ISR
- **scaling either staircase or Poisson and tunable!**



Jet veto in Higgs searches

Jet veto as Higgs analysis tool [Barger, Phillips, Zeppenfeld; Rainwater]

- particularly useful for WBF signals
- remove $t\bar{t}$ and Z +jets backgrounds
- count central (semi-hard) jets
apply survival probability

Table C.1: Summary of veto survival probabilities for $p_T^{\text{veto}} = 20$ GeV used in Chapters 3-5.

search	Hjj	$t\bar{t}$	$t\bar{t}j$, $t\bar{t}jj$	QCD $V(V)jj$	EW $V(V)jj$	QCD $Wjjj$	QCD $b\bar{b}jj$	DPS $\gamma\gamma jj$
$\gamma\gamma jj$	0.89	-	-	0.30	0.75	-	-	0.30
$W^{(*)}W^{(*)}jj$	0.89	0.46	0.29	0.29	0.75	-	-	-
$\tau\tau jj$	0.87	-	-	0.28	0.80	0.28	0.28	-

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individual searches for exclusive fixed n_{jets}
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In terms of jet counting [Gerwick, TP, Schumann]

- avoid survival probability as one number
- study exclusive n_{jets} distribution:
 - 1– predict from theory including error
 - 2– validate by experiments
 - 3– extrapolate to interesting regimes
- understand basic features:
 - staircase scaling for inclusive samples
 - Poisson scaling for hard processes

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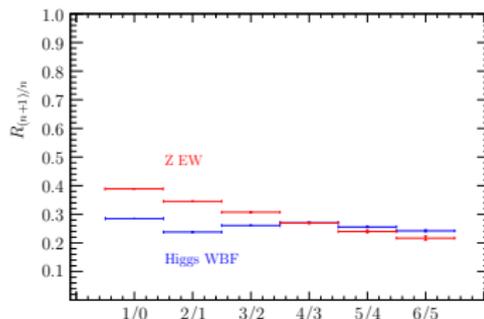
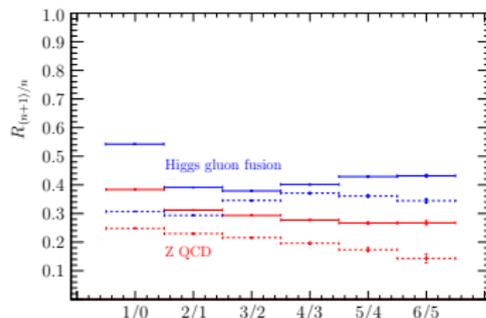
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	staircase scaling	Poisson scaling
σ_n	$\sigma_0 e^{-bn}$	$\sigma_{\text{tot}} \frac{e^{-\bar{n}} \bar{n}^n}{n!}$
$R_{(n+1)/n}^{\text{excl}}$	e^{-b}	$\frac{\bar{n}}{n+1}$
$R_{(n+1)/n}^{\text{incl}}$	e^{-b}	$\left(\frac{(n+1) e^{-\bar{n}} \bar{n}^{-(n+1)}}{\Gamma(n+1) - n\Gamma(n, \bar{n})} + 1 \right)^{-1}$
$\langle n_{\text{jets}} \rangle$	$\frac{1}{2 \cosh b - 1}$	\bar{n}
P_{veto}	$1 - e^{-b}$	$e^{-\bar{n}}$

Jet veto in Higgs searches

Staircase scaling [Gerwick, TP, Schumann]

- example: WBF $H \rightarrow \tau\tau$ [plus GF Hjj and Zjj]
- jet scaling before WBF cuts
staircase, as expected [QCD and e-w processes]
- first emission sensitive to cuts
- e-w Zjj production with too many structures



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Poisson scaling

- apply WBF jet cuts [tagging jets]

$$p_{T,j} > 20 \text{ GeV} \quad |y_j| < 4.5$$

$$y_1 y_2 < 0 \quad |y_1 - y_2| > 4.4 \quad m_{jj} > 600 \text{ GeV}$$
- count add'l jets with: $p_T^{\text{veto}} > 20 \text{ GeV}$, $\min y_{1,2} < y^{\text{veto}} < \max y_{1,2}$
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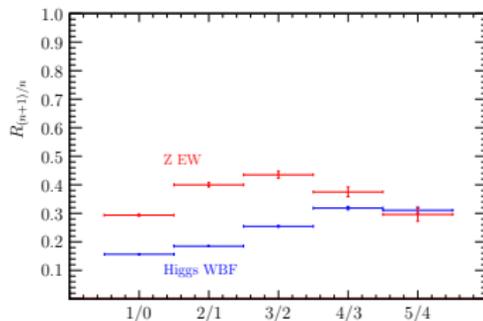
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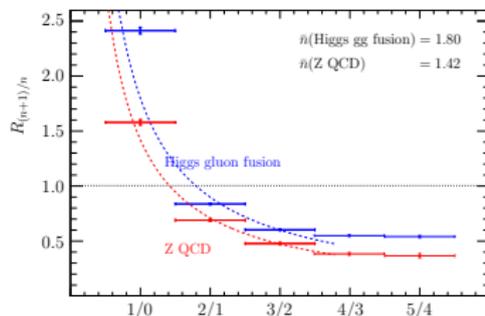
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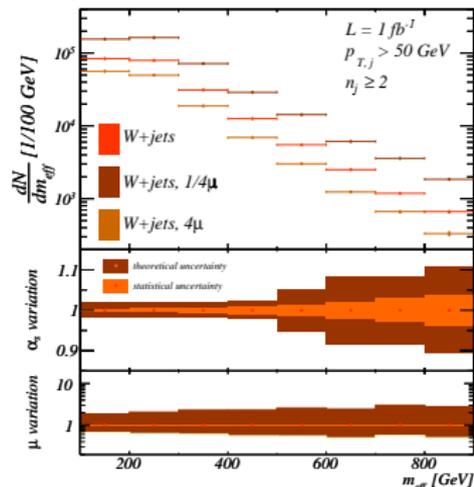
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- kind-of-staircase for e-w processes
- Poisson for QCD processes
- veto on first jet very efficient against QCD
- inclusive n_{jets} distribution key to predictions
- **try it and tell us if we are wrong...**

New physics

Effective mass [Englert, TP, Schichtel, Schumann]

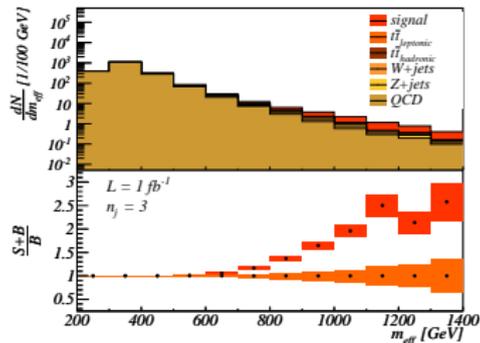
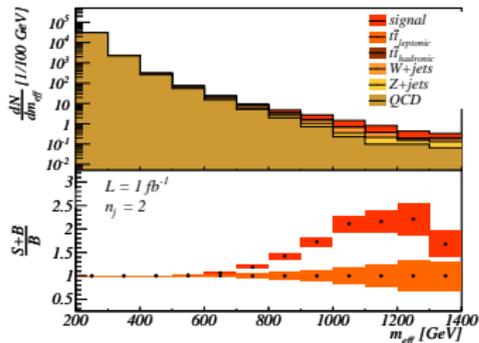
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- correlation $m_{\text{eff}} \sim \langle p_T \rangle \times n_{\text{jets}}$
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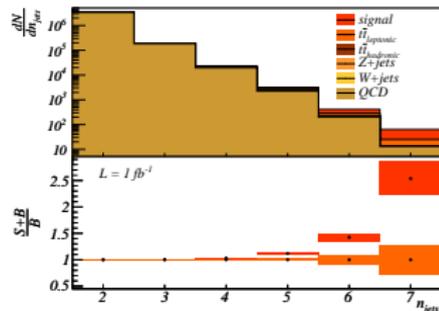
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Mass vs color charge

- now, significance as function of n_{jets}



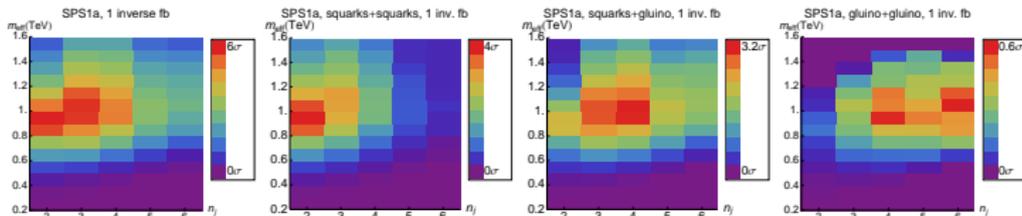
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Mass vs color charge

- now, significance as function of n_{jets}
- representing new physics color charge gluino does not decay via gluon
- compute exclusive 2D likelihood



Understanding many jets

Exclusive jet counting

- either staircase (non-abelian) or Poisson (ordered)
- do not call it Berends scaling [Ellis, Kleiss, Stirling]

- described by ME-PS merging [Sherpa]
- nothing changing with NLO [Blackhat]

- both regimes fully testable at LHC
- photon+jets best laboratory
- key to jet vetos
- key to SUSY signal and backgrounds

New physics at the LHC

	missing energy (p.89)	cascade decays (p.91)	mono-jets/photon (p.15)	lepton resnce (p.109)	di-jet resnce (p.109)	top resnce (p.120)	WW/ZZ resnce (p.15)	W' resnce (p.93)	top partner (p.116)	charged tracks (p.123)	displ. vertex (p.123)	multi-photons (p.29)	spherical events (p.47,76)
SUSY (heavy grav.) (p.17,26)	✓✓	✓✓							✓				
SUSY (light grav.) (p.17,27)	✓	✓	✓						✓	✓	✓		
large extra dim (p.39)	✓✓		✓✓										✓
universal extra dim (p.47)	✓✓	✓✓		✓	✓	✓	✓	✓	✓				
technicolor (vanilla) (p.51)				✓	✓	✓	✓	✓✓					
topcolor/top seesaw (p.53,54)					✓	✓✓	✓						
little Higgs (w/o T) (p.55,58)				✓	✓	✓	✓	✓					
little Higgs (w T) (p.55,58)	✓✓	✓✓	✓	✓	✓	✓	✓	✓	✓				
warped extra dim (IR SM) (p.61,63)				✓	✓	✓	✓						
warped extra dim (bulk SM) (p.61,64)				✓	✓	✓✓	✓	✓					
Higgsless/comp. Higgs (p.69,73)				✓	✓	✓✓	✓✓						
hidden valleys (p.75)	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓