

LHC Theory

Tilman Plehn

LHC

Higgs boson

Higgs couplings

Effective theory

Higgs portal

Dark matter

Theory with and for the LHC

Tilman Plehn

Universität Heidelberg

Freiburg, 5/2017

The LHC

LHC

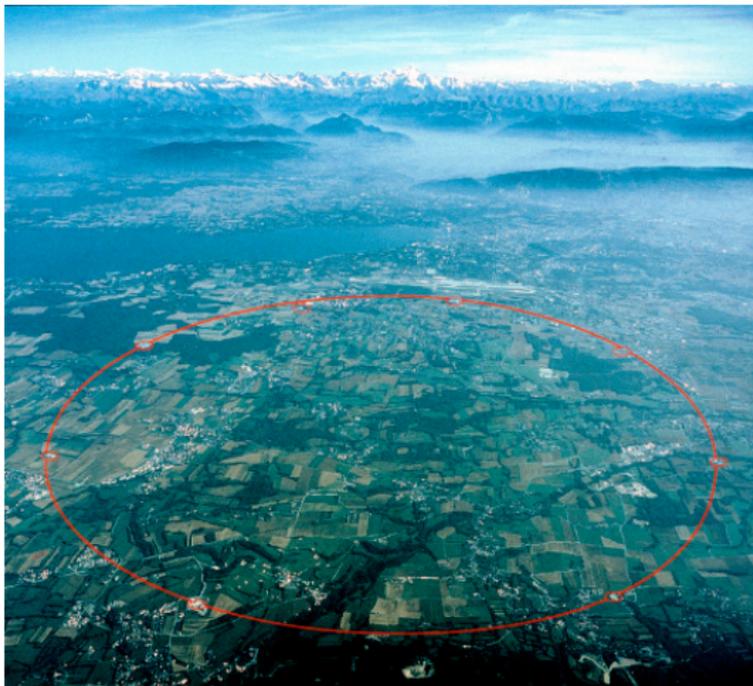
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The LHC

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The LHC

Einstein: beam energy to particle mass $E = mc^2$

- smash 6.5 TeV protons onto 6.5 TeV protons [energy unit GeV: proton mass]
produce anything that interacts with quarks and gluons
search for it in decay products
- huge detectors, actual data → **experiment**
quantum field theory, strong opinions → **theory**



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life as an experimentalist



life as a theorist



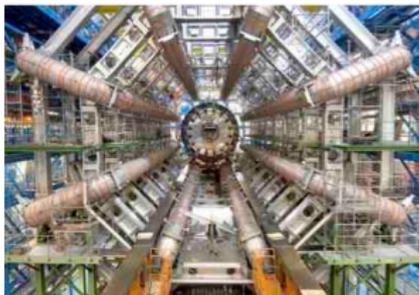
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life as a theorist



The LHC

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- huge detectors, actual data → **experiment** quantum field theory, strong opinions → **theory**
- language: **Lagrangian**



Quantity	Symbol, equation	Value	Uncertainty (ppb)
speed of light in vacuum	c	1	exact
Planck constant	h	1	exact
Planck constant, reduced	$\hbar = h/2\pi$	1	exact
electron charge magnitude	e	1	exact
conversion constant	hc	1	exact
conversion constant	$(hc)^2$	1	exact
electron mass	m_e	1	exact
proton mass	m_p	1	exact
deuteron mass	m_d	1	exact
unified atomic mass unit	$(\text{mass } ^{12}\text{C atom})/12 = (1 \text{ g})/(N_A \text{ mol})$	1	exact
permeability of free space	$\epsilon_0 = 1/\mu_0 c^2$	1	exact
permeability of free space	μ_0	1	exact
fine-structure constant	$\alpha = e^2/4\pi\epsilon_0\hbar c$	1	exact
classical electron radius	$r_e = e^2/4\pi\epsilon_0 m_e c$	1	exact
$(e^- \text{ Compton wavelength})/2\pi$	$\lambda_c/2\pi = \hbar/m_e c = r_e \alpha^{-1}$	1	exact
Bohr radius ($m_{\text{nucleus}} = \infty$)	$a_\infty = 4\pi\epsilon_0 \hbar^2 / m_e e^2 = r_e \alpha^{-2}$	1	exact
wavelength of 1 eV/c particle	$hc/(1 \text{ eV})$	1	exact
Rydberg energy	$hcR_\infty = m_e c^4 / 2(4\pi\epsilon_0)^2 \hbar^2 = m_e c^2 \alpha^2 / 2$	1	exact
Thomson cross section	$\sigma_T = 8\pi r_e^2 / 3$	1	exact
Bohr magneton	$\mu_B = eh/2m_e$	1	exact
nuclear magneton	$\mu_N = eh/2m_p$	1	exact
electron cyclotron freq./field	$\omega_{\text{cycl}}^e/B = e/m_e$	1	exact
proton cyclotron freq./field	$\omega_{\text{cycl}}^p/B = e/m_p$	1	exact
gravitational constant	G_N	1	exact
standard gravitational accel.	g_n	1	exact
Avogadro constant	N_A	1	exact
Boltzmann constant	k	1	exact
molar volume, ideal gas at STP	$N_A k (273.15 \text{ K}) / (101325 \text{ Pa})$	1	exact
Wien displacement law constant	$b = \lambda_{\text{max}} T$	1	exact
Stefan-Boltzmann constant	$\sigma = \pi^2 k^4 / 60\hbar^3 c^2$	1	exact
Fermi coupling constant	$G_F / (\hbar c)^3$	1	exact

Higgs mechanism

Quantum theory with famous problem

– Lagrangian

(quantum) electrodynamics $[F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu]$

$$\mathcal{L} = \underbrace{i \bar{\psi} \gamma_\mu \partial^\mu \psi - \frac{1}{4} F_{\mu\nu} F^{\mu\nu}}_{\text{kinetic terms}} - \underbrace{m \bar{\psi} \psi}_{\text{electron mass}} - \underbrace{e \bar{\psi} \gamma_\mu A^\mu \psi}_{e\bar{e}\gamma \text{ interaction}}$$

symmetries of Lagrangian = symmetries of theory



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symmetries of Lagrangian = symmetries of theory

- **exact and broken symmetries**

massless exchange particle: Coulomb potential $V(r) \propto -1/r$

massive exchange particle: Yukawa potential $V(r) \propto -e^{-mr}/r$

what happens for $m \rightarrow 0$?

- problem 1: **massive gauge theories**

massless gauge bosons have 2 polarizations, massive have 3, and $3 \neq 2$

- problem 2: **Goldstone's theorem**

breaking $SU(2)$ produces 3 massless unobserved scalars



Higgs boson

Solving that problem [also Brout & Englert; Guralnik, Hagen, Kibble]

1964 combining two problems to one predictive solution [Stueckelberg mass]

$$\mathcal{L} = - \underbrace{\frac{1}{4} F_{\mu\nu} F^{\mu\nu}}_{\text{massless photon}} + \underbrace{\frac{1}{2} (\partial_\mu \phi)^2}_{\text{massless scalar}} + \frac{f^2}{2} A_\mu^2 - f A_\mu \partial^\mu \phi = - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \underbrace{\frac{f^2}{2} \left(A_\mu - \frac{1}{f} \partial_\mu \phi \right)^2}_{\text{photon mass}}$$

similar for W^\pm and Z masses, structurally only complex 2-vector possible

⇒ **remaining scalar: Higgs boson**

VOLUME 13, NUMBER 16

PHYSICAL REVIEW LETTERS

19 OCTOBER 1964

BROKEN SYMMETRIES AND THE MASSES OF GAUGE BOSONS

Peter W. Higgs

Tait Institute of Mathematical Physics, University of Edinburgh, Edinburgh, Scotland

(Received 31 August 1964)

In a recent note¹ it was shown that the Goldstone theorem,² that Lorentz-covariant field theories in which spontaneous breakdown of symmetry under an internal Lie group occurs contain zero-mass particles, fails if and only if

about the "vacuum" solution $\varphi_1(x) = 0$, $\varphi_2(x) = \varphi_0$:

$$\partial^\mu \{ \partial_\mu (\Delta \varphi_1) - e \varphi_0 A_\mu \} = 0, \quad (2a)$$

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A detailed discussion of these questions will be presented elsewhere.

It is worth noting that an essential feature of the type of theory which has been described in this note is the prediction of incomplete multiplets of scalar and vector bosons.⁸ It is to be expected that this feature will appear also in theories in which the symmetry-breaking scalar fields are not elementary dynamic variables but bilinear combinations of Fermi fields.⁹

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¹P. W. Higgs, to be published.²J. Goldstone, *Nuovo Cimento* **19**, 154 (1961);J. Goldstone, A. Salam, and S. Weinberg, *Phys. Rev.* **127**, 965 (1962).

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similar for W^\pm and Z masses, structurally only complex 2-vector possible \Rightarrow remaining scalar: Higgs boson

1966 original Higgs phenomenology

Spontaneous Symmetry Breakdown without Massless Bosons*

PETER W. HIGGS†

Department of Physics, University of North Carolina, Chapel Hill, North Carolina

(Received 27 December 1965)

We examine a simple relativistic theory of two scalar fields, first discussed by Goldstone, in which as a result of spontaneous breakdown of $U(1)$ symmetry one of the scalar bosons is massless, in conformity with the Goldstone theorem. When the symmetry group of the Lagrangian is extended from global to local $U(1)$ transformations by the introduction of coupling with a vector gauge field, the Goldstone boson becomes the longitudinal state of a massive vector boson whose transverse states are the quanta of the transverse gauge field. A perturbative treatment of the model is developed in which the major features of these phenomena are present in zero order. Transition amplitudes for decay and scattering processes are evaluated in lowest order, and it is shown that they may be obtained more directly from an equivalent Lagrangian in which the original symmetry is no longer manifest. When the system is coupled to other systems in a $U(1)$ invariant Lagrangian, the other systems display an induced symmetry breakdown, associated with a partially conserved current which interacts with itself via the massive vector boson.

I. INTRODUCTION

THE idea that the apparently approximate nature of the internal symmetries of elementary-particle physics is the result of asymmetries in the stable solutions of exactly symmetric dynamical equations, rather than an indication of asymmetry in the dynamical

appear have been used by Coleman and Glashow³ to account for the observed pattern of deviations from $SU(3)$ symmetry.

The study of field theoretical models which display spontaneous breakdown of symmetry under an internal Lie group was initiated by Nambu,⁴ who had noticed⁵

Higgs boson

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PHYSICAL REVIEW

VOLUME 145, NUMBER 4

27 MAY 1966

Spontaneous Symmetry Breakdown without Massless Bosons*

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Department of Physics, University of North Carolina, Chapel Hill, North Carolina

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II. THE MODEL

The Lagrangian density from which we shall work is given by²⁹

$$\mathcal{L} = -\frac{1}{2} g^{\mu\nu} g^{\lambda\rho} F_{\alpha\lambda} F_{\mu\rho} - \frac{1}{2} g^{\mu\nu} \nabla_\mu \Phi_\alpha \nabla_\nu \Phi_\alpha + \frac{1}{2} m_0^2 \Phi_\alpha \Phi_\alpha - \frac{1}{8} f^2 (\Phi_\alpha \Phi_\alpha)^2. \quad (1)$$

In Eq. (1) the metric tensor $g^{\mu\nu} = -1$ ($\mu = \nu = 0$), $+1$ ($\mu = \nu \neq 0$) or 0 ($\mu \neq \nu$), Greek indices run from 0 to 3 and Latin indices from 1 to 2. The $U(1)$ -covariant derivatives $F_{\mu\nu}$ and $\nabla_\mu \Phi_\alpha$ are given by

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu,$$

of two scalar fields, first discussed by Goldstone, in which a symmetry one of the scalar bosons is massless, in conformity with the $U(1)$ symmetry group of the Lagrangian is extended from global to local $U(1)$ by coupling with a vector gauge field, the Goldstone boson becomes the photon. The transverse states are the quanta of the transverse gauge field. The theory is developed in which the major features of these phenomena are the decay and scattering processes are evaluated in lowest order, more directly from an equivalent Lagrangian in which the original system is coupled to other systems in a $U(1)$ invariant Lagrangian. Spontaneous symmetry breakdown, associated with a partially conserved massive vector boson.

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i. Decay of a Scalar Boson into Two Vector Bosons

The process occurs in first order (four of the five cubic vertices contribute), provided that $m_0 > 2m_1$. Let p be the incoming and k_1, k_2 the outgoing momenta. Then

$$M = i \{ e [a^{*\mu}(k_1) (-ik_{2\mu}) \phi^*(k_2) + a^{*\mu}(k_2) (-ik_{1\mu}) \phi^*(k_1)] - e (i p_\mu) [a^{*\mu}(k_1) \phi^*(k_2) + a^{*\mu}(k_2) \phi^*(k_1)] - 2em_1 a_\mu^*(k_1) a^{*\mu}(k_2) - fm_0 \phi^*(k_1) \phi^*(k_2) \}.$$

By using Eq. (15), conservation of momentum, and the transversality ($k_\mu b^\mu(k) = 0$) of the vector wave functions we reduce this to the form

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1976 Higgs physics for colliders

A PHENOMENOLOGICAL PROFILE OF THE HIGGS BOSON

John ELLIS, Mary K. GAILLARD * and D.V. NANOPOULOS **
CERN, Geneva

Received 7 November 1975

A discussion is given of the production, decay and observability of the scalar Higgs boson H expected in gauge theories of the weak and electromagnetic interactions such as the Weinberg-Salam model. After reviewing previous experimental limits on the mass of the Higgs boson, we give a speculative cosmological argument for a small mass. If its mass is similar to that of the pion, the Higgs boson may be visible in the reactions $\pi^- p \rightarrow Hn$ or $\gamma p \rightarrow Hp$ near threshold. If its mass is $\lesssim 300$ MeV, the Higgs boson may be present in the decays of kaons with a branching ratio $O(10^{-7})$, or in the decays of one of the new particles: $3.7 \rightarrow 3.1 + H$ with a branching ratio $O(10^{-4})$. If its mass is ≤ 4 GeV, the Higgs boson may be visible in the reaction $pp \rightarrow H + X$, $H \rightarrow \mu^+ \mu^-$. If the Higgs boson has a mass $\leq 2m_\mu$, the decays $H \rightarrow e^+ e^-$ and $H \rightarrow \gamma\gamma$ dominate, and the lifetime is $O(6 \times 10^{-4}$ to $2 \times 10^{-12})$ seconds. As thresholds for heavier particles (pions, strange particles, new particles) are crossed, decays into them become dominant, and the lifetime decreases rapidly

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A PHENOMENOLOGICAL PROBLEM OF THE HIGGS BOSON

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J. Ellis et al. / Higgs boson

We should perhaps finish with an apology and a caution. We apologize to experimentalists for having no idea what is the mass of the Higgs boson, unlike the case with charm [3,4] and for not being sure of its couplings to other particles, except that they are probably all very small. For these reasons we do not want to encourage big experimental searches for the Higgs boson, but we do feel that people performing experiments vulnerable to the Higgs boson should know how it may turn up.

the Higgs boson, we give a speculative cosmological argument for a small mass. If its mass is similar to that of the pion, the Higgs boson may be visible in the reactions $\pi^- p \rightarrow H n$ or $\gamma p \rightarrow H p$ near threshold. If its mass is $\lesssim 300$ MeV, the Higgs boson may be present in the decays of kaons with a branching ratio $O(10^{-7})$, or in the decays of one of the new particles: $3.7 \rightarrow 3.1 + H$ with a branching ratio $O(10^{-4})$. If its mass is < 4 GeV, the Higgs boson may be visible in the reaction $pp \rightarrow H + X$, $H \rightarrow \mu^+ \mu^-$. If the Higgs boson has a mass $< 2m_\mu$, the decays $H \rightarrow e^+ e^-$ and $H \rightarrow \gamma\gamma$ dominate, and the lifetime is $O(6 \times 10^{-12})$ to 2×10^{-12} seconds. As thresholds for heavier particles (pions, strange particles, new particles) are crossed, decays into them become dominant, and the lifetime decreases rapidly

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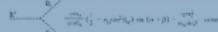
2012 Higgs discovery [ask KarlJ, Schumi]

since really just Standard Model?



FRONTIERS IN PHYSICS

THE HIGGS HUNTER'S GUIDE



LBP

John F. Gunion
Howard E. Haber
Gordon Kane
Sally Dawson

Electroweak Standard Model

Boson and fermion masses

- fundamental symmetry: $SU(2)_L \times U(1)_Y$
observed unbroken: electromagnetism $U(1)_Q$
 - forbidden by $SU(2)_L$: $m_{W,Z}$ and $m_{t,b,\tau}$
- ⇒ masses proportional to **Higgs VEV** $\langle \phi \rangle = 246 \text{ GeV}$

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- ⇒ masses proportional to **Higgs VEV** $\langle \phi \rangle = 246 \text{ GeV}$
- complex $SU(2)$ doublet ϕ
- 3 Goldstone modes 'eaten' by W and Z
- 4th mode $\phi = \langle \phi \rangle + H$
- ⇒ **Higgs particle** coupling proportional to mass



A MODEL OF LEPTONS*

Steven Weinberg†

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Massachusetts Institute of Technology, Cambridge, Ma
(Received 17 October 1967)

Leptons interact only with photons, and with the intermediate bosons that presumably mediate weak interactions. What could be more natural than to unite¹ these spin-one bosons into a multiplet of gauge fields? Standing in the way of this synthesis are the obvious differences in the masses of the photon and intermediate meson, and in their couplings. We might hope to understand these differences by imagining that the symmetries relating the weak and electromagnetic interactions are exact symmetries of the Lagrangian but are broken by the vacuum. However, this raises the specter of unwanted massless Goldstone bosons.² This note will describe a model in which the symmetry between the electromagnetic and weak interactions is spontaneously broken, but in which the Goldstone bosons are avoided by introducing the photon and the intermediate-boson fields as gauge fields.³ The model may be renormalizable.

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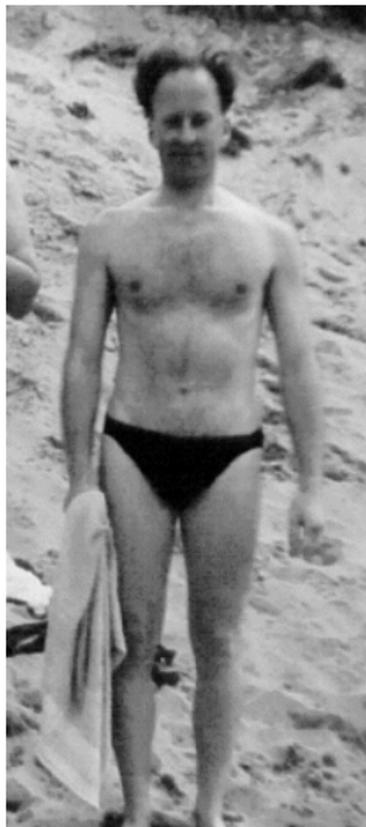
Higgs potential

- Standard Model

$$V = \mu^2 |\phi|^2 + \lambda |\phi|^4 \quad m_H^2 = \left. \frac{\partial^2 V}{\partial H^2} \right|_{\text{minimum}}$$

- ⇒ **why not more terms?**

$$V = \mu^2 |\phi|^2 + \lambda_4 |\phi|^4 + \frac{\lambda_6}{M^2} |\phi|^6 + \dots$$



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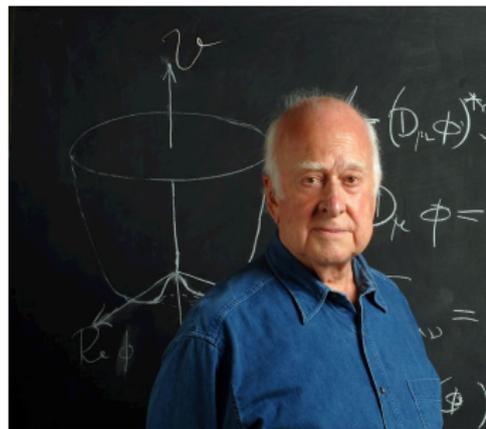
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$$V = \mu^2 |\phi|^2 + \lambda_4 |\phi|^4 + \frac{\lambda_6}{M^2} |\phi|^6 + \dots$$



Unitarity [Lee, Quigg, Thacker]

- predicted transition amplitudes finite for all Higgs masses

$$\sigma_{WW \rightarrow WW} \sim \frac{m_H^2}{v^2} \Rightarrow m_H \lesssim 1 \text{ TeV}$$

⇒ Higgs couplings unitary?



PHYSICAL REVIEW D

VOLUME 16, NUMBER 5

1 SEPTEMBER 1977

Weak interactions at very high energies: The role of the Higgs-boson mass

Benjamin W. Lee,* C. Quigg,¹ and H. B. Thacker

Fermi National Accelerator Laboratory,² Batavia, Illinois 60510

(Received 20 April 1977)

We give an S -matrix-theoretic demonstration that if the Higgs-boson mass exceeds $M_c = (8\pi\sqrt{2/3}G_F)^{1/2}$, partial-wave unitarity is not respected by the tree diagrams for two-body scattering of gauge bosons, and the weak interactions must become strong at high energies. We exhibit the relation of this bound to the structure of the Higgs-Goldstone Lagrangian, and speculate on the consequences of strongly coupled Higgs-Goldstone systems. Prospects for the observation of massive Higgs scalars are noted.

Modern language

Unitarity [Lee, Quigg, Thacker]

- predicted transition amplitudes finite for all Higgs masses

$$\sigma_{WW \rightarrow WW} \sim \frac{m_H^2}{v^2} \quad \Rightarrow \quad m_H \lesssim 1 \text{ TeV}$$

⇒ **Higgs couplings unitary?**

Renormalizability [t Hooft & Veltman, ask StefanD]

- absence of UV cutoff scale defining ‘fundamental theory’
- couplings with inverse mass dimension problematic

$$\mathcal{L} \sim \frac{1}{M^2} \partial_\mu (\phi^\dagger \phi) \partial^\mu (\phi^\dagger \phi) \quad \Rightarrow \quad g_{HHH} \propto \frac{p^2 v}{M^2}$$

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RENORMALIZABLE LAGRANGIANS FOR MASSIVE YANG-MILLS FIELDS

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G. 't HOOFT

Institute for Theoretical Physics, University of Utrecht

Received 13 July 1971

Abstract: Renormalizable models are constructed in which local gauge invariance is broken spontaneously. Feynman rules and Ward identities can be found by means of a path integral method, and they can be checked by algebra. In one of these models, which is studied in more detail, local SU(2) is broken in such a way that local U(1) remains as a symmetry. A renormalizable and unitary theory results, with photons, charged massive vector particles, and additional neutral scalar particles. It has three independent parameters.

Another model has local SU(2) ⊗ U(1) as a symmetry and may serve as a renormalizable theory for ρ-mesons and photons.

In such models electromagnetic mass-differences are finite and can be calculated in perturbation theory.

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In such models electromagnetic mass-differences are finite and calculable in perturbation theory.

REGULARIZATION AND RENORMALIZATION OF GAUGE FIELDS

G. 't HOOFT and M. VELTMAN

Institute for Theoretical Physics, University of Utrecht

Received 21 February 1972

Abstract: A new regularization and renormalization procedure is presented. It is particularly well suited for the treatment of gauge theories. The method works for theories that were known to be renormalizable as well as for Yang-Mills type theories. Overlapping divergences are disentangled. The procedure respects unitarity, causality and allows shifts of integration variables. In non-anomalous cases also Ward identities are satisfied at all stages. It is transparent when anomalies, such as the Bell-Jackiw-Adler anomaly, may occur.

1. INTRODUCTION

Recently it has been shown [1] that it is possible to formulate renormalizable theories of charged massive vector bosons. The derived Feynman rules involve ghost particles, and in order to establish unitarity and causality of the S-matrix Ward identities are needed. The necessary combinatorial techniques were given in ref. [2], in the treatment of massless Yang-Mills fields. It was emphasized that these same techniques work also in the case of massive vector boson theories obtained from the massless theory by means of the Higgs-Kibble [3] mechanism. Stated somewhat dis-

Modern language

LHC

Higgs boson

Higgs couplings

Effective theory

Higgs portal

Dark matter

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⇒ **Higgs sector renormalizable?**

Weakly or strongly interacting Higgs? [Weinberg; Georgi, Kaplan (Dimopoulos)]

- same as: fundamental or composite scalar?
- unitarity ensured by composite Higgs sector
- renormalizability not required with composite Higgs sector

⇒ **Higgs scalar fundamental?**

Modern language

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A detailed discussion of these questions will be presented elsewhere.

It is worth noting that an essential feature of the type of theory which has been described in this note is the prediction of incomplete multiplets of scalar and vector bosons.⁹ It is to be expected that this feature will appear also in theories in which the symmetry-breaking scalar fields are not elementary dynamic variables but bilinear combinations of Fermi fields.⁹

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1. Introduction. The recent discovery of the W and Z bosons confirm the belief that a spontaneously broken $SU(2) \times U(1)$ gauge group correctly describes the electroweak interactions. But how is $SU(2) \times U(1)$ broken? Nobody knows. In the standard model, the scalar Higgs doublet acquires a VEV, and the spectrum includes heavy gauge bosons and the massive, neutral uneaten scalar. Hypercolor models offer an alternative scenario for breaking $SU(2) \times U(1)$: strongly interacting hyperquarks form a condensate which transforms nontrivially under $SU(2) \times U(1)$ [1]. In

Higgs couplings

Standard-Model with free Higgs couplings [Dührssen]

- assume: Higgs-like scalar
Higgs couplings proportional to masses?
- couplings from production & decay combinations
- Higgs Lagrangian

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \Delta_W g m_W H W^\mu W_\mu + \Delta_Z \frac{g}{2c_W} m_Z H Z^\mu Z_\mu - \sum_{\tau, b, t} \Delta_f \frac{m_f}{v} H (\bar{f}_R f_L + \text{h.c.})$$

$$+ \Delta_g F_G \frac{H}{v} G_{\mu\nu} G^{\mu\nu} + \Delta_\gamma F_A \frac{H}{v} A_{\mu\nu} A^{\mu\nu} + \text{invisible} + \text{unobservable}$$

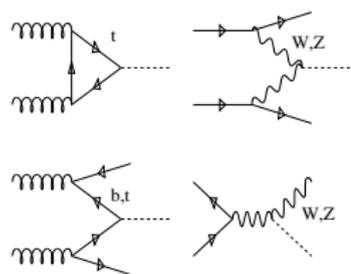
$gg \rightarrow H$
 $gg \rightarrow H_j$ (boosted)
 $gg \rightarrow H^*$ (off-shell)
 $qq \rightarrow qqH$
 $gg \rightarrow t\bar{t}H$
 $qq' \rightarrow VH$

↔

$$g_{HXX} = g_{HXX}^{\text{SM}} (1 + \Delta_X)$$

↔

$H \rightarrow ZZ$
 $H \rightarrow WW$
 $H \rightarrow b\bar{b}$
 $H \rightarrow \tau^+ \tau^-$
 $H \rightarrow \gamma\gamma$
 $H \rightarrow \text{invisible}$



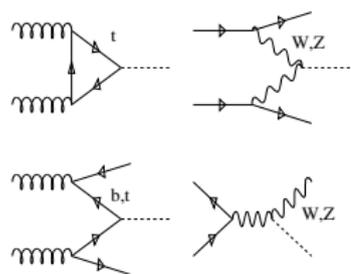
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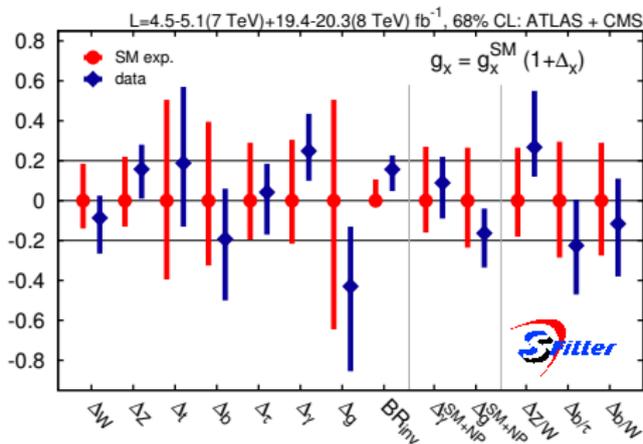
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Exactly the 1964 prediction? [Butter, Corbett, Eboli, Goncalves, Gonzalez-Fraile, TP, Rauch, Zerwas]



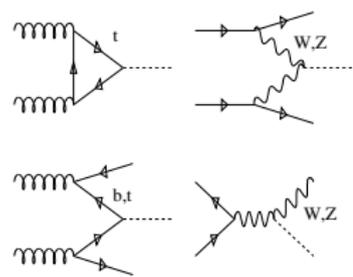
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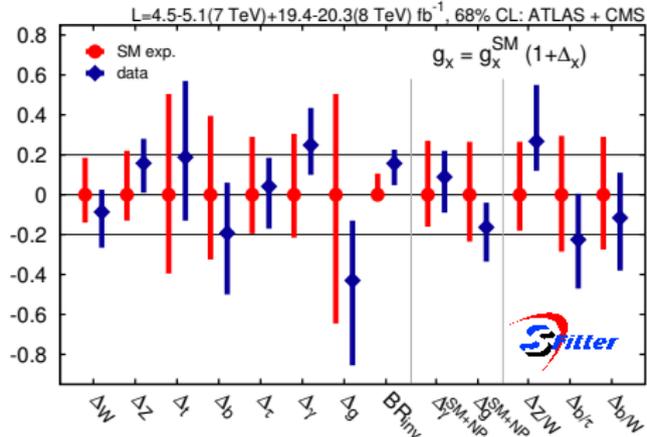
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Exactly the 1964 prediction? [Butter, Corbett, Eboli, Goncalves, Gonzalez-Fraile, TP, Rauch, Zerwas]

- renormalizability broken
 - unitarity broken
 - total rates only
 - no link to Goldstone bosons
 - nothing about mass scales
- ⇒ better framework?



Higgs-gauge effective theory

Back to original Higgs language: effective theory [with Higgs doublet or not?]

- resolved mass scale $m_H \approx 126$ GeV
new physics mass scale $M \gg m_H$
- Lagrangian from particle content and symmetries, but with $1/\text{cutoff}^2$

$$\mathcal{L}^{HVV} = -\frac{\alpha_s v}{8\pi} \frac{f_g}{M^2} \mathcal{O}_{GG} + \frac{f_{BB}}{M^2} \mathcal{O}_{BB} + \frac{f_{WW}}{M^2} \mathcal{O}_{WW} + \frac{f_B}{M^2} \mathcal{O}_B + \frac{f_W}{M^2} \mathcal{O}_W + \frac{f_{\phi,2}}{M^2} \mathcal{O}_{\phi,2}$$

- operator basis [as any basis not unique]

$$\begin{aligned} \mathcal{O}_{BB} &= \phi^\dagger B_{\mu\nu} B^{\mu\nu} \phi & \mathcal{O}_{WW} &= \phi^\dagger W_{\mu\nu} W^{\mu\nu} \phi & \mathcal{O}_{GG} &= \phi^\dagger \phi G_{\mu\nu}^a G^{a\mu\nu} \\ \mathcal{O}_B &= (D_\mu \phi)^\dagger B^{\mu\nu} (D_\nu \phi) & \mathcal{O}_W &= (D_\mu \phi)^\dagger W^{\mu\nu} (D_\nu \phi) & \mathcal{O}_{\phi,2} &= \partial^\mu (\phi^\dagger \phi) \partial_\mu (\phi^\dagger \phi) \end{aligned}$$

- plus t, b, τ couplings

9 operators, 7 Δ shifts, 4 new Lorentz structures

A detailed discussion of these questions will be presented elsewhere.

It is worth noting that an essential feature of the type of theory which has been described in this note is the prediction of incomplete multiplets of scalar and vector bosons.⁸ It is to be expected that this feature will appear also in theories in which the symmetry-breaking scalar fields are not elementary dynamic variables but bilinear combinations of Fermi fields.⁹

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Low energy effects of new interactions in the electroweak boson sector

K. Hagiwara

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(Received 17 March 1993)

Novel strong interactions in the electroweak bosonic sector are expected to induce effective interactions between the Higgs doublet field and the electroweak gauge bosons which lead to anomalous WWZ and $WW\gamma$ vertices once the Higgs field acquires a vacuum expectation value. Using a linear realization of the Goldstone bosons, we consider a complete set of dimension-six operators which are $SU(2) \times U(1)$ gauge invariant and conserve C and P . This approach allows us to study effects of new physics which originates above 1 TeV and the Higgs boson mass dependence of the results can be investigated. Four of the dimension-six operators affect low energy and present CERN LEP experiments at the tree level. Another five influence neutral and charged current experiments at

The other five operators are

$$\mathcal{O}_{WWW} = \text{Tr}[\hat{W}_{\mu\nu} \hat{W}^{\nu\rho} \hat{W}_\rho^\mu], \quad (2.7a)$$

$$\mathcal{O}_{WW} = \Phi^\dagger \hat{W}_{\mu\nu} \hat{W}^{\mu\nu} \Phi, \quad (2.7b)$$

$$\mathcal{O}_{BB} = \Phi^\dagger \hat{B}_{\mu\nu} \hat{B}^{\mu\nu} \Phi, \quad (2.7c)$$

$$\mathcal{O}_W = (D_\mu \Phi)^\dagger \hat{W}^{\mu\nu} (D_\nu \Phi), \quad (2.7d)$$

$$\mathcal{O}_B = (D_\mu \Phi)^\dagger \hat{B}^{\mu\nu} (D_\nu \Phi). \quad (2.7e)$$

As we shall see they all contribute to four-fermion amplitudes at the one-loop level. In addition \mathcal{O}_{WWW} , \mathcal{O}_W , and \mathcal{O}_B give rise to nonstandard triple gauge boson couplings. Conventionally the WWV vertices ($V = Z, \gamma$) are parametrized by the effective Lagrangian [2]

$$\begin{aligned} \mathcal{L}_{\text{eff}}^{WWV} &= i g_{WWV} \left(g_1^V (W_\mu^+ W^-{}^\mu - W^{+\mu} W_{\mu}^-) V^\nu \right. \\ &\quad \left. + \kappa_V W_\mu^+ W_\nu^- V^{\mu\nu} \right. \\ &\quad \left. + \frac{\lambda_V}{m_W^2} W_\mu^+ W_\nu^-{}^\rho V_\rho^\mu \right), \quad (2.8) \end{aligned}$$

Higgs-gauge effective theory

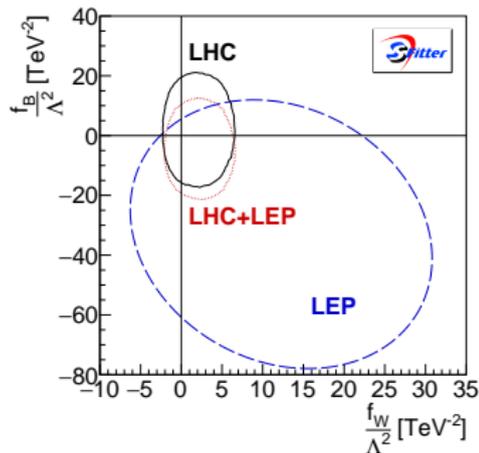
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New physics in Higgs-gauge sector? [ask BeateH]

- Higgs couplings re-written as operators
theoretically sound
distributions included
- gauge bosons included
LHC exceeding LEP
many analyses not done



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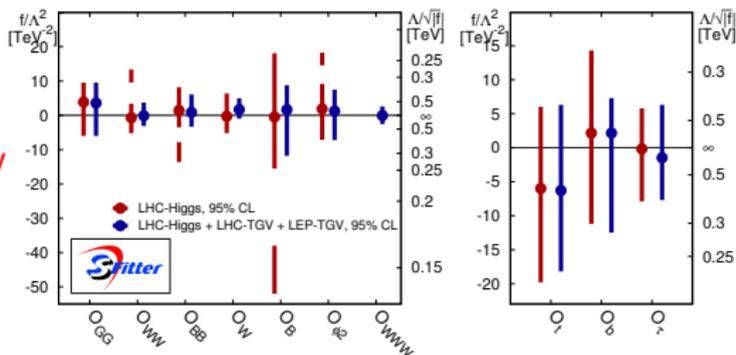
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⇒ new physics $M \gtrsim 500$ GeV



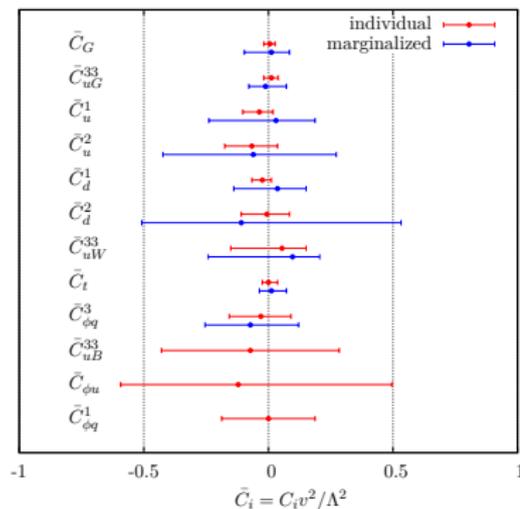
More effective theories

Effective theory of top sector [Glasgow TopFitter]

- all available top production and decay measurements
- dimension-6 operators

$$\mathcal{O}_{qq} = \bar{q}\gamma_{\mu}q\bar{t}\gamma^{\mu}t \quad \dots$$

⇒ new physics $M \gtrsim 500$ GeV



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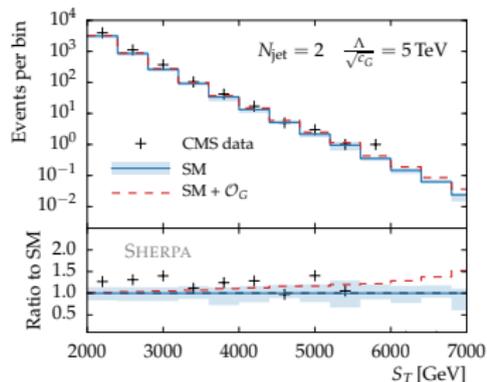
Effective theory of QCD [with Sherpa]

- multi-jet production rates

$$S_T \approx \sum_{\text{jets}} E_T$$

- dimension-6 operators

$$\underbrace{\mathcal{O}_{qq} = \bar{q}\gamma_\mu q \bar{q}'\gamma^\mu q'}_{2-3 \text{ jets}} \quad \underbrace{\mathcal{O}_G = f_{abc} G_\mu^{a\nu} G_\nu^{b\lambda} G_\lambda^{c\mu}}_{\gtrsim 5 \text{ jets}}$$



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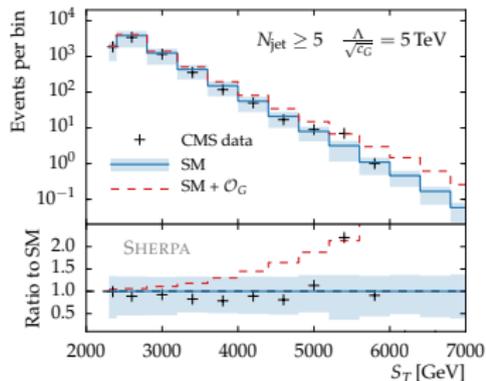
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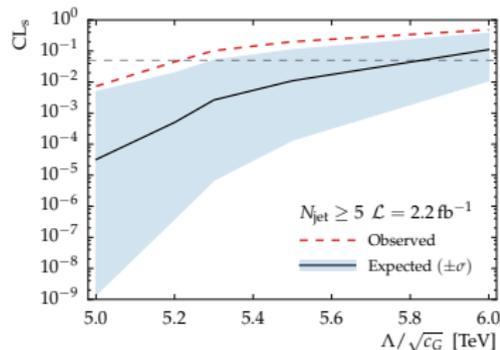
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⇒ new physics $M \gtrsim 5 \text{ TeV}$, EFTs work!



Higgs portal

New Higgs physics without effective Lagrangian

- renormalizable, extended scalar potential

$$V(\Phi, S) = \mu_1^2 (\Phi^\dagger \Phi) + \lambda_1 |\Phi^\dagger \Phi|^2 + \mu_2^2 |S|^2 + \lambda_2 |S|^4 + \lambda_3 |\Phi^\dagger \Phi| |S|^2$$

- $\langle S \rangle \neq 0$: mixing with Higgs particle
- $\langle S \rangle = 0$: **simplest dark matter model ever**
- change in all Higgs couplings
- invisible Higgs decays $[m_S < m_H/2]$

The Minimal Model of nonbaryonic dark matter: a singlet scalar

C.P. Burgess^{a,b}, Maxim Pospelov^c, Tonnis ter Veldhuis^c

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^b *Physics Department, McGill University, 3600 University St., Montréal, PQ, Canada H3A 2T8*

^c *Department of Physics, University of Minnesota, Minneapolis, MN 55455, USA*

Received 17 January 2001; accepted 9 October 2001

Abstract

We propose the simplest possible renormalizable extension of the Standard Model—the addition of just one singlet scalar field—as a minimalist model for nonbaryonic dark matter. Such a model

Higgs portal

New Higgs physics without effective Lagrangian

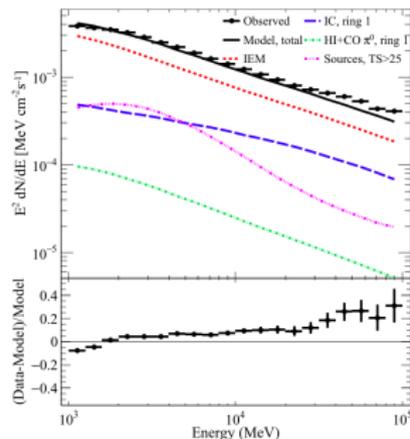
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Dark matter models means anomalies

- Fermi galactic center excess [Goodenough, Hooper]



Higgs portal

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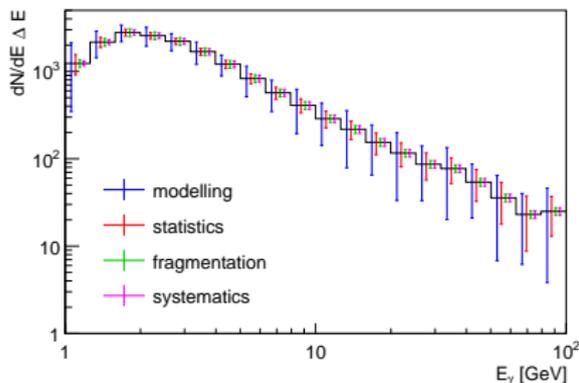
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- $\langle S \rangle = 0$: **simplest dark matter model ever**
- change in all Higgs couplings
- invisible Higgs decays $[m_S < m_H/2]$

Dark matter models means anomalies

- Fermi galactic center excess [Goodenough, Hooper]



Higgs portal

New Higgs physics without effective Lagrangian

- renormalizable, extended scalar potential

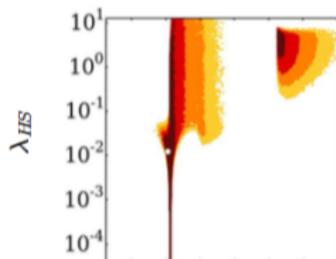
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- constrained by LHC

GCE+BR_{inv}



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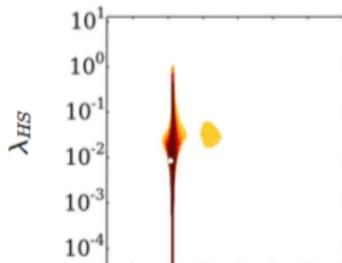
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Dark matter models means anomalies

- Fermi galactic center excess [Goodenough, Hooper]
 - explained by Higgs portal [Cuoco, Eiteneuer, Heisig, Krämer]
 - constrained by LHC
 - most constrained by direct detection
- ⇒ **key question: link to LHC?**

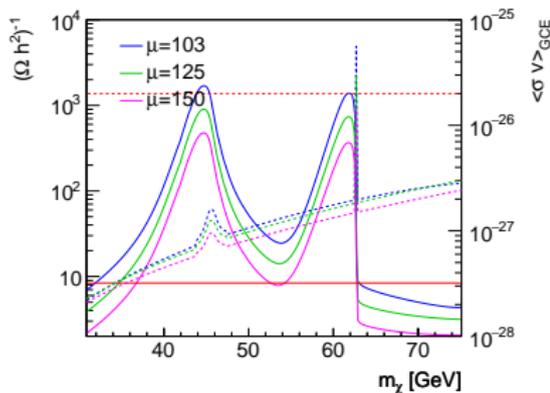
GCE+BR_{inv}+LUX+dwarfs



Hooperons at the LHC

Supersymmetric dark matter candidates [ask GregorH]

- superposition of $SU(2)_L$ representations: neutralinos/charginos
 - singlet — bino, singlino
 - double-doublet — higgsino
 - triplet — wino
- annihilation $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow b\bar{b}, W^+ W^-, t\bar{t}$
- Higgs portal to Majorana fermions
- **no smoking LHC gun (yet)**



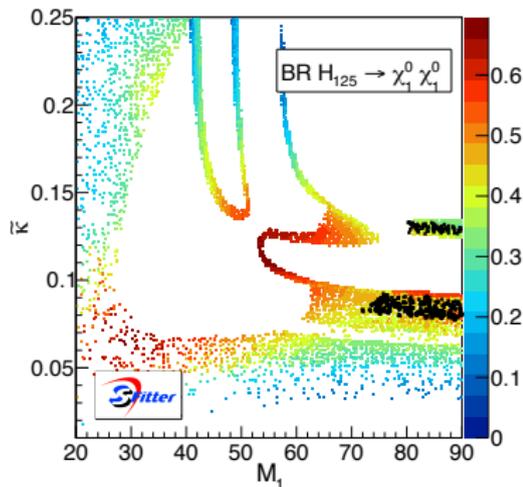
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Link to invisible Higgs decays

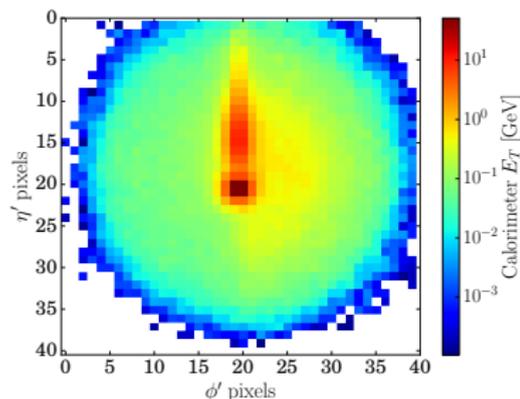
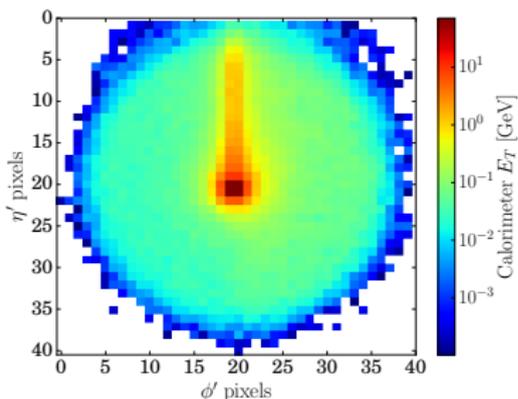
- no Fermi-Higgs link in MSSM
 - strong correlation for NMSSM
 - $BR(H \rightarrow \text{inv}) \approx 10 \dots 30\%$ expected
- ⇒ **LHC physics not only QCD and EFT**



Theory for and at the LHC

Data driven era

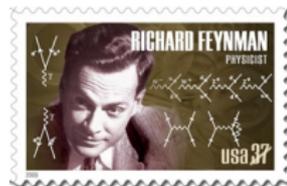
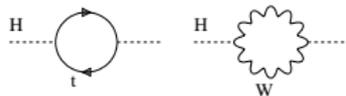
- Higgs physics a triumph, LHC one of the great experiments
- many open questions, some very old, but new data
- requiring experts, not preachers
- currently no 'hot' LHC anomaly [as far as I am concerned]
but who knows what happens next
- **new ideas by young people still crucial, welcome, and acknowledged**



Naturalness

Problem with scalars

- quantum corrections to Higgs mass... [$\Delta t \Delta E < 1$]



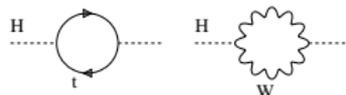
Naturalness

Problem with scalars

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$$m_H^2 \longrightarrow m_H^2 - \frac{g^2}{(4\pi)^2} \frac{3}{2} \frac{\Lambda^2}{m_W^2} \left[m_H^2 + 2m_W^2 + m_Z^2 - 4m_t^2 \right] + \dots$$

- Higgs mass pulled to cut-off $\Lambda \gg 126 \text{ GeV}$ [where Higgs at Λ does not work]
no protecting symmetry in Standard Model [no idea where Higgs field comes from]



Renormalization Group and Strong Interactions*

KENNETH G. WILSON

Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305

and

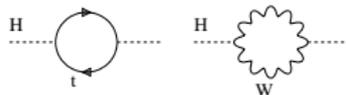
Laboratory of Nuclear Studies, Cornell University, Ithaca, New York 14850†

(Received 30 November 1970)

The renormalization-group method of Gell-Mann and Low is applied to field theories of strong interactions. It is assumed that renormalization-group equations exist for strong interactions which involve one or several momentum-dependent coupling constants. The further assumption that these coupling constants approach fixed values as the momentum goes to infinity is discussed in detail. However, an alternative is suggested, namely, that these coupling constants approach a limit cycle in the limit of large momenta. Some results of this paper are: (1) The e^+e^- annihilation experiments above 1-GeV energy may distinguish a fixed point from a limit cycle or other asymptotic behavior. (2) If electrodynamic or weak interactions become strong above some large momentum Λ , then the renormalization group can be used (in principle) to determine the renormalized coupling constants of strong interactions, except for $U(3) \times U(3)$ symmetry-breaking parameters. (3) Mass terms in the Lagrangian of strong, weak, and electromagnetic interactions must break a symmetry of the combined interactions with zero mass. (4) The $\Delta I = \frac{1}{2}$ rule in nonleptonic weak interactions can be understood assuming only that a renormalization group exists for strong interactions.

This discussion can be summarized by saying that mass or symmetry-breaking terms must be "protected" from large corrections at large momenta due to various interactions (electromagnetic, weak, or strong). A symmetry-breaking term, such as $h_{1\lambda}$, $h_{2\lambda}$, or $h_{3\lambda}$, is protected if, in the renormalization-group equation for $h_{1\lambda}$, $h_{2\lambda}$, or $h_{3\lambda}$, the right-hand side is proportional to $h_{1\lambda}$, $h_{2\lambda}$, $h_{3\lambda}$ or other small coupling constants even when high-order strong, electromagnetic, or weak corrections are taken into account. The mass terms for the electron and muon and the weak boson, if any, must also be protected. This requirement means that weak interactions cannot be mediated by scalar particles.³⁶

Naturalness



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⇒ **valid theoretical guiding principle?**

NATURALNESS, CHIRAL SYMMETRY, AND SPONTANEOUS

CHIRAL SYMMETRY BREAKING

G. 't Hooft

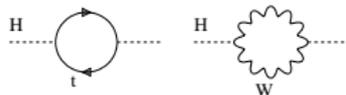
Institute for Theoretical Physics

Utrecht, The Netherlands

ABSTRACT

A properly called "naturalness" is imposed on gauge theories. It is an order-of-magnitude restriction that must hold at all energy scales μ . To construct models with complete naturalness for elementary particles one needs more types of confining gauge theories besides quantum chromodynamics. We propose a search program for models with improved naturalness and concentrate on

Naturalness



Problem with scalars

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no protecting symmetry in Standard Model [no idea where Higgs field comes from]

⇒ **valid theoretical guiding principle?**

If Higgs mass is a problem...

- protecting symmetries: supersymmetry?
 - low cut-off in composite models?
 - something totally different?
 - maybe combined with **dark matter particle?**
- ⇒ **LHC theory beyond precision QCD and EFT...**



LHC Theory

Tilman Plehn

LHC

Higgs boson

Higgs couplings

Effective theory

Higgs portal

Dark matter