

# Generative and Invertible Networks for LHC Theory

Tilman Plehn

Universität Heidelberg

STRUCTURES 6/2021



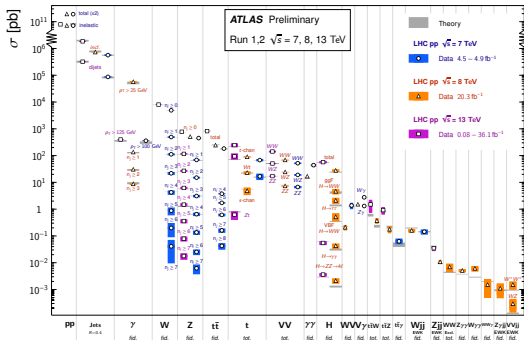
# LHC goals

## Fundamental questions

- particle nature of dark matter?
- origin of the Higgs mechanism? [hierarchy problem?]
- matter-antimatter asymmetry? [CP-symmetry]
- Standard Model all there is?

## Impressive measurements

- many processes
- vastly different rates
- high precision
- predicted by theory



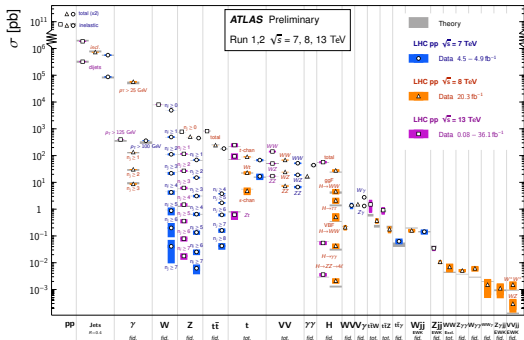
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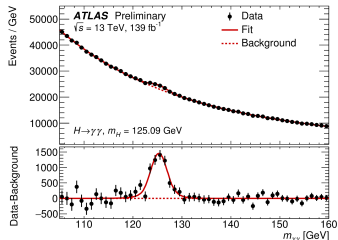
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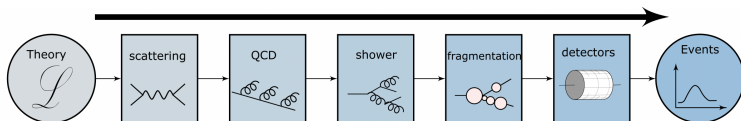
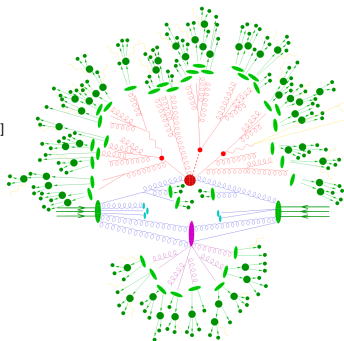
## Rates not interesting

- energy distributions dropping
  - new physics heavy
- ⇒ bumps, tails, kinematics instead



## Simulation-based inference [likelihood-free inference]

- start with Lagrangian
  - calculate scattering in perturbative QFT
  - simulate events [theory: Sherpa, Madgraph, Pythia]
  - simulate detectors [experiment: ATLAS, CMS, Delphes]
- ⇒ LHC events in virtual worlds



## LHC simulations

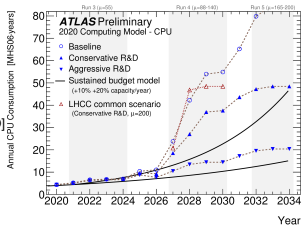
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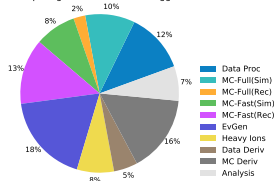
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## HL-LHC: preparing for 25-fold data set

- simulated event numbers  $\sim$  expected events
- statistics requiring 1%-2% uncertainty [ $\text{NNLO}/N^3\text{LO}$ ]
- flexible signal hypotheses [time-dependent]
- low-rate high-multiplicity backgrounds



ATLAS Preliminary  
2020 Computing Model -CPU: 2030: Aggressive R&D



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## Three ways to use ML

- improve **current tools**: iSherpa, ML-MadGraph...
- new ideas: fast **ML-generator-networks**...
- **conceptual ideas** for simulations and analyses



## ML for LHC

## LHC and Ben Nachman [EPS prize 2021]

- 1991: NN-based quark-gluon tagger
- 2005: TMVA in Root — analysis
- 2015: jet images — classification
- 2017: CaloGAN — jet generation

## Heidelberg history

- 2017: top-jet tagger — classification
  - 2018: jet autoencoder — unsupervised
  - 2019: jet classification with uncertainties [w/ Manuel Haußmann]
  - 2019: event GAN — generation [How to GAN #1-5]
  - 2020: conditional INN — unfolding [w/ Ulli Köthe, Lynton Ardizzone]
  - 2020: BayesFlow — inference [w/ Ulli Köthe, Stefan Radev]
  - 2021: Bayesian INN — generation with uncertainties [w/ Manuel Haußmann]
  - 2021: Dirichlet VAE — unsupervised
- ⇒ unsupervised, uncertainties, generation

## USING NEURAL NETWORKS TO IDENTIFY JETS

Leif LÖNNBLAD\*, Carsten PETERSON\*\* and Thorsteinn RÖGNVALDSSON\*\*\*

*Department of Theoretical Physics, University of Lund, Sölvegatan 14A, S-22362 Lund, Sweden*

Received 29 June 1990

A neural network method for identifying the ancestor of a hadron jet is presented. The idea is to find an efficient mapping between certain observed hadronic kinematical variables and the quark-gluon identity. This is done with a neuron-like expansion in terms of a network of sigmoidal functions using a gradient descent procedure, where the errors are back-propagated through the network. With this method we are able to separate gluon from quark jets originating from Monte Carlo generated  $e^+e^-$  events with  $\sim 85\%$  accuracy. The result is independent of the MC model used. This approach for isolating the gluon jet is then used to study the so-called string effect.

In addition, heavy quarks (b and c) in  $e^+e^-$  reactions can be identified on the 50% level by just observing the hadrons. In particular we are able to separate b-quarks with an efficiency and purity, which is comparable with what is expected from vertex detectors. We also speculate on how the neural network method can be used to disentangle different hadronization schemes by compressing the dimensionality of the state space of hadrons.

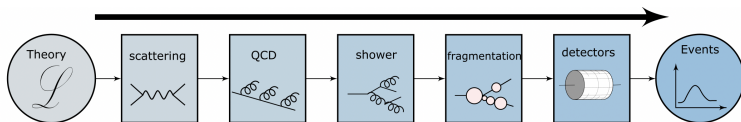
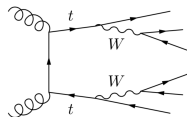




# INN-generating LHC events

## LHC scattering benchmarks

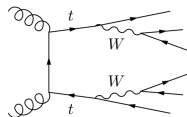
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training from event samples [optimal transport vs likelihoods]  
energy-momentum conservation learned  
no detector effects [smoother structures]
- top-quark pairs  $t\bar{t} \rightarrow 6$  jets  
 $t/\bar{t}$  and  $W^\pm$  on-shell [Breit-Wigner  $\Gamma/m \sim \mathcal{O}(\%)$ ]
- $n$ -jets/ $WZ$ +jets  
variable number of particles  
topology through jet-jet separation



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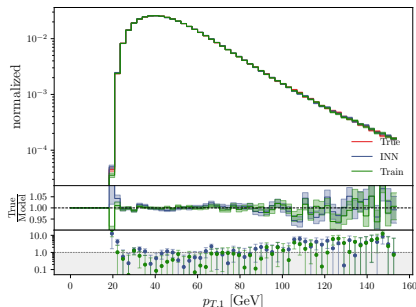
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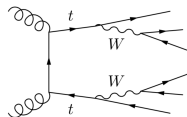
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bijective, stable mapping  
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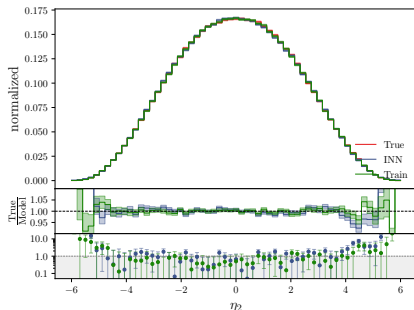
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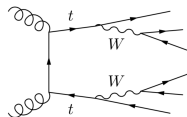
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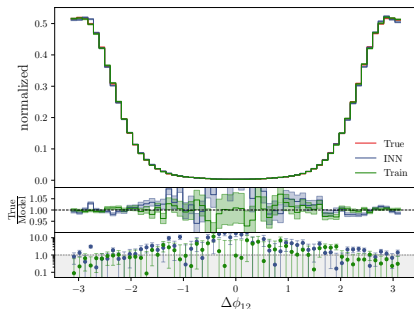
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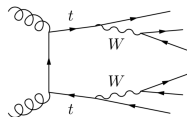
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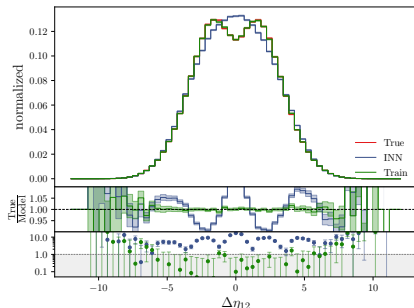
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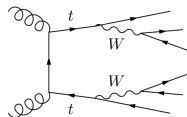
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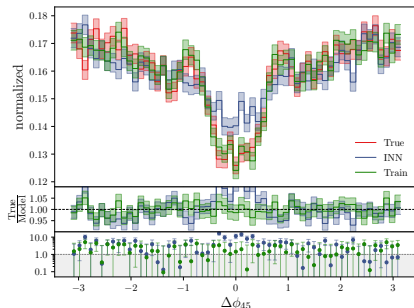
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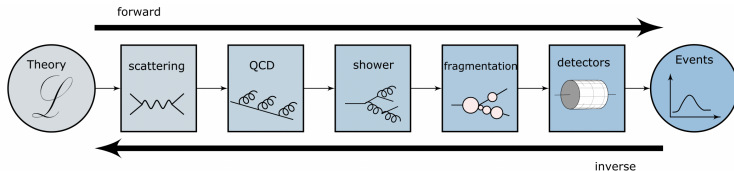
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## Inverting LHC simulations

- unfolding QCD-shower to hard parton standard [jet algorithm]
  - unfolding detector common
  - unfolding top-quark decays useful
  - matrix element method for hypothesis test
- ⇒ systematic approach through generative network



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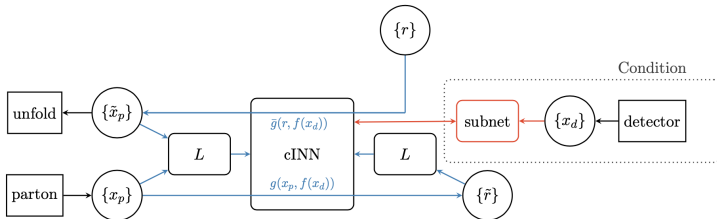
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## Conditional INN

- standard INN/cINN setup: parton-level events from  $\{r\}$
- maximum likelihood loss

$$L = - \langle \log p(\theta | x_p, x_d) \rangle_{x_p, x_d}$$

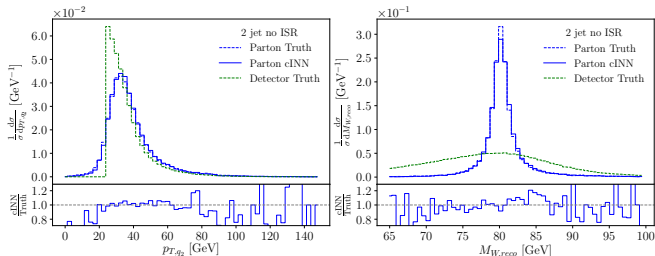
$$= - \left\langle \log p(g(x_p, x_d)) + \log \left| \frac{\partial g(x_p, x_d)}{\partial x_p} \right| \right\rangle_{x_p, x_d} - \log p(\theta) + \text{const.}$$





Hard process  $q\bar{q} \rightarrow ZW \rightarrow (\ell\ell) (jj)$ 

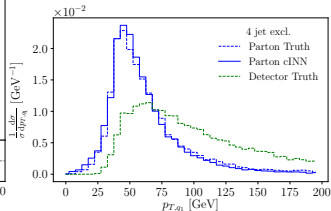
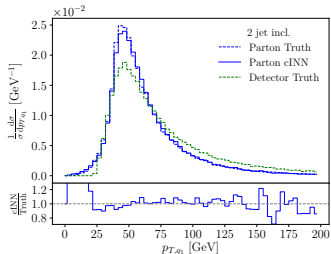
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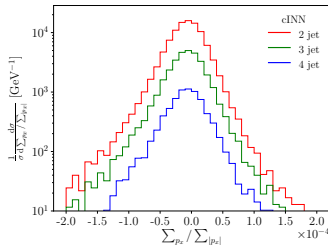
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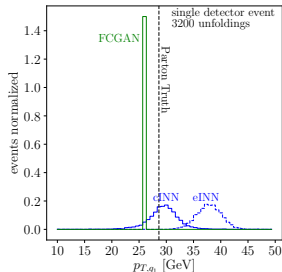
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single detector event  
3200 unfoldings to partonic phase space



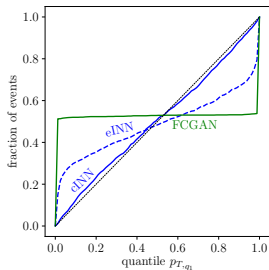
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## Proper statistical inversion

- distribution  
single detector event  
3200 unfoldings to partonic phase space
  - calibration  
1500 detector-parton event pairs  
60 unfoldings per pair, in quantiles  
truth within given quantile for fraction of pairs
- ⇒ **Probability distribution in parton phase space!**

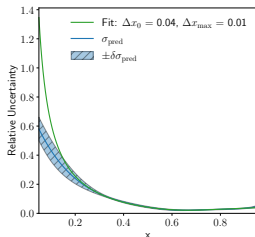
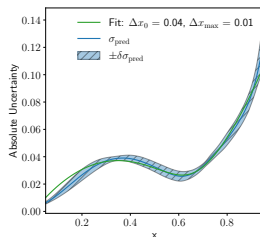
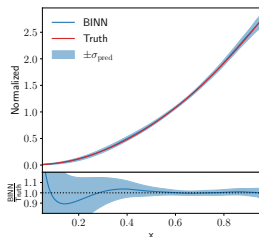


# One number not a prediction

## Bayesian INN

- generate events with error bars  
learn density and uncertainty maps over phase space
- 2D toy models: wedge ramp, kicker ramp, Gaussian ring

⇒ **Uncertainty estimate works...**



...and we see how the network learns!



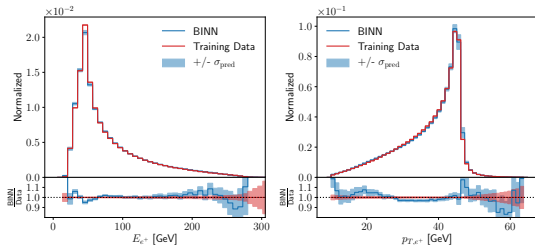
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## LHC toy process: $pp \rightarrow e^+e^-$

- kinematic distributions with errors



- ⇒ **Crucial step for LHC-simulations**



# Machine learning for LHC in Heidelberg

Thank you to all collaborators here and elsewhere!

Lynton Ardizzone, Mathias Backes, Pierre Baldi, Marco Bellagente, Lukas Blecher, Sebastian Bieringer, Johann Brehmer, Anja Butter, Sascha Diefenbacher, Barry Dillon, Manuel Haußmann, Theo Heimel, Jessica Howard, Sander Hummerich, Gregor Kasieczka, Fabian Keilbach, Ulli Köthe, Tobias Krebs, Michel Luchmann, Ben Nachman, Stefan Radev, Armand Rousselot, Michael Russell, Christof Sauer, Torben Schell, Peter Sorrensen, Natalie Soybelman, Jennifer Thompson, Sophia Vent, Lorenz Vogel, Daniel Whiteson, Ramon Winterhalder



The poster features a scenic view of Heidelberg with a stone bridge over a river. The text is overlaid on the image. In the top right, there are logos for the Institute for Theoretical Physics and the University of Heidelberg. The main title is 'ML4Jets hybrid' with the dates 'July 6-8 2021'. A QR code is in the bottom left. Two boxes list the local organizers and the international organization committee.

**ML4Jets hybrid**  
July 6-8 2021

INSTITUTE FOR THEORETICAL PHYSICS

UNIVERSITÄT HEIDELBERG  
ZUKUNFT SEIT 1386

Local Organizers  
Anja Butter  
Barry Dillon  
Ulrich Köthe  
Tilman Plehn  
Hans-Christian Schultz-Coulon

International Organization Committee  
Kyle Cranmer (NYU)  
Ben Nachman (LBNL)  
Maurizio Pierini (CERN)  
Tilman Plehn (Heidelberg)  
Jesse Thaler (MIT)

<https://indico.cern.ch/event/980214>

Photo: Systemz / Fotolia / Adobe Stock; Composition: Anne Heroldmann

Generative  
Networks

Tilman Plehn

LHC

Events

Inverting

Uncertainties

