

Challenges in Theory and AI/ML

Tilman Plehn

Universität Heidelberg

SLAC Summer Institute, August 2023

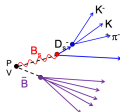


Modern LHC physics

Classic motivation

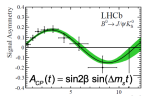
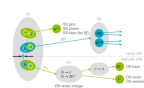
- dark matter?
- baryogenesis?
- origin of Higgs field?

Flavor Tagging und CP

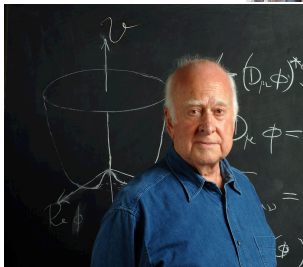
Dortmunder
„Steckenpferd“

$$\sin 2\beta = 0.73 \pm 0.08$$

Julian Tarek Wishah,
Doktorarbeit TU DO 2013



Kevin Heinicke, Masterarbeit 2016



Modern LHC physics

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- dark matter?
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LHC physics

- fundamental questions
- huge data set
- first-principle, precision simulations
- complete uncertainty control



Classic motivation

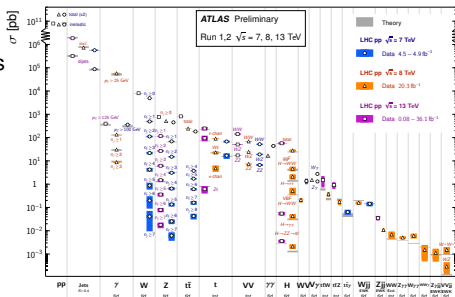
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Successful past

- measurements of event counts
- analyses inspired by simulation
- model-driven Higgs discovery



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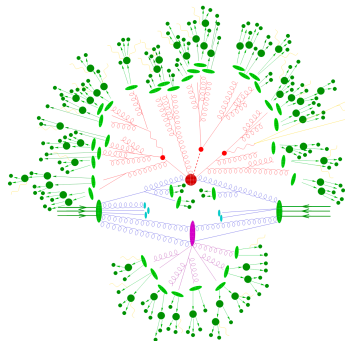
Successful past

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First-principle, precision simulations

- start with Lagrangian
- calculate scattering using QFT
- simulate collisions
- simulate detectors

→ LHC collisions in virtual worlds



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First-principle, precision simulations

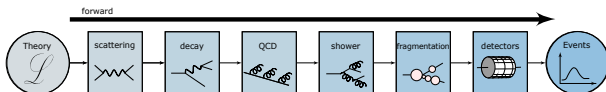
- start with Lagrangian
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→ LHC collisions in virtual worlds

BSM searches

- compare simulations and data
- understand LHC dataset systematically
- infer underlying theory [SM or BSM]
- publish useable results

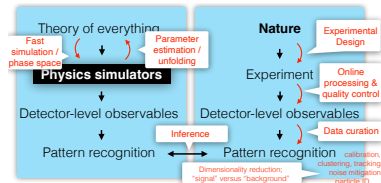
→ Lots of data science...



Role of theory

First-principle simulations

- start with Lagrangian
generate Feynman diagrams
 - compute hard scattering amplitudes
for on-shell, include decays
add QCD jet radiation [ISR/FSR]
 - add parton shower [still QCD]
push fragmentation towards QCD
 - all theory, except for detectors
- **Simulations, not modeling!**

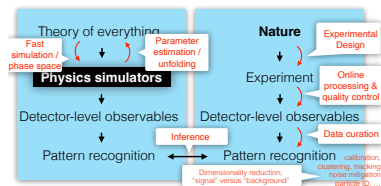
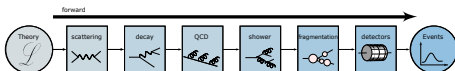


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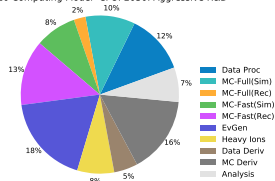


Pythia/Madgraph/Sherpa... for HL-LHC

- factor 25 more expected (= simulated) data
- more complex final states
higher-orders precision
- parameter coverage for signals
- enable analysis reinterpretation?
enable global LHC analyses?

→ **Theory nightmare**

ATLAS Preliminary
2020 Computing Model -CPU: 2030: Aggressive R&D

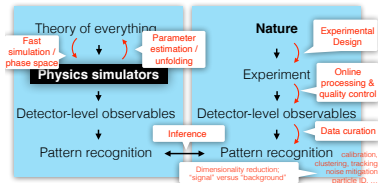


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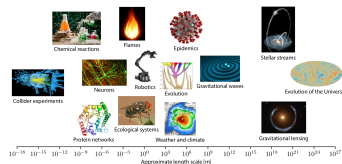


LHC-specific explainable AI

- SBI conditional on theory simulations
- understanding LHC data is QFT
- computing speed means precision
- control critical
- uncertainties crucial
- phase space interpretable

→ **Well-defined, but non-standard AI/ML**

Scientific simulators

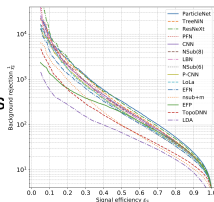


ML-applications in experiment

Top tagging [supervised classification]

- 'hello world' of LHC-ML
- end of QCD-taggers
- different NN-architectures

→ Non-NN left in the dust...



SciPost Physics

Submission

The Machine Learning Landscape of Top Taggers

G. Kasieczko^{1(a)}, T. Plehn^{1(a)}, A. Butter², K. Craner³, D. DeLauter⁴, B. M. Ertel⁵, M. Fairman⁶, D. A. Farrelly⁷, W. Fickel⁸, C. Gay¹, L. Gossiaux⁹, J. F. Kerner^{10,11}, P. T. Komiske¹², S. Lester¹, A. Lister¹, S. Maciunas¹³, E. M. Metodiev¹⁴, L. Moore¹⁵, B. Nachman^{1,11}, K. Nandoriya^{1,11}, J. Puckett¹⁶, H. Qiu¹, R. Rahn¹⁶, M. Rieger¹⁶, D. Shih⁴, J. M. Thompson¹⁶, and S. Voznes¹⁶

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³ Center for Cosmology and Particle Physics and Center for Data Science, NYU, USA

⁴ NHETC, Dept. of Physics and Astronomy, Rutgers, The State University of NJ, USA

⁵ Joint Institute for Nuclear Research, Dubna, Russia

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⁸ Department of Physics, University of California, Santa Barbara, USA

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¹² Physics Division, Lawrence Berkeley National Laboratory, Berkeley, USA

¹³ Simons Inst. for the Theory of Computing, University of California, Berkeley, USA

¹⁴ National Institute for Subatomic Physics (Nikhef), Amsterdam, Netherlands

¹⁵ LPTHE, CNRS & Sorbonne Université, Paris, France

¹⁶ III. Physikalisches Institut A, RWTH Aachen University, Germany

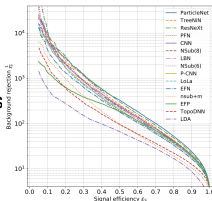


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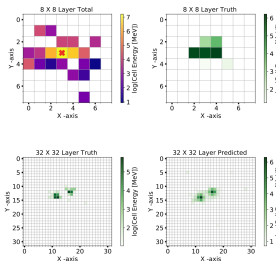
G. Kasieczko^[a], T. Plehn^[a], A. Butter^[b], K. Craner^[c], D. DeLoraine^[d], B. M. Ertel^[e], M. Fairhead^[f], D. A. Farrelly^[g], W. Fickel^[h], C. Gay^[i], L. Goulet^[j], J. F. Kerner^[k,l], P. T. Komoda^[m], S. Loebl^[n], A. Lister^[o], S. Maclean^[p,q], E. M. Metcalfe^[r], L. Moore^[s], B. Naudus^[t,u], K. Nandoriya^[v,w], J. Puckett^[x], H. Qiu^[y], Y. Ruan^[z], M. Sager^[aa], D. Shih^[ab], J. M. Thompson^[ac], and S. Varma^[ad]

- ¹ Institut für Experimentelle Physik, Universität Hamburg, Germany
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Particle flow [classification, super-resolution]

- mother of jet tools
- combined detector channels
- similar studies in CMS

→ Beyond just concepts



Towards a Computer Vision Particle Flow *

Francesco Armando Di Belle^[a], Samay Ganguly^[b], Eliam Gross^[c], Marumi Kado^[d,e], Michael Pitt^[f], Lorenzo Santi^[g], Jonathan Shmida^[h]

^[a]Weizmann Institute of Science, Rehovot 76100, Israel

^[b]CERN, CH 1211, Geneva 23, Switzerland

^[c]Università di Roma Sapienza, Piazza Aldo Moro, 2, 00185 Roma, Italy & INFN, Italy

^[d]Université Paris-Saclay, CNRS/IN2P3, DCLab, 91195, Orsay, France

Fig. 7: An event display of total energy shower (within topocluster), as captured by a calorimeter layer of 8×8 granularity, along with the location of the track, denoted by a red cross (left) and the same shower is captured by a calorimeter layer of 32×32 granularity (middle). The bottom right panel shows the corresponding event predicted by the NN. The figure shows that the shower originating from a $m^0 \rightarrow \gamma\gamma$ is resolved by a 32×32 granularity layer.



Jets and parton densities

Anomaly searches [unsupervised training]

- train on QCD-jets, SM-events
- look for non-QCD jets, non-SM events

→ Autoencoders

arXiv:1907.04472

arXiv:1907.04472

Better Latent Spaces for Better Autoencoders

Harry M. Dickinson¹, Tilman Plehn², Christian Bauer³, and Peter Schwenn⁴

¹ Institut für Theoretische Physik, Universität Heidelberg, Germany

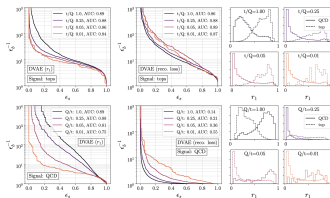
² Physikalisches Institut, Universität Heidelberg, Germany

³ Heidelberg Collaboratory for Large Accelerators, Universität Heidelberg, Germany

April 26, 2020

Abstract

Autoencoders as tools to find unusual anomalies at the LHC have the structural problem that they only work in one direction, reconstructing jets with higher complexity but not the other way around. To address this, we derive classifiers from the latent space of (variational) autoencoders, specifically in Gaussian mixtures and Dirichlet latent spaces. In particular, the Dirichlet setup solves the problem and improves both the performance and the interpretability of the networks.



Jets and parton densities

Anomaly searches [unsupervised training]

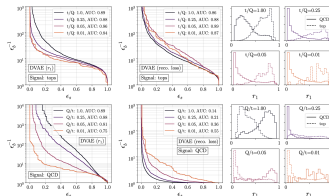
- train on QCD-jets, SM-events
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→ Autoencoders



Abstract

Autoencoders as tools to detect anomaly events at the LHC have the structural problem that they only work in one direction, returning jets with higher complexity but not the other way around. To address this, we derive classifiers from the latent space of variational autoencoders, specifically in Gaussian mixtures and Dirichlet latent space. In particular, the Dirichlet setup solves the problem and improves both the performance and the interpretability of the networks.



NNPDF/N3PDF parton densities [full blast]

- starting point: pdfs without functional ansatz
- moving on: cutting-edge ML everywhere

→ Leaders in ML-theory

N3PDF
Machine Learning - PDFs - QCD

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A data-based parametrization of parton distribution functions

Stefano Caronni^{1,2*}, Juan Cruz-Martinez¹, and Ryo Suganuma³

¹ INFN, Dipartimento di Fisica, Università degli Studi di Milano and INFN Sezione di Milano.

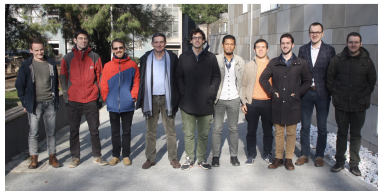
² INFN, Teorietische Physik Department, CH-611 Geneva 23, Switzerland

³ Quantum Research Center, Technology Innovation Institute, Abu Dhabi, U.A.E.

Received date / Revised version date

Abstract. Since the first determination of a structure function many decades ago, all methodologies used to determine structure functions or parton distribution functions (PDFs) have employed a common procedure as part of the parametrization. The NNPDF collaboration pioneered the use of neural networks to overcome the inherent bias of constraining the space of solutions with a fixed functional form while still keeping the same common procedure as a preprocessing. Over the years various, increasingly sophisticated, techniques have been introduced to consider the effect of the prior on the PDF determination. In this paper we present a methodology to ensure the posterior robustness, thereby significantly simplifying the methodology, without a loss of efficiency and finding good agreement with previous results.

PACS. 22.20.+g Quantum chromodynamics · 12.20.+g Phenomenological quark models · 81.20.+v Neural Networks

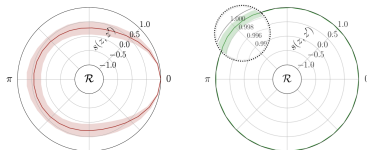


Symmetries

Symmetric networks [contrastive learning, transformer network]

- rotations, translations, permutations, soft splittings, collinear splittings
- learn symmetries/augmentations

→ Symmetric latent representation



SelfPost Physics

Schubert

Symmetries, Safety, and Self-Supervision

Barry M. D'Eka¹, Grigor Kasieczko², Hans Gieseler¹, Tilman Plehn²,
Peter Sorensen³, and Lorenz Vogt¹

¹ Institut für Theoretische Physik, Universität Heidelberg, Germany

² Institut für Experimentalphysik, Universität Hamburg, Germany

³ Heidelberg Collaboratory for Image Processing, Universität Heidelberg, Germany

August 11, 2021

Abstract

Collider searches face the challenge of defining a representation of high-dimensional data such that physical symmetries are manifest, the discriminating features are retained, and the choice of representation is non-polygenic agnostic. We introduce JetCLR to solve the mapping from low-level data to optimized observables through self-supervised contrastive learning. As an example, we construct a data representation for top and QCD jets using a permutation-invariant transformer-encoder network and validate its symmetry properties. We compare the JetCLR representation with alternative representations using linear classifier tests and find it to work quite well.



Integrals and perturbative QFT

Learning integrands and integrals [differentiable activations]

- learn integrand through differentiable network
- evaluate integral as primitive

→ **Novel ML-integrator**

formulas. Analytically, we would compute the primitive F ,

$$\frac{d^2 F(x, y)}{dx_1 dx_2} = f(x, y), \quad (3.80)$$

and then the integral by evaluating the integration boundaries

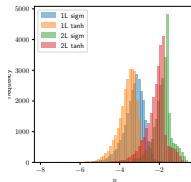
$$\begin{aligned} F(x) &= \int_{x_1}^x dx_1 \int_{x_2}^x dx_2 \frac{d^2 F(x, y)}{dx_1 dx_2} \\ &= \int_{x_1}^x dx_1 \int_{x_2}^x dx_2 \frac{d^2 F(x, y)}{dx_1 dx_2} \Big|_{x_1=x_2}^{x_1=x} \\ &= \sum_{i=1}^n \int_{x_1}^x dx_1 \int_{x_2}^x dx_2 \frac{d^2 F(x, y)}{dx_1 dx_2} \Big|_{x_1=x_2}^{x_1=x} \end{aligned} \quad (3.81)$$

In particle physics we really never know the primitive of a phase space integrand, but we can try to construct it and encode it in a neural network,

$$F_{\text{NN}}(x, y) \approx F(x, y). \quad (3.82)$$

On the other hand, we do not have data to train a regression network for F directly. The idea is to instead train on integrated integrands, such that its 1D-th derivative matches f ,

$$\mathcal{L}_{\text{int}} \left(f(x, y), \frac{dF_{\text{NN}}(x, y)}{dx_1} \right). \quad (3.83)$$



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Multi-variable integration with a neural network

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^bDepartment of Electronics and Computing, University of Santiago de Compostela, Santiago de Compostela, Spain

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ABSTRACT: In this article we present a method for automatic integration of parametric integrals over the unit hypercube using a neural network. The method fits a neural network to the primitive of the integrand using a loss function designed to minimize the difference between multiple derivatives of the network and the function to be integrated. We apply the method to two example integrals resulting from the sector decomposition of a one-loop and two-loop scalar integrals. Our method can achieve per-mille and percent accuracy for these integrals over a range of invariant values. Once the neural network is fitted, the evaluation of the integral is between 40 and 125 times faster than the usual numerical integration method for our examples, and we expect the speed gain to increase with the complexity of the integrand.



Event generation

Speeding up Sherpa and MadNIS [INNs, sampling]

- precision simulations limiting factor for Runs 3&4
- unweighting critical

→ Phase space sampling

	$gg \rightarrow H_{\text{eff}}$	$u\bar{u} \rightarrow H_{\text{eff}}$	$s\bar{s} \rightarrow H_{\text{eff}}$	$b\bar{b} \rightarrow H_{\text{eff}}$
σ_{tot}	$1.1\text{e-}2$	$7.3\text{e-}3$	$6.6\text{e-}3$	$6.6\text{e-}4$
$\sigma_{H_{\text{eff}}}$	$8.7\text{e-}3$	$5.8\text{e-}3$	$4.7\text{e-}3$	$3.0\text{e-}4$
$(\sigma_{\text{tot}}/\sigma_{H_{\text{eff}}})$	30312	2417	199	64
$\mu_{\text{eff}}^{\text{Higgs}}$	52.03	32.52	69.75	326.19
$\mu_{\text{fact,0.500}}^{\text{Higgs}}$	$2.4\text{e-}2$	$3.5\text{e-}2$	$2.1\text{e-}2$	$5.5\text{e-}3$
$\mu_{\text{fact}}^{\text{Higgs}}$	0.0669	0.3904	0.3904	0.0481
$\mu_{\text{eff}}^{\text{Higgs}}$	2.21	4.89	1.47	0.19
$\mu_{\text{eff}}^{\text{gluon}}$	20.40	19.14	27.75	35.34
$\mu_{\text{fact,0.500}}^{\text{gluon}}$	$4.3\text{e-}2$	$6.4\text{e-}2$	$5.1\text{e-}2$	$7.1\text{e-}2$
$\mu_{\text{fact}}^{\text{gluon}}$	0.0683	0.0906	0.0903	0.0321
$\mu_{\text{eff}}^{\text{gluon}}$	3.95	8.26	5.91	2.22

Table 6: Performance measures for partonic channels contributing to $H \rightarrow 3$ jets production at the LHC.

SciPost Physics

Submissions

MCNET-21-13

Accelerating Monte Carlo event generation – rejection sampling using neural network event-weight estimates

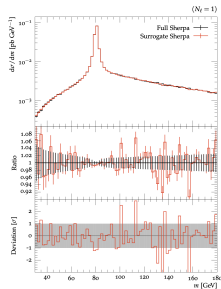
K. Danziger¹, T. Jocher², S. Schaefer², F. Siegel¹

¹ Institut für Kern- und Teilchenphysik, TU Dresden, Dresden, Germany
² Institut für Theoretische Physik, Georg-August-Universität Göttingen, Göttingen, Germany

September 27, 2021

Abstract

The generation of unit-weight events for complex scattering processes presents a severe challenge to modern Monte Carlo event generation. Even when using sophisticated phase-space sampling techniques adapted to the underlying transition matrix elements, the efficiency for generating unit-weight events from weighted samples can become a limiting factor in practical applications. Here we present a novel two-stage unweighting procedure that makes use of a neural-network surrogate for the full event weight. The algorithm can significantly accelerate the unweighting process, while it still guarantees unbiased sampling from the correct target distribution. We apply, validate and benchmark the new approach in high-multiplicity LHC production processes, including $2/\bar{W}+4$ jets and $2/\bar{W}+3$ jets, where we find speed-up factors up to ten.



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- precision simulations limiting factor for Runs 3&4
 - unweighting critical
- Phase space sampling

	$gg \rightarrow H_{\text{eff}}$	$gg \rightarrow t\bar{t}gg$	$gg \rightarrow t\bar{t}gg$	$gg \rightarrow H_{\text{eff}}$
r_{full}	1.1e-2	7.3e-3	6.8e-3	6.6e-4
$r_{\text{full,full}}$	8.7e-3	5.8e-3	4.7e-3	3.6e-4
$(r_{\text{full}}/r_{\text{full}})$	30013	5017	149	66
$r_{\text{full}}^{\text{MC}}$	52.03	32.52	69.75	206.19
$r_{\text{full}}^{\text{MC,full}}$	2.4e-2	3.8e-2	3.1e-2	5.6e-3
$r_{\text{full}}^{\text{MC,full}}$	0.0689	0.0884	0.0904	0.0961
$r_{\text{full}}^{\text{MC,full}}$	2.21	1.89	1.47	0.19
$r_{\text{full}}^{\text{MC,full}}$	30.01	19.14	27.78	35.34
$r_{\text{full}}^{\text{MC,full}}$	4.3e-2	6.4e-2	5.1e-2	7.1e-2
$r_{\text{full}}^{\text{MC,full}}$	0.0563	0.0060	0.0943	0.0021
$r_{\text{full}}^{\text{MC,full}}$	3.00	8.20	3.91	2.22

Table 6: Performance measures for partonic channels contributing to $gg \rightarrow 3$ jet production at the LHC.

RePost Physics

Substitution

MCNET-21-13

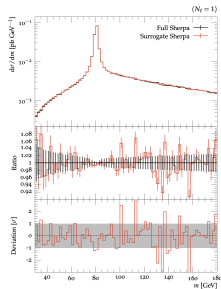
Accelerating Monte Carlo event generation – rejection sampling using neural network event-weight estimates

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September 27, 2023

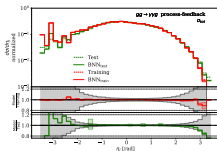
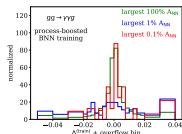
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Speeding up amplitudes [precision regression]

- loop-amplitudes expensive
 - interpolation standard
- Precision NN-amplitudes



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Optimising simulations for diphoton production at hadron colliders using amplitude neural networks

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ABSTRACT: Machine learning technology has the potential to dramatically optimise event generation and simulation. We continue to investigate the use of neural networks to approximate matrix elements for high-multiplicity scattering processes. We focus on the case of loop-induced diphoton production through gluon fusion, and develop a modular simulation method that can be applied to hadron collider observables. Neural networks are trained using the one-loop amplitudes implemented in the *Black*++ library, and interfaced to the *Sherpa* Monte Carlo event generator, where we perform a detailed study for 2 → 3 and 2 → 4 scattering problems. We also consider how the trained networks perform when varying the kinematic cuts affecting the phase space and the reliability of the neural network simulations.



Invertible event generation

Precision NN-generators [Bayesian generative models]

- control through discriminator [GAN-like]
- uncertainties through Bayesian networks

→ Flow, diffusion, transformer

SciPost Physics

Generative Networks for Precision Enthusiasts

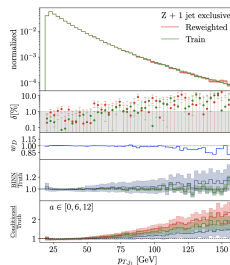
Arijj Butte¹, Theo Heinzl², Sander Himmerickx¹, Tobias Kuhn¹,
Tizian Plehn¹, Armand Roussel², and Sophia Viret¹

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November 16, 2021

Abstract

Generative networks are opening new avenues in fast event generation for the LHC. We show how generative flow networks can reach percent-level precision for kinematic distributions, how they can be trained jointly with a discriminator, and how this discriminator improves the generation. Our joint training relies on a novel coupling of the two networks which does not require a Nash equilibrium. We then estimate the generation uncertainties through a Bayesian network setup and through conditional data augmentation, while the discriminator ensures that there are no systematic inconsistencies compared to the training data.

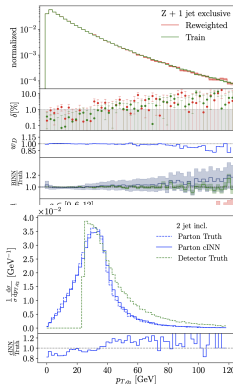
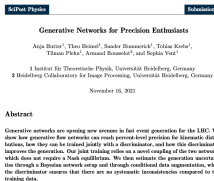


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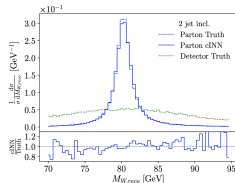
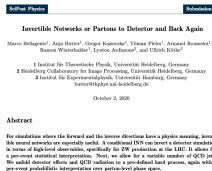
→ Flow, diffusion, transformer



Unfolding and inversion [conditional normalizing flows]

- detector/decays/QCD unfolded
- calibrated inverse sampling

→ Publishing analysis results



Proper theory

Navigating string landscape [reinforcement learning]

- searching for viable vacua
- high dimensions, unknown global structure

→ **Model space sampling**

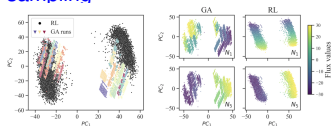


Figure 1: *Left:* Cluster structure in dimensionally reduced flux samples for RL and 25 GA runs (PCA) on all samples of GA and RL. The colors indicate individual GA runs. *Right:* Dependence on flux (input) values (N_3 and N_5 respectively) in relation to principal components for a PCA fit of the individual output of GA and RL.

Probing the Structure of String Theory Vacua with Genetic Algorithms and Reinforcement Learning

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Abstract

Identifying string theory vacua with desired physical properties at low energies requires searching through high-dimensional solution spaces – collectively referred to as the string landscape. We highlight that this search problem is amenable to reinforcement learning and genetic algorithms. In the context of flux vacua, we are able to reveal novel features (suggesting previously unidentified symmetries) in the string theory solutions required for properties such as the string coupling. In order to identify these features robustly, we combine results from both search methods, which we argue is imperative for reducing sampling bias.



Proper theory

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- searching for viable vacua
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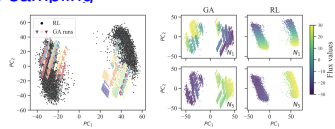


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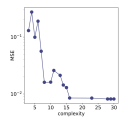
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Learning formulas [genetic algorithm, symbolic regression]

- approximate numerical function through formula
 - example: score/optimal observables
- **PySR**

comp	dx/function	MSE
3	1 $\alpha \Delta \phi$	$1.30 \cdot 10^{-1}$
4	1 $\sin(\alpha \Delta \phi)$	$2.75 \cdot 10^{-1}$
5	1 $\alpha \Delta \phi \mp_{p,1}$	$9.50 \cdot 10^{-2}$
6	1 $-\mp_{p,1} \sin(\Delta \phi + a)$	$1.90 \cdot 10^{-1}$
7	1 $(-\mp_{p,1} - a) \sin(\sin(\Delta \phi))$	$5.63 \cdot 10^{-2}$
8	1 $(a - \mp_{p,1}) \mp_{p,2} \sin(\Delta \phi)$	$1.61 \cdot 10^{-2}$
14	2 $\mp_{p,1} (\alpha \Delta \phi - \sin(\sin(\Delta \phi))) (\mp_{p,2} + b)$	$1.44 \cdot 10^{-2}$
15	3 $-(\mp_{p,2} (\alpha \Delta \phi^2 + \mp_{p,1}) + b) \sin(\Delta \phi + c)$	$1.30 \cdot 10^{-2}$
16	4 $-\mp_{p,1} (a - b \Delta \phi) (\mp_{p,2} + c) \sin(\Delta \phi + d)$	$8.50 \cdot 10^{-3}$
28	7 $(\mp_{p,2} + a) ((\mp_{p,1} (c - \Delta \phi) - \mp_{p,1} (\Delta \phi^2 + \mp_{p,2} + f) \sin(\Delta \phi + g)))$	$8.18 \cdot 10^{-3}$

Table 8: Score hall of fame for simplified WBF Higgs production with $f_{W\tilde{W}} = 0$, including a optimization fit.



SciPost Physics Submission

Back to the Formula — LHC Edition

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¹ Institut für Theoretische Physik, Universität Heidelberg, Germany
² Center for Data Science, New York University, New York, United States
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 November 16, 2021

Abstract

While neural networks offer an attractive way to numerically encode functions, actual formulas remain the language of theoretical particle physics. We use symbolic regression trained on matrix-element information to extract, for instance, optimal LHC observables. This way we invert the usual simulation paradigm and extract easily interpretable formulas from complex simulated data. We introduce the method using the effect of a dimension-8 coefficient on associated ZH production. We then validate it for the known case of CP-violation in weak-boson-fusion Higgs production, including interference effects.



Generative-network revolution

Generative networks

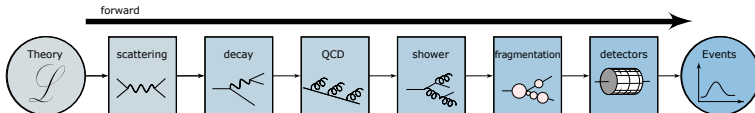
- generate **new** images, text blocks, LHC events
- encode density in target space
sample from Gaussian into target space
- reproduce training data, statistically independently
- include uncertainty on estimated density [Bayesian NN]



Generative-network revolution

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- generate **new** images, text blocks, LHC events
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 - Variational Autoencoder
→ low-dimensional physics, high-dimensional representation
 - Generative Adversarial Network
→ generator trained by discriminator
 - Normalizing Flow/Diffusion Model
→ stable (bijective) mapping
 - Generative Transformer
→ learning correlations successively
- **Pick model for purpose**



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Fundamental question: GANplification

- first generated instances reproducing structures
- too many generated instances reproducing noise?



Precision generator

Phase-space generators [typical LHC task]

- training from event samples
no energy-momentum conservation
- every correlation counts
- $Z_{\mu\mu} + \{1, 2, 3\}$ jets [Z-peak, variable jet number, jet-jet topology]



Precision generator

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INN-generator

- stable bijective mapping

$$\text{latent } r \sim p_{\text{latent}} \quad \begin{array}{c} \xrightarrow{G_{\theta}(r)} \\ \xleftarrow{\bar{G}_{\theta}(x)} \end{array} \quad \text{phase space } x \sim p_{\text{data}}$$

- tractable Jacobian

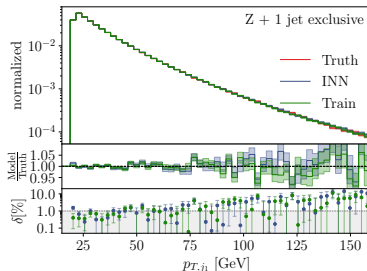
$$dx \, p_{\text{model}}(x) = dr \, p_{\text{latent}}(r)$$

$$p_{\text{model}}(x) = p_{\text{latent}}(\bar{G}_{\theta}(x)) \left| \frac{\partial \bar{G}_{\theta}(x)}{\partial x} \right|$$

- likelihood loss

$$\mathcal{L}_{\text{INN}} = - \left\langle \log p_{\text{model}}(x) \right\rangle_{p_{\text{data}}}$$

⇒ Per-cent precision possible



Controlled precision generator

Best of GANs: discriminator

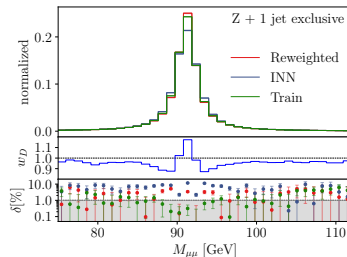
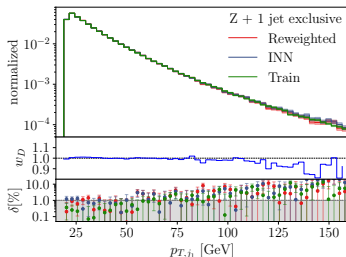
- $D = 0$ (generator) vs $D = 1$ (training)
- NP-optimal discriminator

$$D(x) \rightarrow \frac{p_{\text{data}}(x)}{p_{\text{data}}(x) + p_{\text{model}}(x)} \rightarrow \frac{1}{2}$$

- learned event weight

$$w(x) \rightarrow \frac{D(x)}{1 - D(x)} = \frac{p_{\text{data}}(x)}{p_{\text{model}}(x)} \rightarrow 1$$

⇒ Dual purpose: control and reweight



Controlled precision generator

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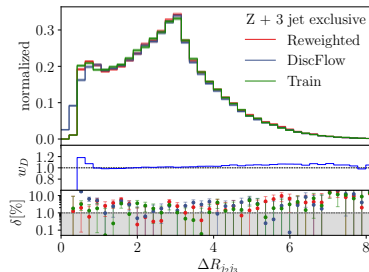
⇒ Dual purpose: control and reweight

Joint training [GAN inspiration]

- GAN-like training unstable [Nash equilibrium??]
- coupling through weights

$$\mathcal{L} = - \int dx \frac{p_{\text{data}}^{\alpha+1}(x)}{p_{\text{model}}^{\alpha}(x)} \log \frac{p_{\text{model}}(x)}{p_{\text{data}}(x)}$$

⇒ Unweighted, controlled events

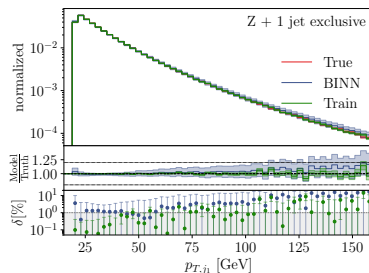


Precision generator with uncertainties

Bayesian network generator

- network with weight distributions [Gal (2016)]
- sample weights [defining error bar]
- working for regression, classification
- frequentist: efficient ensembling

⇒ Training-related error bars



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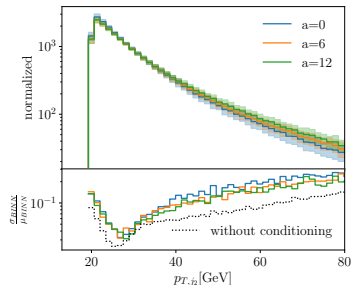
Theory uncertainties

- BNN regression/classification: systematics from data augmentation
- systematic uncertainties in tails

$$w = 1 + a \left(\frac{p_{T,j_1} - 15 \text{ GeV}}{100 \text{ GeV}} \right)^2$$

- augment training data [$a = 0 \dots 30$]
- train conditionally on a
- error bar from sampling a

⇒ Systematic/theory error bars



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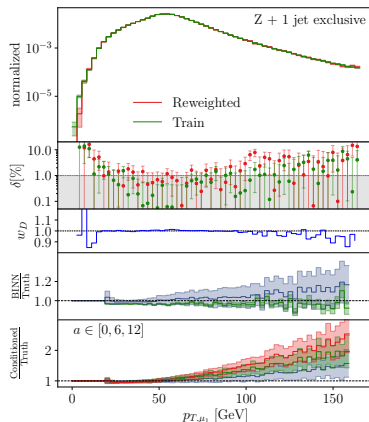
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Testing generative networks

Compare network to training/test data

- supervised: histogram deviation [or pull]
- unsupervised density \rightarrow histogram discriminator

$$w(x_i) = \frac{D(x_i)}{1 - D(x_i)} = \frac{p_{\text{data}}(x_i)}{p_{\text{model}}(x_i)}$$

\rightarrow Using interpretable phase space



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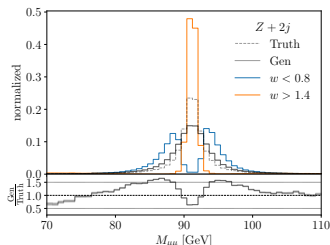
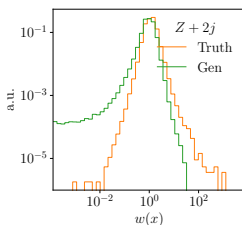
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\rightarrow Using interpretable phase space

Applied to event generators [also jets, calorimeter showers]

- shape and width of w -histogram
- pattern in (interpretable) phase space?



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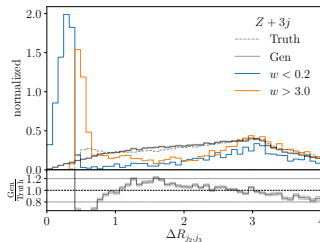
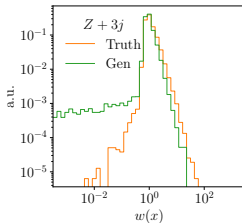
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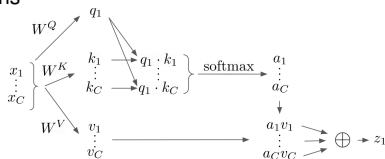
\rightarrow Generative xAI for LHC physicists



JetGPT

Correlations through self-attention

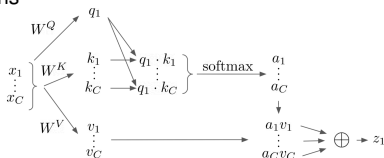
- think of data as bins in phase-space directions
self-attention: encode relation between bins
input x , learn relation $x_i \leftrightarrow x_j$
- latent query representation $q = W^Q x$
latent key representation $k = W^K x$
define correlation as $A_{ij} = q_i \cdot k_j$
- latent value representation $v = W^V x$
output $z = A v$



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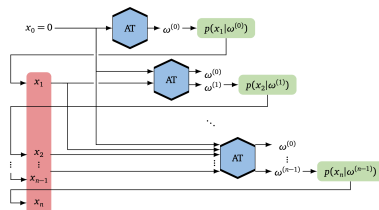


Autoregressive transformer

- factorized density

$$p_{\text{model}}(x|\theta) = \prod_i p(x_i | x_1, \dots, x_{i-1})$$

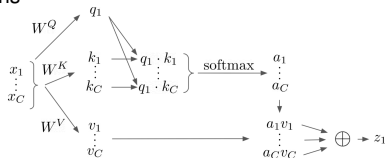
- bins \rightarrow Gaussian mixture model
 - autoregressive $A_{ij} = 0$ for $j > i$
- \rightarrow Bayesian version for uncertainties



JetGPT

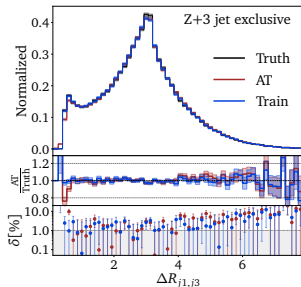
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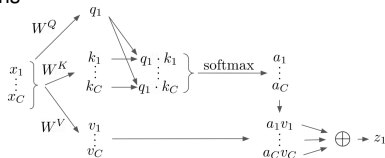
- sometimes you win...



JetGPT

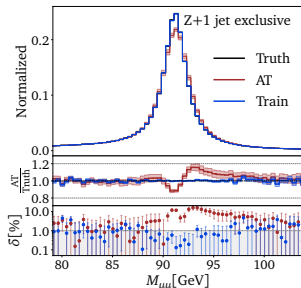
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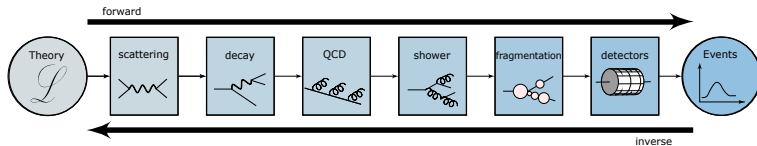
- sometimes you win...
- ...and sometimes there is work to do...



Inverse simulation

Invertible ML-simulation

- forward: $r \rightarrow$ events trained on model
- inverse: $r \rightarrow$ anything trained on model, conditioned on event



Inverse simulation

Invertible ML-simulation

- forward: $r \rightarrow$ events trained on model
- inverse: $r \rightarrow$ anything trained on model, conditioned on event
- individual steps known problems

detector unfolding

unfolding to QCD parton means jet algorithm

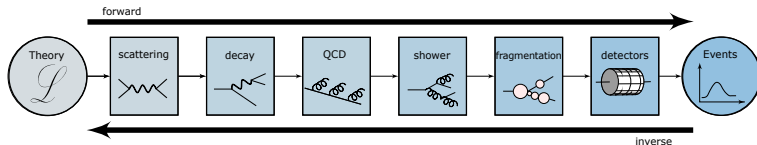
unfolding jet radiation known combinatorics problem

unfolding to hard process standard in top groups [needed for global analyses]

matrix element method an old dream

- improved through coherent ML-method
- free choice of data-theory inference point

→ Transformative progress for HL-LHC



Inverting to QCD

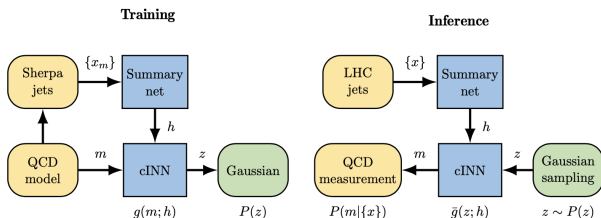
cINN for inference [Bieringer, Butter, Heimgel, Höche, Köthe, TP, Radev]

- condition jets with QCD parameters
- train model parameters \rightarrow Gaussian latent space
- test Gaussian sampling \rightarrow parameter measurement
- beyond C_A vs C_F

$$P_{qq} = C_F \left[D_{qq} \frac{2z(1-y)}{1-z(1-y)} + F_{qq}(1-z) + C_{qq}yz(1-z) \right]$$

$$P_{gg} = 2C_A \left[D_{gg} \left(\frac{z(1-y)}{1-z(1-y)} + \frac{(1-z)(1-y)}{1-(1-z)(1-y)} \right) + F_{gg}z(1-z) + C_{gg}yz(1-z) \right]$$

$$P_{gq} = T_R \left[F_{gq} (z^2 + (1-z)^2) + C_{gq}yz(1-z) \right]$$



Inverting to QCD

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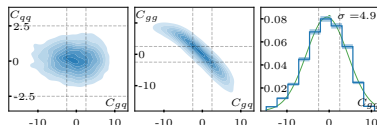
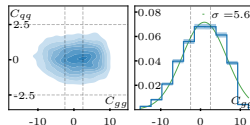
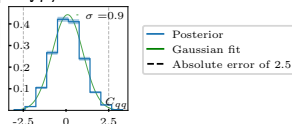
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$$P_{gq} = T_R \left[F_{qq} (z^2 + (1-z)^2) + C_{gq}yz(1-z) \right]$$

- idealized shower [Sherpa]
- More ML-opportunities...



ML for LHC Theory

ML-applications

- just another numerical tool for a numerical field
- driven by money from data science and medical research
- goals are...
 - ...improve established tasks
 - ...develop new tools for established tasks
 - ...transform through new ideas
- xAI through...
 - ...precision control
 - ...uncertainties
 - ...symmetries
 - ...formulas

→ Lots of fun with hard LHC problems

Modern Machine Learning for LHC Physicists

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Abstract

Modern machine learning is transforming particle physics, faster than we can follow, and bullying its way into our numerical tool box. For young researchers it is crucial to stay on top of this development, which means applying cutting-edge methods and tools to the full range of LHC physics problems. These lecture notes are meant to lead students with basic knowledge of particle physics and significant enthusiasm for machine learning to relevant applications as fast as possible. They start with an LHC-specific motivation and a non-standard introduction to neural networks and then cover classification, unsupervised classification, generative networks, and inverse problems. Two themes defining much of the discussion are well-defined loss functions reflecting the problem at hand and uncertainty-aware networks. As part of the applications, the notes include some aspects of theoretical LHC physics. All examples are chosen from particle physics publications of the last few years. Given that these notes will be outdated already at the time of submission, the week of ML4lets 2022, they will be updated frequently.



Learning optimal observables

Measure model parameter θ optimally [Butter, TP, Soybelman, Brehmer]

- single-event likelihood

$$p(x|\theta) = \frac{1}{\sigma_{\text{tot}}(\theta)} \frac{d^m \sigma(x|\theta)}{dx^m}$$

- expanded in θ around θ_0 , define score

$$\log \frac{p(x|\theta)}{p(x|\theta_0)} \approx (\theta - \theta_0) \left. \nabla_{\theta} \log p(x|\theta) \right|_{\theta_0} \equiv (\theta - \theta_0) t(x|\theta_0) \equiv (\theta - \theta_0) \phi^{\text{opt}}(x)$$

- to leading order at parton level

$$p(x|\theta) \approx |\mathcal{M}|_0^2 + \theta |\mathcal{M}|_{\text{int}}^2 \quad \Rightarrow \quad t(x|\theta_0) \sim \frac{|\mathcal{M}|_{\text{int}}^2}{|\mathcal{M}|_0^2}$$

\Rightarrow And including everything?



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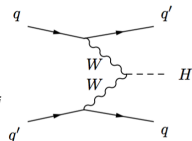
CP-violating Higgs production

- unique CP-observable

$$t \propto \epsilon_{\mu\nu\rho\sigma} k_1^\mu k_2^\nu q_1^\rho q_2^\sigma \text{sign}[(k_1 - k_2) \cdot (q_1 - q_2)] \xrightarrow{\text{lab frame}} \sin \Delta\phi_{jj}$$

- CP-effect in $\Delta\phi_{jj}$
D6-effect in $p_{T,j}$

\Rightarrow Established LHC task



Symbolic regression

Symbolic regression of score [PySR (M Cranmer) + final fit]

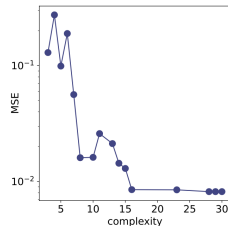
- function to approximate $t(x|\theta)$
- phase space parameters $x_p = p_T/m_H, \Delta\eta, \Delta\phi$ [node]
- operators $\sin x, x^2, x^3, x + y, x - y, x * y, x/y$ [node]
- represent formula as tree [complexity = number of nodes]

⇒ **Figures of merit**

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n [g_i(x) - t(x, z|\theta)]^2 \rightarrow \text{MSE} + \text{parsimony} \cdot \text{complexity}$$

Score around Standard Model

compl	dof	function	MSE
3	1	$a \Delta\phi$	$1.30 \cdot 10^{-1}$
4	1	$\sin(a\Delta\phi)$	$2.75 \cdot 10^{-1}$
5	1	$a\Delta\phi x_{p,1}$	$9.93 \cdot 10^{-2}$
6	1	$-x_{p,1} \sin(\Delta\phi + a)$	$1.90 \cdot 10^{-1}$
7	1	$(-x_{p,1} - a) \sin(\sin(\Delta\phi))$	$5.63 \cdot 10^{-2}$
8	1	$(a - x_{p,1}) x_{p,2} \sin(\Delta\phi)$	$1.61 \cdot 10^{-2}$
14	2	$x_{p,1}(a\Delta\phi - \sin(\sin(\Delta\phi)))(x_{p,2} + b)$	$1.44 \cdot 10^{-2}$
15	3	$-(x_{p,2}(a\Delta\eta^2 + x_{p,1}) + b) \sin(\Delta\phi + c)$	$1.30 \cdot 10^{-2}$
16	4	$-x_{p,1}(a - b\Delta\eta)(x_{p,2} + c) \sin(\Delta\phi + d)$	$8.50 \cdot 10^{-3}$
28	7	$(x_{p,2} + a)(bx_{p,1}(c - \Delta\phi) - x_{p,1}(d\Delta\eta + ex_{p,2} + f) \sin(\Delta\phi + g))$	$8.18 \cdot 10^{-3}$



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Score around Standard Model

- expected limits:
very wrong formula
wrong formula
- same within statistical limitation:
right formula
MadMiner

⇒ **Formulas to numerics and back**

