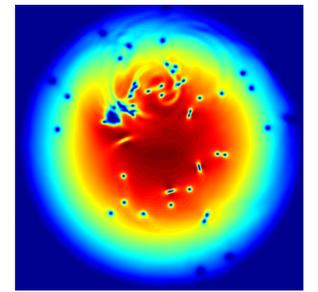


# Two-dimensional Quantum Turbulence in Bose-Einstein condensates



**Brian P. Anderson**

*College of Optical Sciences  
University of Arizona*

## Experiments (*U. Arizona*)

T.W. Neely (*now at U. Queensland*)

Z.L. Newman

E.C. Samson (*now at Ga. Tech.*)

K.E. Wilson

BPA

## Theory and Computation

A.S. Bradley (*U. Otago*)

R. Carretero-González (*San Diego S. U.*)

M.J. Davis (*U. Queensland*)

P.G. Kevrekidis (*U. Mass. at Amherst*)

K.J.H. Law (*U. Warwick*)

S.J. Rooney (*U. Otago*)

E.M. Wright (*U. Arizona*)

## Funding



US National  
Science  
Foundation



US Dept of  
Energy GRF



US Army  
Research Office



NZ Foundation for  
Research, Science,  
and Technology

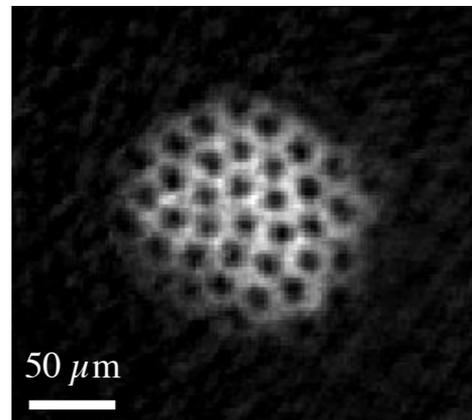


Over 10 years of experiments with vortices in BECs

*Resource Article: Experiments with Vortices in Superfluid Atomic Gases*

**B. P. Anderson, JLTP 161, 574 (2010)**

Lots of work on  
quantum state engineering,  
rotating BECs and vortex  
lattices



Until now there has been relatively little study of

- far-from-equilibrium phenomena
- turbulence
- highly oblate and 2D systems
- vortex manipulation
- vortex dynamics
- persistent currents

**All topics of emphasis in current  
BEC vortex experiments**

Studies of 2D vortex turbulence in superfluids are sparse in comparison to 3D superfluid turbulence: lots still to understand

- What vortex distributions arise in 2DQT ?
- What spectral signatures exist for vortex distributions in 2DQT?
- Can an inverse energy cascade be observed? A double cascade? Is there any connection to an enstrophy cascade?
- Can large-scale flow develop from small-scale forcing?
- Can vortices cluster together, or will annihilation dominate?

## Goals

To understand the range of vortex dynamics and spectra that can occur in forced 2DQT.

Learn a wide range of experimental tools for generating, observing, and manipulating vortices and 2DQT

## Progress so far

- Many ways to generate 2DQT
- Stirring with laser beam: low excitation 2DQT (*expt/num*)
  - simulations: energy spectra, vortex aggregation, suppression of vortex annihilation (*num*)
  - development of large-scale flows (*expt/num*)
- Demonstrated new ways to generate and manipulate vortices (*expt*)

## Why BECs ?

Adjustable trapping geometry: 2D is straightforward

Vortex visualization techniques

Vortex manipulation techniques

Dilute superfluid: modeling, theoretical approaches

Compressible: vortex and/or wave turbulence

Tunable interactions

Single or multiple component wavefunction

...

## Why *not* BECs (?)

Microscopic

*... but much bigger than vortex size*

Short lifetimes / loss of atoms

*... but lifetime can greatly exceed  
vortex dynamics timescales*

Few vortices

*... but plenty to show complex,  
turbulent, chaotic dynamics*

Heating

*... can be minimized with optimal  
forcing*

BECs are not as limiting as they  
might at first appear.

# I. Experimental methods for 2DQT

[preprint \(available by request, soon to be on arXiv\)](#)

**Experimental Methods for Generating Two-Dimensional Turbulence in Bose-Einstein Condensates**

K.E. Wilson, C.E. Samson, Z.L. Newman, T.W. Neely, B.P. Anderson

# II. 2DQT in a BEC: stirring with a laser beam

[arXiv: 1204.1102](#)

**Characteristics of Two-Dimensional Quantum Turbulence in a Compressible Superfluid**

Neely, Bradley, Samson, Rooney, Wright, Law, Carretero, Kevrekidis, Davis, Anderson *Experiment and simulations*

# III. On-demand vortex generation and manipulation

[in preparation](#)

**On-demand vortex generation and manipulation**

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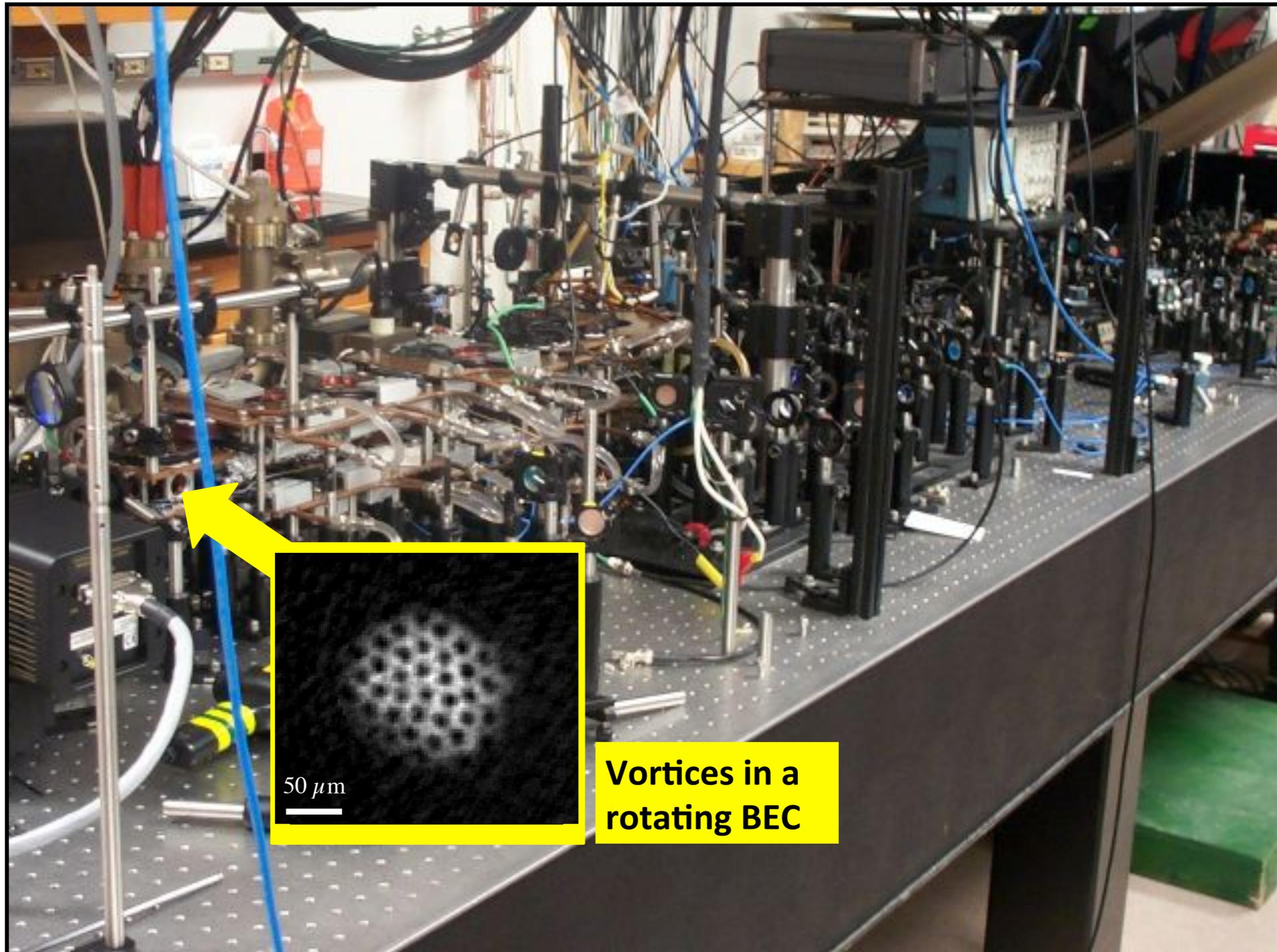
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**On-demand vortex generation and manipulation**

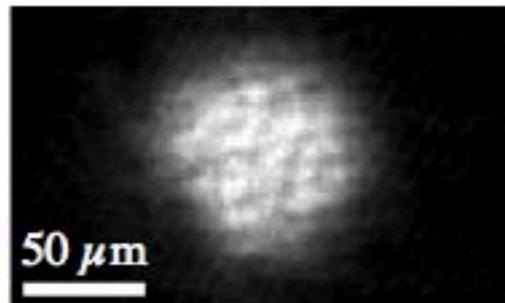
C.E. Samson, K.E. Wilson, Z.L. Newman, B.P. Anderson



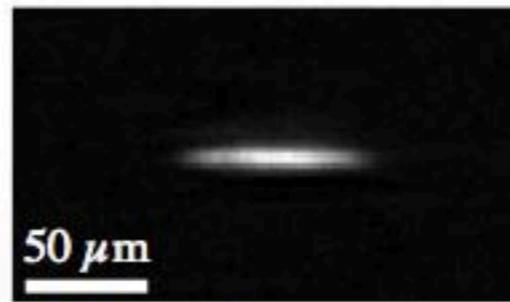
# Our system: Highly oblate trap

Magnetic trap (TOP) + **laser light sheet**

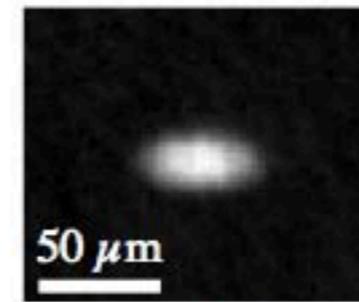
top view



side view



Side view of TOP trap  
(2:1 aspect ratio, *not* highly oblate)



**Vortex bending, tilting inhibited:  
2D vortex dynamics**

Atom:  $^{87}\text{Rb}$  ( $F=1, m_F=-1$ )

$N_c = 2 \times 10^6$

$T_c \sim 100$  nK

$\omega_r = 2\pi \times 8$  Hz

$\omega_z = 2\pi \times 90$  Hz

$\mu = 8 \hbar \omega_z$  (not Q2D, no BKT!)

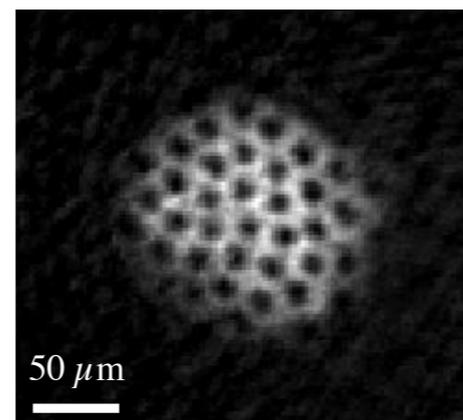
lifetimes  $\sim 50$  sec

$\xi \sim 0.4 \mu\text{m}$

$R \sim 50 \mu\text{m}$

$R/\xi \sim 100$

**Not as limited as it appears from images  
- expansion, dimensionality**

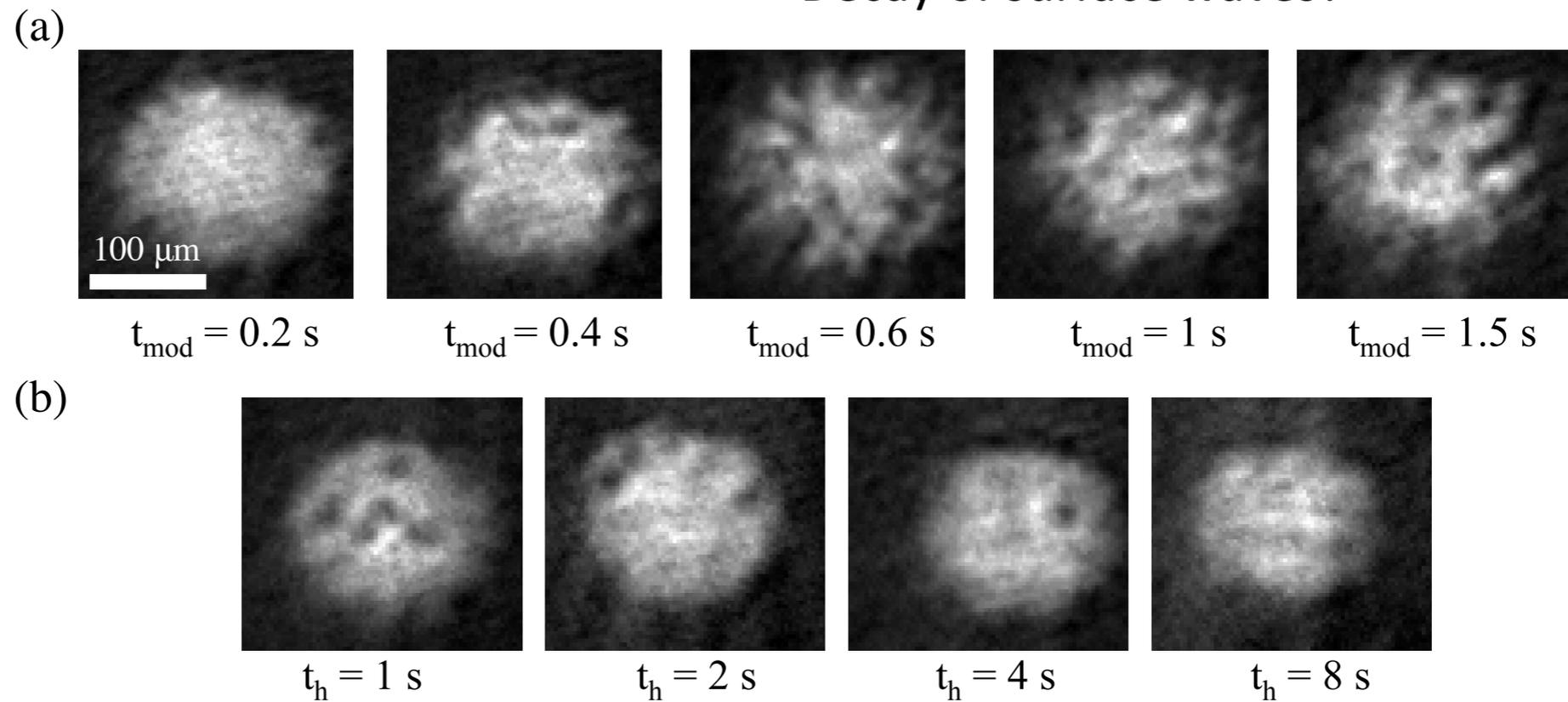


Expansion!!!

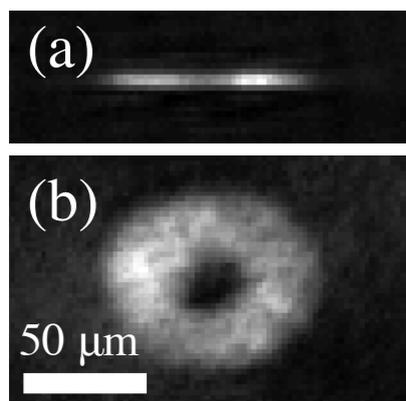
## Modulate the trapping potential (trap frequency modulation)

Decay of surface waves?

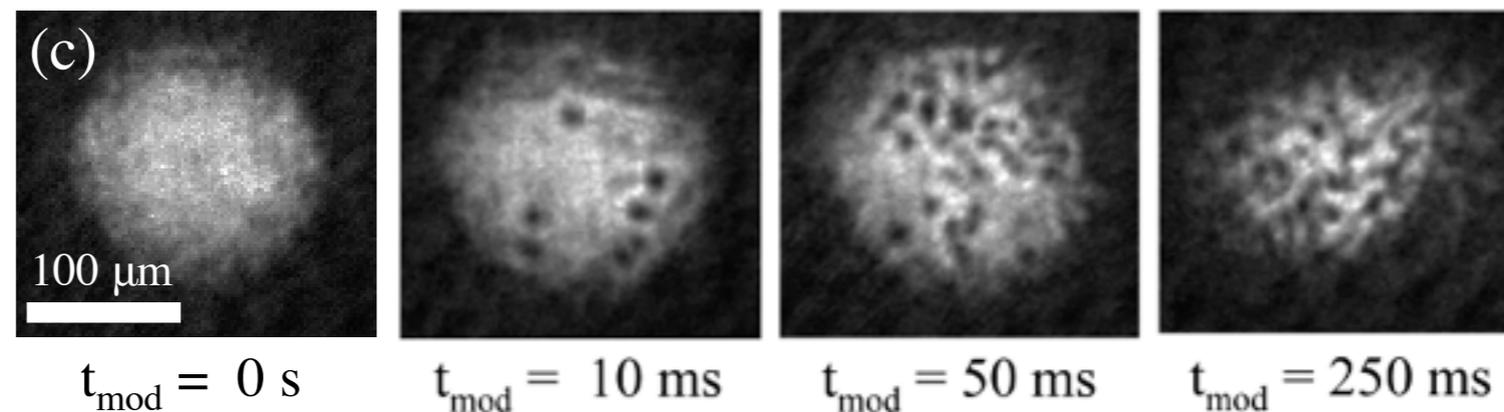
### Harmonic trap



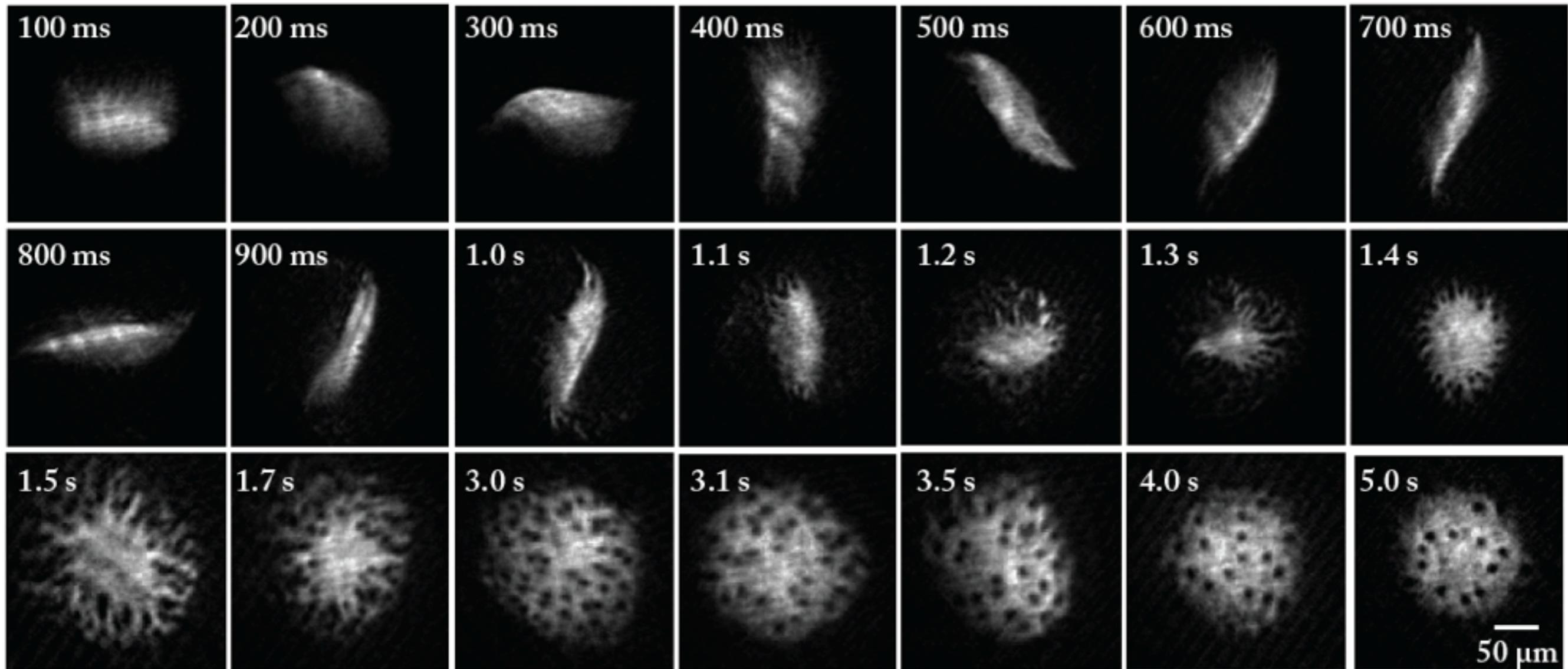
### Toroidal trap



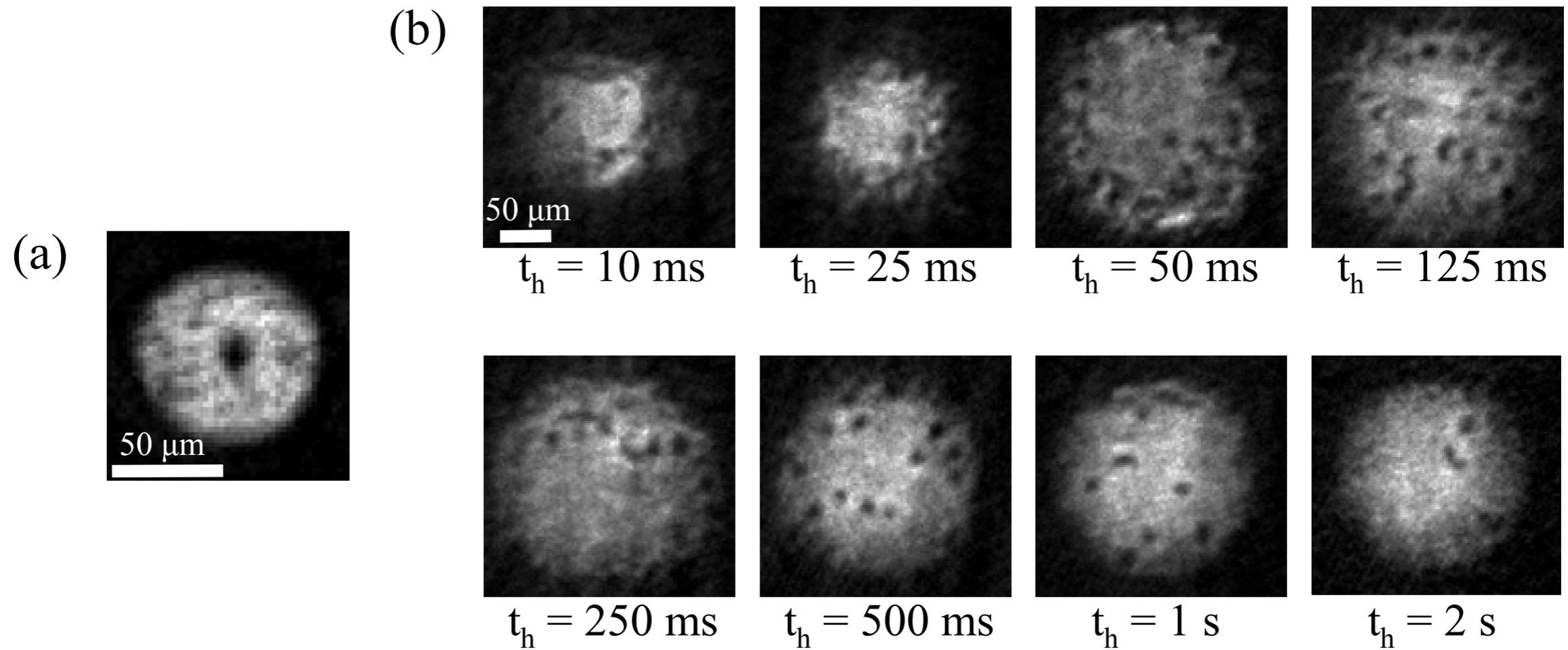
No surface excitation. Vortices nucleated within BEC



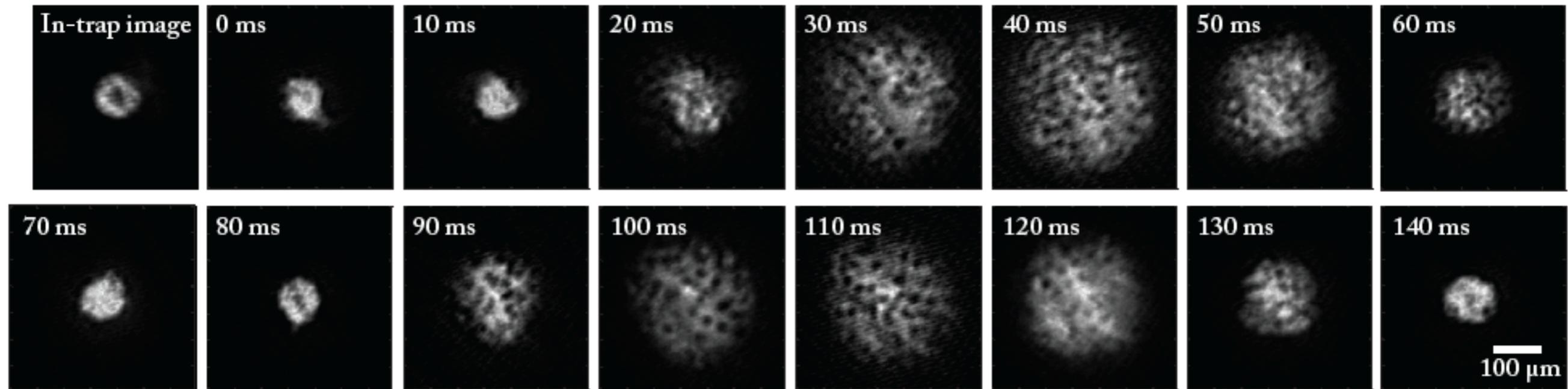
# Spin the highly oblate trap (slightly elliptical)



## Blast BEC with focused laser beam

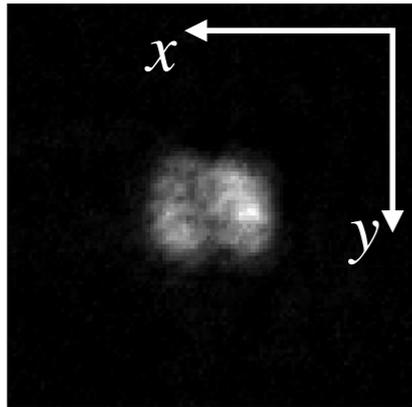


3 cycles of amplitude modulation,  $2 \times \omega_r$ ,  $1/2 \mu$

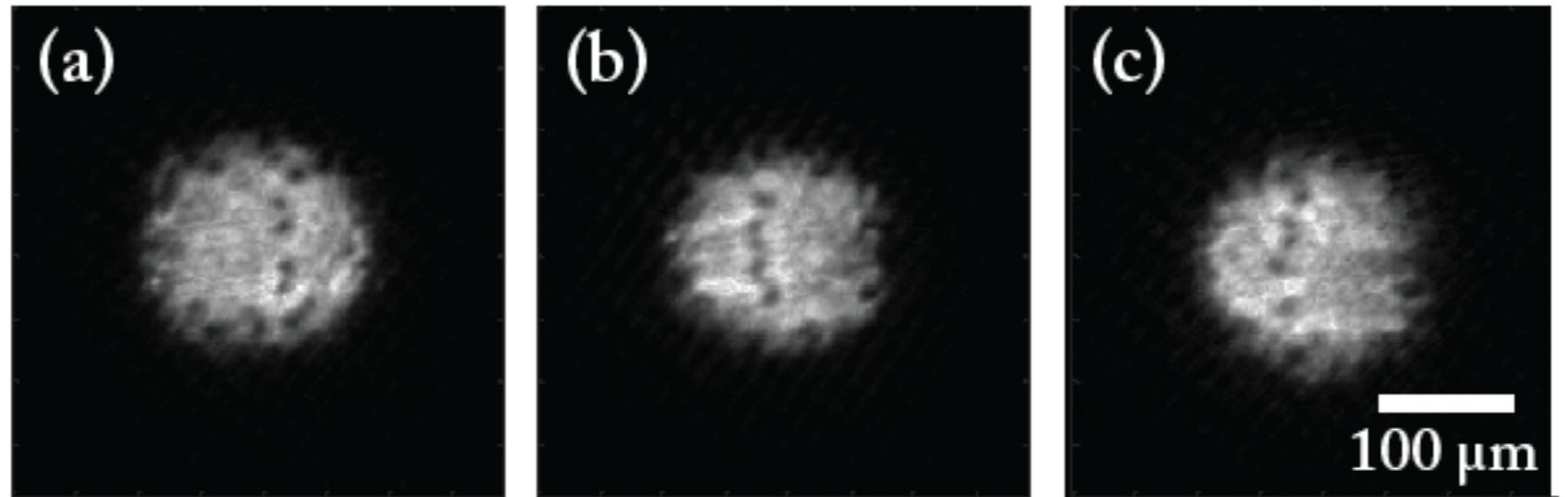


Where do the vortices come from?

Elongated laser beam



One period modulation,  $2 \times \omega_r$



Origin of vortices?

**Making vortices, generating 2DQT turns out to be surprisingly easy!**

**Hard parts:**

- understanding what is going on
- minimizing other excitations, shape oscillations, sound
- reaching a continuous injection of energy, vortices
- understanding the injection mechanisms

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K.E. Wilson, C.E. Samson, Z.L. Newman, T.W. Neely, B.P. Anderson

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Neely, Bradley, Samson, Rooney, Wright, Law, Carretero, Kevrekidis, Davis, Anderson *Experiment and simulations*

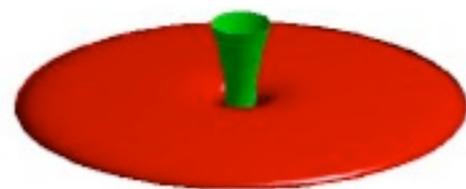
# III. On-demand vortex generation and manipulation

in preparation

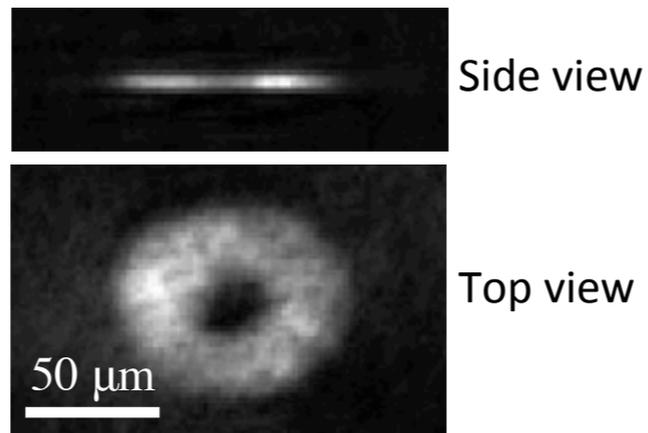
On-demand vortex generation and manipulation

C.E. Samson, K.E. Wilson, Z.L. Newman, B.P. Anderson

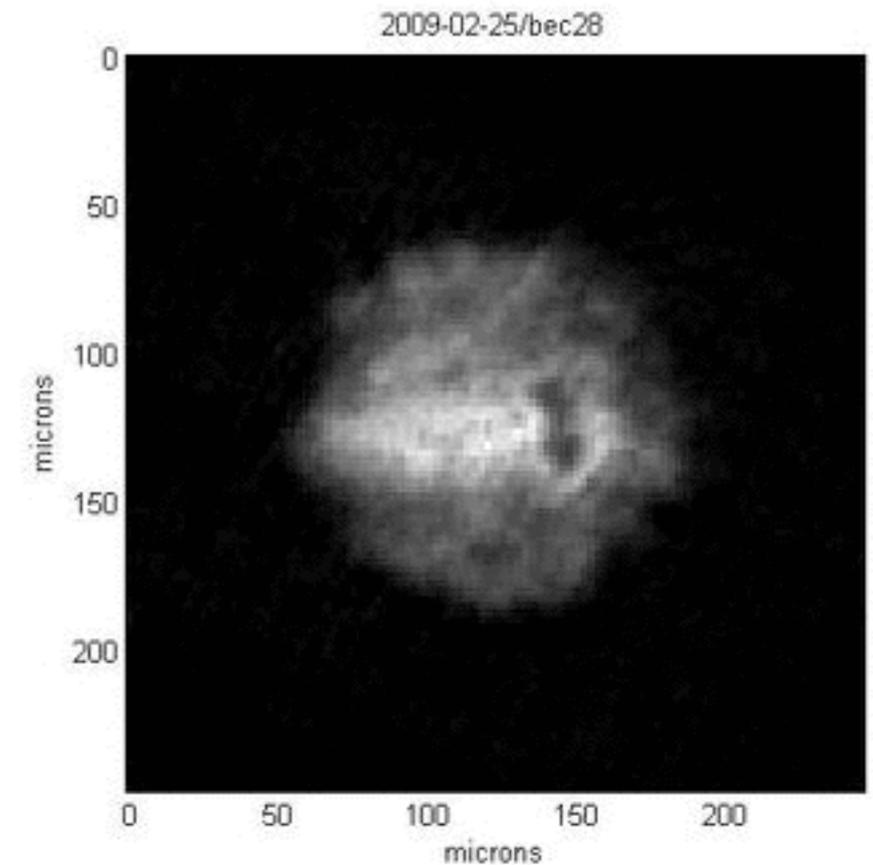
# Stirring the BEC with a laser beam: vortex dipoles



BEC in trap (not expansion)



Beam swipes through BEC to the right. Above a critical velocity ( $\sim 0.1 c$ ) a vortex dipole forms.



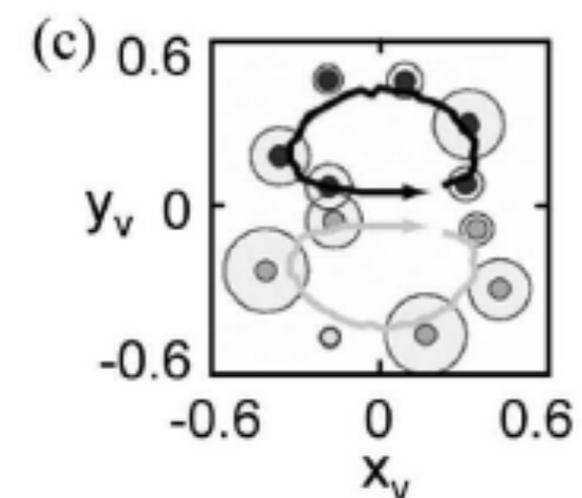
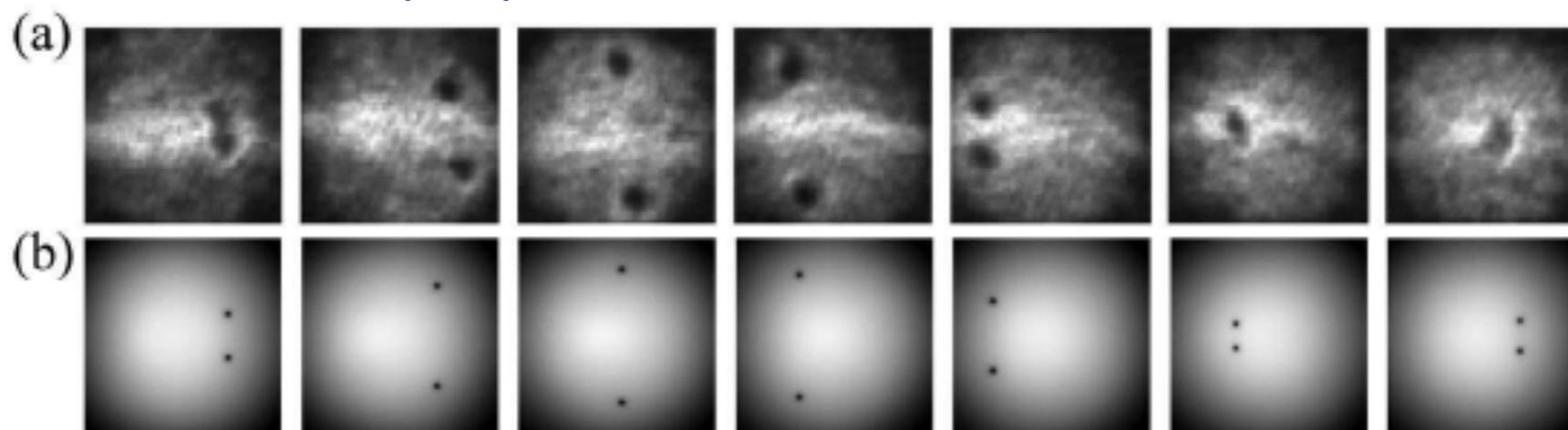
200 ms between images,  $\sim 1.25$  sec orbital period

(1 orbit shown, continuous loop)

## Observation of Vortex Dipoles in an Oblate Bose-Einstein Condensate

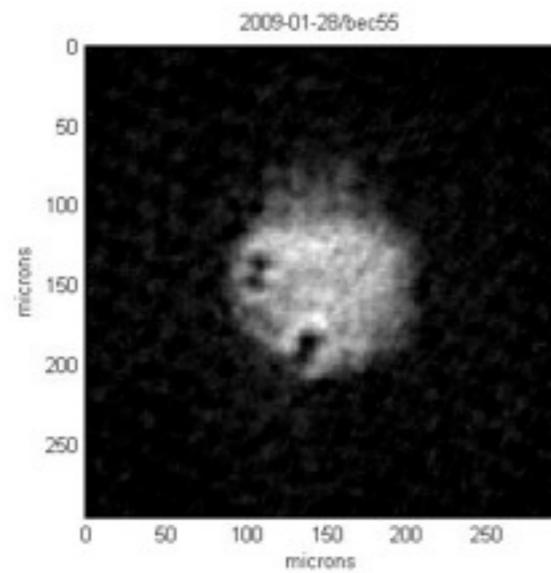
Neely, Samson, Bradley, Davis, Anderson

[PRL 104, 160401 \(2010\)](#)

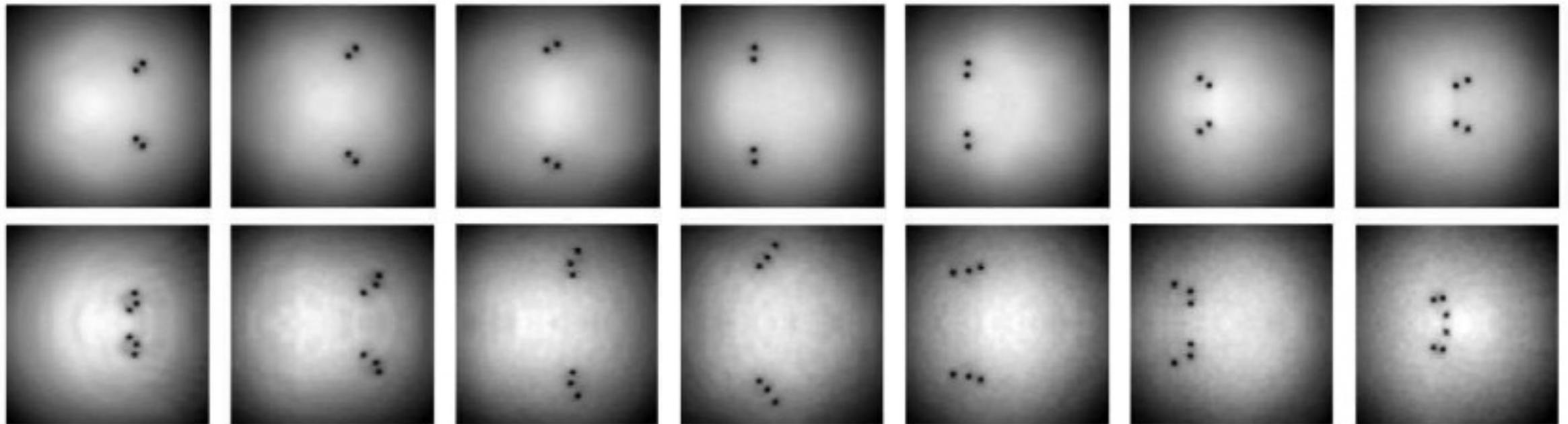
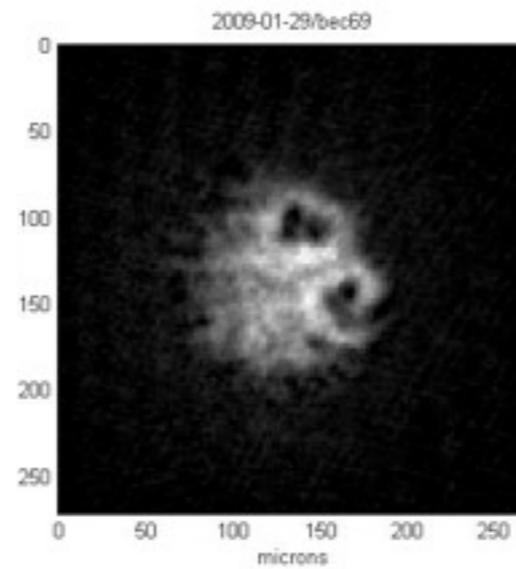


Faster swipes: vortex clusters *can* be supported in BEC and may stick together for long times

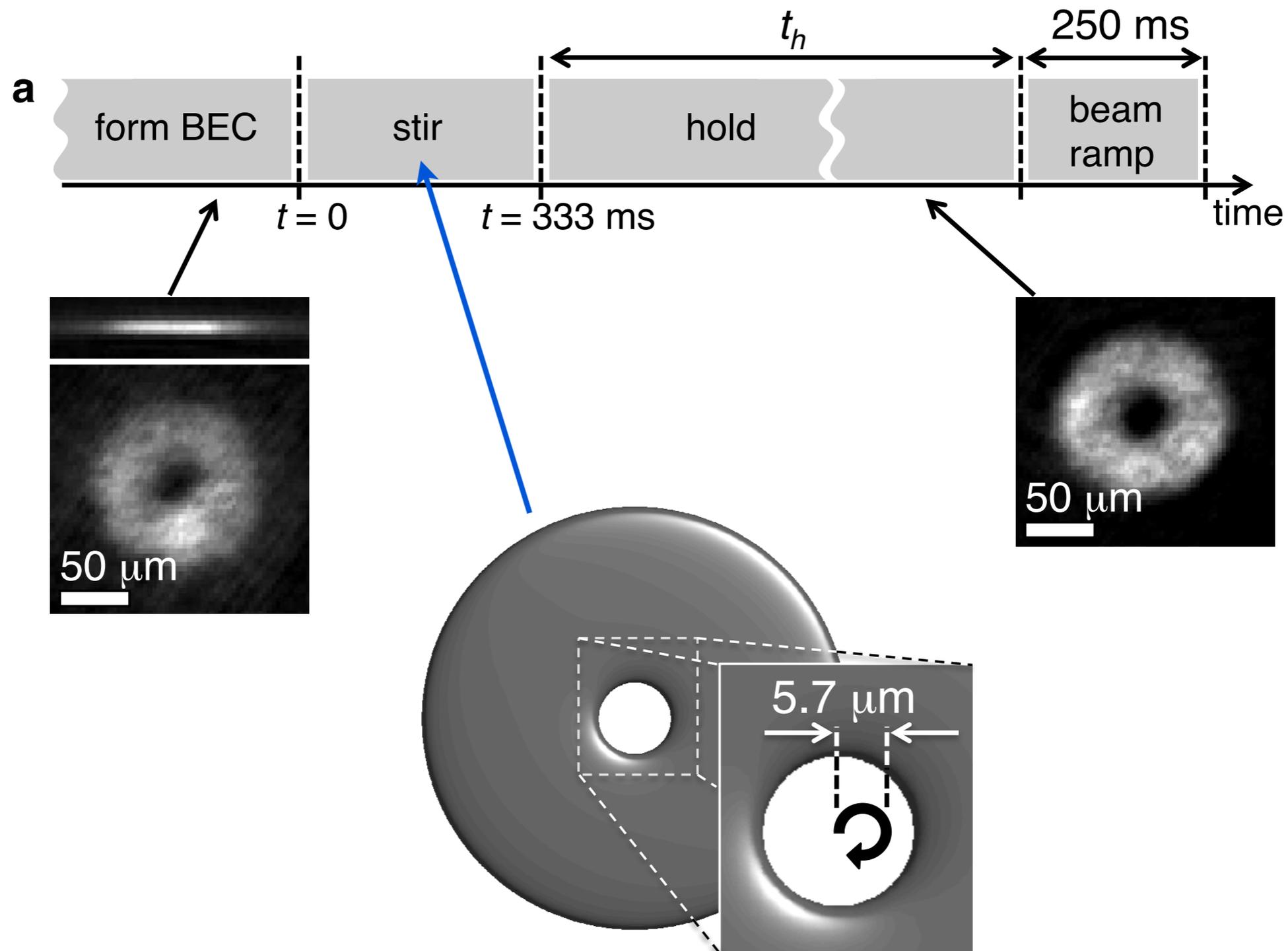
2 vortex pairs



3 pairs



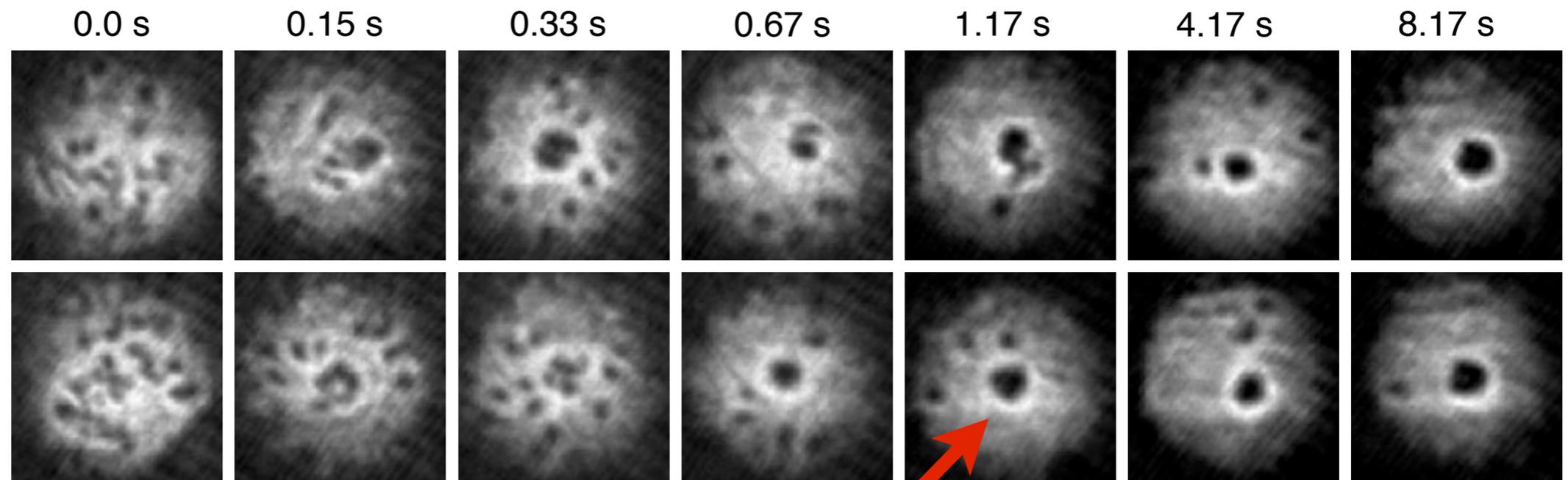
## Inject more vortices: use circular stir



## EXPT

- ramp off beam
- expand

## Hold after end of stir



2DQT

Large fluid-free hole  
= large vorticity  
= flow at large length scale

large-scale  
flows

- Experimental generation of 2DQT from small-scale forcing.
- Development of large-scale flows during decay.

- Can not (yet)
  - determine circulation direction of vortices
  - measure energy spectra
  - determine vortex dynamics (image method is destructive)

## Simulation: Stir using Damped GPE

1. Initial condition: BEC in ground state of toroidal trap
2. Stir, as in the experiment
3. Hold, then observe vortex distribution

# Two-Dimensional Quantum Turbulence

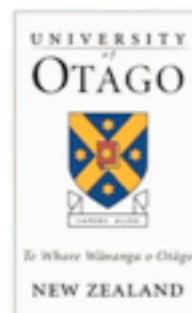
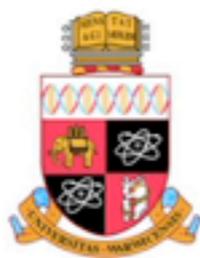
T. W. Neely, A. S. Bradley, E. C. Samson, S. J. Rooney, E. M. Wright,  
K. J. H. Law, R. Carretero-González, P. G. Kevrekidis, M. J. Davis, B. P. Anderson

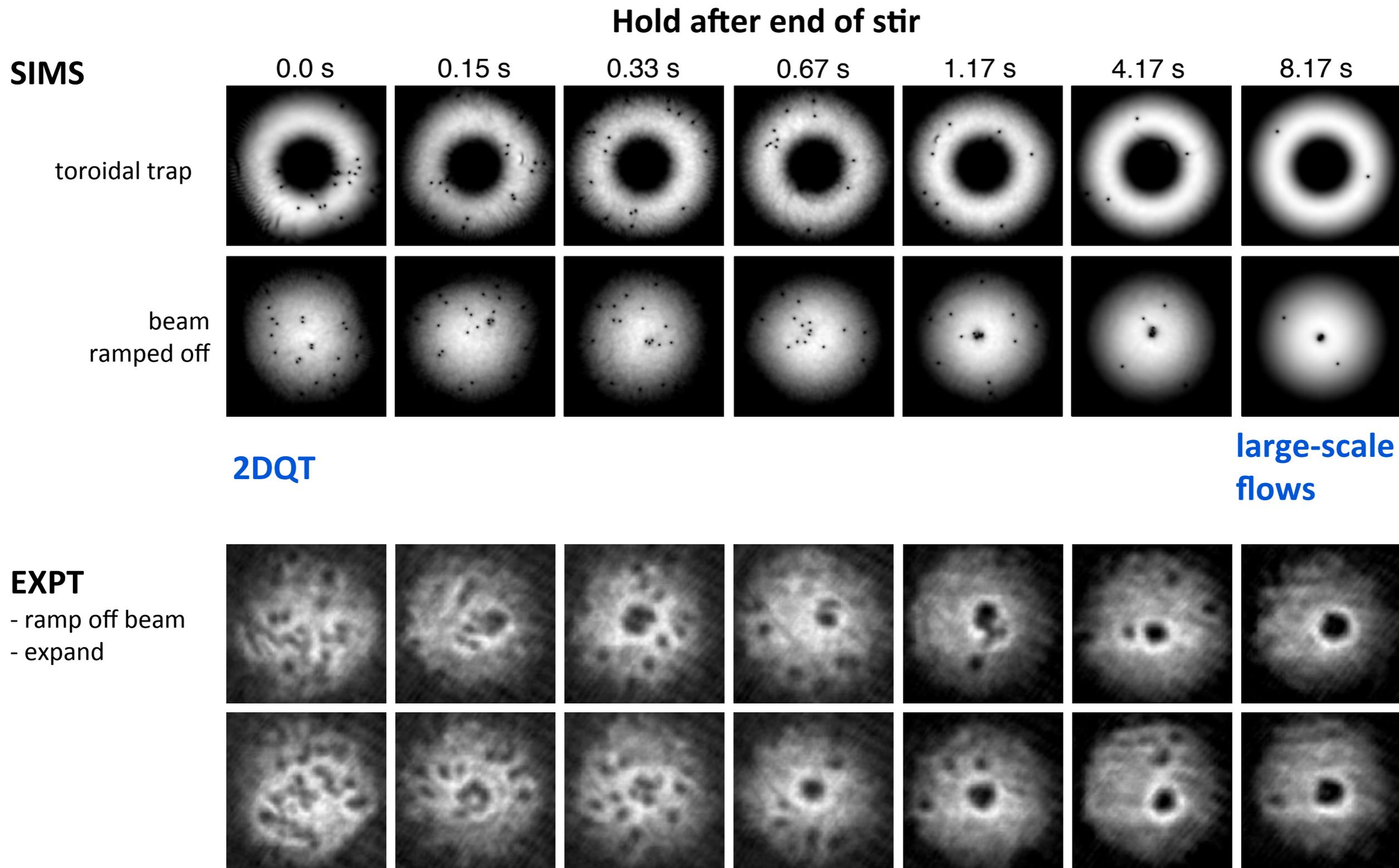
## Movie S1

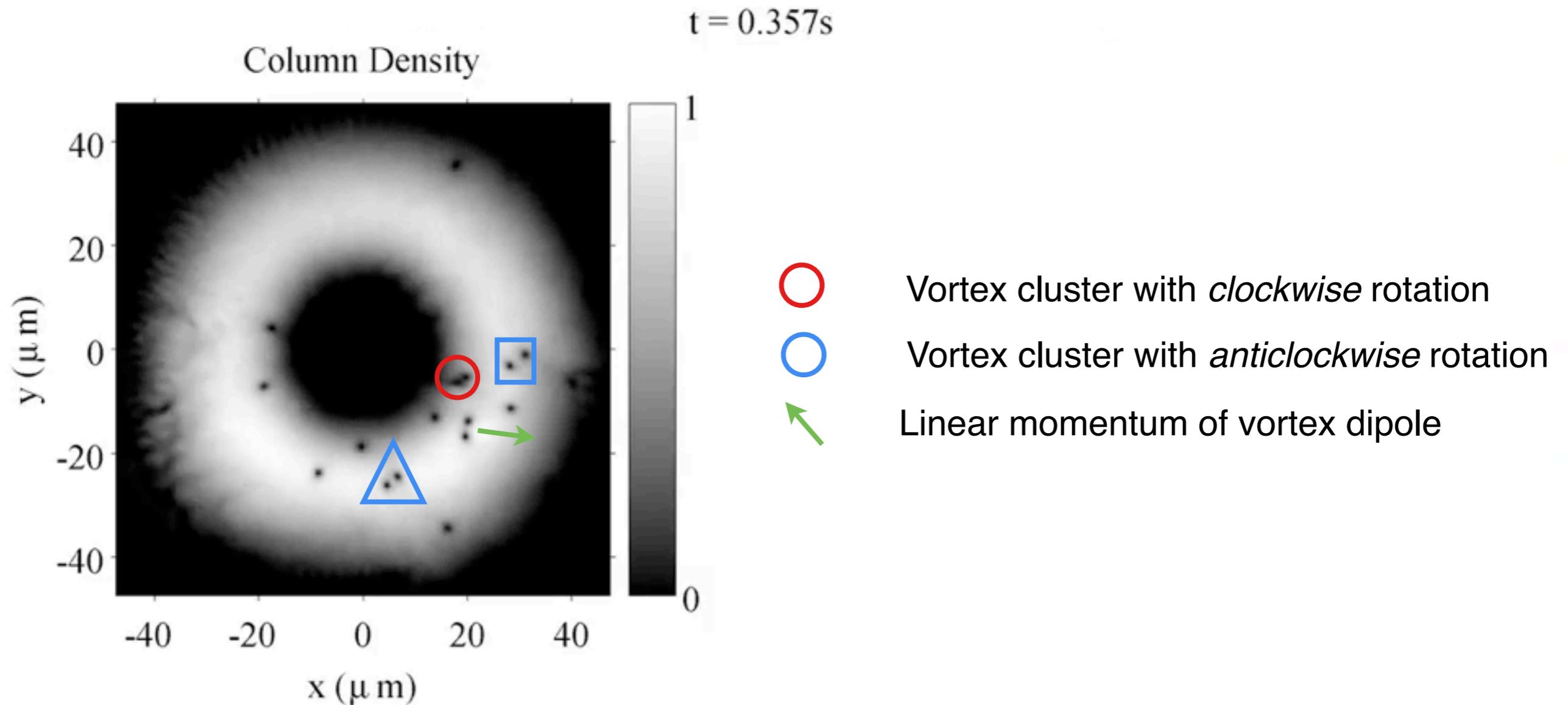
### DPGPE simulation parameters

Trap frequencies  $(\omega_r, \omega_z) = 2\pi \times (8, 90)$  Hz  
Scattering rate  $\gamma = 8 \times 10^{-4}$   
Chemical potential  $\mu = 34\hbar\bar{\omega}$

Gaussian potential height  $U_0 = 58\hbar\bar{\omega}$   
Gaussian potential half width  $\sigma_0 = 16.3 \mu\text{m}$   
Stirring radius  $r_0 = 2.85 \mu\text{m}$

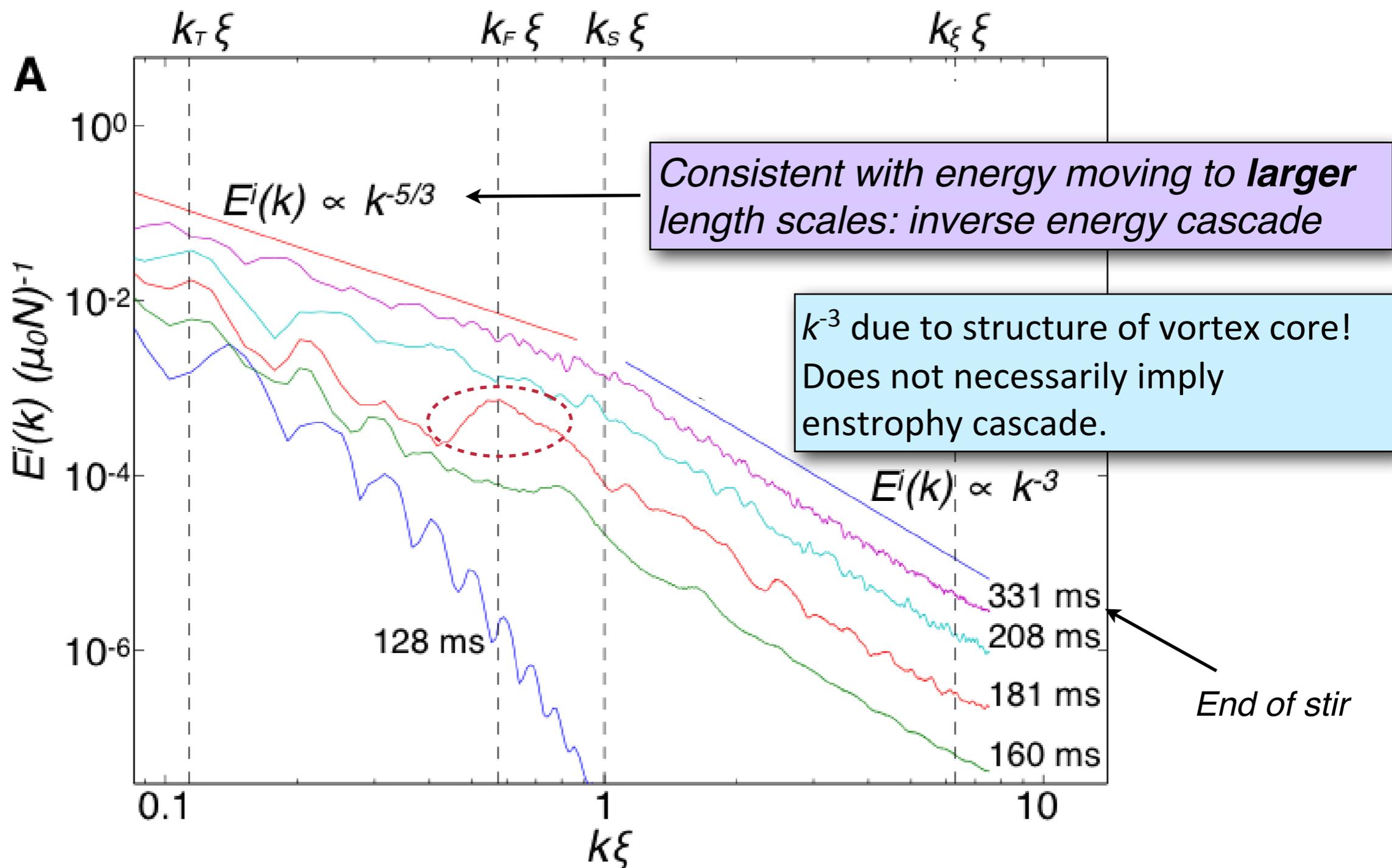






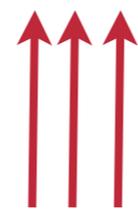
Vortex pair lifetime: over 600 ms,  $\sim 15x$  longer than turnover time

- Observation of vortex clusters in numerics
- Observed suppression of vortex annihilation (vortex number stays constant immediately after stirring)



Consistent with energy moving to **larger** length scales: inverse energy cascade

$k^{-3}$  due to structure of vortex core!  
Does not necessarily imply enstrophy cascade.



Forcing: breakdown of sound into vortices.  
Injection of vortices separated by  $\sim 10\xi$

2DQT in a BEC seems to share striking similarities with 2D classical turbulence

- Experimental generation of 2DQT.
- Development of large-scale flows from small-scale forcing.

- Observation of vortex clusters in numerics
- Observed suppression of vortex annihilation (vortex number stays constant immediately after stirring)

- $k^{-5/3}$  energy spectrum for large length scales ( $k <$  forcing scale)
- $k^{-3}$  energy spectrum for short length scales ( $k >$  forcing scale)
- Observed suppression of vortex annihilation (vortex number stays constant immediately after stirring)

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# III. On-demand vortex generation and manipulation

**in preparation**

**On-demand vortex generation and manipulation**

C.E. Samson, K.E. Wilson, Z.L. Newman, B.P. Anderson

## Precision studies of 2DQT ?

**Goal: Build up vortex distributions one by one.**

A bottom-up approach to vortex dynamics, turbulence.

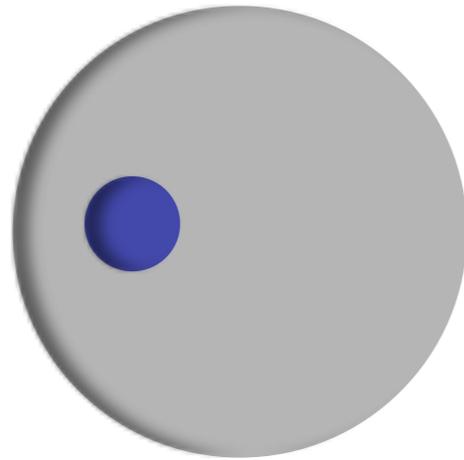
### Investigate:

- dynamics of vortex structures,
- interactions between vortices,
- roles of impurities and trap shape,
- roles of dimensionality of trap
- effects of temperature/thermal bath

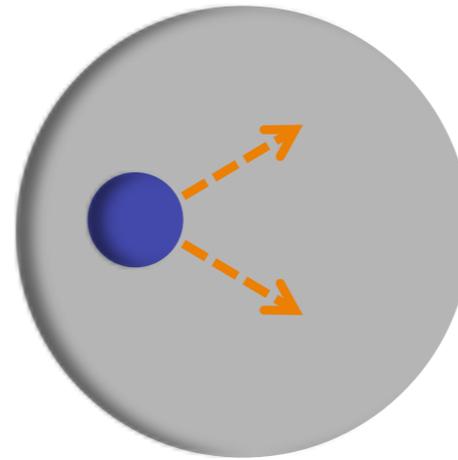
### Initial goals: demonstrate

- (1) On-demand vortex generation
- (2) Manipulation of vortices with laser beams (pinning)
- (2) Control of winding number of pinned vortices

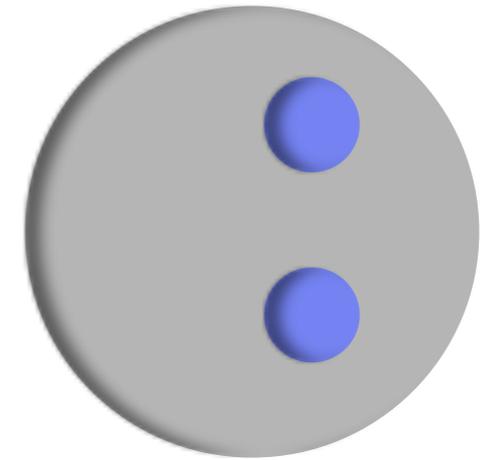




Two coincident  
laser beams



Separate beams

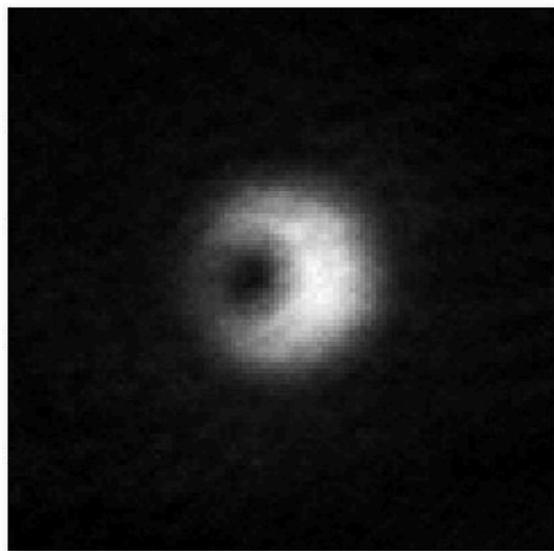


Final positions

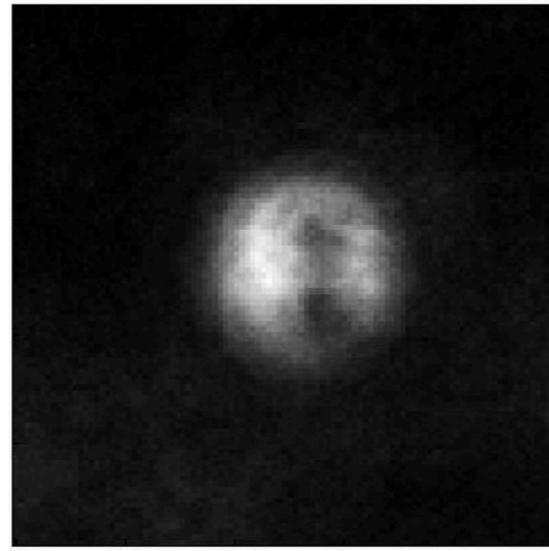
Slow linear swipe,  $\sim 40 \text{ } \mu\text{m/s}$

About 25% of critical velocity for vortex dipole nucleation ( $180 \text{ } \mu\text{m/s}$ )

Prior to swipe

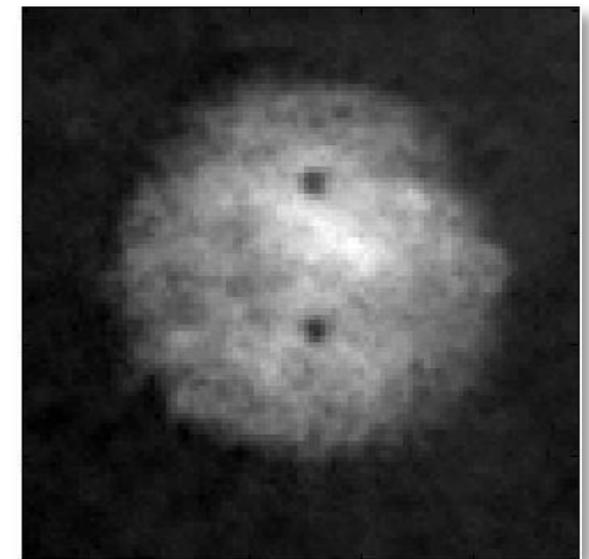


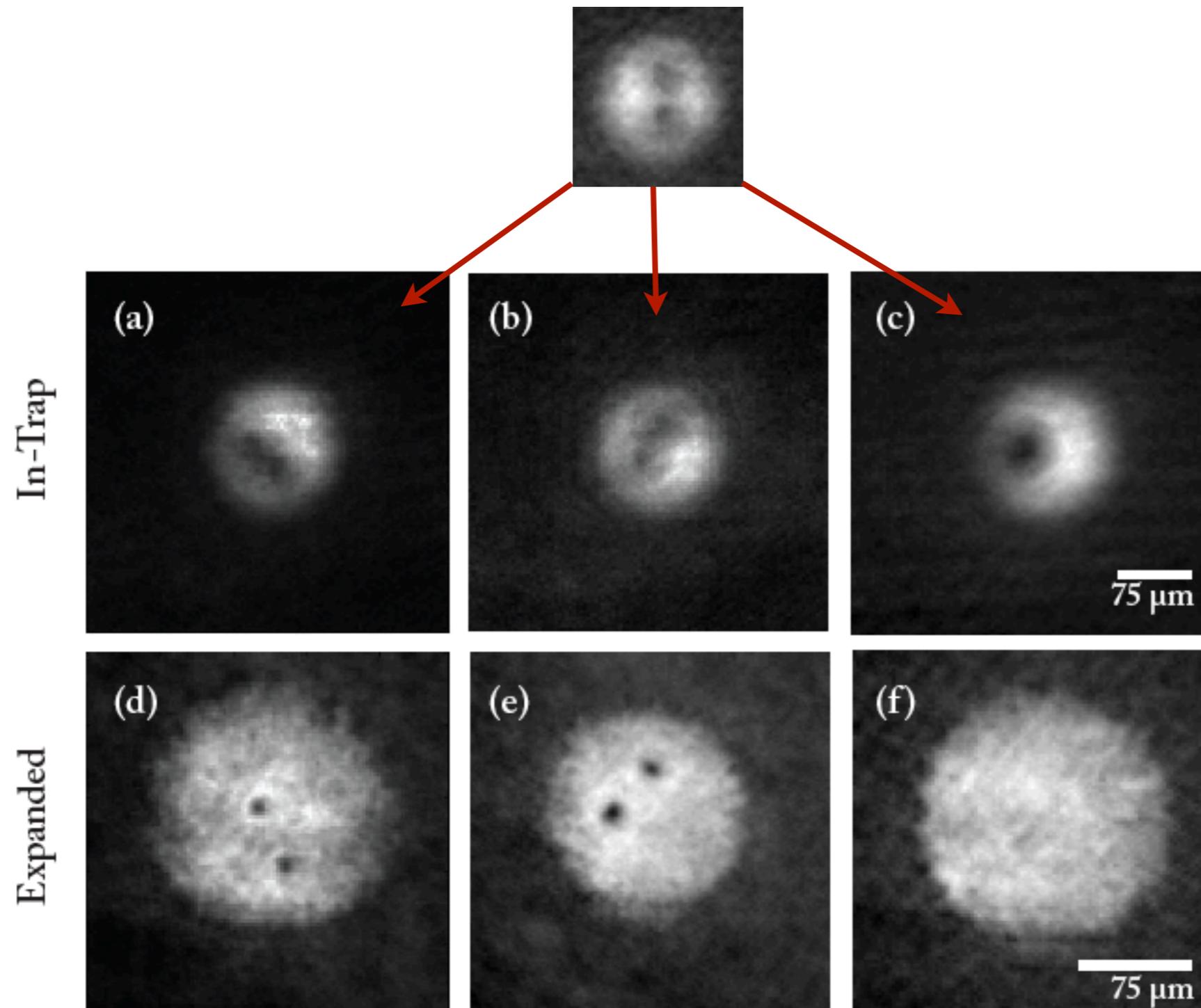
Final beam positions



Trapped BECs

Expanded BEC with vortices





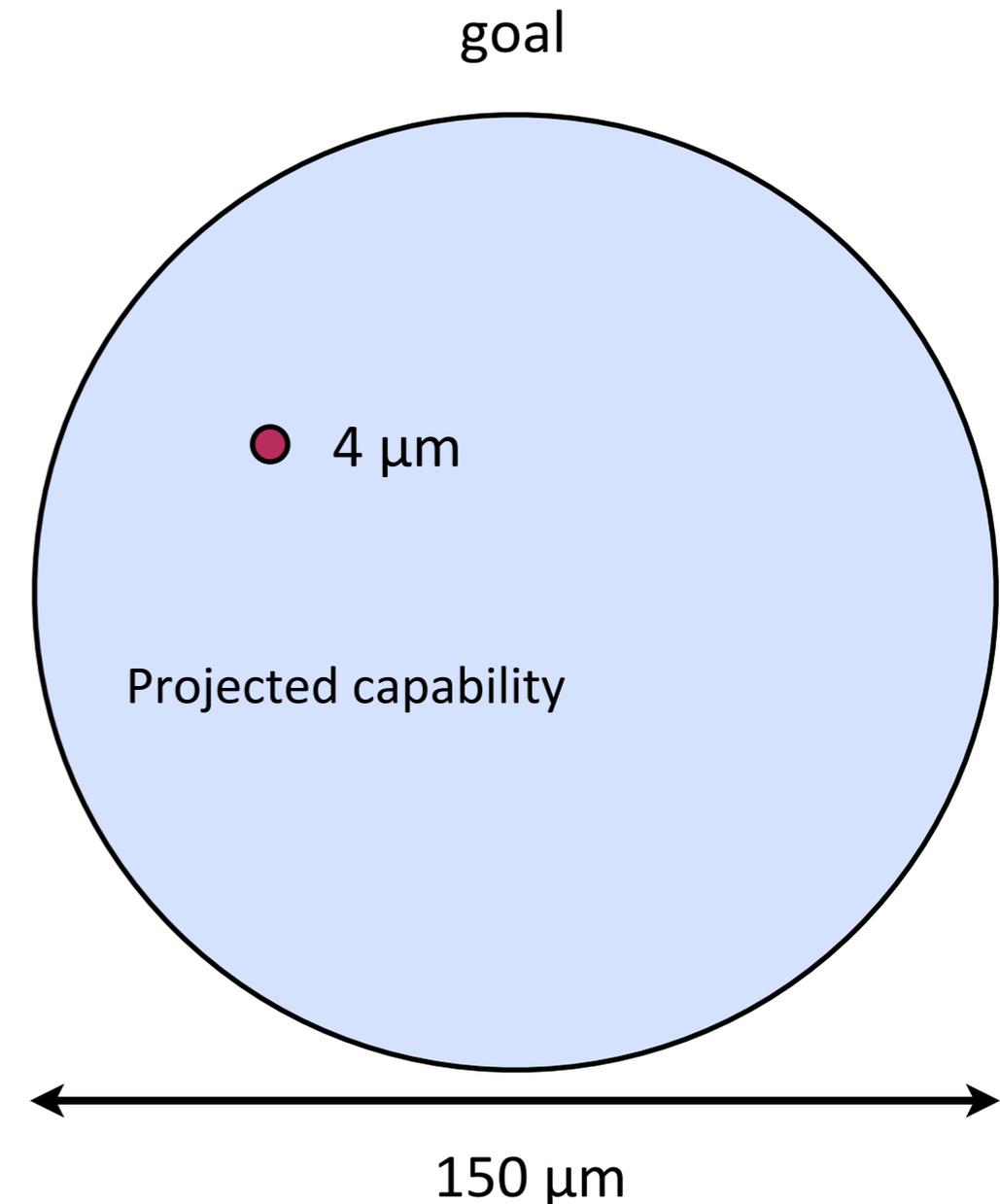
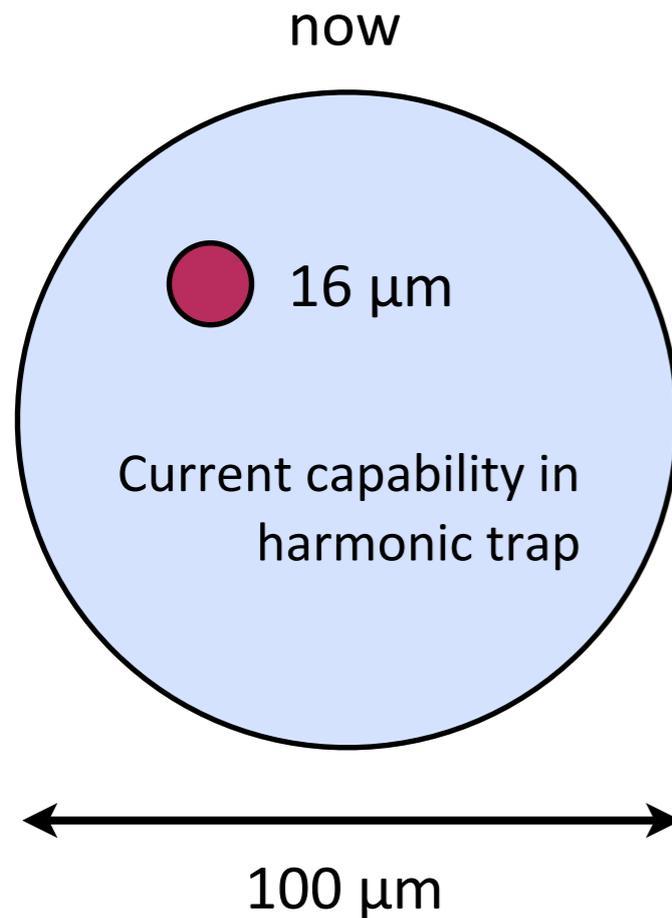
Next to do:

- remove one beam (and one vortex) from system
- transfer a vortex to another pinning site
- generation of more vortices

# Optimized vortex manipulation: projection

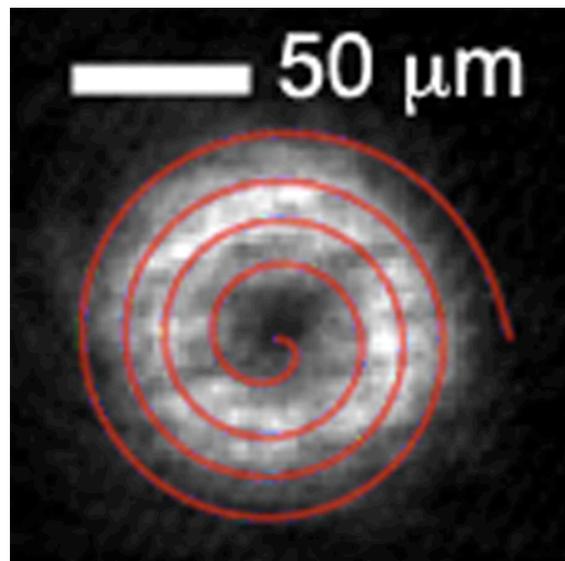
## High-resolution microscopy: vortex manipulation

### BEC size - laser spot size comparison

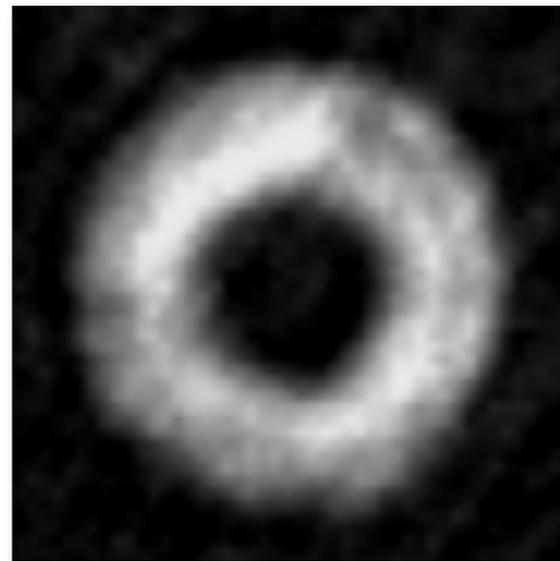


An array of individual focused laser beams is probably not the ideal solution for many-vortex manipulation.

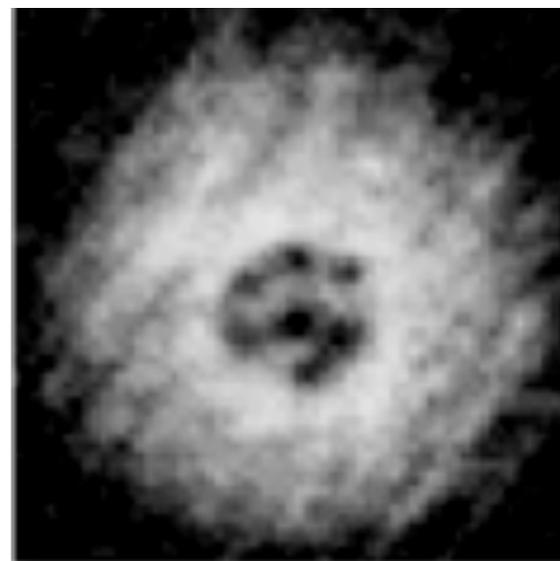
**Alternative: spatial light modulator, transfer vortices to stationary sites**



Spiral trajectory of laser beam



Large pinned circulation

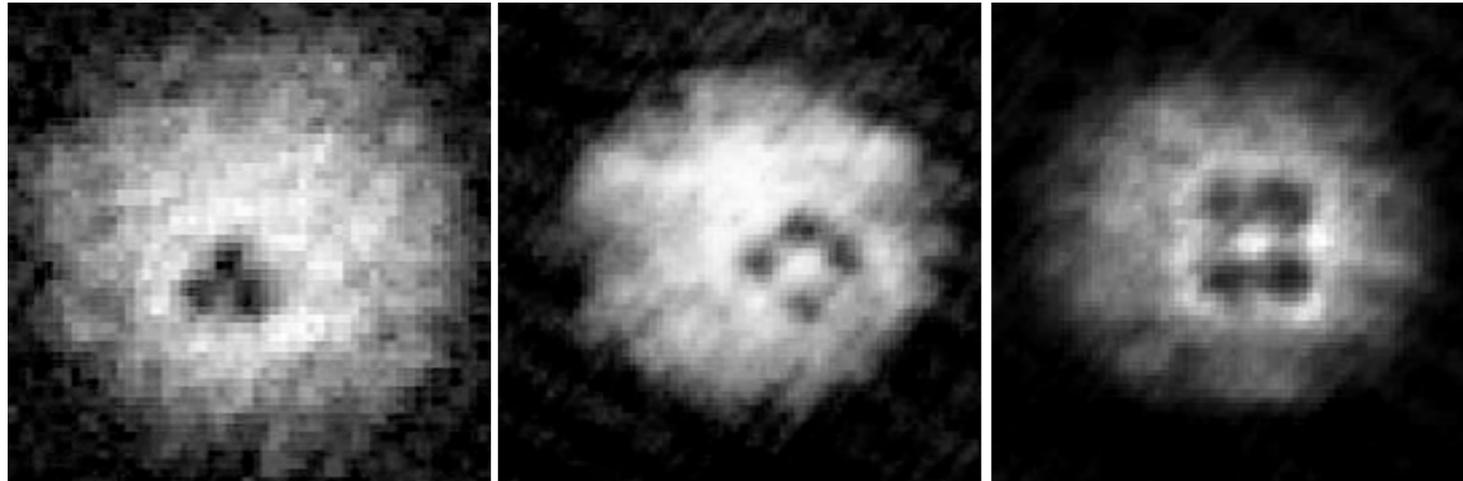


Vortices separate with extra hold time (160 ms)

3

4

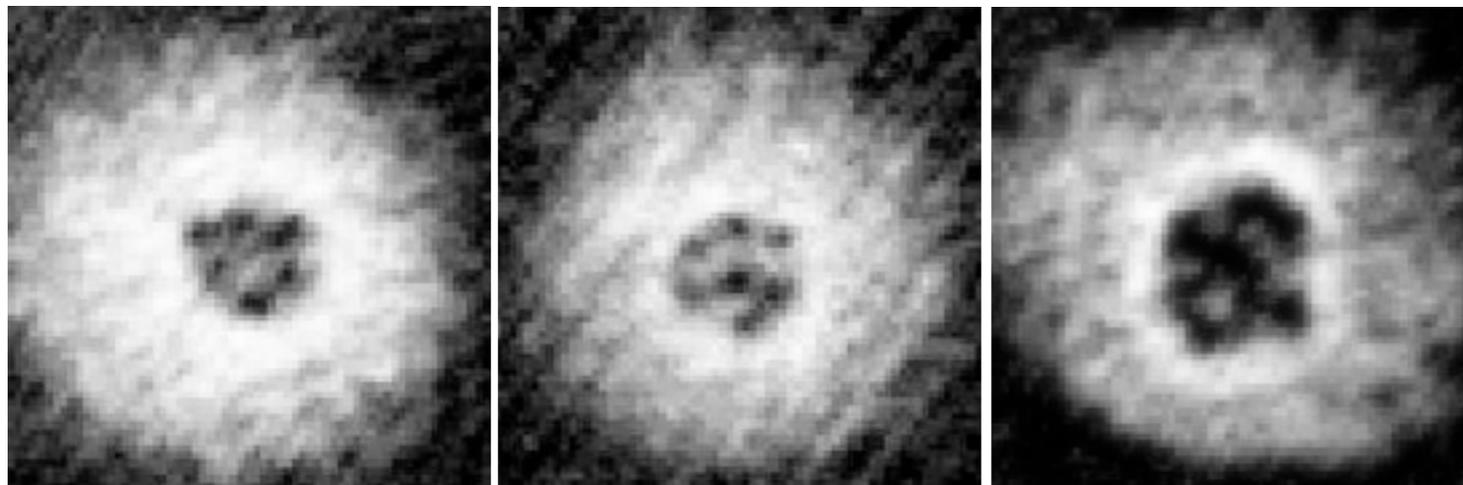
4



6

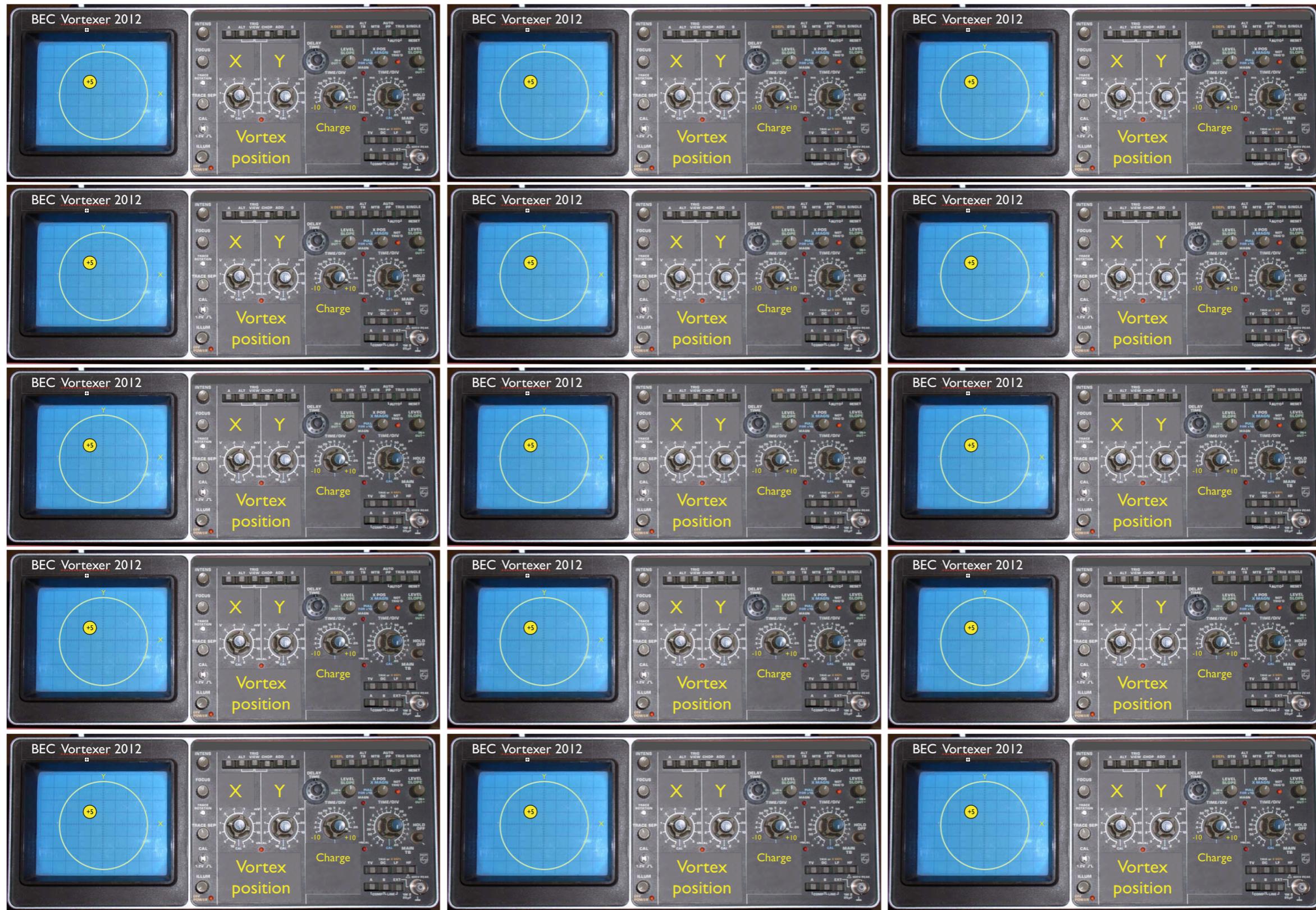
7

8?



2 pinning sites is feasible:  
**release of vortex  
bundles into BEC (2D or  
3D BEC)**

(Images from various vortex generation techniques)



### **Sustaining a turbulent state**

- steady-state forcing and dissipation
- minimal heating, atom loss, and excitation of BEC

### **Multiple-image *in situ* vortex imaging**

- watch the inverse energy cascade in real time (clustering of vortices)
- measure chaotic dynamics of few-vortex systems
- characterize vortex interactions with impurities
- characterize vortex-antivortex annihilation and generation

**Eventually: Real-time imaging, generation, and manipulation of vortices will lead to precision experimental studies and control of 2D quantum turbulence!**

**arXiv: 1204.1102**

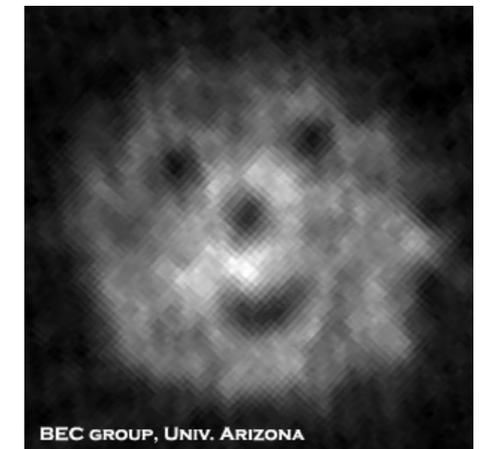
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**arXiv: 1204.1103 (not discussed)**

**Energy Spectra of Vortex Distributions in Two-Dimensional Quantum Turbulence**

A.S. Bradley and B.P. Anderson. *Analytical approach*

**Resource Article: Experiments with Vortices in Superfluid Atomic Gases**

B. P. Anderson, JLTP 161, 574 (2010)

**2DQT Team**

A.S. Bradley (*U. Otago*)

R. Carretero-González (*San Diego S. U.*)

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T.W. Neely (*U. Arizona -> U. Queensland*)

Z.L. Newman (*U. Arizona*)

S.J. Rooney (*U. Otago*)

E.C. Samson (*U. Arizona -> Ga. Tech*)

K.E. Wilson (*U. Arizona*)

E.M. Wright (*U. Arizona*)

BPA (*U. Arizona*)

