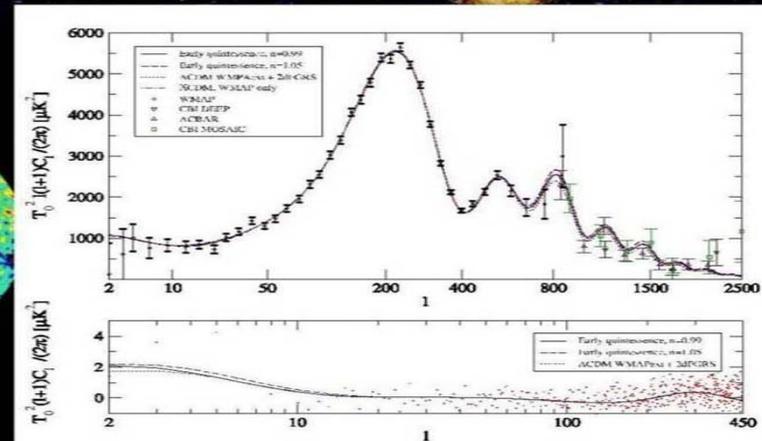
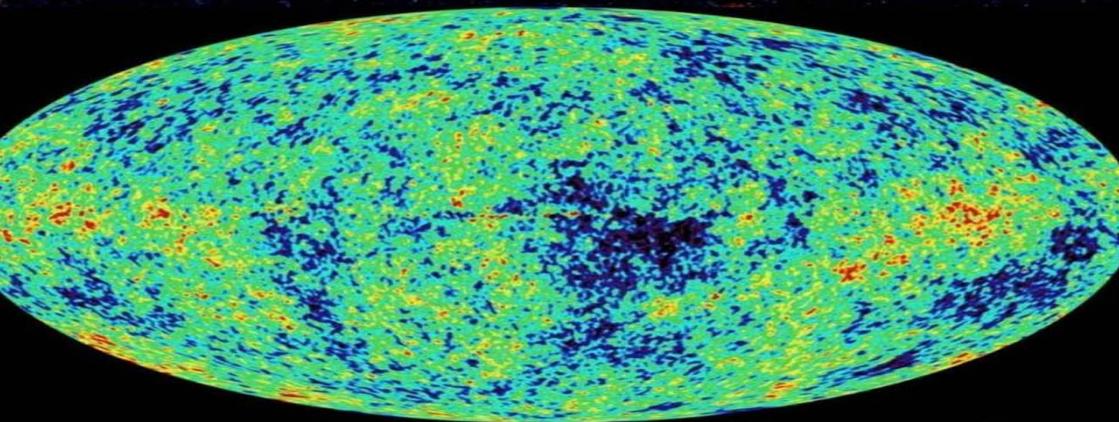


Dynamical Dark Energy and varying fundamental constants



Quintessence

C.Wetterich

A.Hebecker, M.Doran, M.Lilley, J.Schwindt,
C.Müller, G.Schäfer, E.Thommes,
R.Caldwell, M.Bartelmann,
K.Kharwan, G.Robbers, T.Dent, S.Steffen,
L.Amendola, M.Baldi

What is our universe made of ?



Dark Energy dominates the Universe

Energy - density in the Universe

=

Matter + Dark Energy

25 % + 75 %

Composition of the universe

$$\Omega_b = 0.045$$

$$\Omega_{dm} = 0.225$$

$$\Omega_h = 0.73$$

critical density

- $\rho_c = 3 H^2 M^2$

critical energy density of the universe

(M : reduced Planck-mass , H : Hubble parameter)

- $\Omega_b = \rho_b / \rho_c$

fraction in baryons

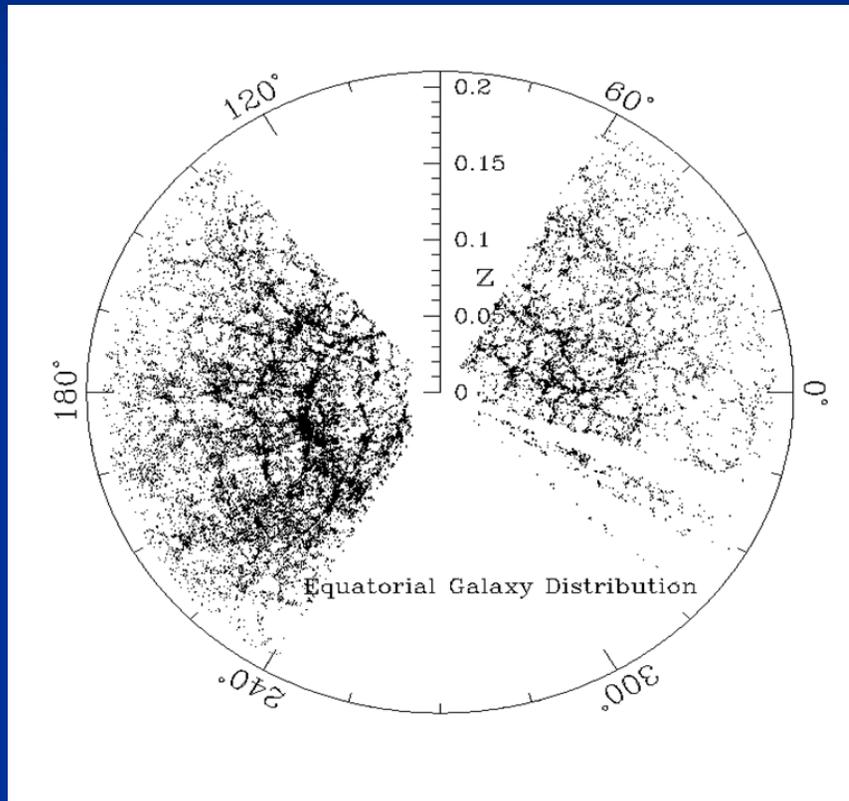
energy density in baryons over critical
energy density

$$H = \dot{a}/a$$

Baryons/Atoms

SDSS

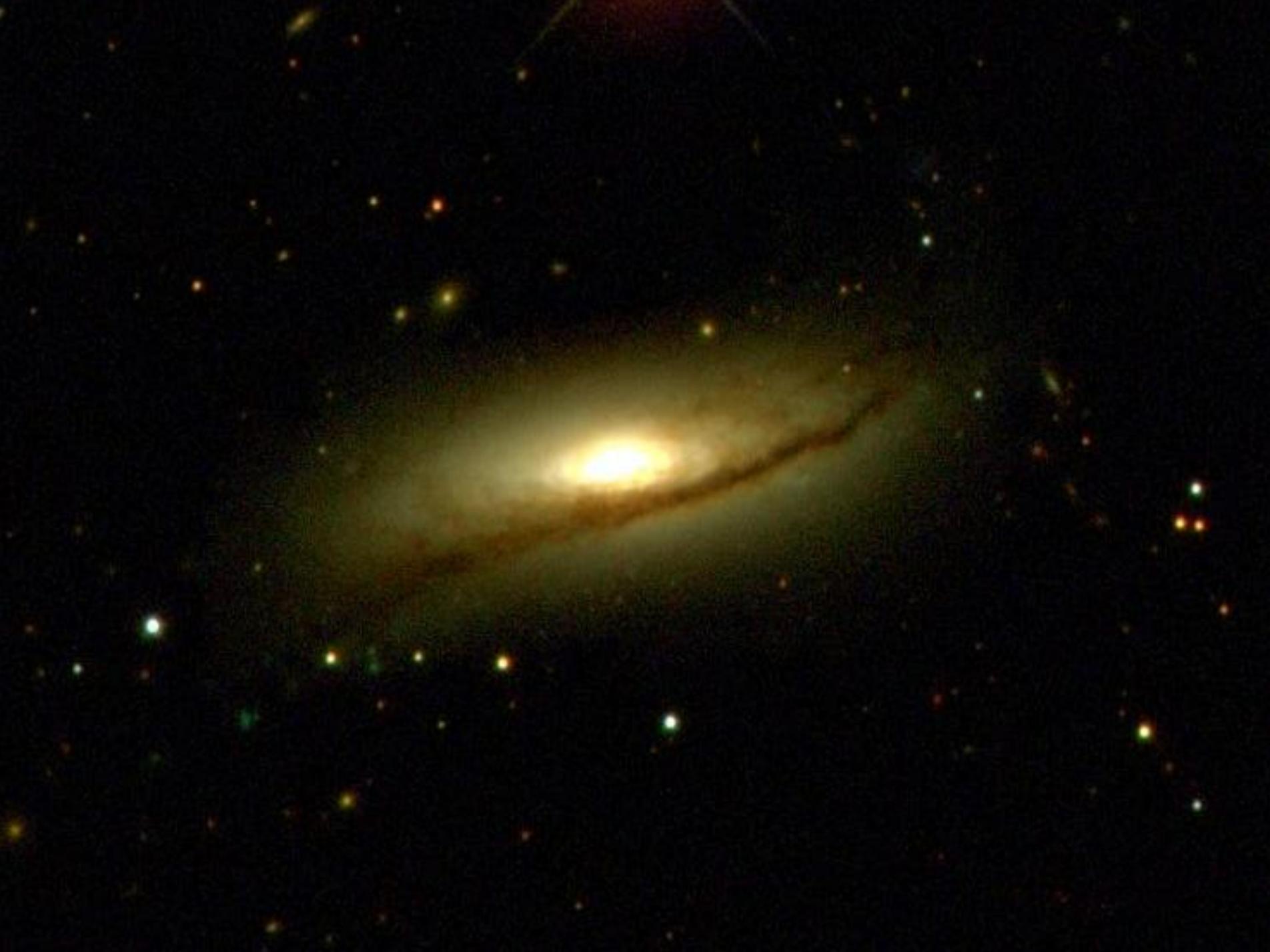
~60,000 of
>300,000
Galaxies



- Dust
- $\Omega_b = 0.045$
- Only 5 percent of our Universe consist of known matter !

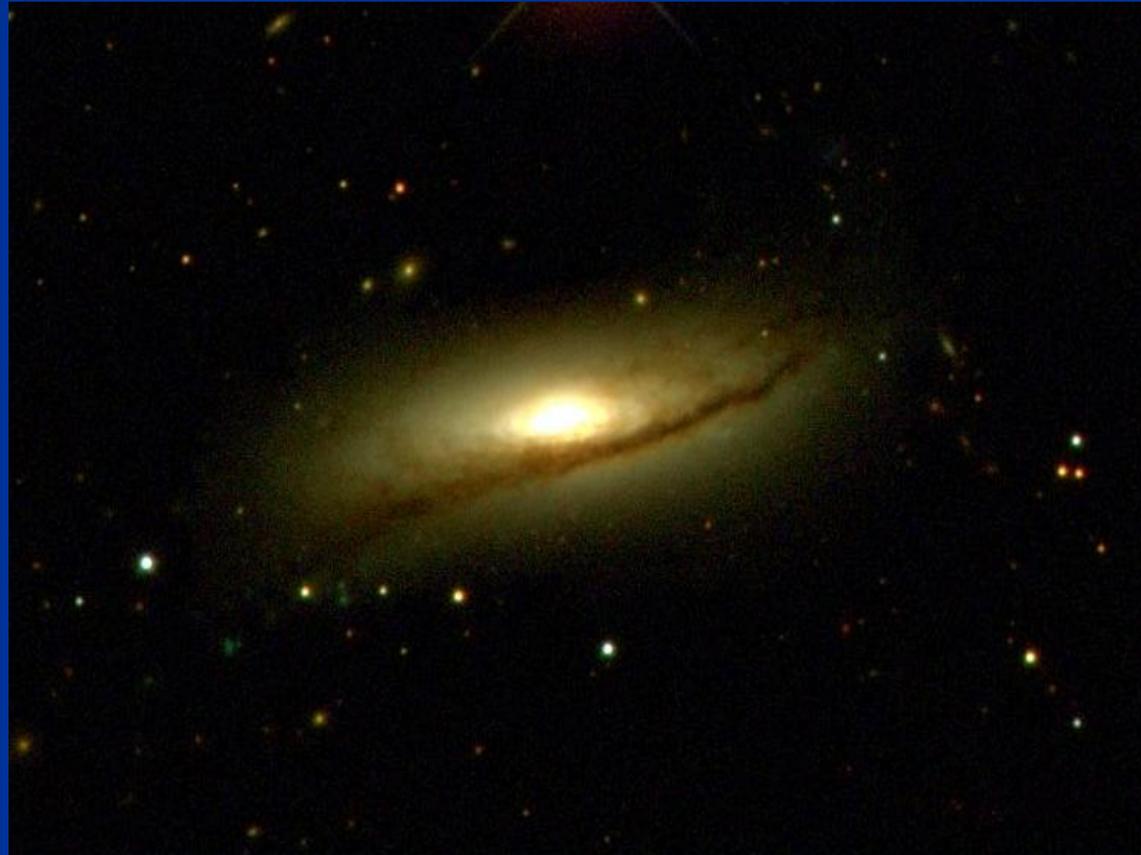


Abell 2255 Cluster
~300 Mpc



$$\Omega_b = 0.045$$

from
nucleosynthesis,
cosmic
background
radiation



What is Dark Energy ?

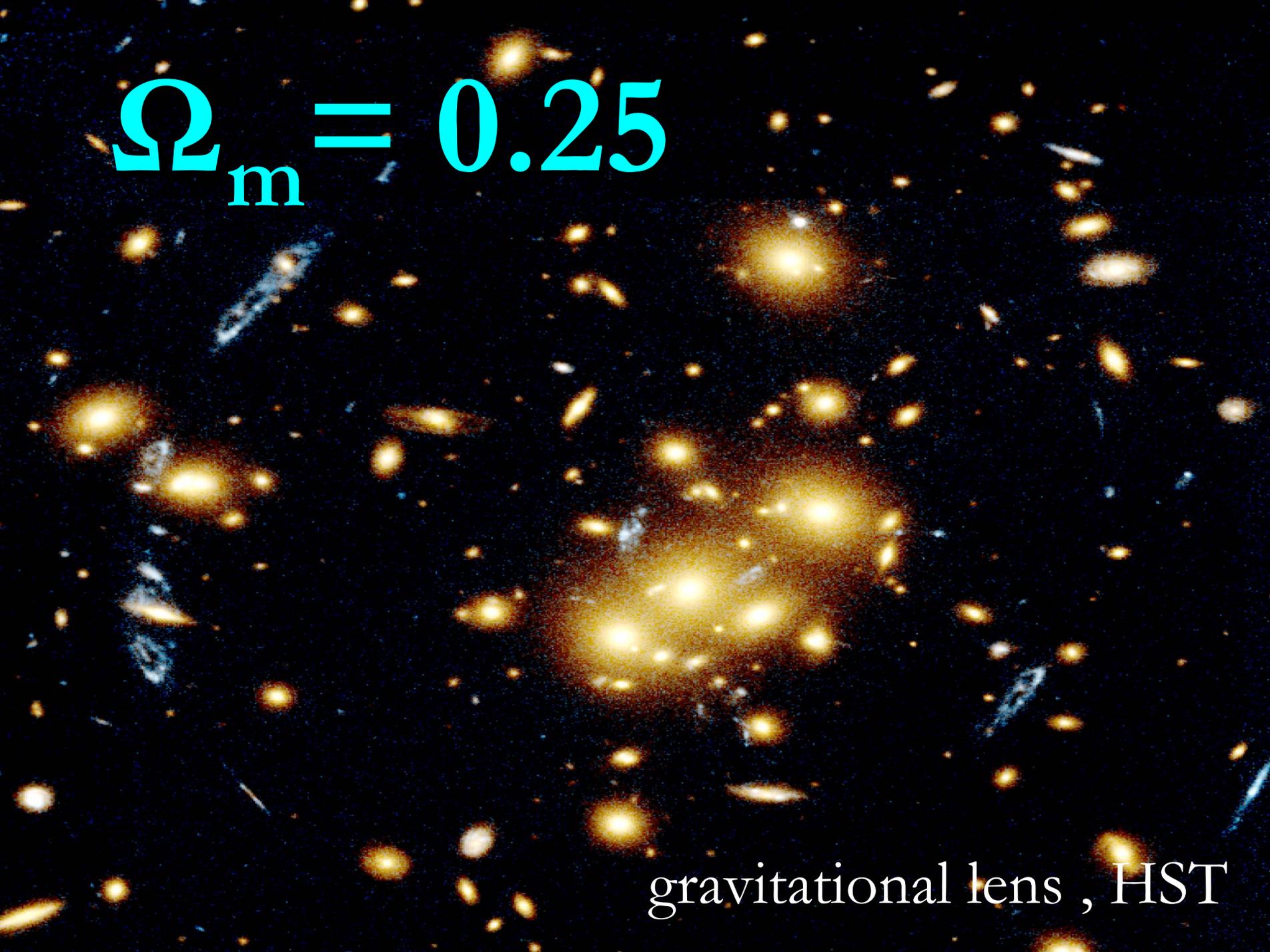
Matter : Everything that clumps



Abell 2255 Cluster
~300 Mpc

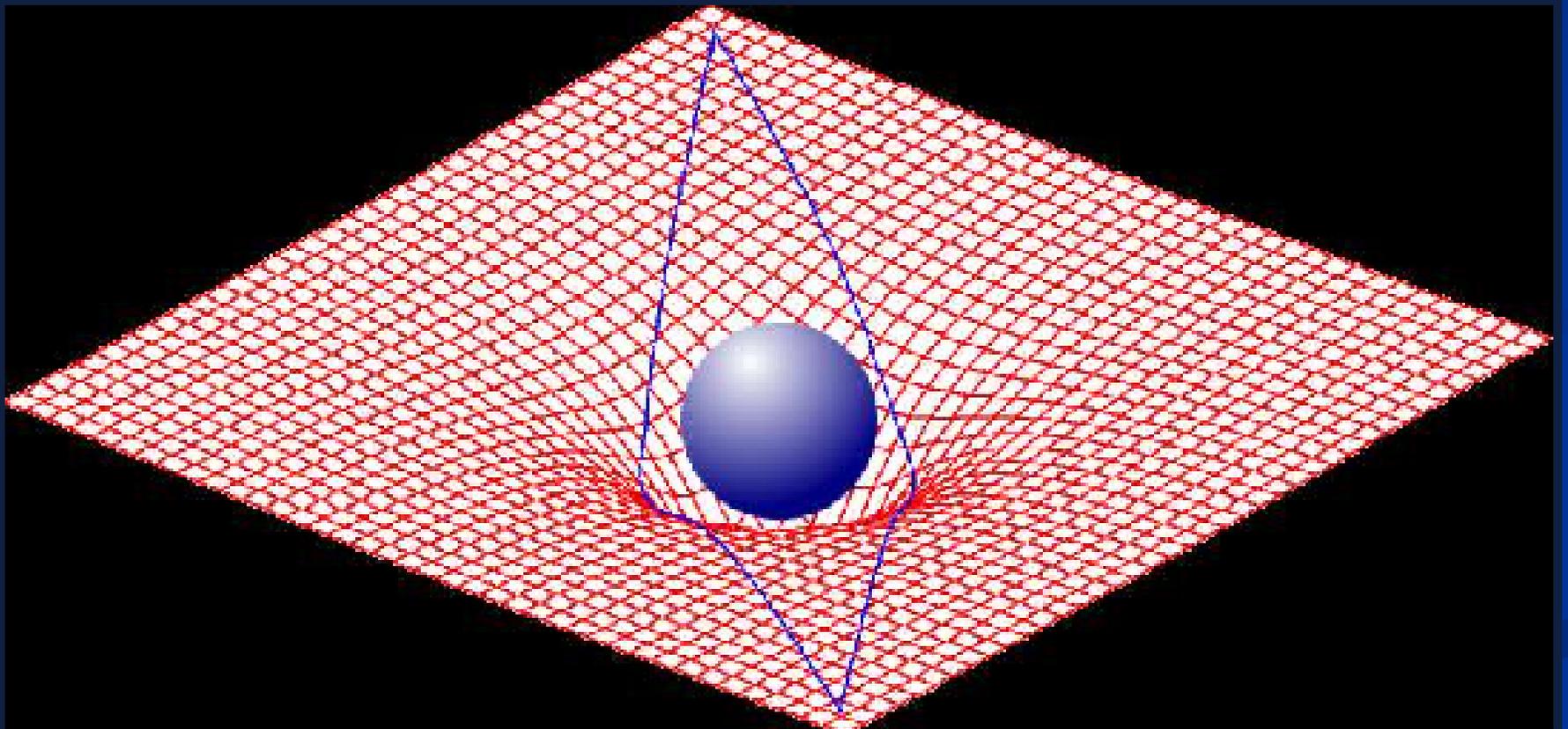
Dark Matter

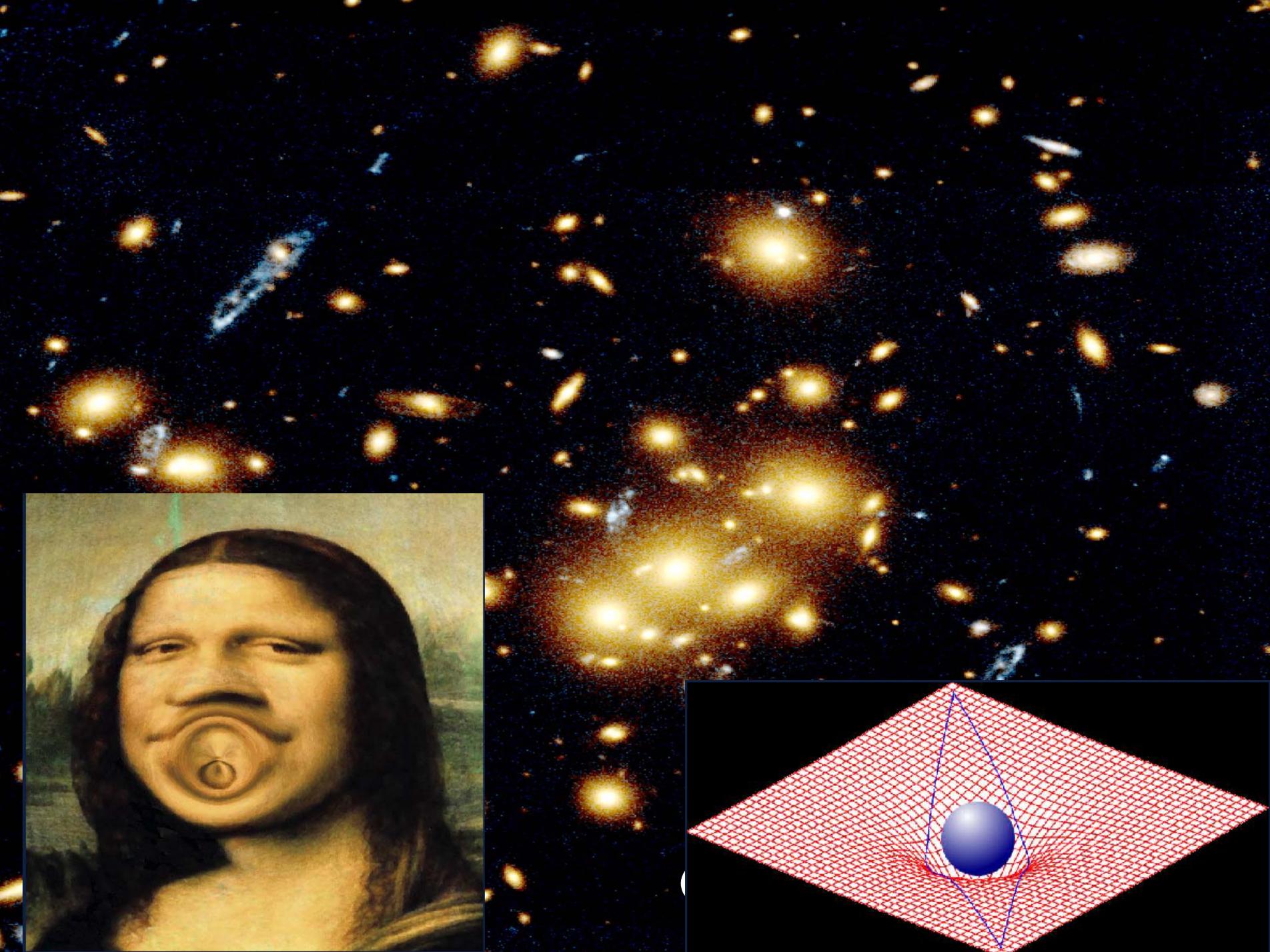
- $\Omega_m = 0.25$ total “matter”
- Most matter is dark !
- So far tested only through gravity
- Every local mass concentration →
gravitational potential
- Orbits and velocities of stars and galaxies →
measurement of gravitational potential
and therefore of local matter distribution

A deep-field astronomical image showing a large number of galaxies. In the center, there is a prominent, bright, yellowish-white galaxy cluster. Surrounding this central cluster are numerous other galaxies, many of which appear distorted or stretched, indicating they are being gravitationally lensed by the central mass. The background is dark, with some faint, blueish galaxies scattered throughout.
$$\Omega_m = 0.25$$

gravitational lens , HST

Light rays are deflected by mass





spatially flat universe

$$\Omega_{\text{tot}} = 1$$

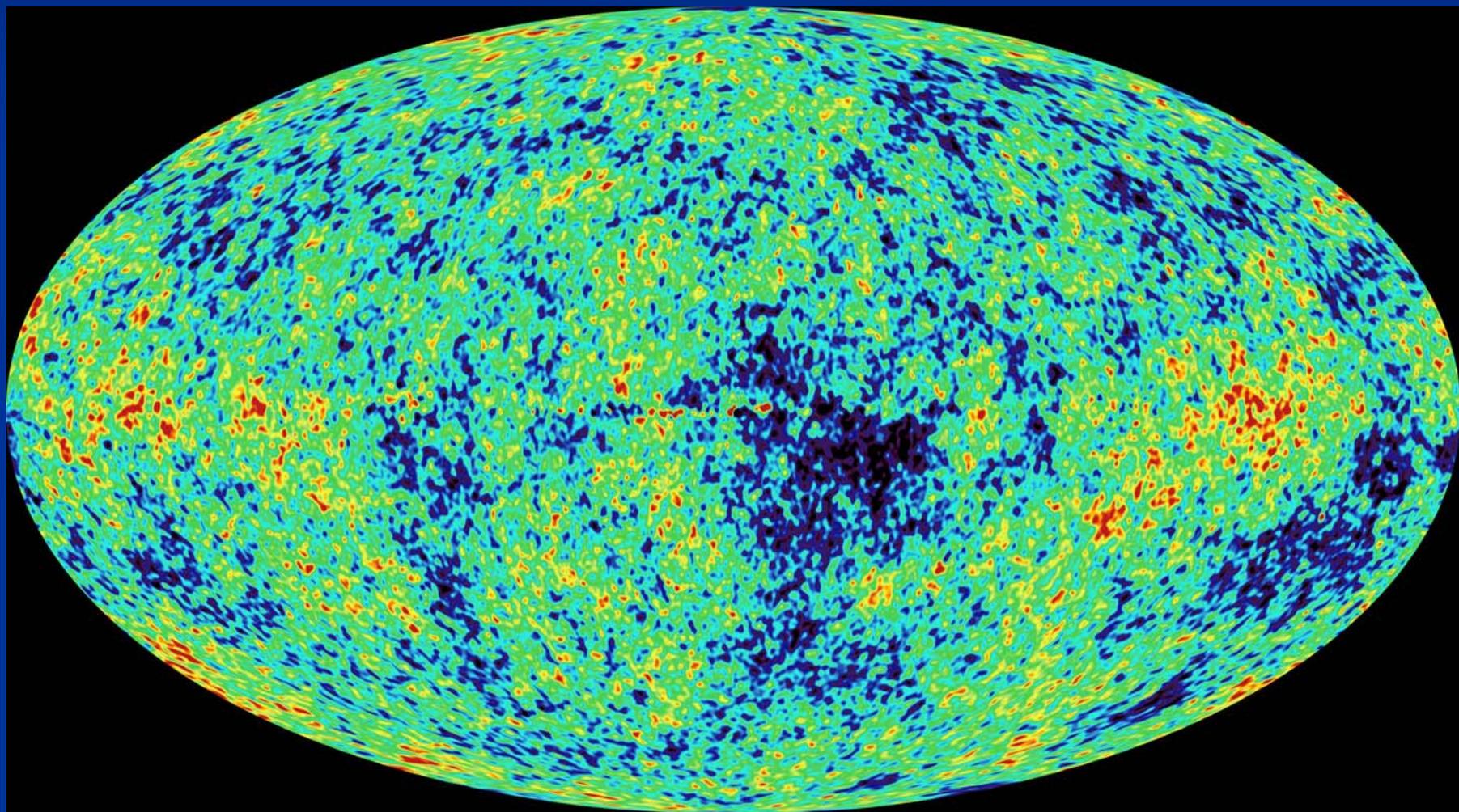
- theory (inflationary universe)

$$\Omega_{\text{tot}} = 1.0000\dots\dots\dots x$$

- observation (WMAP)

$$\Omega_{\text{tot}} = 1.02 (0.02)$$

picture of the big bang



Wilkinson Microwave Anisotropy Probe

*A partnership between
NASA/GSFC and Princeton*

Science Team:

NASA/GSFC

Chuck Bennett (PI)

Michael Greason

Bob Hill

Gary Hinshaw

Al Kogut

Michele Limon

Nils Odegard

Janet Weiland

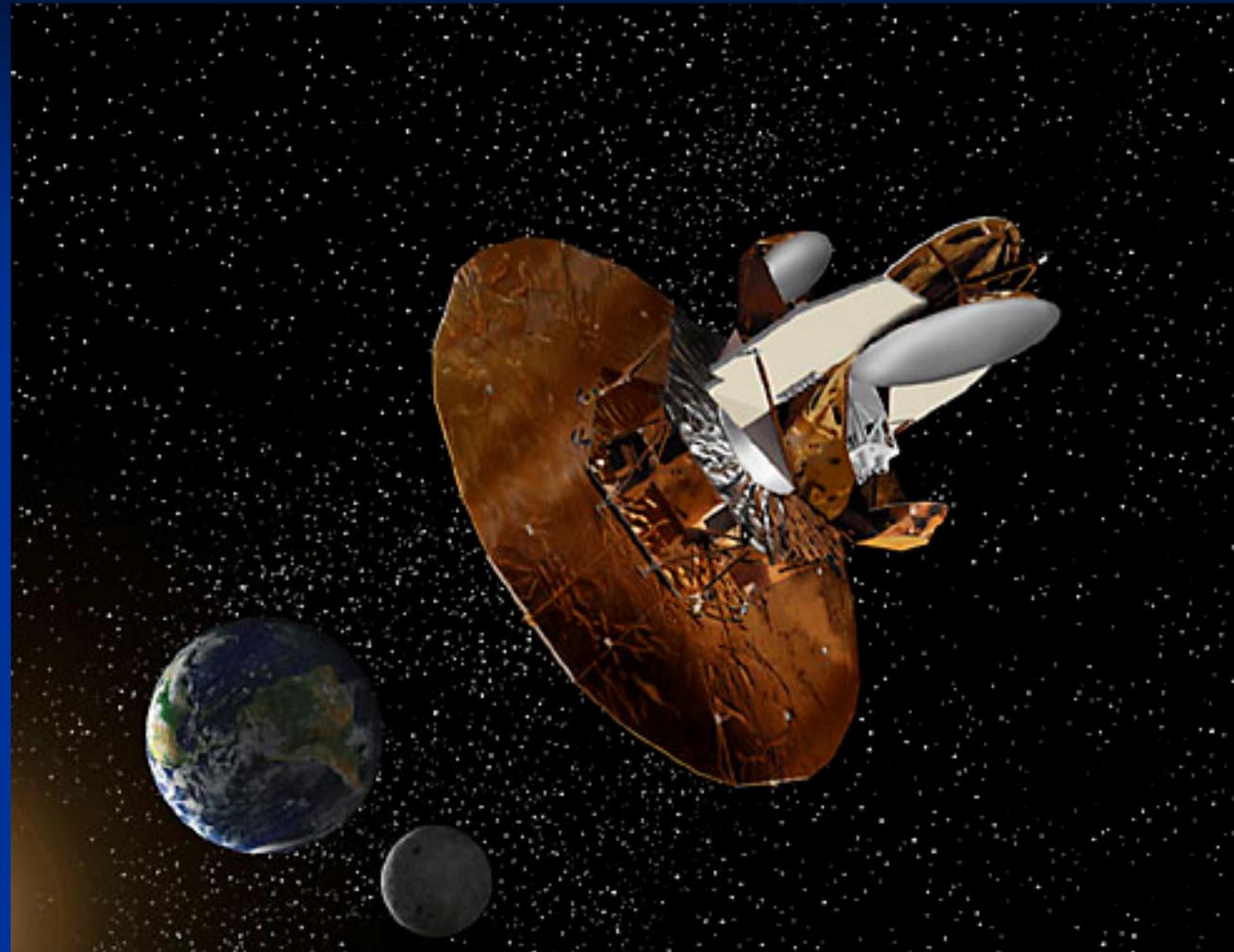
Ed Wollack

Brown

Greg Tucker

UCLA

Ned Wright



UBC

Mark Halpern

Chicago

Stephan Meyer

Princeton

Chris Barnes

Norm Jarosik

Eiichiro Komatsu

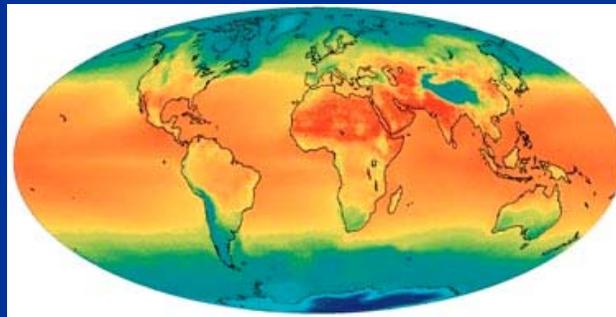
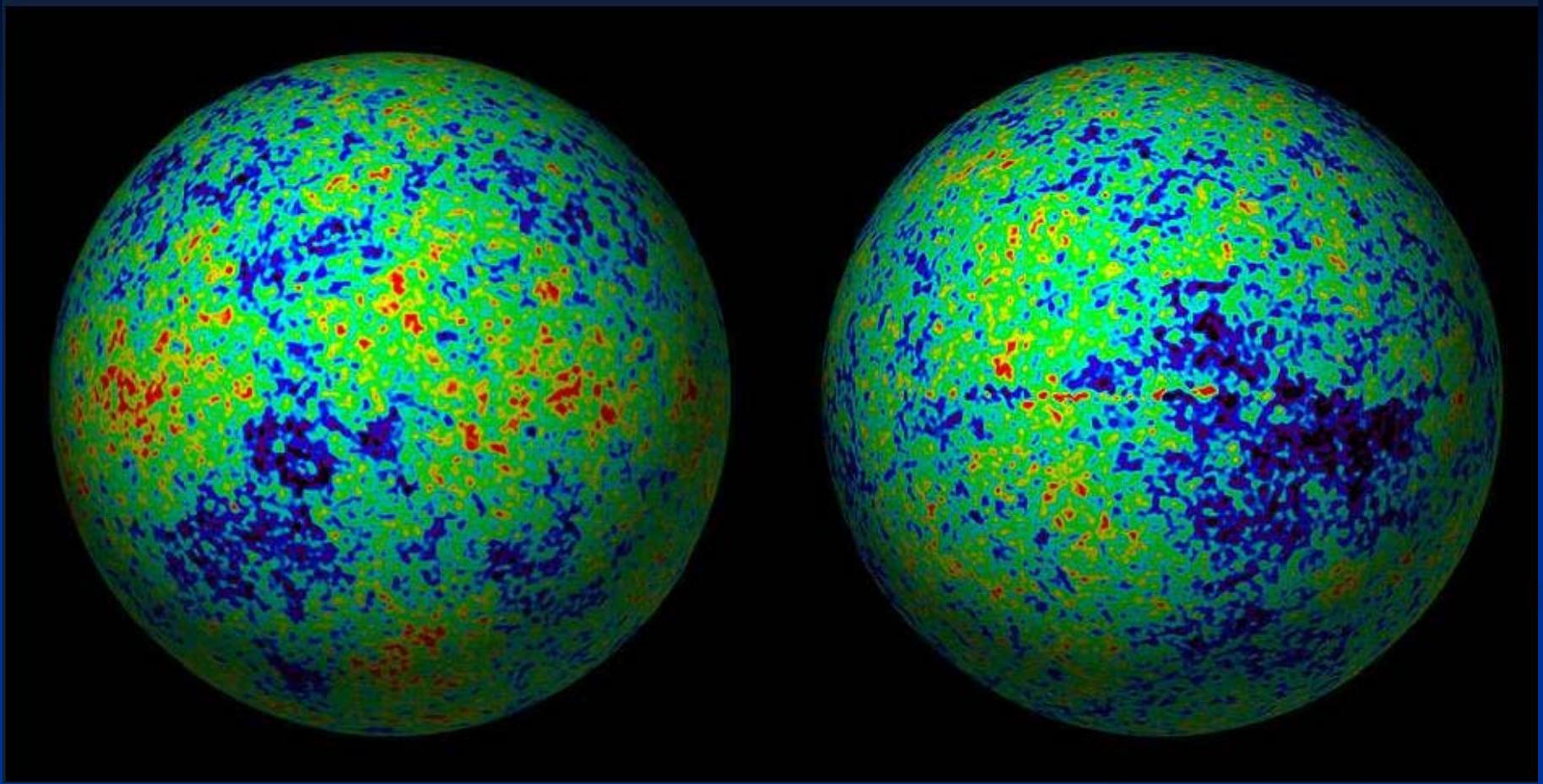
Michael Nolte

Lyman Page

Hiranya Peiris

David Spergel

Licia Verde



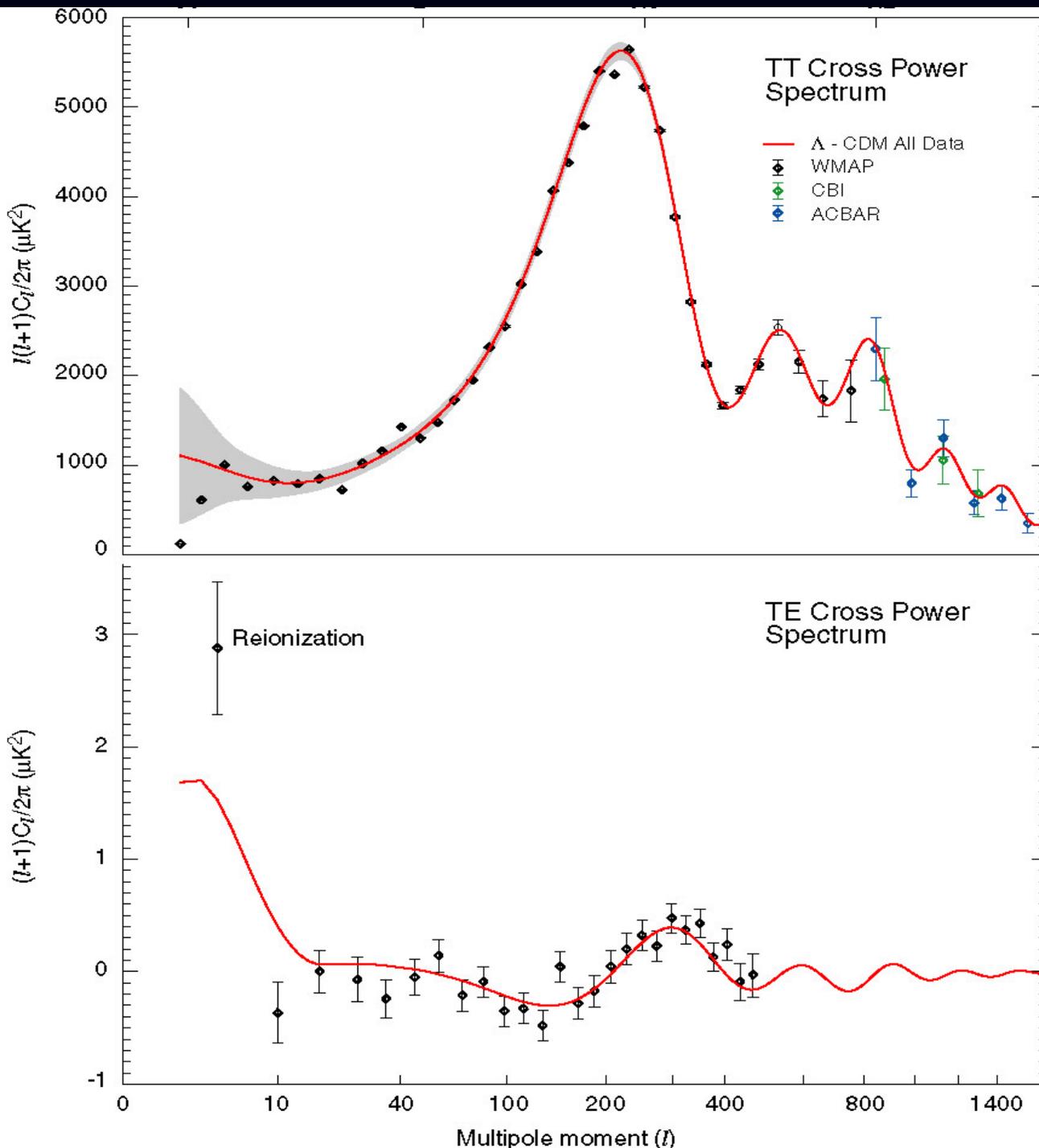
Mean values WMAP 2003

$$\Omega_{\text{tot}} = 1.02$$

$$\Omega_{\text{m}} = 0.27$$

$$\Omega_{\text{b}} = 0.045$$

$$\Omega_{\text{dm}} = 0.225$$



Wilkinson Microwave Anisotropy Probe

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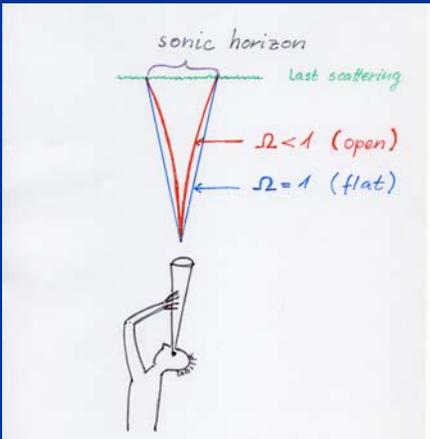
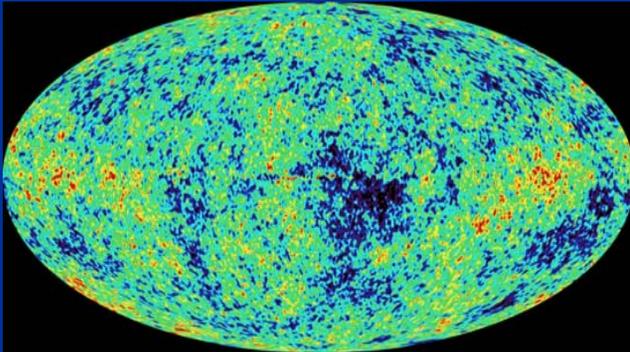
Mark Halpern

Chicago

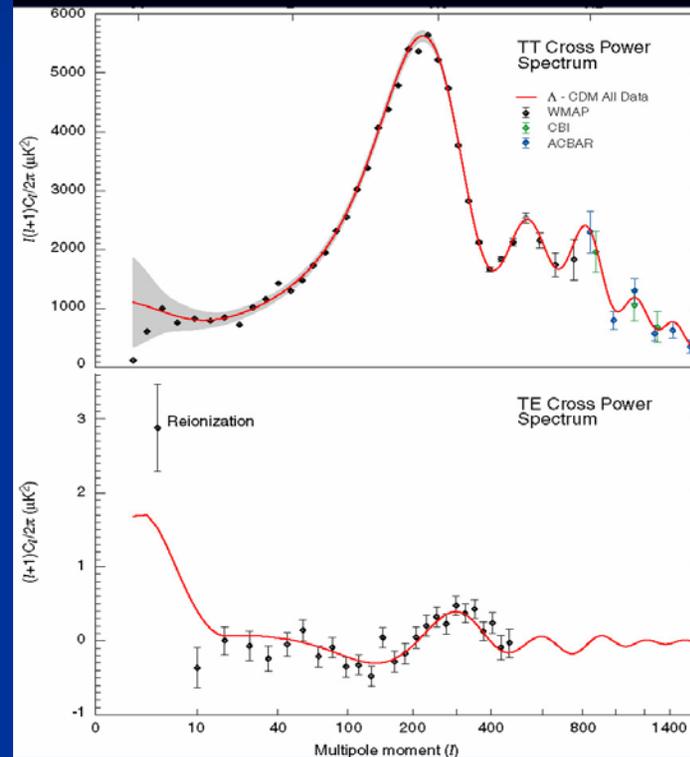
Stephan Meyer

Princeton

Chris Barnes
Norm Janotik
Eiichiro Komatsu
Michael Nolte
Lyman Page
Hiranya Peiris
David Spergel
Licia Verde



$$\Omega_{\text{tot}} = 1$$



mean values

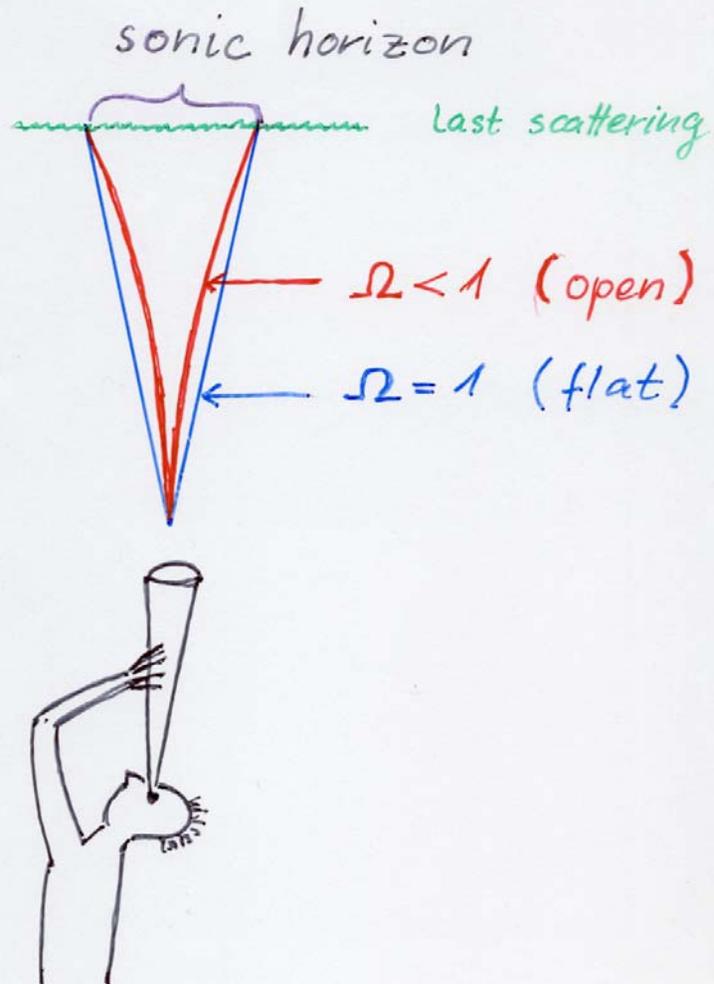
$$\Omega_{\text{tot}} = 1.02$$

$$\Omega_{\text{m}} = 0.27$$

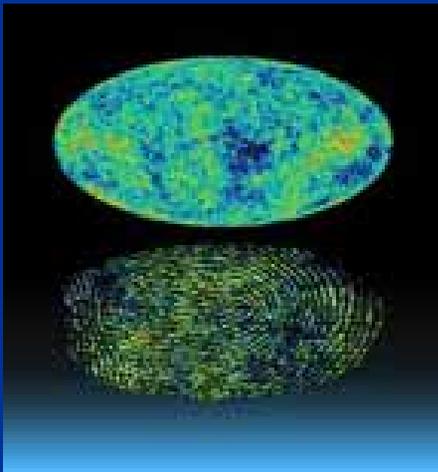
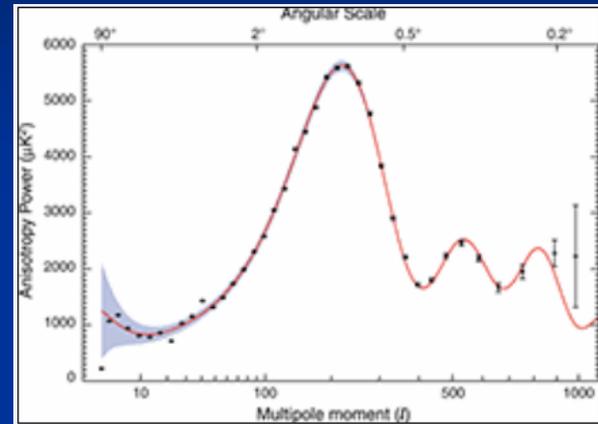
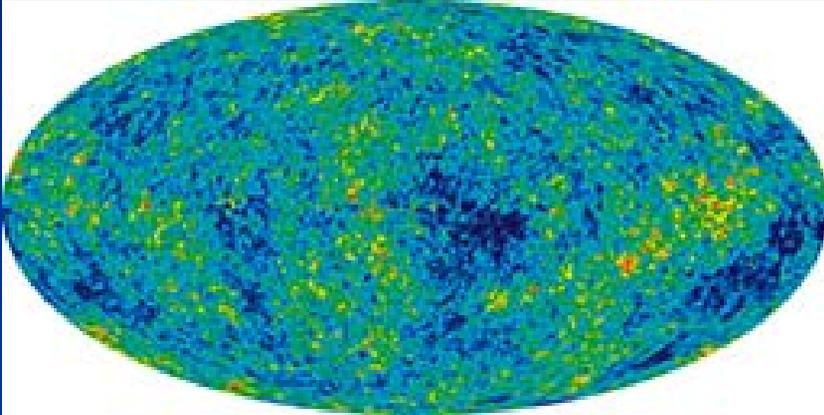
$$\Omega_{\text{b}} = 0.045$$

$$\Omega_{\text{dm}} = 0.225$$

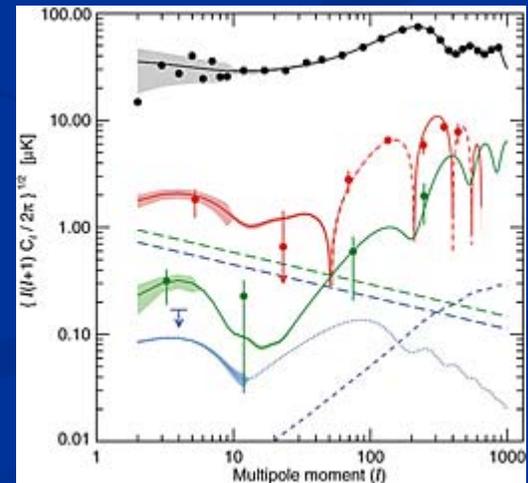
$$\Omega_{\text{tot}} = 1$$



WMAP 2006



Polarization



Dark Energy

$$\Omega_m + X = 1$$

$$\Omega_m : 25\%$$

$$\Omega_h : 75\% \quad \text{Dark Energy}$$

h : homogenous , often Ω_Λ instead of Ω_h

**Space between clumps
is not empty :**

Dark Energy !

**Dark Energy density is
the same at every point of space**

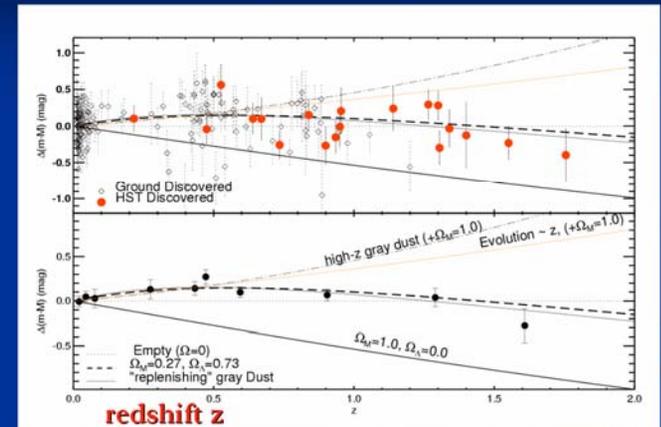
“ homogeneous “

**No force in absence of matter –
“ In what direction should it draw ? “**

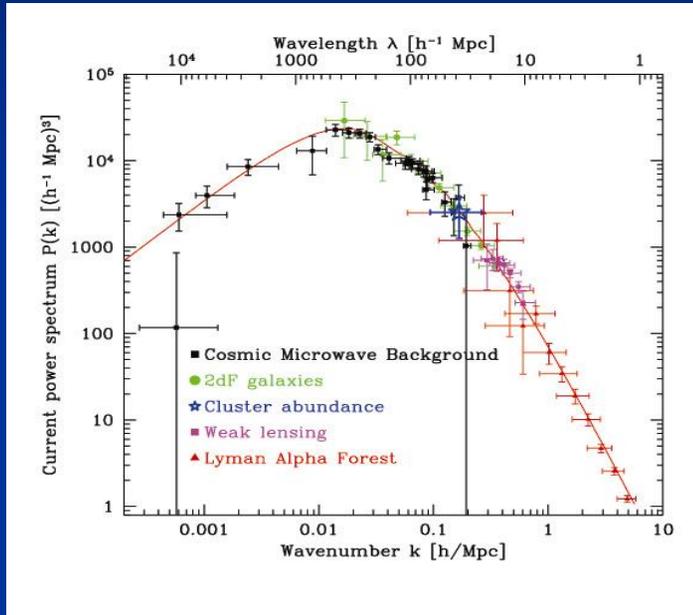
Predictions for dark energy cosmologies

*The expansion of the Universe
accelerates today !*

Supernovae 1a Hubble diagram

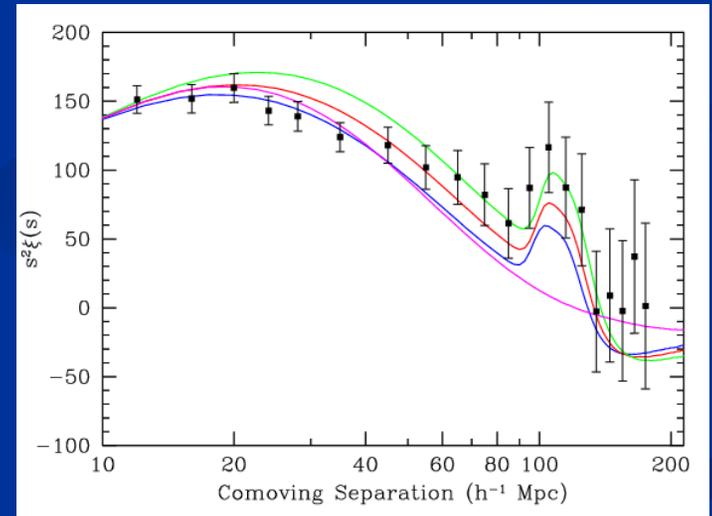


Power spectrum



Baryon - Peak

galaxy –
correlation –
function



*Structure formation :
One primordial
fluctuation- spectrum*

SDSS

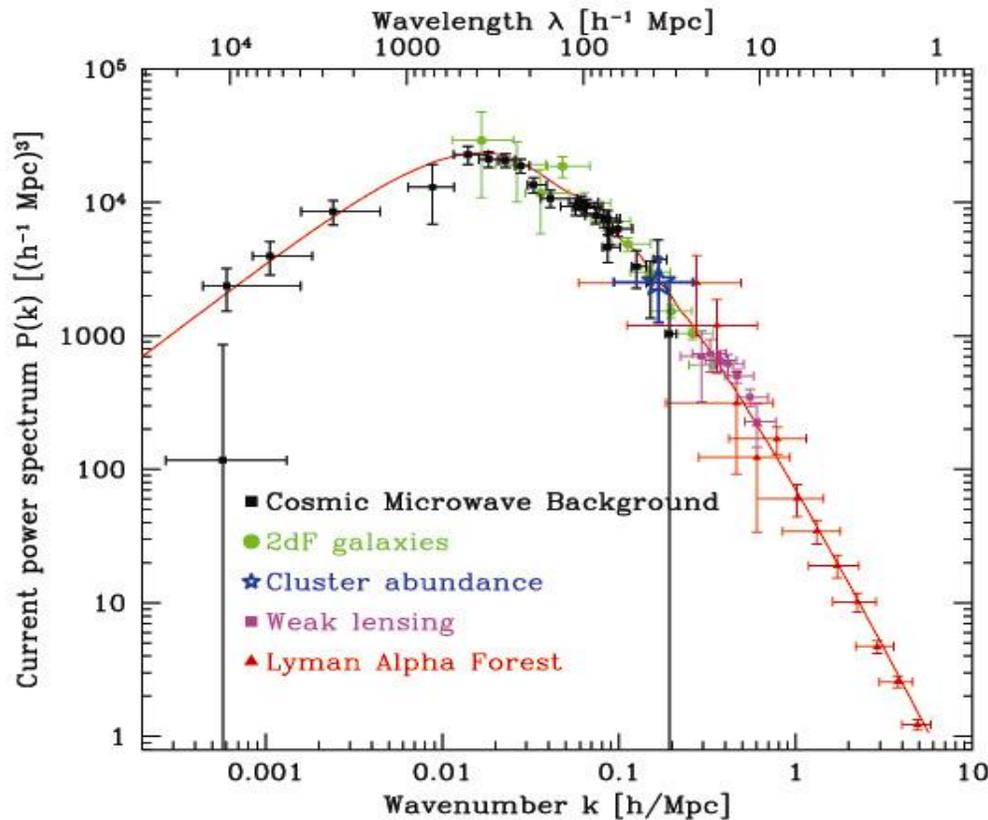
Structure formation

All structures of the Universe grow from tiny anisotropies at time of CMB emission

Stars , Galaxies, Clusters

One primordial fluctuation spectrum describes all correlation functions !

Structure formation : One primordial fluctuation spectrum



Waerbeke

CMB agrees with
Galaxy distribution
Lyman - α
and
Gravitational
Lensing !

Composition of the Universe

$$\Omega_b = 0.045$$

visible

clumping

$$\Omega_{dm} = 0.2$$

invisible

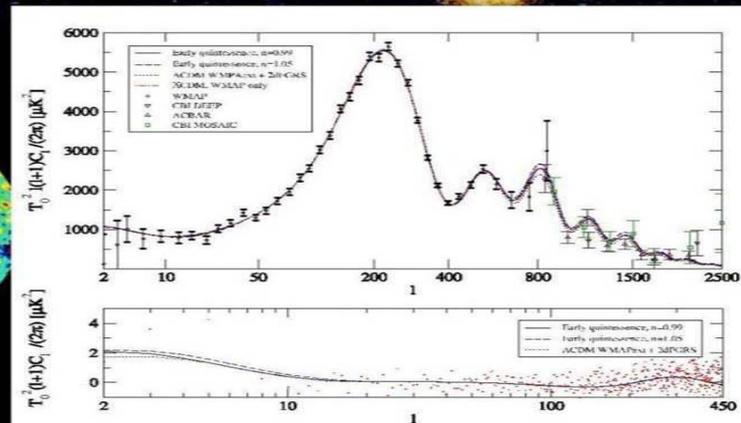
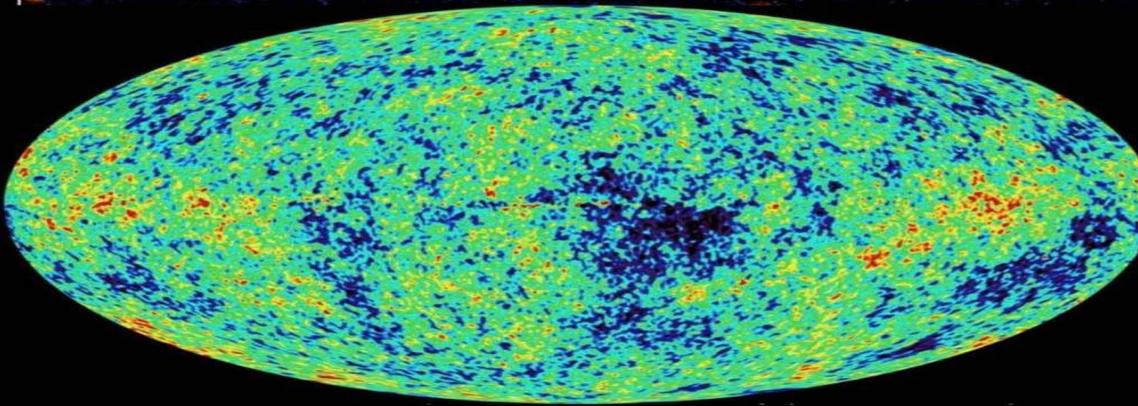
clumping

$$\Omega_h = 0.75$$

invisible

homogeneous

Dark Energy- a cosmic mystery



Cosmological Constant

- Einstein -

- Constant λ compatible with all symmetries
- No time variation in contribution to energy density
- Why so small ? $\lambda/M^4 = 10^{-120}$
- Why important just today ?

Einstein equation

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = -\frac{8\pi}{M_p^2} T_{\mu\nu}$$

$$M_p = 1.22 \cdot 10^{19} \text{ GeV} = G_N^{-1/2}$$

Energy - momentum - tensor

$$\begin{aligned} T_{\mu\nu} &= T_{\mu\nu}^{(\text{baryon})} + T_{\mu\nu}^{(\text{radiation})} \\ &+ T_{\mu\nu}^{(\text{dark matter})} \\ &+ T_{\mu\nu}^{(\text{homogeneous})} \end{aligned}$$

$T_{\mu\nu}$ (homogenous) ?
=

{ $\lambda g_{\mu\nu}$: cosmological const.
 $T_{\mu\nu}^{(q)}$: quintessence

scalar field ?

nonlocal gravity ?

⋮

Gravitational action

$$S = + \int d^4x g^{1/2} \left(-\frac{M_p^2}{16\pi} R + \lambda \right)$$

λ : cosmological constant

Field equations

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = \frac{8\pi}{M_p^2} (T_{\mu\nu}^M + \lambda g_{\mu\nu})$$

$M_p \approx 10^{19}$ GeV : Planck mass

$T_{\mu\nu}^M$: matter energy momentum tensor

accounts for nonvanishing
entropy in the universe

without matter:

$$R = + \frac{32\pi}{M_p^2} \lambda$$

Cosmological constant

$$T_{\mu\nu} = T_{\mu\nu}^M - \lambda g_{\mu\nu}$$

$$\rho \rightarrow \rho + \lambda = \rho + p_\lambda$$

$$p \rightarrow p - \lambda = p + p_\lambda$$

$$\rho + p \rightarrow \rho + p$$

—
"Equation of state"

$$p_\lambda / \rho_\lambda = -1$$

Friedman universe ($\lambda = 0$)

Einstein equations \rightarrow

$$(i) \quad H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi}{3M_p^2} \rho - \frac{k}{a^2}$$

(evolution equation)

$$(ii) \quad \dot{\rho} + 3H(\rho + p) = 0$$

(energy - momentum - conservation)

$$\Leftrightarrow \frac{d}{dt} [a^3(\rho + p)] = a^3 \frac{d}{dt} p$$

radiation ($p = \frac{1}{3}\rho$) $\rho \sim a^{-4}$

matter ($p = 0$) $\rho \sim a^{-3}$

$k = 0$ (always applicable for early universe)

Field equations involve only the Hubble -

parameter $H = \dot{a}/a$

$$\lambda \neq 0$$

Einstein equations \rightarrow

$$(i) \quad H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi}{3M_p^2} (\rho + \lambda) - \frac{k}{a^2}$$

(evolution equation)

$$(ii) \quad \dot{\rho} + 3H(\rho + p) = 0$$

(energy - momentum - conservation)

$$\Leftrightarrow \frac{d}{dt} [a^3(\rho + p)] = a^3 \frac{d}{dt} p$$

radiation ($p = \frac{1}{3}\rho$) $\rho \sim a^{-4}$

matter ($p = 0$) $\rho \sim a^{-3}$

$k = 0$ (always applicable for early universe)

Field equations involve only the Hubble -
parameter $H = \dot{a}/a$

Only minor modification for

$$\lambda \ll \rho$$

For $t \rightarrow \infty$: $\lambda \neq 0$ has
always important effects !

asymptotic solution for cosmological constant ($k=0$)

$$\lambda > 0$$

$$H^2 \rightarrow \frac{8\pi}{3M_p^2} \lambda$$

$$a \sim \exp H_0 t$$

$$\lambda = 0$$

$$H \rightarrow \eta t^{-1}$$

$$a \sim t^\eta$$

$$\lambda < 0$$

$$H \rightarrow \left(\frac{8\pi}{3M_p^2} |\lambda| \right)^{\frac{1}{2}} \operatorname{tg}(c_1 - c_2 t)$$

e.g. a expands to maximal a_0
and shrinks subsequently

Cosmological Constant

Why so small ?

$$\lambda/M^4 = 10^{-120}$$

Anthropic principle

For

$$\lambda \leq -\frac{1}{2} \rho_c$$

or

$$\lambda > (10-100) \rho_c$$

we simply would not exist !

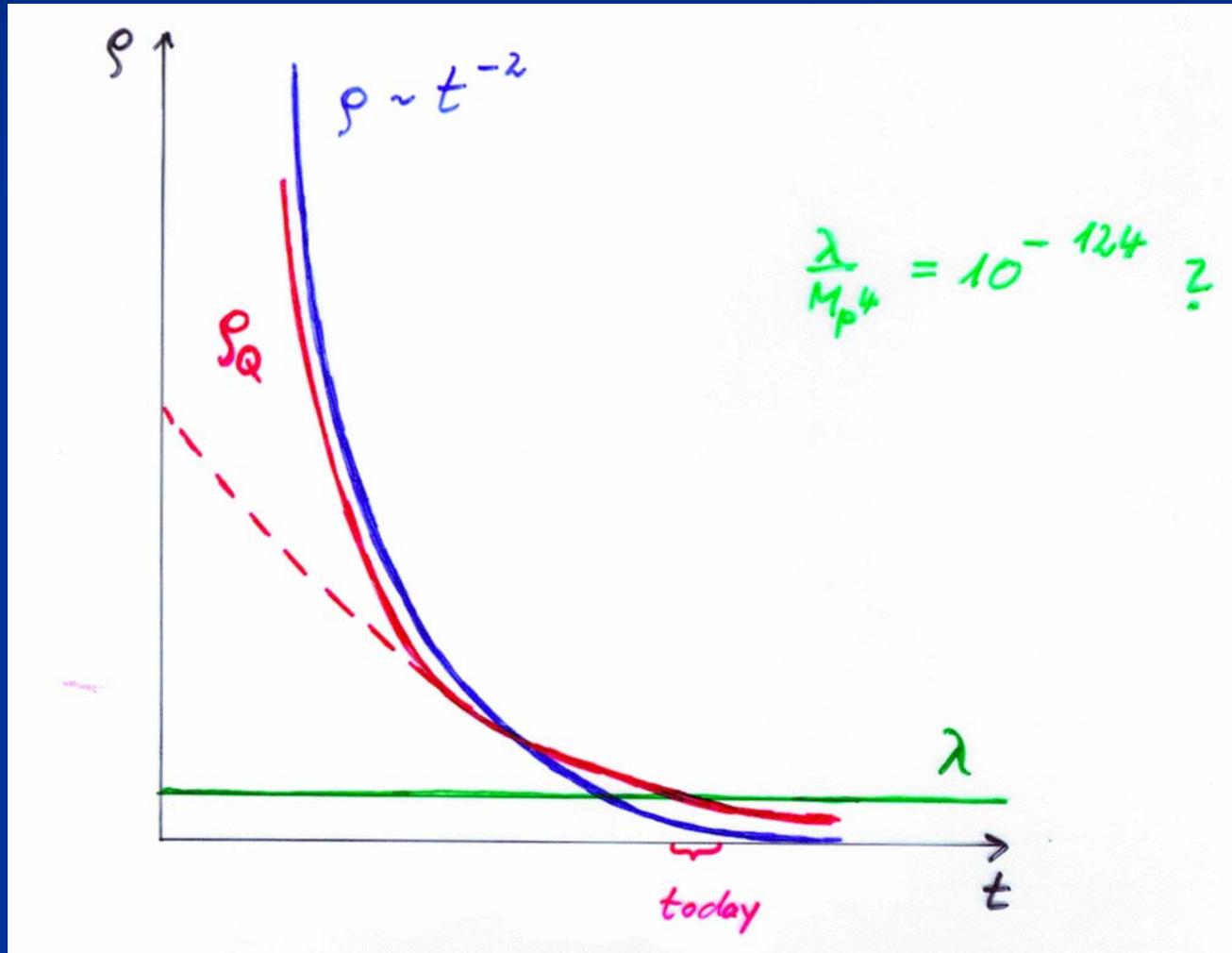
Banks
Weinberg
Linde

Cosmological Constant

Why important just today ?

Cosm. Const.
static

Quintessence
dynamical



Cosmological mass scales

- Energy density

$$\rho \sim (2.4 \times 10^{-3} \text{ eV})^{-4}$$

- Reduced Planck mass

$$M = 2.44 \times 10^{18} \text{ GeV}$$

- Newton's constant

$$G_N = (8\pi M^2)$$

Only ratios of mass scales are observable !

homogeneous dark energy: $\rho_h/M^4 = 6.5 \cdot 10^{-121}$

matter: $\rho_m/M^4 = 3.5 \cdot 10^{-121}$

Time evolution

- $\rho_m/M^4 \sim a^{-3} \sim t^{-2}$ matter dominated universe
- $\rho_r/M^4 \sim a^{-4} \sim t^{-3/2}$ radiation dominated universe
- $\rho_r/M^4 \sim a^{-4} \sim t^{-2}$ radiation dominated universe

Huge age \Rightarrow small ratio

Same explanation for small dark energy?

Quintessence

Dynamical dark energy ,
generated by scalar field

(cosmon)

C.Wetterich, Nucl.Phys.B302(1988)668, 24.9.87

P.J.E.Peebles, B.Ratra, ApJ.Lett.325(1988)L17, 20.10.87

Prediction :

**homogeneous dark energy
influences recent cosmology**

- of same order as dark matter -

Original models do not fit the present observations
.... modifications

Quintessence

Cosmon – Field $\varphi(\mathbf{x},y,z,t)$

similar to electric field , but no direction (scalar field)

Homogeneous und isotropic Universe : $\varphi(\mathbf{x},y,z,t)=\varphi(t)$

Potential und kinetic energy of the cosmon -field
contribute to a dynamical energy density of the Universe !

Cosmon

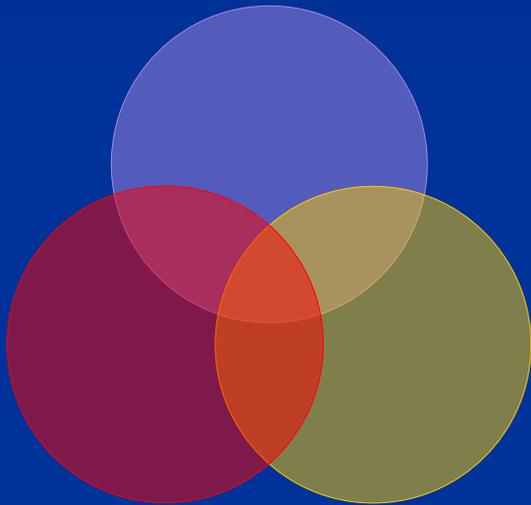
- *Scalar field changes its value even in the **present** cosmological epoch*
- *Potential und kinetic energy of cosmon contribute to the energy density of the Universe*
- *Time - variable dark energy :
 $\rho_b(t)$ decreases with time !*

Cosmon

- *Tiny mass*
- $m_c \sim H$
- *New long - range interaction*

“Fundamental” Interactions

Strong, electromagnetic, weak interactions



gravitation

cosmodynamics

On astronomical length scales:

graviton

+

cosmon

Evolution of cosmological field

Field equations

$$\ddot{\phi} + 3H\dot{\phi} = -dV/d\phi$$

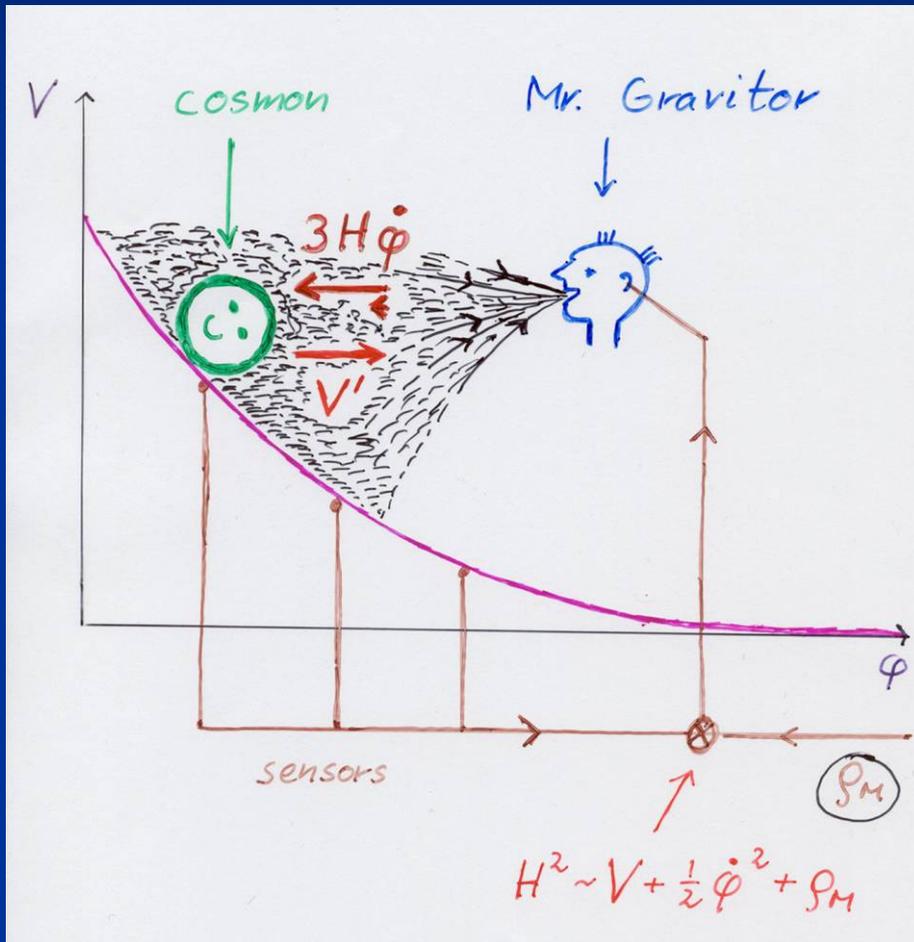
$$3M^2H^2 = V + \frac{1}{2}\dot{\phi}^2 + \rho$$

Potential $V(\varphi)$ determines details of the model

e.g. $V(\varphi) = M^4 \exp(-\alpha\varphi/M)$

for increasing φ the potential decreases towards zero !

Cosmological equations



$$\ddot{\phi} + 3H\dot{\phi} = -dV/d\phi$$

$$3M^2H^2 = V + \frac{1}{2}\dot{\phi}^2 + \rho$$

Cosmic Attractors

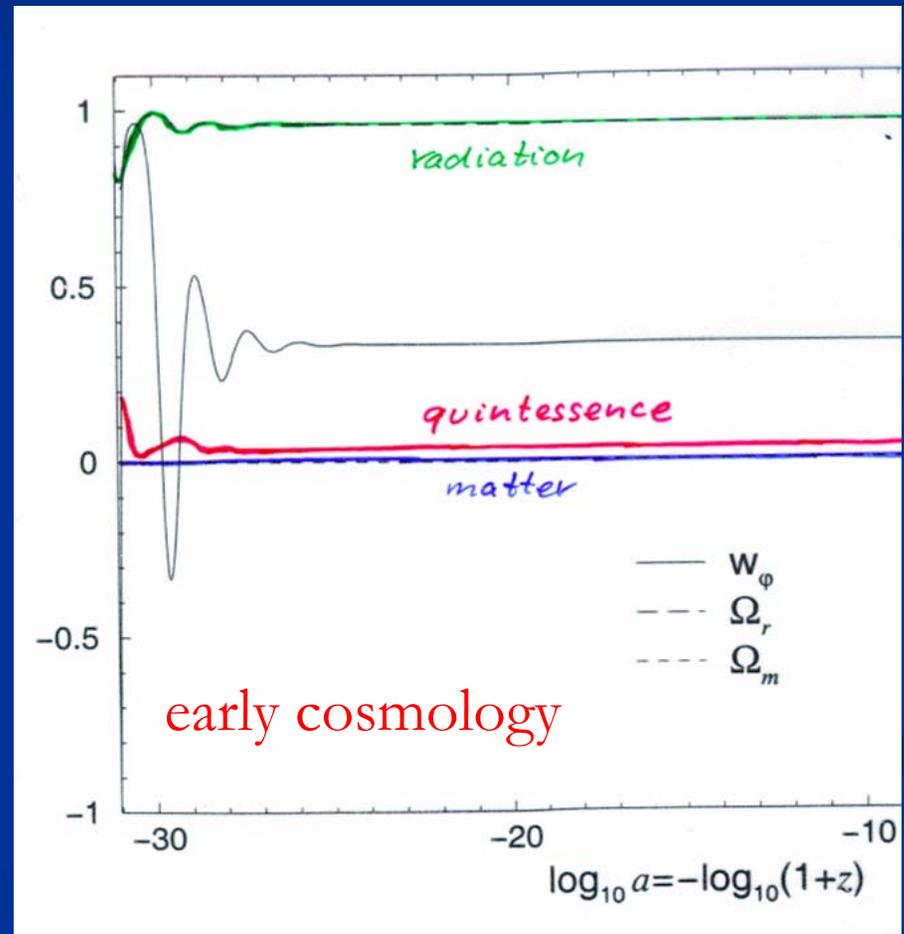
Solutions independent
of initial conditions

typically $V \sim t^{-2}$

$\varphi \sim \ln(t)$

$\Omega_h \sim \text{const.}$

details depend on $V(\varphi)$
or kinetic term



Cosmological equations

$$\mathcal{L} = \sqrt{g} \left\{ \frac{1}{2} \partial^\mu \phi \partial_\mu \phi + V(\phi) \right\}$$

(homogeneous and isotropic Robertson-Walker metric, $k = 0$)

$$\ddot{\phi} + 3H\dot{\phi} + \frac{\partial V}{\partial \phi} = 0$$

matter/radiation

$$3M^2 H^2 = V + \frac{1}{2} \dot{\phi}^2 + \rho$$

$$\dot{\rho}_M + 3H(\rho_M + p_M) = 0$$

$$p_M = \frac{n-3}{3} \rho_M$$

asymptotic solution for large time

Cosmological solutions with scalar field
(cosmon)

for exponential potential $V \sim \exp(-a\frac{\varphi}{M})$

\implies

asymptotic solution for $t \rightarrow \infty$:

$$V \sim t^{-2} \quad , \quad \dot{\varphi}^2 \sim t^{-2}$$

$$\varphi = \frac{2M}{a} \ln t$$

stable attractor!

independent of initial conditions
“tracker solution”

$$\phi = \frac{2M}{\alpha} \ln(t/\bar{t}) \quad , \quad \frac{1}{2}\dot{\phi}^2 = \frac{2M^2}{\alpha^2} t^{-2} \quad , \quad V = \frac{2M^2(6-n)}{\alpha^2} t^{-2}$$

$$H = \frac{2}{n} t^{-1} \quad , \quad \rho \sim t^{-2}$$

exponential potential →
constant fraction in dark energy

$$\Omega_h = n/\alpha^2$$

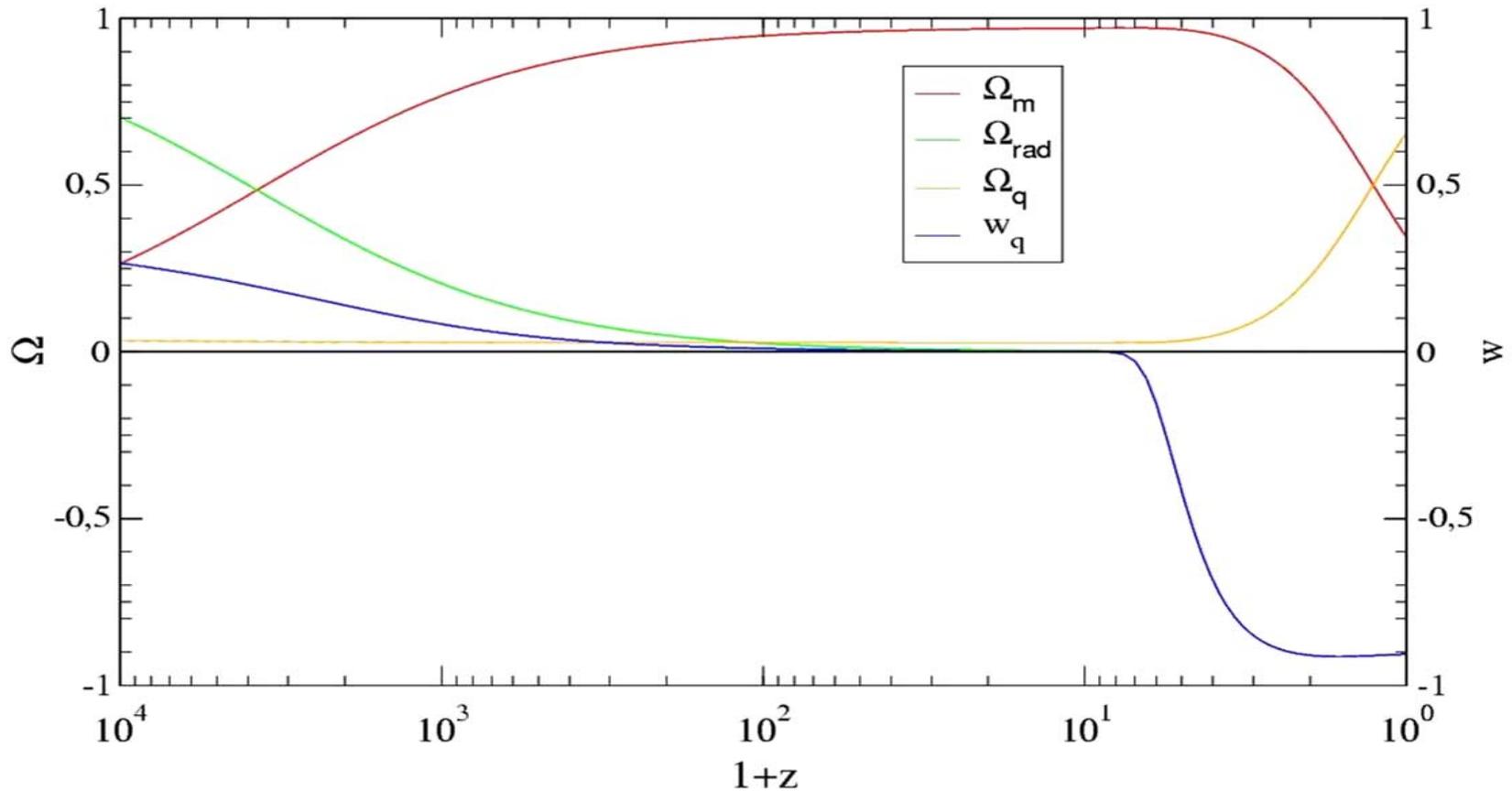
can explain order of magnitude
of dark energy !

realistic quintessence

fraction in dark energy has to
increase in “recent time” !

Quintessence becomes important “today”

Crossover Quintessence Evolution



Equation of state

$$p = T - V$$

pressure

kinetic energy

$$\rho = T + V$$

energy density

$$T = \frac{1}{2} \dot{\phi}^2$$

Equation of state

$$w = \frac{p}{\rho} = \frac{T - V}{T + V}$$

Depends on specific evolution of the scalar field

Negative pressure

- $w < 0$ Ω_h increases (with decreasing z)

late universe with
small radiation component :

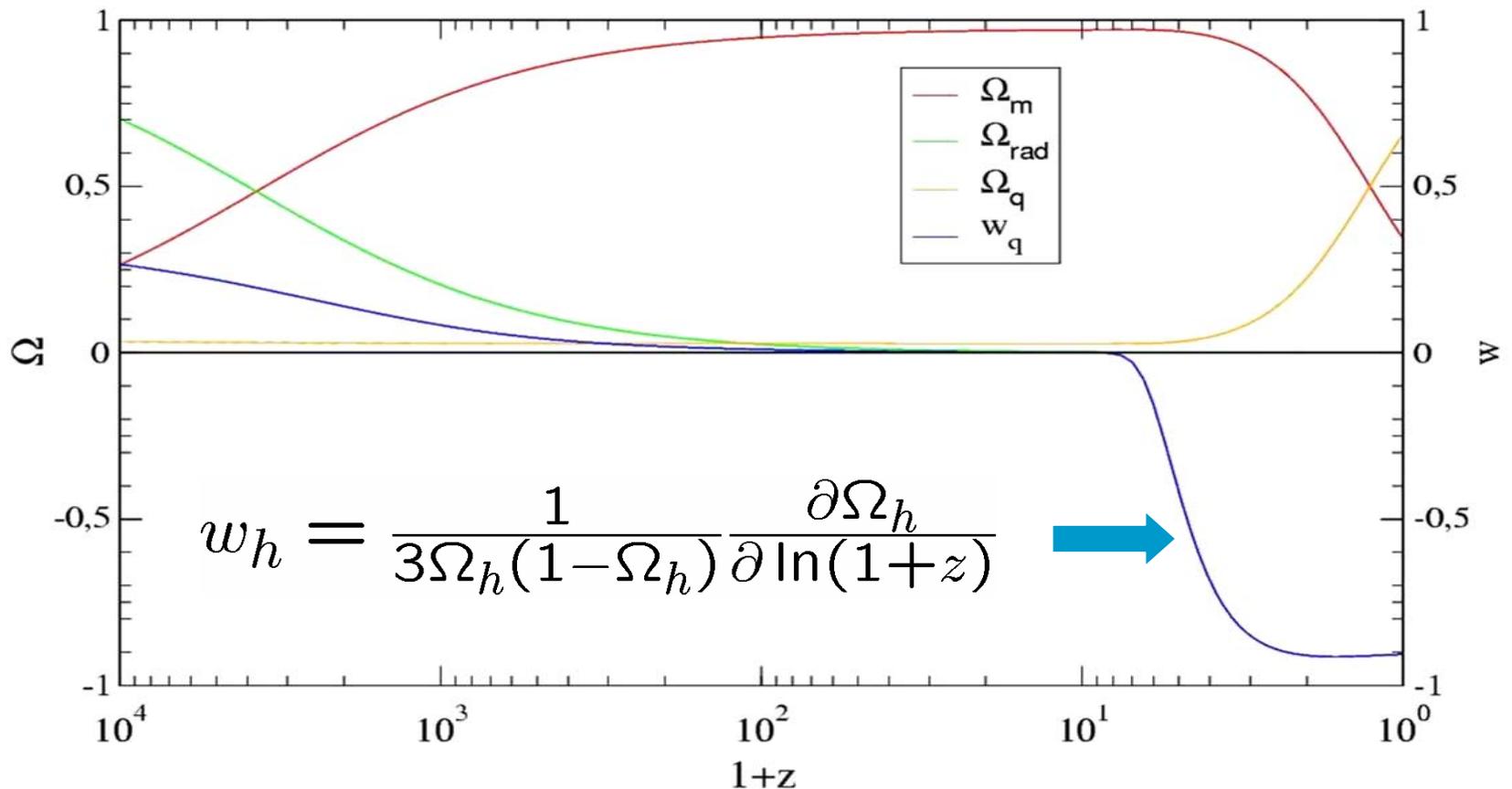
$$w_h = \frac{1}{3\Omega_h(1-\Omega_h)} \frac{\partial \Omega_h}{\partial \ln(1+z)}$$

- $w < -1/3$ expansion of the Universe is
accelerating

- $w = -1$ cosmological constant

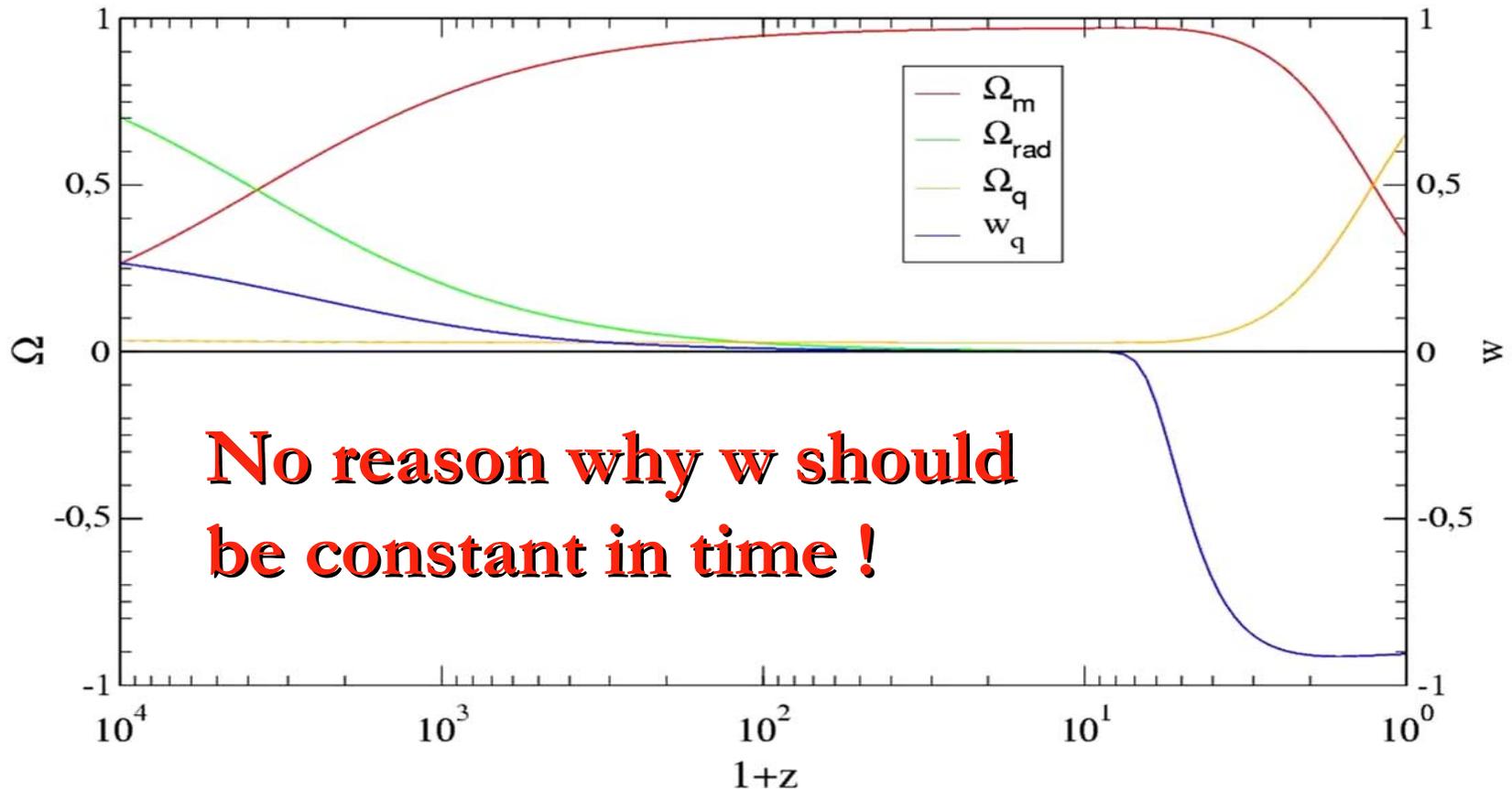
Negative pressure

Crossover Quintessence Evolution



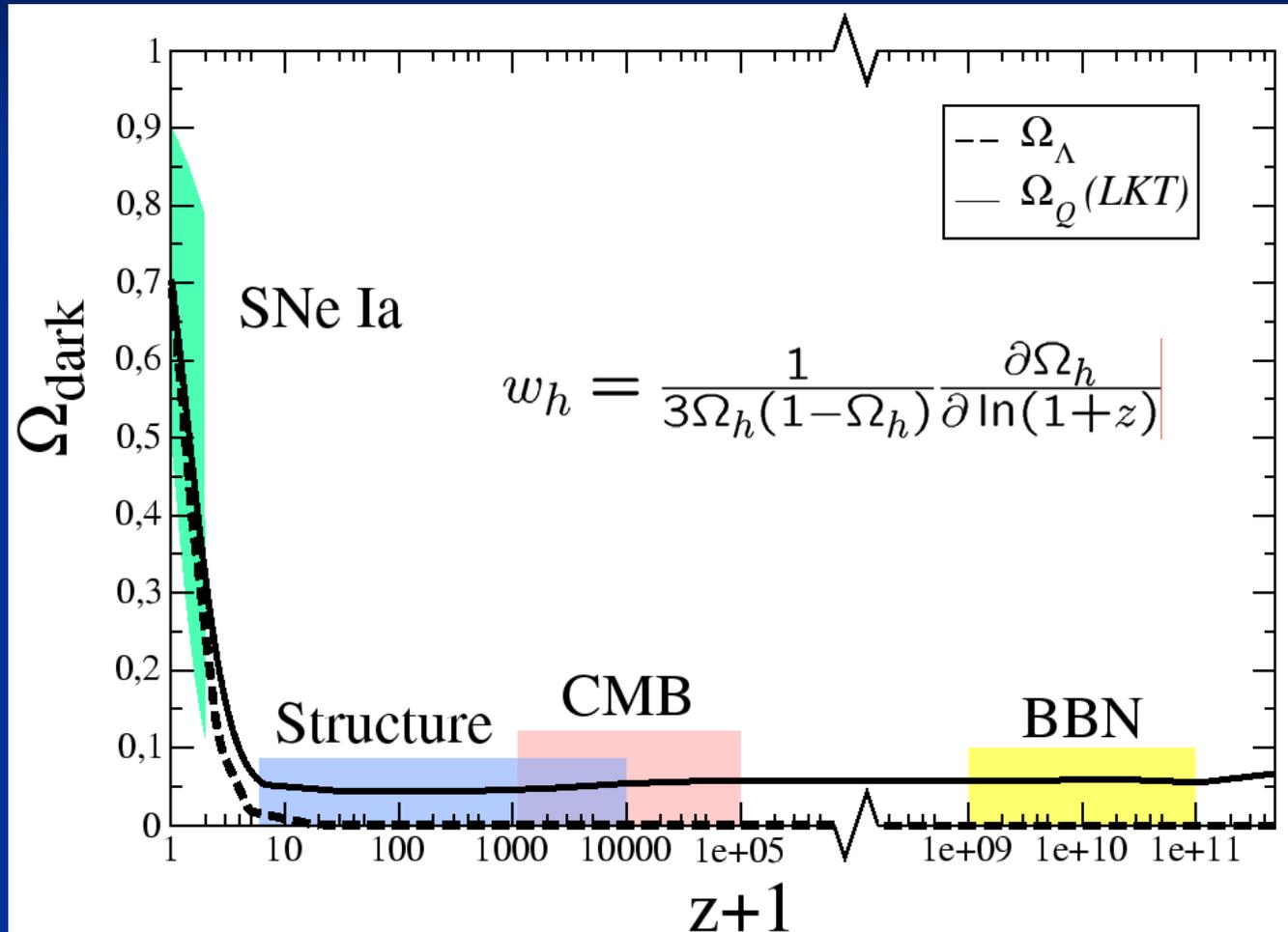
Quintessence becomes important “today”

Crossover Quintessence Evolution



How can quintessence be distinguished from a cosmological constant ?

Time dependence of dark energy



cosmological constant : $\Omega_h \sim t^2 \sim (1+z)^{-3}$

small early and large present dark energy

fraction in dark energy has substantially
increased since end of structure formation



expansion of universe accelerates in present
epoch

$$w_h = \frac{1}{3\Omega_h(1-\Omega_h)} \frac{\partial \Omega_h}{\partial \ln(1+z)}$$

effects of early dark energy

- modifies cosmological evolution (CMB)
- slows down the growth of structure

Growth of density fluctuations

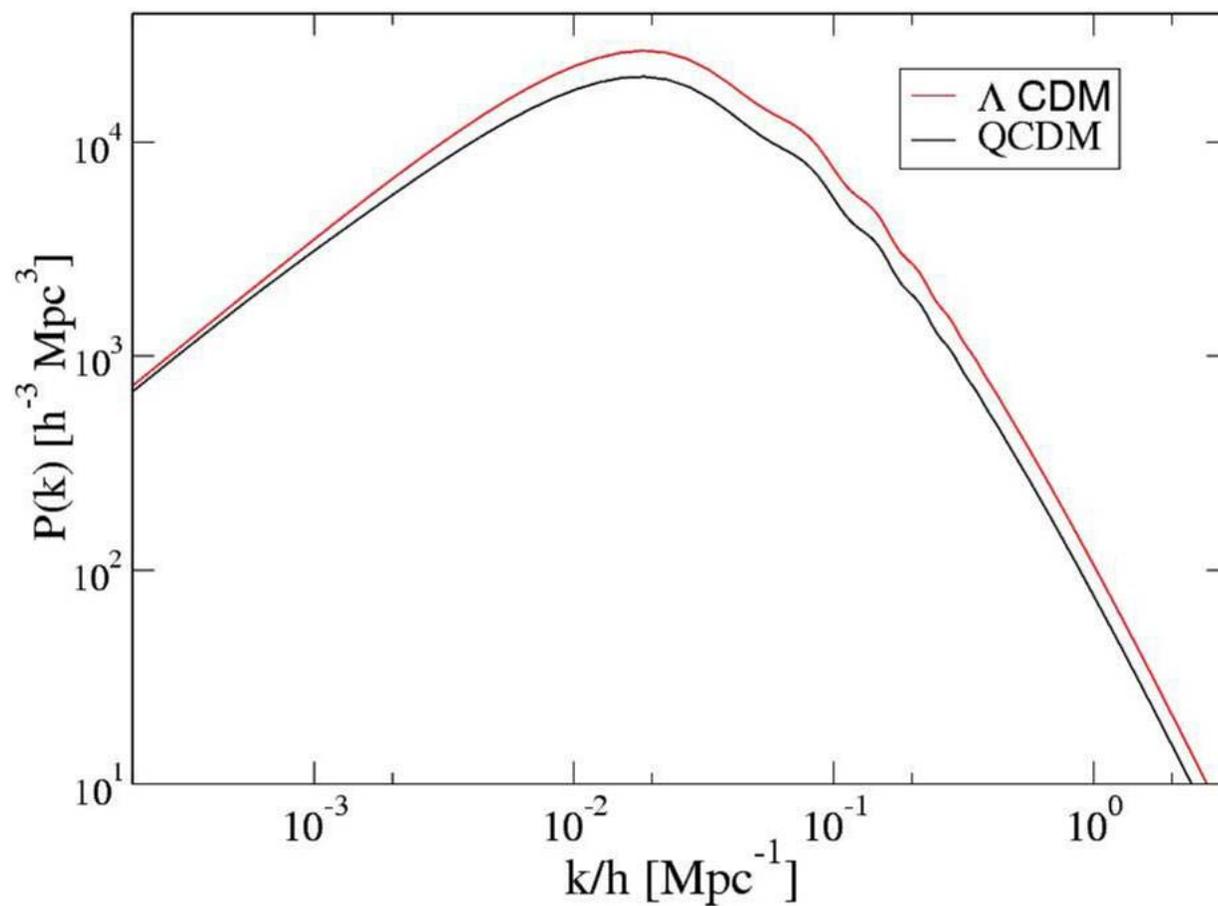
- Matter dominated universe with constant Ω_h :

$$\Delta\rho \sim a^{1-\frac{\epsilon}{2}}, \quad \epsilon = \frac{5}{2}\left(1 - \sqrt{1 - \frac{24}{25}\Omega_h}\right)$$

P.Ferreira,M.Joyce

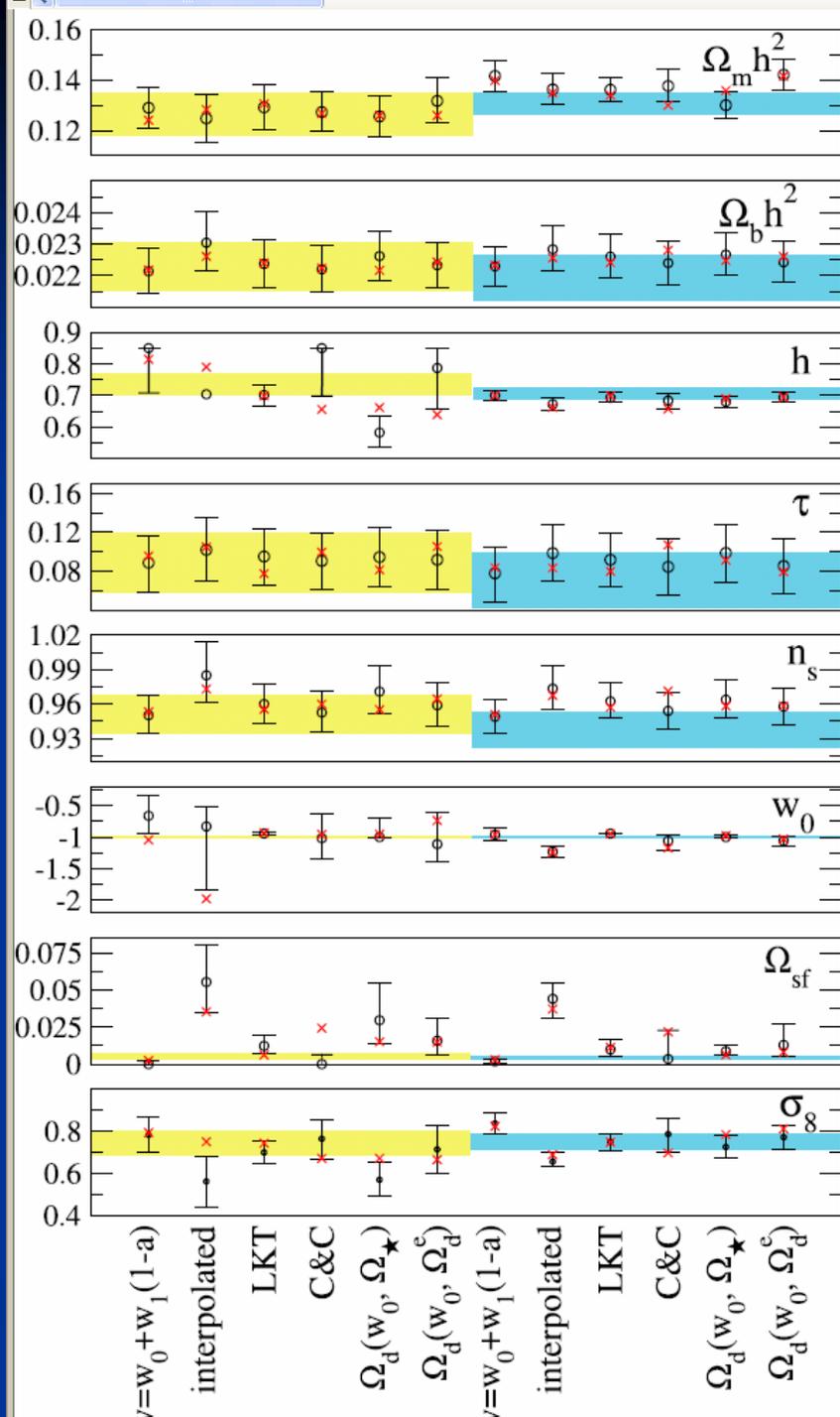
- Dark energy slows down structure formation
→ $\Omega_h < 10\%$ during structure formation

Early quintessence slows down the growth of structure

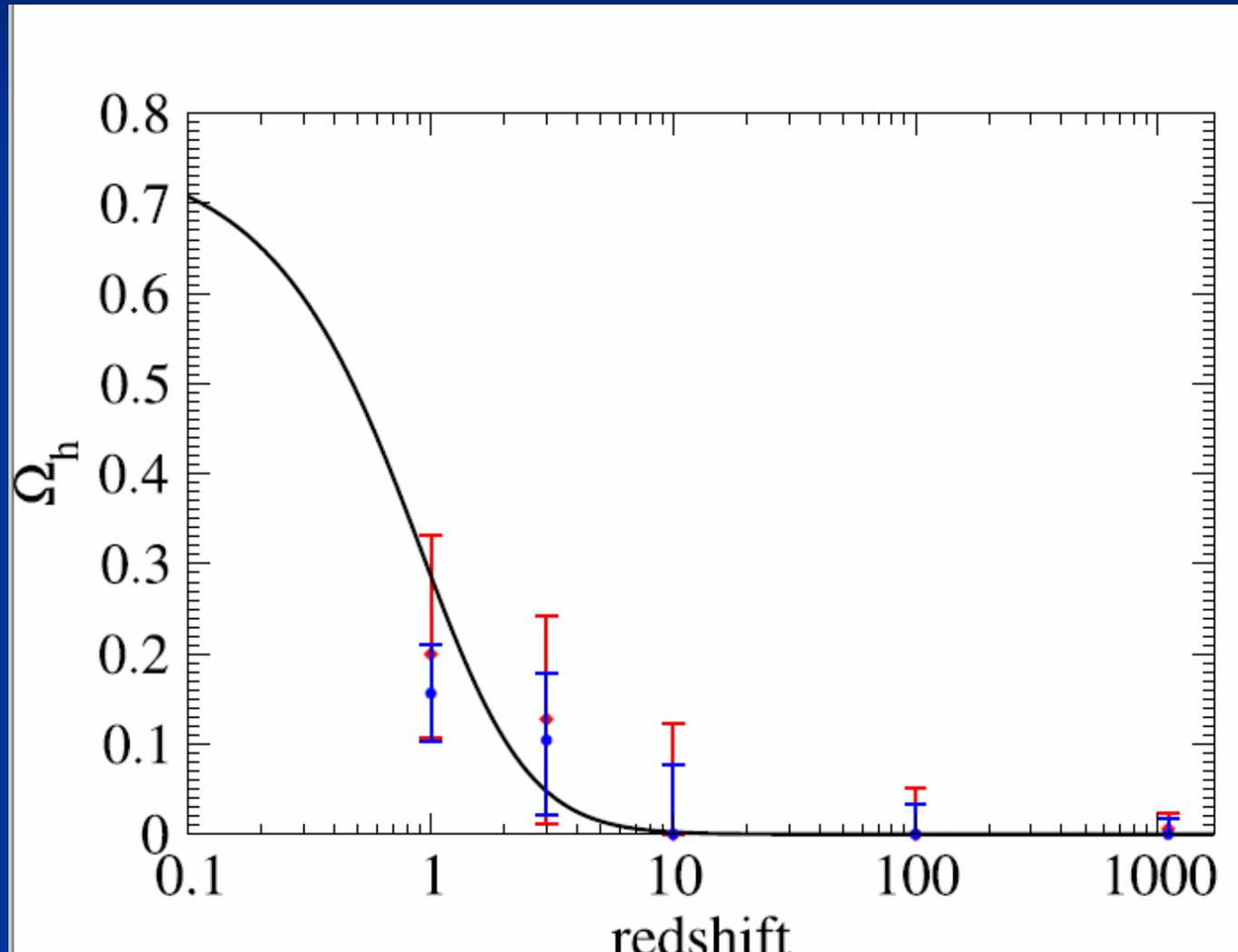


bounds on Early Dark Energy after WMAP'06

G.Robbers, M.Doran, ...

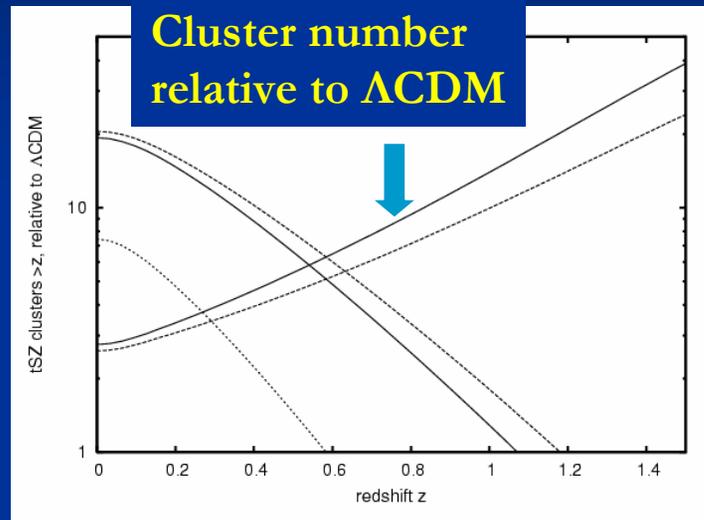


interpolation of Ω_h



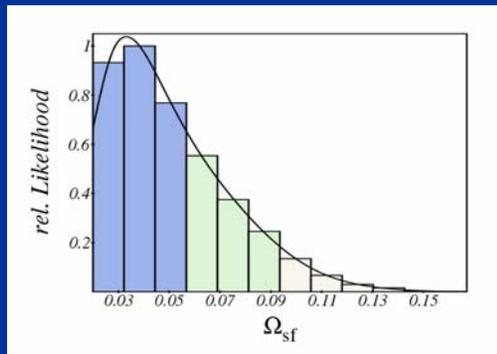
Little Early Dark Energy can make large effect !

More clusters at high redshift

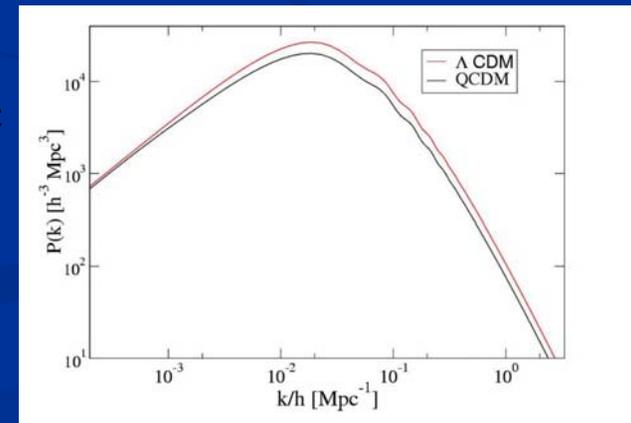


Two models with 4% Dark Energy during structure formation

Fixed σ_8 (normalization dependence !)



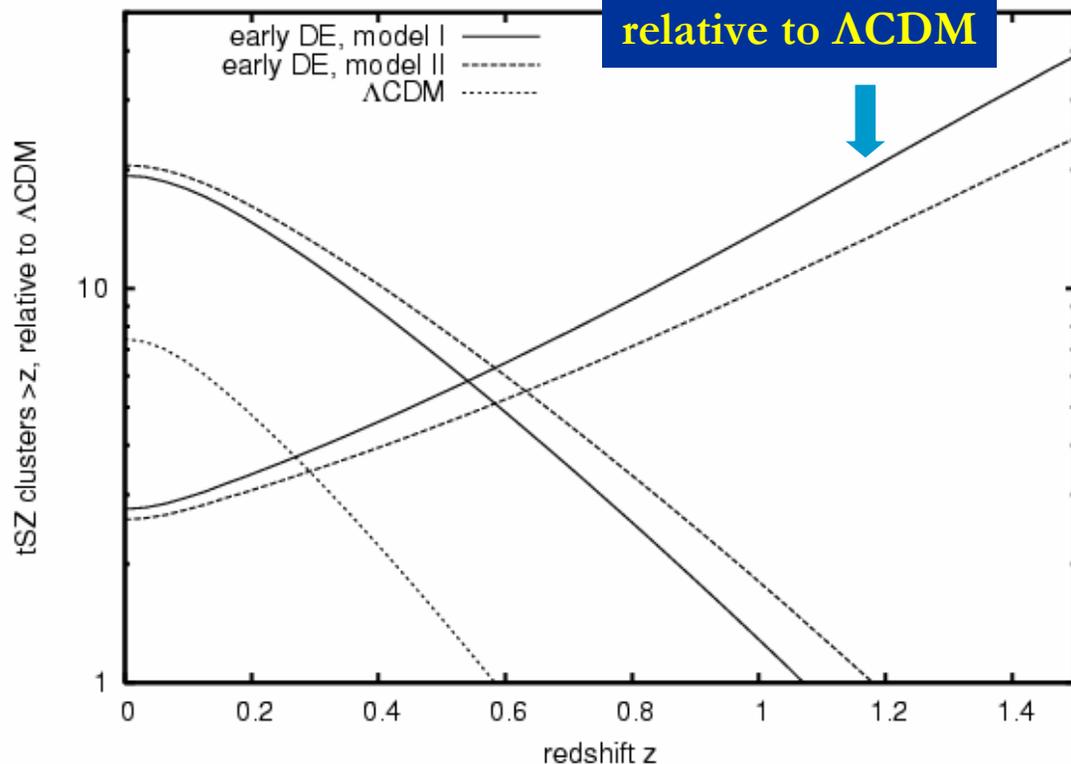
Early Quintessence slows down the growth of structure



Little Early Dark Energy can make large effect !

Non – linear enhancement

Cluster number
relative to Λ CDM



Two models with
4% Dark Energy
during structure
formation

Fixed σ_8
(normalization
dependence !)

More clusters at high redshift !

Bartelmann, Doran, ...

How to distinguish Q from Λ ?

A) Measurement $\Omega_h(z) \iff H(z)$

i) $\Omega_h(z)$ at the time of structure formation, CMB - emission or nucleosynthesis

ii) equation of state $w_h(\text{today}) > -1$

B) Time variation of fundamental “constants”

C) Apparent violation of equivalence principle

D) Possible coupling between Dark Energy and Dark Mater

Cosmodynamics

Cosmon mediates new long-range interaction

Range : size of the Universe – horizon

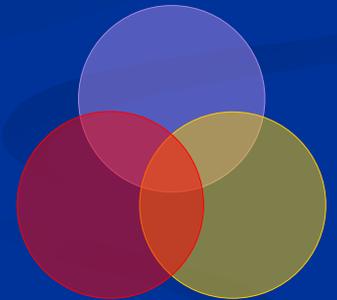
Strength : weaker than gravity

photon	electrodynamics
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graviton	gravity
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cosmon	cosmodynamics
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Small correction to Newton's law



“Fifth Force”

- Mediated by scalar field

R.Peccei,J.Sola,C.Wetterich,Phys.Lett.B195,183(1987)

- Coupling strength: weaker than gravity
(nonrenormalizable interactions $\sim M^{-2}$)

- Composition dependence

→ violation of equivalence principle

- Quintessence: connected to time variation of fundamental couplings

C.Wetterich , Nucl.Phys.B302,645(1988)

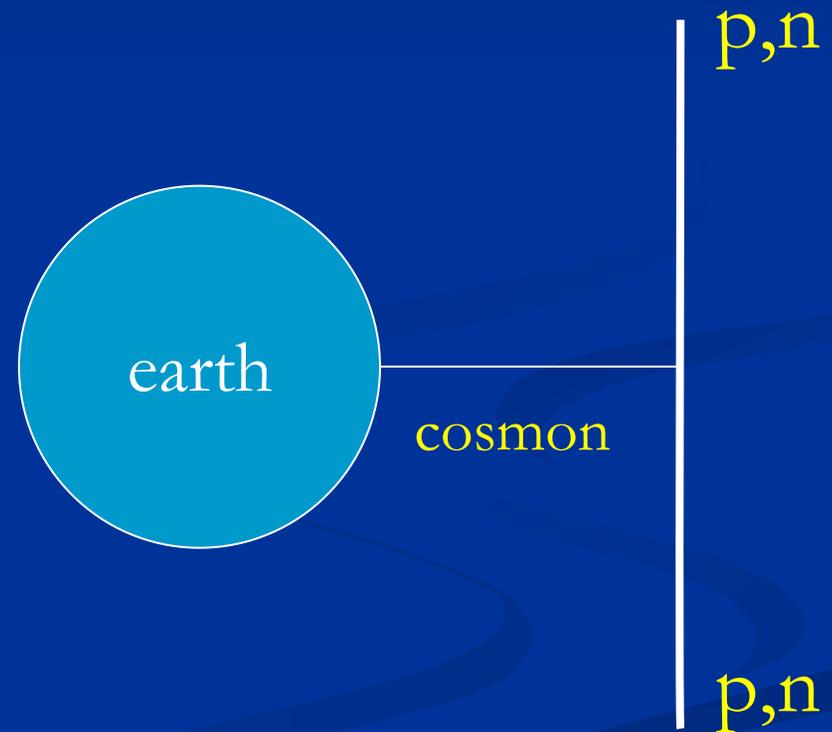
Violation of equivalence principle

Different couplings of
cosmon to proton and
neutron

Differential acceleration

“Violation of
equivalence principle”

only apparent : new “fifth force” !



$$(1) \quad \alpha_x(\varphi) \rightarrow \Lambda_{\text{QCD}}(\varphi) \rightarrow m_n(\varphi)$$

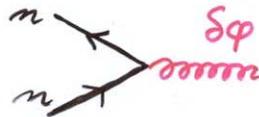
nucleon mass depends on value
of the cosmon field
(and therefore on time)

(2) expand around cosmological
value $\varphi_0(t)$:

$$\varphi(\vec{x}, t) = \varphi_0(t) + \delta\varphi(\vec{x}, t)$$

$$m_n = m_n(\varphi_0) + \frac{\partial m_n}{\partial \varphi} \Big|_{\varphi_0} \delta\varphi$$

\Rightarrow cosmon - nucleon vertex $\sim \bar{n}n \delta\varphi$



\Rightarrow earth is source for surrounding
local cosmon field $\delta\varphi(|\vec{r}|)$

(3) Test body carries effective
"cosmon charge"

$$Q_c = k^{-1} \frac{\partial m_t}{\partial \varphi}$$

to be compared with "gravitational charge"

$$Q_g = \frac{m_t}{\sqrt{2} M_p}$$

⇒ Correction to Newtonian potential

$$V_N = - \frac{G_N M m_t}{r} (1 + \alpha_t)$$

$$\alpha_t = \frac{2 M_p^2}{k^2} \frac{\partial \ln M}{\partial \varphi} \frac{\partial \ln m_t}{\partial \varphi}$$

(4) Protons and neutrons have different

$$\text{cosmon charges, } \frac{\partial m_p}{\partial \varphi} \neq \frac{\partial m_n}{\partial \varphi}$$

Differential acceleration

Two bodies with equal mass experience
a different acceleration !

$$\eta = (a_1 - a_2) / (a_1 + a_2)$$

$$\text{bound : } \eta < 3 \cdot 10^{-14}$$

Cosmon coupling to atoms

- Tiny !!!
- Substantially weaker than gravity.
- Non-universal couplings bounded by tests of equivalence principle.
- Universal coupling bounded by tests of Brans-Dicke parameter ω in solar system.
- Only very small influence on cosmology.

Cosmon coupling to Dark Matter

- Only bounded by cosmology
- Substantial coupling possible
- Can modify scaling solution and late cosmology
- Role in clustering of extended objects ?

L. Amendola

Cosmon coupling to neutrinos

- can be large !
- interesting effects for cosmology if neutrino mass is growing
- growing neutrinos can stop the evolution of the cosmon
- transition from early scaling solution to cosmological constant dominated cosmology

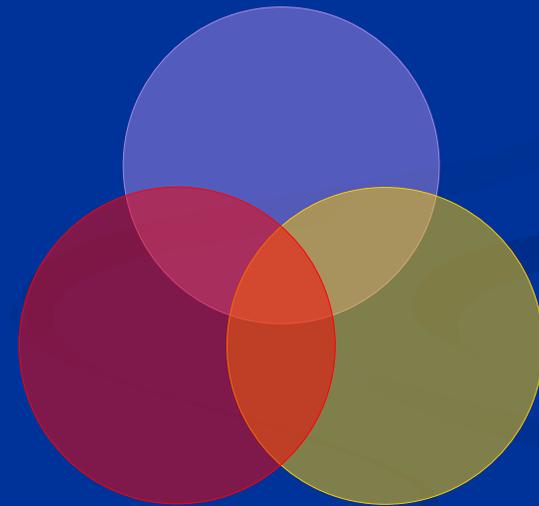
L.Amendola, M.Baldi, ...

Quintessence and time variation of fundamental constants

Generic prediction

Strength unknown

Strong, electromagnetic, weak interactions



gravitation

cosmodynamics

C.Wetterich ,
Nucl.Phys.B302,645(1988)

Time varying constants

- It is not difficult to obtain quintessence potentials from higher dimensional or string theories
- Exponential form rather generic
(after Weyl scaling)
- But most models show too strong time dependence of constants !

Are fundamental “constants” time dependent ?

Fine structure constant α (electric charge)

Ratio electron mass to proton mass

Ratio nucleon mass to Planck mass

Quintessence and Time dependence of “fundamental constants”

- Fine structure constant depends on value of
cosmon field : $\alpha(\varphi)$

*(similar in standard model: couplings depend on
value of Higgs scalar field)*

- Time evolution of φ 
Time evolution of α

Jordan,...

Standard – Model of electroweak interactions : Higgs - mechanism

- The masses of all fermions and gauge bosons are proportional to the (vacuum expectation) value of a scalar field φ_H (Higgs scalar)
- For electron, quarks , W- and Z- bosons :

$$m_{\text{electron}} = h_{\text{electron}} * \varphi_H \quad \text{etc.}$$

Restoration of symmetry at high temperature in the early Universe

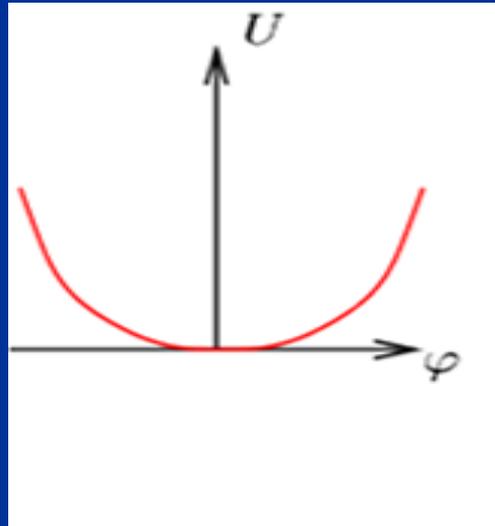
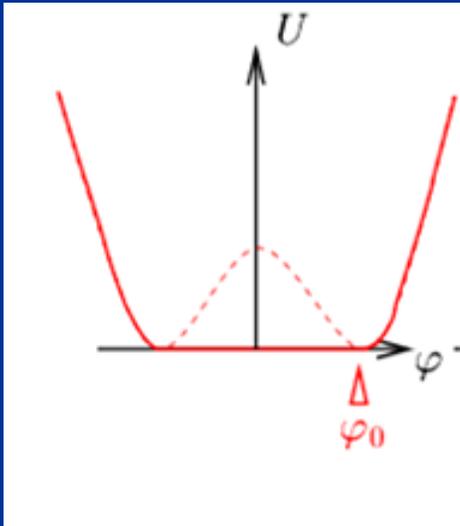
Low T
SSB

$$\langle \phi_H \rangle = \phi_0 \neq 0$$

High T
SYM

$$\langle \phi_H \rangle = 0$$

high T :
less order
more symmetry



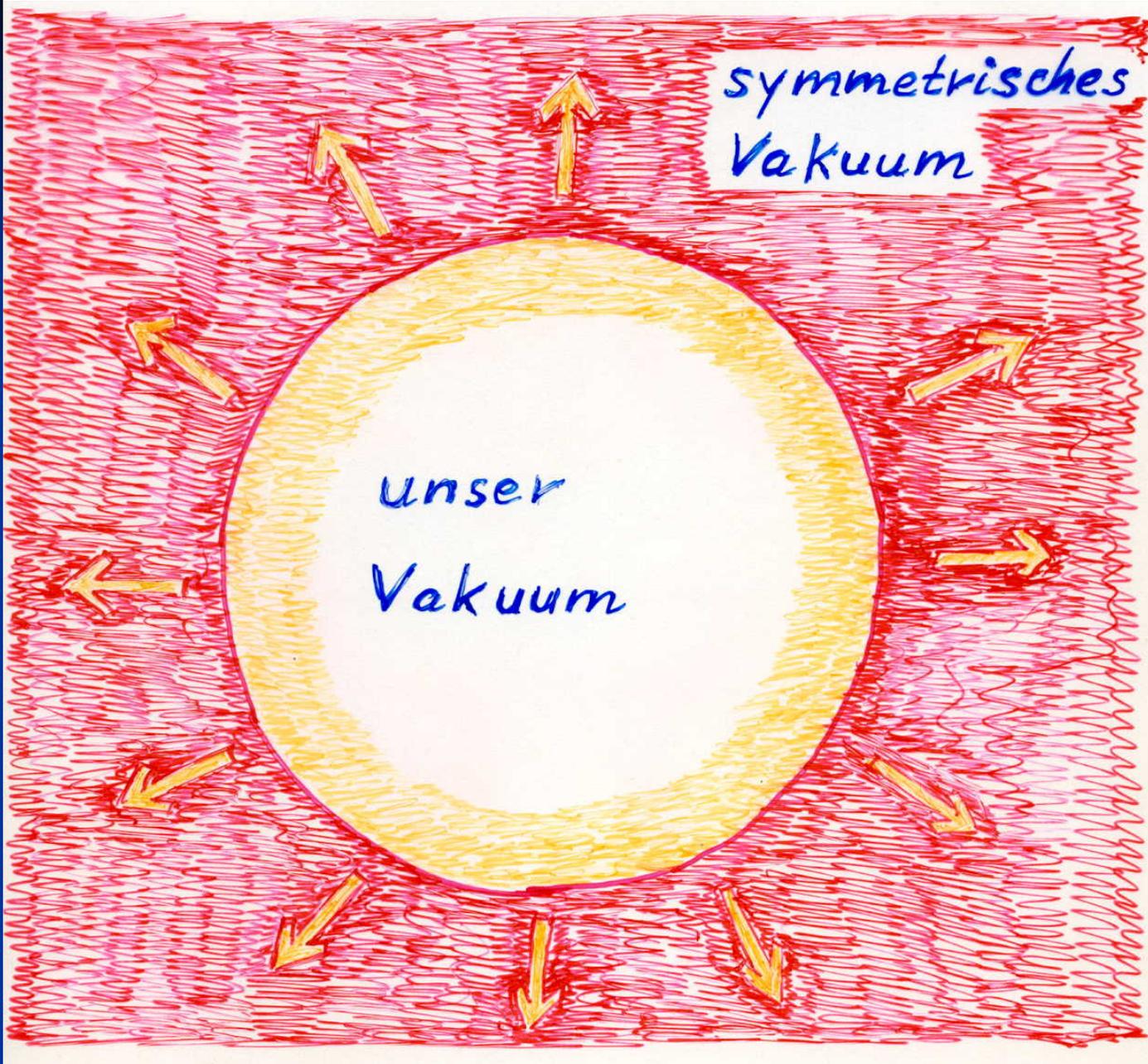
example:
magnets

In the hot plasma
of the early Universe :

**No difference in mass for
electron and muon !**

symmetrisches
Vakuum

unser
Vakuum

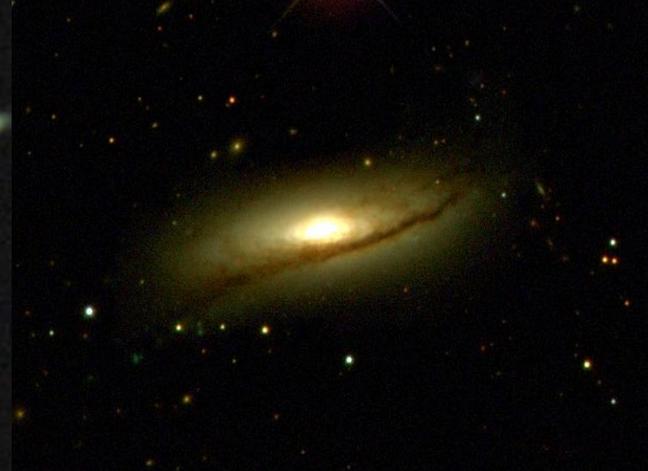
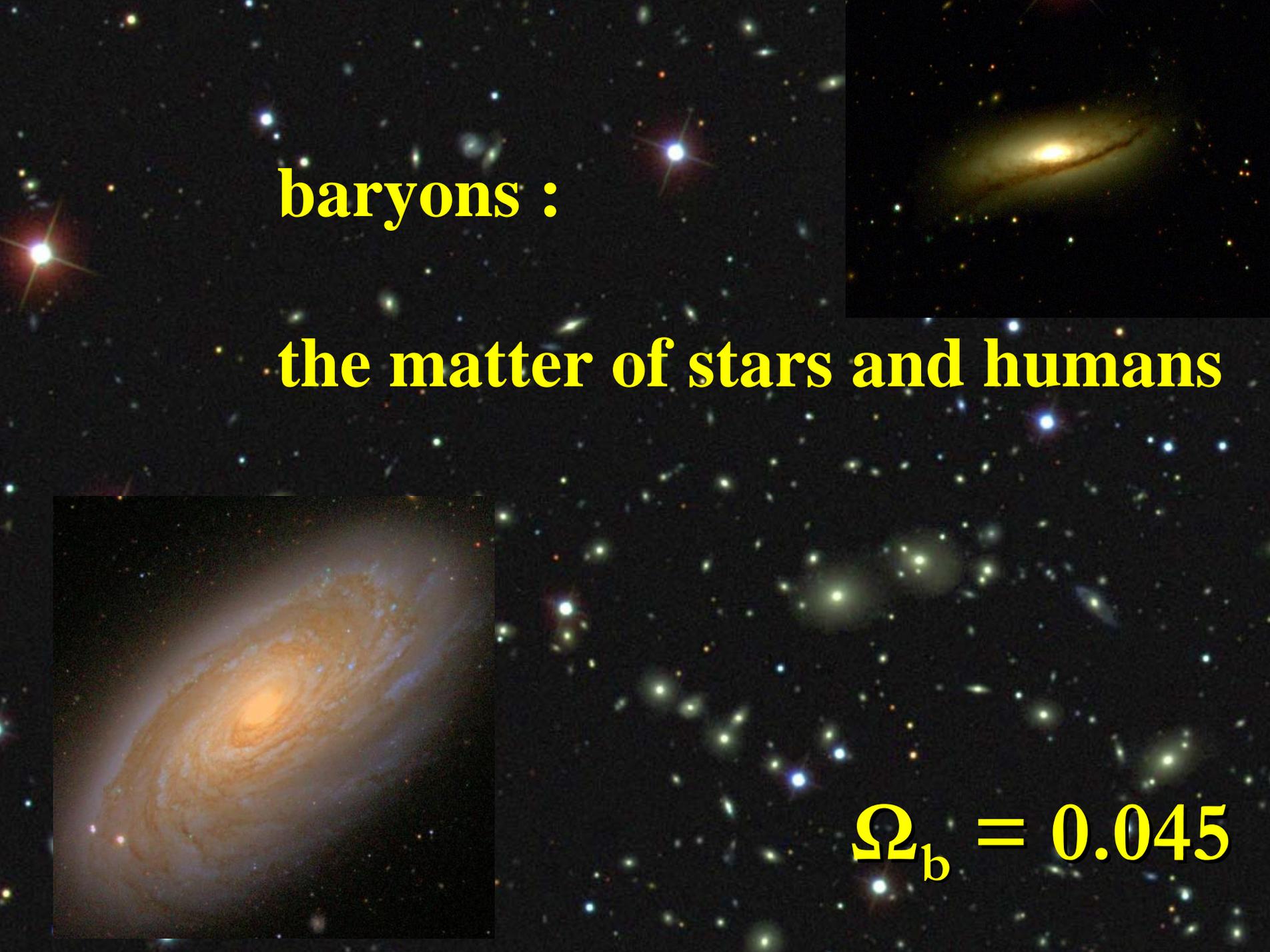


Quintessence :
Couplings are still varying *now* !

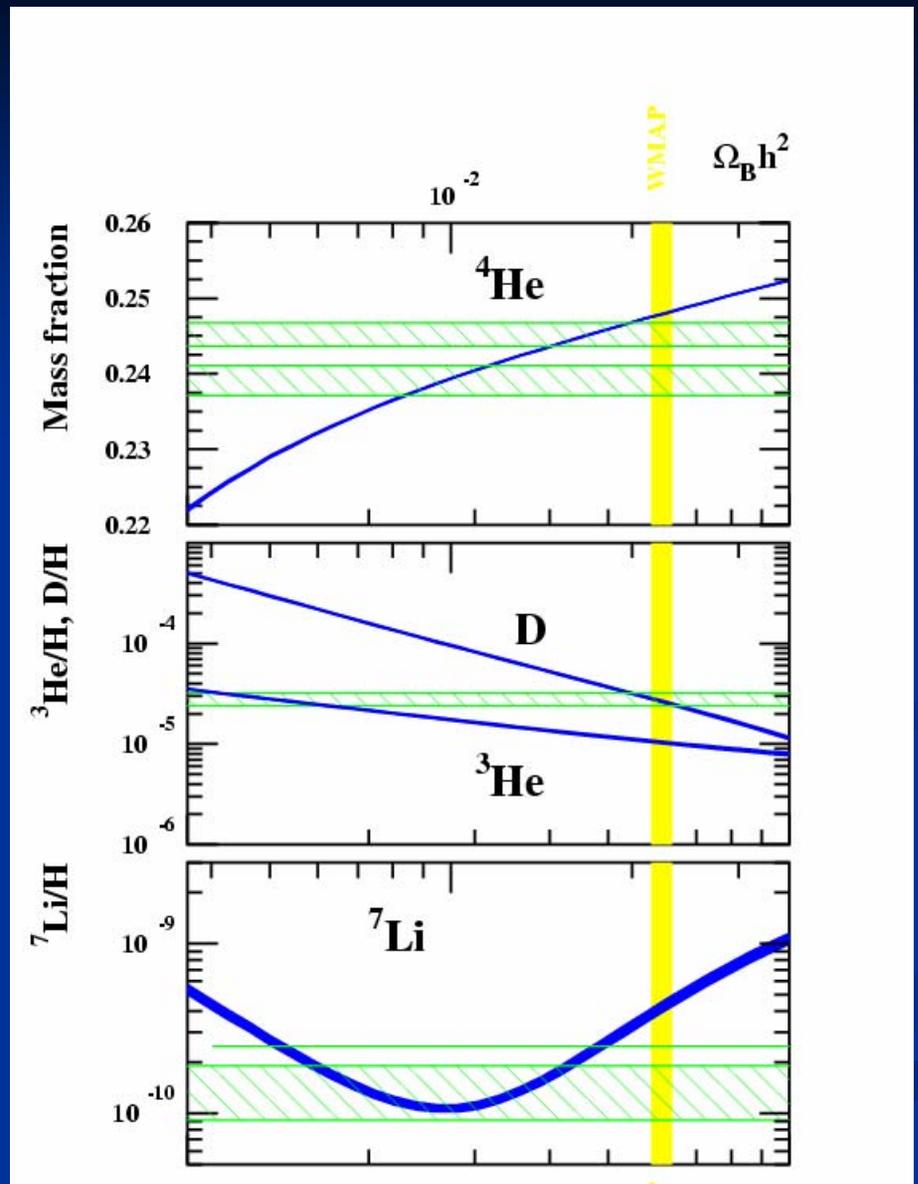
**Strong bounds on
the variation of couplings -
interesting perspectives for
observation !**

baryons :

the matter of stars and humans


$$\Omega_b = 0.045$$

Abundancies of
primordial
light elements
from
nucleosynthesis



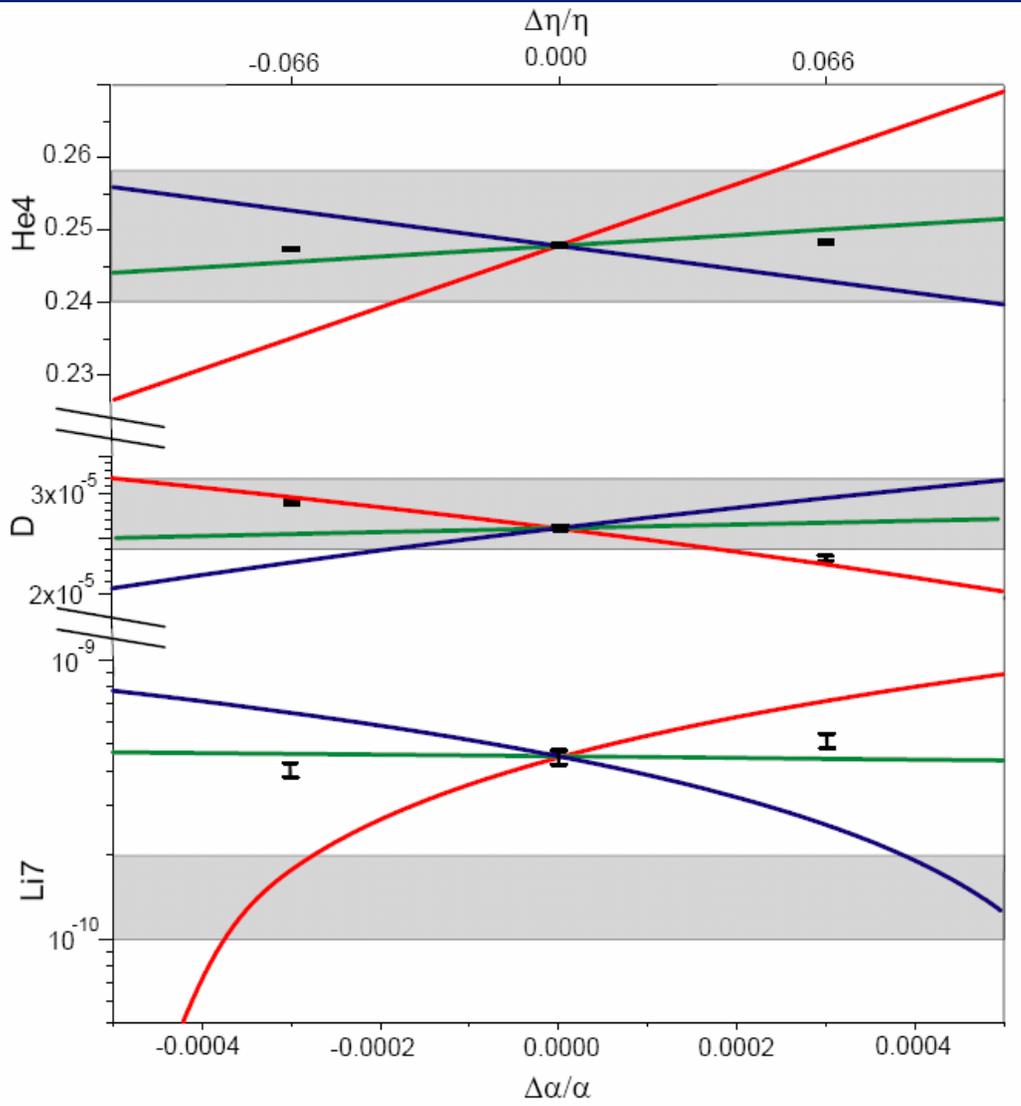
Allowed values for variation of
fine structure constant :

$$\Delta\alpha/\alpha (z=10^{10}) = -1.0 \cdot 10^{-3} \quad \text{GUT 1}$$

$$\Delta\alpha/\alpha (z=10^{10}) = -2.7 \cdot 10^{-4} \quad \text{GUT 2}$$

primordial abundances for three GUT models

He



D

Li

present
observations :
 1σ

T.Dent,
S.Stern,...

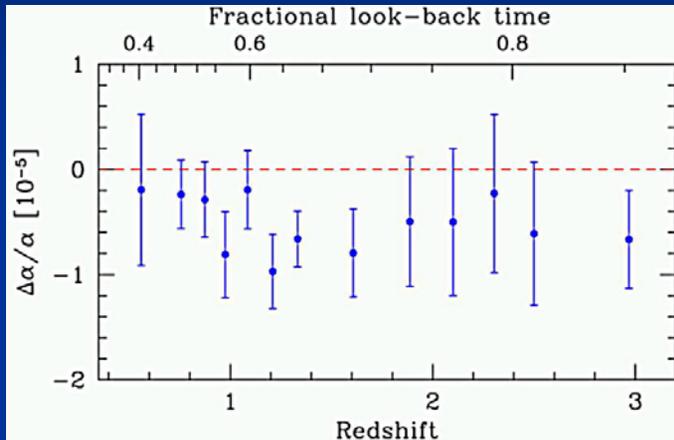
three GUT models

- unification scale \sim Planck scale
- 1) All particle physics scales $\sim \Lambda_{\text{QCD}}$
- 2) Fermi scale and fermion masses \sim unification scale
- 3) Fermi scale varies more rapidly than Λ_{QCD}

$\Delta\alpha/\alpha \approx 4 \cdot 10^{-4}$ allowed for GUT 1 and 3 , larger for GUT 2

$\Delta\ln(M_n/M_p) \approx 40 \Delta\alpha/\alpha \approx 0.015$ allowed

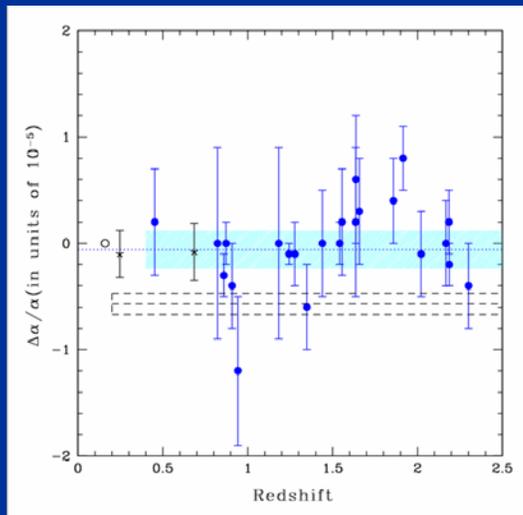
Variation of fine structure constant as function of redshift



Three independent data sets from
Keck/HIRES

$$\Delta\alpha/\alpha = -0.54 (12) 10^{-5}$$

Murphy, Webb, Flammbaum, June
2003



VLT

$$\Delta\alpha/\alpha = -0.06 (6) 10^{-5}$$

Srianand, Chand, Petitjean, Aracil,
Feb. 2004

$z \approx 2$

Atomic clocks and OKLO

* Atomic clocks:

$$\frac{\dot{\alpha}_{em}}{\alpha_{em}} = -5.4 \cdot 10^{-10} \frac{\Delta \alpha_{em}}{\alpha_{em}} (z=0.13) \text{ yr}^{-1}$$

$$\text{observation } \frac{\dot{\alpha}_{em}}{\alpha_{em}} = (4.2 \pm 6.9) \cdot 10^{-15} \text{ yr}^{-1}$$

Sortais et al.

assumes that both effects are dominated
by change of fine structure constant

Atomic clocks and OKLO

Oklo natural reactor: $\Delta\alpha/\alpha < 10^{-7}$

Atomic clocks:

$$\frac{\dot{\alpha}_{em}}{\alpha_{em}} = -5.4 \cdot 10^{-10} \frac{\Delta\alpha_{em}(z=0.13)}{\alpha_{em}} \text{ yr}^{-1}$$

Atom clocks : $\Delta\alpha/\alpha < 10^{-15} \text{ yr}^{-1}$ Fortier et al

assumes that both effects are dominated
by change of fine structure constant

Time variation of coupling constants
must be tiny –

would be of very high significance !

Possible signal for Quintessence

Πάντα ρεῖ

Everything is flowing

Apparent violation of equivalence principle

and

time variation of fundamental couplings

measure both the

cosmon – coupling to ordinary matter

Differential acceleration η

For unified theories (GUT) :

$$\eta = -1.75 \cdot 10^{-2} \Delta R_z \left(\frac{\partial \ln \alpha}{\partial z} \right)^2 \frac{1 + \tilde{Q}}{\Omega_h (1 + w_h)}$$

$$\Delta R_z = \frac{\Delta Z}{Z + N} \approx 0.1$$

$$\eta = \Delta a / 2a$$

Q : time dependence of other parameters

Link between time variation of α

and violation of equivalence principle

typically : $\eta = 10^{-14}$

if time variation of α

near Oklo upper bound

to be tested (**MICROSCOPE** , ...)



small change of couplings in space

- Fine structure constant depends on location in space
- Experiments with satellites ?

for $r = 2 R_E$

$$\delta \alpha_{em} / \alpha_{em} = 3 \cdot 10^{-19} / \text{k}^2$$

Summary

- o $\Omega_h = 0.7$
- o Q/Λ : dynamical und static dark energy
will be distinguishable
- o Q : time varying fundamental coupling “constants”
violation of equivalence principle

????????????????????????????????

Why becomes Quintessence dominant in the present cosmological epoch ?

Are dark energy and dark matter related ?

Can Quintessence be explained in a fundamental unified theory ?

**Quintessence and solution of
cosmological constant
problem should be related !**



End

A few references

C.Wetterich , Nucl.Phys.B302,668(1988) , received 24.9.1987

P.J.E.Peebles,B.Ratra , Astrophys.J.Lett.325,L17(1988) , received 20.10.1987

B.Ratra,P.J.E.Peebles , Phys.Rev.D37,3406(1988) , received 16.2.1988

J.Frieman,C.T.Hill,A.Stebbins,I.Waga , Phys.Rev.Lett.75,2077(1995)

P.Ferreira, M.Joyce , Phys.Rev.Lett.79,4740(1997)

C.Wetterich , Astron.Astrophys.301,321(1995)

P.Viana, A.Liddle , Phys.Rev.D57,674(1998)

E.Copeland,A.Liddle,D.Wands , Phys.Rev.D57,4686(1998)

R.Caldwell,R.Dave,P.Steinhardt , Phys.Rev.Lett.80,1582(1998)

P.Steinhardt,L.Wang,I.Zlatev , Phys.Rev.Lett.82,896(1999)

Dynamics of quintessence

- **Cosmon** φ : scalar singlet field
- Lagrange density $L = V + \frac{1}{2} \mathbf{k}(\varphi) \partial\varphi \partial\varphi$
(units: reduced Planck mass $M=1$)
- Potential : $V = \exp[-\varphi]$
- “Natural initial value” in Planck era $\varphi=0$
- today: $\varphi=276$

kinetial

$$\mathcal{L}(\varphi) = \frac{1}{2} (\partial\varphi)^2 k^2(\varphi) + \exp[-\varphi]$$

Small almost constant k :

- Small almost constant Ω_h

Large k :

- Cosmon dominated universe (like inflation)

cosmon mass changes with time !

for standard kinetic term

- $m_c^2 = V''$

for standard exponential potential , $k = \text{const.}$

- $m_c^2 = V'' / k^2 = V / (k^2 M^2)$
 $= 3 \Omega_h (1 - w_h) H^2 / (2 k^2)$

Quintessence models

- Kinetic function $k(\varphi)$: parameterizes the details of the model - “kinetial”
 - $k(\varphi) = k = \text{const.}$ Exponential Q.
 - $k(\varphi) = \exp((\varphi - \varphi_1)/\alpha)$ Inverse power law Q.
 - $k^2(\varphi) = “1/(2E(\varphi_c - \varphi))”$ Crossover Q.
- possible naturalness criterion:

$k(\varphi=0) / k(\varphi_{\text{today}})$: not tiny or huge !

- else: explanation needed -

More models ...

- **Phantom energy** (Caldwell)
negative kinetic term ($w < -1$)
consistent quantum theory ?
- **K – essence** (Amendariz-Picon, Mukhanov, Steinhardt)
higher derivative kinetic terms
why derivative expansion not valid ?
- **Coupling cosmon / (dark) matter** (C.W., Amendola)
why substantial coupling to dark matter and not to ordinary matter ?
- **Non-minimal coupling to curvature scalar – $f(\varphi) R$** -
can be brought to standard form by Weyl scaling !